2.2 Formula Recognition Using seq2seq Models - Training the model

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1 2.2 Formula Recognition Using seq2seq Models - Training the model

In this notebook, we train a seq2seq model that transcribes typeset formulas from images into Latex markup. The model consists of a few components:

An encoder

• This is the same model as we used in the previous notebook, consisting of 3 convolutional layers with increasing hidden units.

A decoder

• the decoder takes the features from our encoder, and generates an "embedding" for them, which is a fixed-sized vector that represents the visual content of the input image. We apply Bahdanau attention over this feature vector, and concatenate it with the hidden state of a GRU. This is then fed back into a GRU. Finally, we use two fully-connected layers where the last layer has a softmax activation in order to produce our final prediction.

References

- Image Captioning With Attention
- im2latex paper
- Guillaume Genthial's im2latex implementation

As before, the directory structure is defined as:

```
project/
   data/ -- Contains the data used in the project (both original and derived)
   doc/ -- Project documentation (including report & summary)
   figs/ -- Any saved figures generated by the project
   notebooks/ -- All notebooks for the project
    scripts/ -- Scripts used for various reasons, such as pre-processing
    src/ -- Regular python code
In [41]: import os
         import glob
         ### Make sure our data is in order
         data_base_dir = "../data"
         figs_base_dir = "../figs"
         original_data_path = data_base_dir + "/original/formula/"
         processed_data_path = data_base_dir + "/processed/formula/"
         pickle data path = data base dir + "/pickle/formula/"
         assert os.path.exists(original_data_path), "Original data path does not exist."
In [42]: import re
         def atoi(text):
             return int(text) if text.isdigit() else text
         def natural_keys(text):
             alist.sort(key=natural_keys) sorts in human order
             http://nedbatchelder.com/blog/200712/human_sorting.html
             (See Toothy's implementation in the comments)
             return [ atoi(c) for c in re.split(r'(\d+)', text) ]
In [67]: training_images = glob.glob(f"{processed_data_path}/images/train/*.png")
         training_images.sort(key=natural_keys)
         validation_images = glob.glob(f"{processed_data_path}/images/validate/*.png")
         validation_images.sort(key=natural_keys)
         test_images = glob.glob(f"{processed_data_path}/images/test/*.png")
         test_images.sort(key=natural_keys)
         print(f"Found {len(training_images)} training images.")
         print(f"Found {len(validation_images)} validation images.")
         print(f"Found {len(test_images)} test images.")
Found 17 training images.
Found 17 validation images.
```

```
Found 17 test images.
```

```
In [44]: import pandas as pd
         import numpy as np
         def load_labels(labels_path, matches_path):
             with open(labels_path) as f:
                 labels = np.array(f.read().splitlines())
            matches = pd.read_csv(matches_path, sep=' ', header=None).values
             return labels[[list(map(lambda f: f[1], matches))][0]]
         train_labels_path = f"{original_data_path}train.formulas.norm.txt"
         train_matches_path = f"{processed_data_path}images/train/train.matching.txt"
         train labels = load labels(train labels path, train matches path)
         print(f"Got {len(train_labels)} training labels.")
         validate_labels_path = f"{original_data_path}val.formulas.norm.txt"
         validate_matches_path = f"{processed_data_path}images/validate/val.matching.txt"
         validate_labels = load_labels(validate_labels_path, validate_matches_path)
         print(f"Got {len(validate_labels)} validation labels.")
Got 17 training labels.
Got 17 validation labels.
```

The vocabulary class encapsulates the vocabulary (in other words, all possible tokens). It also has methods for tokenizing, padding, and performing a reverse lookup.

```
In [45]: class Vocab(object):
             def __init__(self, vocab_path):
                 self.build_vocab(vocab_path)
             def build_vocab(self, vocab_path):
                Builds the complete vocabulary, including special tokens
                 111
                 self.unk = "<UNK>"
                 self.start = "<SOS>"
                 self.end = "<END>"
                 self.pad = "<PAD>"
                 # First, load our vocab from disk & determine
                 # highest index in mapping.
                 vocab = self.load_vocab(vocab_path)
                 max_index = max(vocab.values())
                 # Compile special token mapping
                 special_tokens = {
```

```
self.unk : max_index + 1,
            self.start : max_index + 2,
            self.end : max_index + 3,
            self.pad : max_index + 4
        }
        # Merge dicts to produce final word index
        self.token_index = {**vocab, **special_tokens}
        self.reverse_index = {v: k for k, v in self.token_index.items()}
    def load_vocab(self, vocab_path):
        Load vocabulary from file
        token_index = {}
        with open(vocab_path) as f:
            for idx, token in enumerate(f):
                token = token.strip()
                token_index[token] = idx
        assert len(token_index) > 0, "Could not build word index"
        return token_index
    def tokenize_formula(self, formula):
        Converts a formula into a sequence of tokens using the vocabulary
        def lookup_token(token):
            return self.token_index[token] if token in self.token_index else self.token
        tokens = formula.strip().split(' ')
        return list(map(lambda f: lookup_token(f), tokens))
    def pad_formula(self, formula, max_length):
        Pads a formula to max_length with pad_token, appending end_token.
        # Extra space for the end token
        padded_formula = self.token_index[self.pad] * np.ones(max_length + 1)
        padded_formula[len(formula)] = self.token_index[self.end]
        padded_formula[:len(formula)] = formula
        return padded_formula
    @property
    def length(self):
        return len(self.token_index)
vocab = Vocab(f"{processed_data_path}/vocab.txt")
```

1.0.1 Hyperparameters

While a full hyperparameter search was not performed, the below hyperparameters seemed to get reasonable results.

```
In [46]: buffer_size = 1000
    batch_size = 16
    embedding_dim = 256
    vocab_size = vocab.length
    hidden_units = 256
    num_datapoints = 35000
    num_training_steps = num_datapoints // batch_size
    num_validation_datapoints = 8474
    num_validation_steps = num_validation_datapoints // batch_size
    epochs = 50
    train_new_model = False
    max_image_size=(80,400)
    max_formula_length = 150
```

1.0.2 Loading the data

Tensorflow provides the tf.data.Dataset API for doing ETL – loading, transforming and streaming your data to the appropriate compute device. Originally, our implementation used regular numpy based processing, but that had some limitations: - No parallel processing – bound by the performance of a single thread - No streaming operations – all data must be put into memory

Using the tf.data.Dataset API had it's own limitations; mainly that it was somewhat tricky to rewrite the operations to be nodes in the Tensorflow graph.

Note that this API also allows you to distribute your data easily to multiple GPUs or TPUs - a fact that will come in handy once we start training the model.

```
In [47]: # This hash table is used to perform token lookups in the vocab
         table = tf.lookup.StaticHashTable(
             initializer=tf.lookup.KeyValueTensorInitializer(
                 keys=tf.constant(list(vocab.token index.keys())),
                 values=tf.constant(list(vocab.token_index.values())),
             default_value=tf.constant(vocab.token_index[vocab.unk]),
             name="class_weight"
         )
         def load_and_decode_img(path):
             ''' Load the image and decode from png'''
             image = tf.io.read_file(path)
             image = tf.image.decode_png(image)
             return tf.image.rgb_to_grayscale(image)
         0tf.function
         def lookup_token(token):
             ''' Lookup the given token in the vocab'''
```

```
table.lookup(token)
            return table.lookup(token)
        def process_label(label):
            ''' Split to tokens, lookup & append <END> token'''
            tokens = tf.strings.split(label, " ")
            tokens = tf.map_fn(lookup_token, tokens, dtype=tf.int32)
            return tf.concat([tokens, [vocab.token_index[vocab.end]]], 0)
        def process_datum(path, label):
            return load_and_decode_img(path), process_label(label)
        # Tokenize formulas
        train_dataset = tf.data.Dataset.from_tensor_slices((training_images, train_labels)).me
        validation_dataset = tf.data.Dataset.from_tensor_slices((validation_images, validate_
  "Visualize" what data we have before filtering:
In [48]: # Print some values from the dataset (pre-filter)
        for datum in train_dataset.take(5):
            print(datum[1])
            print("\n")
tf.Tensor(
3 1 3 3 3 2 2 2 3 3 3 5], shape=(49,), dtype=int32)
tf.Tensor([3 3 3 3 3 3 3 1 3 2 1 3 3 3 1 3 2 2 3 3 1 3 2 3 1 3 2 1 3 3 3 1 3 2 2 3 5], shape=(
tf.Tensor([3 3 1 3 2 3 3 3 3 3 3 3 3 3 3 5], shape=(18,), dtype=int32)
tf.Tensor([3 3 3 1 3 2 3 3 1 3 2 3 3 1 0 2 3 1 3 3 2 3 5], shape=(25,), dtype=int32)
tf.Tensor(
[1\ 3\ 1\ 3\ 3\ 2\ 1\ 3\ 3\ 2\ 2\ 3\ 3\ 1\ 3\ 1\ 3\ 3\ 2\ 1\ 3\ 3\ 1\ 3\ 2\ 2\ 3\ 1\ 0\ 2\ 2\ 2\ 3\ 3
5], shape=(38,), dtype=int32)
```

We want to exclude large images because they will make the training process slower, as well as long formulas. Due to the vanishing gradient problem, long formulas will likely not be predicted very well.

```
label_length = tf.shape(label)
              image_size = tf.shape(image)
              # Does this image meet our size constraint?
             keep_image = tf.math.reduce_all(
                  tf.math.greater_equal(max_image_size, image_size[:2])
             # Does this image meet our formula length constraint?
             keep_label = tf.math.reduce_all(
                  tf.math.greater_equal(max_formula_length, label_length[0])
             return tf.math.logical_and(keep_image, keep_label)
         train_dataset = train_dataset.filter(filter_by_size).take(num_datapoints)
         validation_dataset = validation_dataset.filter(filter_by_size).take(num_validation_dataset)
In [50]: for datum in train_dataset.take(5):
             print(datum[1])
             print("\n")
tf.Tensor(
[3\ 3\ 1\ 3\ 2\ 3\ 3\ 3\ 3\ 3\ 1\ 3\ 3\ 3\ 2\ 3\ 1\ 3\ 2\ 3\ 3\ 1\ 3\ 2\ 3\ 3\ 3\ 1\ 3\ 1\ 3\ 1\ 3\ 2\ 1\ 3
3 1 3 3 3 2 2 2 3 3 3 5], shape=(49,), dtype=int32)
tf.Tensor([3 3 3 3 3 3 1 3 2 1 3 3 3 1 3 2 2 3 3 1 3 2 2 3 3 1 3 2 1 3 3 3 1 3 2 2 3 5], shape=(
tf.Tensor([3 3 1 3 2 3 3 3 3 3 3 3 3 3 3 5], shape=(18,), dtype=int32)
tf.Tensor([3 3 3 1 3 2 3 3 1 3 2 3 3 1 0 2 3 1 3 3 2 3 5], shape=(25,), dtype=int32)
tf.Tensor(
[1\ 3\ 1\ 3\ 3\ 2\ 1\ 3\ 3\ 2\ 2\ 3\ 3\ 1\ 3\ 1\ 3\ 3\ 2\ 1\ 3\ 3\ 1\ 3\ 2\ 2\ 3\ 1\ 0\ 2\ 2\ 2\ 3\ 3
5], shape=(38,), dtype=int32)
```

Leverage the power of the tf.data.Dataset API to shuffle, batch, pad and cache, all in just a few lines of python code!

```
train_dataset = train_dataset.shuffle(buffer_size).padded_batch(
             batch_size,
             padded_shapes=shapes,
             padding_values=values,
             drop_remainder=True
         train_dataset = train_dataset.prefetch(buffer_size=tf.data.experimental.AUTOTUNE).cac
         validation_dataset = validation_dataset.shuffle(buffer_size).padded_batch(
             batch_size,
             padded_shapes=shapes,
             padding_values=values,
             drop_remainder=True
         )
         # Prefetch and cache for performance
         validation_dataset = validation_dataset.prefetch(buffer_size=tf.data.experimental.AUT)
In [52]: import random
         import textwrap
         import matplotlib.pyplot as plt
         def plot_example(example):
             ''' Plot a single example'''
             if example is None:
                 return
             image_tensor, label = example
             label = "".join([vocab.reverse_index[token.numpy()] for token in label])
             label = label.replace("<PAD>","")
             fig = plt.figure(figsize=(20,20))
             plt.imshow(image_tensor[:,:,0], cmap='gray')
             plt.title(textwrap.wrap(label,100))
             plt.show()
         # Plot a few image from a random batch
         for img_tensor, labels in train_dataset.take(5):
             if len(img_tensor.shape) == 4:
                 image = img_tensor[0, :, :, :]
                 label = labels[0]
                 plot_example((image, label))
             else:
                 plot_example((img_tensor, labels))
```



1.0.3 Model definition

Below are the components of the network: - The timing signal function – adds sinusoids to the features so that our flattening operations doesn't mean we lose a sense of order - Bahdanau attenntion - The encoder (from the last notebook) - The decoder (using the timing signal function and the attention layer)

```
In [53]: from __future__ import division
    import math
    import numpy as np
    from six.moves import xrange
    import tensorflow as tf
```

taken from https://github.com/tensorflow/tensor2tensor/blob/37465a1759e278e8f073cd0.
def add_timing_signal_nd(x, min_timescale=1.0, max_timescale=1.0e4):
 """Adds a bunch of sinusoids of different frequencies to a Tensor.

Each channel of the input Tensor is incremented by a sinusoid of a difft frequency and phase in one of the positional dimensions.

This allows attention to learn to use absolute and relative positions. Timing signals should be added to some precursors of both the query and the memory inputs to attention.

The use of relative position is possible because sin(a+b) and cos(a+b) can be expressed in terms of b, sin(a) and cos(a).

x is a Tensor with n "positional" dimensions, e.g. one dimension for a sequence or two dimensions for an image

We use a geometric sequence of timescales starting with $min_timescale$ and ending with $max_timescale$. The number of different timescales is equal to channels // (n * 2). For each timescale, we generate the two sinusoidal signals sin(timestep/timescale) and cos(timestep/timescale). All of these sinusoids are concatenated in the channels dimension.

Args:

```
min_timescale: a float
                 max_timescale: a float
             Returns:
                 a Tensor the same shape as x.
             static_shape = x.get_shape().as_list()
             num_dims = len(static_shape) - 2
             channels = tf.shape(x)[-1]
             num_timescales = channels // (num_dims * 2)
             log_timescale_increment = (
                     math.log(float(max_timescale) / float(min_timescale)) /
                     (tf.cast(num_timescales, tf.float32) - 1))
             inv_timescales = min_timescale * tf.exp(
                     tf.cast(tf.range(num_timescales), tf.float32) * -log_timescale_increment)
             for dim in xrange(num_dims):
                 length = tf.shape(x)[dim + 1]
                 position = tf.cast(tf.range(length), tf.float32)
                 scaled_time = tf.expand_dims(position, 1) * tf.expand_dims(
                         inv timescales, 0)
                 signal = tf.concat([tf.sin(scaled_time), tf.cos(scaled_time)], axis=1)
                 prepad = dim * 2 * num_timescales
                 postpad = channels - (dim + 1) * 2 * num_timescales
                 signal = tf.pad(signal, [[0, 0], [prepad, postpad]])
                 for _ in xrange(1 + dim):
                     signal = tf.expand_dims(signal, 0)
                 for _ in xrange(num_dims - 1 - dim):
                     signal = tf.expand_dims(signal, -2)
                 x += signal
             return x
In [54]: from tensorflow.keras import metrics, layers, Model
         class BahdanauAttention(layers.Layer):
             def __init__(self, units):
                 super(BahdanauAttention, self).__init__()
                 self.W1 = tf.keras.layers.Dense(units)
                 self.W2 = tf.keras.layers.Dense(units)
                 self.V = tf.keras.layers.Dense(1)
             def call(self, features, hidden):
                 # First, flatten the image
                 shape = tf.shape(features)
                 if len(shape) == 4:
                     batch_size = shape[0]
                     img_height = shape[1]
```

x: a Tensor with shape [batch, d1 ... dn, channels]

```
img_width = shape[2]
                     channels = shape[3]
                     features = tf.reshape(features, shape=(batch_size, img_height*img_width,
                 else:
                     print(f"Image shape not supported: {shape}.")
                     raise NotImplementedError
                 # features(CNN_encoder_output)
                 # shape => (batch_size, flattened_image_size, embedding_size)
                 # hidden shape == (batch_size, hidden_size)
                 # hidden_with_time_axis shape == (batch_size, 1, hidden_size)
                 hidden_with_time_axis = tf.expand_dims(hidden, 1)
                 # score
                 # shape => (batch_size, flattened_image_size, hidden_size)
                 score = tf.nn.tanh(self.W1(features) + self.W2(hidden_with_time_axis))
                 # attention_weights
                 # shape => (batch_size, flattened_image_size, 1)
                 attention_weights = tf.nn.softmax(self.V(score), axis=1)
                 # context_vector
                 # shape after sum => (batch_size, hidden_size)
                 context_vector = attention_weights * features
                 context_vector = tf.reduce_sum(context_vector, axis=1)
                 return context_vector, attention_weights
In [55]: class CNNEncoder(tf.keras.Model):
             def __init__(self, embedding_dim):
                 super(CNNEncoder, self).__init__()
                 self.fc = tf.keras.layers.Dense(embedding_dim)
             def build(self, input_shape):
                 self.cnn_1 = layers.Conv2D(64, (3, 3), activation='relu', input_shape=(input_shape=)
                 self.max_pool_1 = layers.MaxPooling2D((2, 2))
                 self.cnn_2 = layers.Conv2D(256, (3, 3), activation='relu')
                 self.max_pool_2 = layers.MaxPooling2D((2, 2))
                 self.cnn_3 = layers.Conv2D(512, (3, 3), activation='relu')
             def call(self, images):
                 images = tf.cast(images, tf.float32)
                 x = self.cnn_1(images)
                 x = self.max_pool_1(x)
```

```
x = self.cnn_2(x)
                 x = self.max_pool_2(x)
                 x = self.cnn_3(x)
                 return add_timing_signal_nd(x)
In [56]: class RNNDecoder(tf.keras.Model):
             def __init__(self, embedding_dim, units, vocab_size):
                 super(RNNDecoder, self).__init__()
                 self.units = units
                 self.embedding = tf.keras.layers.Embedding(vocab_size, embedding_dim)
                 self.gru = tf.keras.layers.GRU(self.units,
                                                return_sequences=True,
                                                return_state=True,
                                                recurrent_initializer='glorot_uniform')
                 self.fc1 = tf.keras.layers.Dense(self.units)
                 self.fc2 = tf.keras.layers.Dense(vocab size)
                 self.attention = BahdanauAttention(self.units)
             def call(self, x, features, hidden):
                 # attend over the image features
                 context_vector, attention_weights = self.attention(features, hidden)
                 # convert our input vector to an embedding
                 x = self.embedding(x)
                 # concat the embedding and the context vector (from attention)
                 x = tf.concat([tf.expand_dims(context_vector, 1), x], axis=-1)
                 # pass to GRU
                 output, state = self.gru(x)
                 x = self.fc1(output)
                 x = tf.reshape(x, (-1, x.shape[2]))
                 # This produces a distribution over the vocab
                 x = self.fc2(x)
                 return x, state, attention_weights
             def reset_state(self, batch_size):
                 return tf.zeros((batch_size, self.units))
In [57]: encoder = CNNEncoder(embedding_dim=embedding_dim)
         decoder = RNNDecoder(embedding_dim, hidden_units, vocab_size)
```

1.0.4 Loss function

Define a loss function for our model: Sparse categorical cross-entropy is appropriate here since we're making multi-class predictions using integer labels.

```
In [58]: optimizer = tf.keras.optimizers.Adam(learning_rate=0.0001)
    loss_object = tf.keras.losses.SparseCategoricalCrossentropy(from_logits=True, reduction)

def loss_function(real, pred):
    # In order to avoid <PAD> tokens contributing to the loss, we mask those tokens.
    # First, we create the mask, and compute the loss.
    mask = tf.math.logical_not(tf.math.equal(real, vocab.token_index[vocab.pad]))
    loss_ = loss_object(real, pred)

# Second, we multiply the computed loss by the mask to zero out contributions from mask = tf.cast(mask, dtype=loss_.dtype)
    loss_ *= mask
    return tf.reduce_mean(loss_)
```

Checkpoints allow us to save state during training – a real boon since training will take quite a while.

1.0.5 Training

Finally, we define a custom training and validation loop for our model. This is heavily inspired by the Tensorflow example linked at the top the notebook. Notable is the use of teacher forcing (described nit he code comment below).

```
In [73]: train_epoch_losses = []
     validation_epoch_losses = []
```

Did not restore from a checkpoint -- training new model!

```
In [61]: Otf.function
         def train_step(img_tensor, target):
             ''' Function that encapsulates training logic'''
             loss = 0
             # reset the decoder state, since Latex is different for each image
             hidden = decoder.reset state(batch size=target.shape[0])
             # shape => (batch size, 1)
             dec_input = tf.expand_dims([vocab.token_index[vocab.start]] * batch_size, 1)
             sequence_length = target.shape[1]
             with tf.GradientTape() as tape:
                 features = encoder(img_tensor)
                 for i in range(0, sequence_length):
                     # passing the features through the decoder
                     predictions, hidden, _ = decoder(dec_input, features, hidden)
                     ground_truth_token = target[:, i]
                     loss += loss_function(ground_truth_token, predictions)
                     # Teacher forcing: feed the correct word in as the next input to the
                     # encoder, to provide the decoder with the proper context to predict
                     # the following token in the sequence
                     dec_input = tf.expand_dims(ground_truth_token, 1)
             total_loss = (loss / int(sequence_length))
             trainable_variables = encoder.trainable_variables + decoder.trainable_variables
             gradients = tape.gradient(loss, trainable_variables)
             optimizer.apply_gradients(zip(gradients, trainable_variables))
             return loss, total_loss
In [62]: Otf.function
         def validate_step(img_tensor, target):
             ''' Function that encapsulates training logic'''
             loss = 0
             # reset the decoder state, since Latex is different for each image
             hidden = decoder.reset_state(batch_size=target.shape[0])
             # shape => (batch_size, 1)
             dec input = tf.expand dims([vocab.token index[vocab.start]] * batch size, 1)
             sequence_length = target.shape[1]
             features = encoder(img_tensor)
             for i in range(0, sequence_length):
                 # passing the features through the decoder
                 predictions, hidden, _ = decoder(dec_input, features, hidden)
```

```
ground_truth_token = target[:, i]
                 loss += loss_function(ground_truth_token, predictions)
                 dec_input = tf.expand_dims(ground_truth_token, 1)
             total_loss = (loss / int(sequence_length))
             return loss, total_loss
In [74]: import time
         import datetime
         print(f"[Started training at: {datetime.datetime.now()}. Training for {epochs} epochs
         print(f"[Starting epoch: {start_epoch}]")
         for epoch in range(start_epoch, epochs):
             start = time.time()
             train_loss = 0
             validation_loss = 0
             # Training loop
             train_batches = 0
             for (batch, (img_tensor, target)) in enumerate(train_dataset):
                 batch_loss, sequence_loss = train_step(img_tensor, target)
                 train_loss += sequence_loss
                 train_batches = batch
                 if batch % 50 == 0:
                     print(f"[Epoch: {epoch + 1} | Batch: {batch} | Loss: {sequence_loss:.4f}]
             # Print training loss before starting validation loop
             print(f"[Epoch: {epoch + 1} | Training loss: {train_loss / (train_batches + 1)}]"
             # Validation loop
             validation_batches = 0
             for (batch, (img_tensor, target)) in enumerate(validation_dataset):
                 batch_loss, sequence_loss = validate_step(img_tensor, target)
                 validation_loss += sequence_loss
                 validation_batches = batch
             print(f"[Epoch: {epoch + 1} | Validation loss: {validation_loss / (validation_bat
             # Save epoch losses
             train_epoch_losses.append(train_loss / (train_batches + 1))
             validation_epoch_losses.append(validation_loss / (validation_batches + 1))
             # Save checkpoint (if required)
             if epoch % save_at_epoch == 0:
                 checkpoint_manager.save()
             print(f"[Time elapsed for epoch: {format(time.time() - start)} seconds.] \n")
```

```
[Started training at: 2019-08-04 16:30:50.073180. Training for 50 epochs.]
[Starting epoch: 0]
[Epoch: 1 | Batch: 0 | Loss: 0.4328]
[Epoch: 1 | Training loss: 0.43280482292175293]
[Epoch: 1 | Validation loss: 0.3729066848754883]
[Time elapsed for epoch: 6.088000059127808 seconds.]
[Epoch: 2 | Batch: 0 | Loss: 0.4337]
[Epoch: 2 | Training loss: 0.433720201253891]
[Epoch: 2 | Validation loss: 0.37391233444213867]
[Time elapsed for epoch: 6.141319751739502 seconds.]
[Epoch: 3 | Batch: 0 | Loss: 0.4323]
[Epoch: 3 | Training loss: 0.43230941891670227]
[Epoch: 3 | Validation loss: 0.3752366602420807]
[Time elapsed for epoch: 6.029435873031616 seconds.]
[Epoch: 4 | Batch: 0 | Loss: 0.4321]
[Epoch: 4 | Training loss: 0.4320918321609497]
[Epoch: 4 | Validation loss: 0.374604731798172]
[Time elapsed for epoch: 6.068495988845825 seconds.]
[Epoch: 5 | Batch: 0 | Loss: 0.4319]
[Epoch: 5 | Training loss: 0.4319472908973694]
[Epoch: 5 | Validation loss: 0.3743206262588501]
[Time elapsed for epoch: 5.908013105392456 seconds.]
[Epoch: 6 | Batch: 0 | Loss: 0.4318]
[Epoch: 6 | Training loss: 0.4317789375782013]
[Epoch: 6 | Validation loss: 0.37626776099205017]
[Time elapsed for epoch: 6.077317714691162 seconds.]
[Epoch: 7 | Batch: 0 | Loss: 0.4315]
[Epoch: 7 | Training loss: 0.4315233826637268]
[Epoch: 7 | Validation loss: 0.3764217495918274]
[Time elapsed for epoch: 5.957525014877319 seconds.]
[Epoch: 8 | Batch: 0 | Loss: 0.4312]
[Epoch: 8 | Training loss: 0.43122947216033936]
[Epoch: 8 | Validation loss: 0.3756418526172638]
[Time elapsed for epoch: 5.928221940994263 seconds.]
[Epoch: 9 | Batch: 0 | Loss: 0.4308]
[Epoch: 9 | Training loss: 0.43078044056892395]
[Epoch: 9 | Validation loss: 0.3763998746871948]
[Time elapsed for epoch: 6.061295747756958 seconds.]
```

[Epoch: 10 | Batch: 0 | Loss: 0.4309]

```
[Epoch: 10 | Training loss: 0.4309038519859314]
[Epoch: 10 | Validation loss: 0.37639573216438293]
[Time elapsed for epoch: 6.174771308898926 seconds.]
[Epoch: 11 | Batch: 0 | Loss: 0.4301]
[Epoch: 11 | Training loss: 0.4301297664642334]
[Epoch: 11 | Validation loss: 0.37671521306037903]
[Time elapsed for epoch: 6.158113956451416 seconds.]
[Epoch: 12 | Batch: 0 | Loss: 0.4301]
[Epoch: 12 | Training loss: 0.43014100193977356]
[Epoch: 12 | Validation loss: 0.37675824761390686]
[Time elapsed for epoch: 6.271286249160767 seconds.]
[Epoch: 13 | Batch: 0 | Loss: 0.4300]
[Epoch: 13 | Training loss: 0.42999178171157837]
[Epoch: 13 | Validation loss: 0.376176118850708]
[Time elapsed for epoch: 6.631333827972412 seconds.]
[Epoch: 14 | Batch: 0 | Loss: 0.4296]
[Epoch: 14 | Training loss: 0.4296094477176666]
[Epoch: 14 | Validation loss: 0.3766115605831146]
[Time elapsed for epoch: 6.179867267608643 seconds.]
[Epoch: 15 | Batch: 0 | Loss: 0.4298]
[Epoch: 15 | Training loss: 0.4297952353954315]
[Epoch: 15 | Validation loss: 0.3769102990627289]
[Time elapsed for epoch: 7.319034099578857 seconds.]
[Epoch: 16 | Batch: 0 | Loss: 0.4292]
[Epoch: 16 | Training loss: 0.4291546642780304]
[Epoch: 16 | Validation loss: 0.3776816129684448]
[Time elapsed for epoch: 8.729957103729248 seconds.]
[Epoch: 17 | Batch: 0 | Loss: 0.4291]
[Epoch: 17 | Training loss: 0.429097443819046]
[Epoch: 17 | Validation loss: 0.37767019867897034]
[Time elapsed for epoch: 8.920700788497925 seconds.]
[Epoch: 18 | Batch: 0 | Loss: 0.4290]
[Epoch: 18 | Training loss: 0.4289799630641937]
[Epoch: 18 | Validation loss: 0.3759458363056183]
[Time elapsed for epoch: 9.11909008026123 seconds.]
[Epoch: 19 | Batch: 0 | Loss: 0.4297]
[Epoch: 19 | Training loss: 0.42968228459358215]
[Epoch: 19 | Validation loss: 0.3839322626590729]
```

[Time elapsed for epoch: 9.045357942581177 seconds.]

```
[Epoch: 20 | Batch: 0 | Loss: 0.4345]
[Epoch: 20 | Training loss: 0.43449097871780396]
[Epoch: 20 | Validation loss: 0.37716159224510193]
[Time elapsed for epoch: 8.704407930374146 seconds.]
[Epoch: 21 | Batch: 0 | Loss: 0.4323]
[Epoch: 21 | Training loss: 0.4323433041572571]
[Epoch: 21 | Validation loss: 0.3760915696620941]
[Time elapsed for epoch: 8.484700918197632 seconds.]
[Epoch: 22 | Batch: 0 | Loss: 0.4305]
[Epoch: 22 | Training loss: 0.430453896522522]
[Epoch: 22 | Validation loss: 0.37813010811805725]
[Time elapsed for epoch: 7.396198034286499 seconds.]
[Epoch: 23 | Batch: 0 | Loss: 0.4312]
[Epoch: 23 | Training loss: 0.43124625086784363]
[Epoch: 23 | Validation loss: 0.37761902809143066]
[Time elapsed for epoch: 6.945310354232788 seconds.]
[Epoch: 24 | Batch: 0 | Loss: 0.4300]
[Epoch: 24 | Training loss: 0.4300049841403961]
[Epoch: 24 | Validation loss: 0.37535855174064636]
[Time elapsed for epoch: 7.035900354385376 seconds.]
[Epoch: 25 | Batch: 0 | Loss: 0.4305]
[Epoch: 25 | Training loss: 0.43047434091567993]
[Epoch: 25 | Validation loss: 0.3757206201553345]
[Time elapsed for epoch: 7.86501407623291 seconds.]
[Epoch: 26 | Batch: 0 | Loss: 0.4297]
[Epoch: 26 | Training loss: 0.42966702580451965]
[Epoch: 26 | Validation loss: 0.3771822154521942]
[Time elapsed for epoch: 7.487479209899902 seconds.]
[Epoch: 27 | Batch: 0 | Loss: 0.4295]
[Epoch: 27 | Training loss: 0.4295448362827301]
[Epoch: 27 | Validation loss: 0.3771308958530426]
[Time elapsed for epoch: 7.531407117843628 seconds.]
[Epoch: 28 | Batch: 0 | Loss: 0.4291]
[Epoch: 28 | Training loss: 0.42905667424201965]
[Epoch: 28 | Validation loss: 0.37456297874450684]
[Time elapsed for epoch: 7.878756761550903 seconds.]
[Epoch: 29 | Batch: 0 | Loss: 0.4294]
```

[Epoch: 29 | Training loss: 0.42941874265670776]

```
[Epoch: 29 | Validation loss: 0.37630295753479004]
[Time elapsed for epoch: 8.038648843765259 seconds.]
[Epoch: 30 | Batch: 0 | Loss: 0.4280]
[Epoch: 30 | Training loss: 0.42800599336624146]
[Epoch: 30 | Validation loss: 0.3784244954586029]
[Time elapsed for epoch: 7.902118921279907 seconds.]
[Epoch: 31 | Batch: 0 | Loss: 0.4289]
[Epoch: 31 | Training loss: 0.4289153516292572]
[Epoch: 31 | Validation loss: 0.3763226568698883]
[Time elapsed for epoch: 7.8783040046691895 seconds.]
[Epoch: 32 | Batch: 0 | Loss: 0.4276]
[Epoch: 32 | Training loss: 0.4275738000869751]
[Epoch: 32 | Validation loss: 0.37549081444740295]
[Time elapsed for epoch: 7.289207935333252 seconds.]
[Epoch: 33 | Batch: 0 | Loss: 0.4282]
[Epoch: 33 | Training loss: 0.42817196249961853]
[Epoch: 33 | Validation loss: 0.3797770142555237]
[Time elapsed for epoch: 7.223494291305542 seconds.]
[Epoch: 34 | Batch: 0 | Loss: 0.4299]
[Epoch: 34 | Training loss: 0.4299106001853943]
[Epoch: 34 | Validation loss: 0.3763534128665924]
[Time elapsed for epoch: 7.393735885620117 seconds.]
[Epoch: 35 | Batch: 0 | Loss: 0.4282]
[Epoch: 35 | Training loss: 0.4282092750072479]
[Epoch: 35 | Validation loss: 0.3770476281642914]
[Time elapsed for epoch: 7.576486110687256 seconds.]
[Epoch: 36 | Batch: 0 | Loss: 0.4295]
[Epoch: 36 | Training loss: 0.42953768372535706]
[Epoch: 36 | Validation loss: 0.3779384195804596]
[Time elapsed for epoch: 7.850259065628052 seconds.]
[Epoch: 37 | Batch: 0 | Loss: 0.4279]
[Epoch: 37 | Training loss: 0.42790350317955017]
[Epoch: 37 | Validation loss: 0.37824326753616333]
[Time elapsed for epoch: 7.939767122268677 seconds.]
[Epoch: 38 | Batch: 0 | Loss: 0.4285]
[Epoch: 38 | Training loss: 0.42851522564888]
[Epoch: 38 | Validation loss: 0.37616968154907227]
[Time elapsed for epoch: 7.516835689544678 seconds.]
```

```
[Epoch: 39 | Batch: 0 | Loss: 0.4276]
[Epoch: 39 | Training loss: 0.42755377292633057]
[Epoch: 39 | Validation loss: 0.37854263186454773]
[Time elapsed for epoch: 7.407878160476685 seconds.]
[Epoch: 40 | Batch: 0 | Loss: 0.4280]
[Epoch: 40 | Training loss: 0.42799124121665955]
[Epoch: 40 | Validation loss: 0.3787980079650879]
[Time elapsed for epoch: 7.327160120010376 seconds.]
[Epoch: 41 | Batch: 0 | Loss: 0.4273]
[Epoch: 41 | Training loss: 0.4273271858692169]
[Epoch: 41 | Validation loss: 0.37788906693458557]
[Time elapsed for epoch: 7.549849271774292 seconds.]
[Epoch: 42 | Batch: 0 | Loss: 0.4272]
[Epoch: 42 | Training loss: 0.4272112250328064]
[Epoch: 42 | Validation loss: 0.37594982981681824]
[Time elapsed for epoch: 7.200824975967407 seconds.]
[Epoch: 43 | Batch: 0 | Loss: 0.4269]
[Epoch: 43 | Training loss: 0.42693156003952026]
[Epoch: 43 | Validation loss: 0.3782337009906769]
[Time elapsed for epoch: 7.465975761413574 seconds.]
[Epoch: 44 | Batch: 0 | Loss: 0.4268]
[Epoch: 44 | Training loss: 0.426753968000412]
[Epoch: 44 | Validation loss: 0.38179242610931396]
[Time elapsed for epoch: 7.403193950653076 seconds.]
[Epoch: 45 | Batch: 0 | Loss: 0.4285]
[Epoch: 45 | Training loss: 0.42850354313850403]
[Epoch: 45 | Validation loss: 0.37620317935943604]
[Time elapsed for epoch: 7.5887370109558105 seconds.]
[Epoch: 46 | Batch: 0 | Loss: 0.4271]
[Epoch: 46 | Training loss: 0.42706650495529175]
[Epoch: 46 | Validation loss: 0.3790723383426666]
[Time elapsed for epoch: 7.768675088882446 seconds.]
[Epoch: 47 | Batch: 0 | Loss: 0.4266]
[Epoch: 47 | Training loss: 0.42657536268234253]
[Epoch: 47 | Validation loss: 0.3783749043941498]
[Time elapsed for epoch: 7.7456676959991455 seconds.]
[Epoch: 48 | Batch: 0 | Loss: 0.4257]
[Epoch: 48 | Training loss: 0.42569392919540405]
```

[Epoch: 48 | Validation loss: 0.3764776587486267]

```
[Time elapsed for epoch: 8.05068325996399 seconds.]

[Epoch: 49 | Batch: 0 | Loss: 0.4262]

[Epoch: 49 | Training loss: 0.42618921399116516]

[Epoch: 49 | Validation loss: 0.3764073848724365]

[Time elapsed for epoch: 8.146775960922241 seconds.]

[Epoch: 50 | Batch: 0 | Loss: 0.4252]

[Epoch: 50 | Training loss: 0.42520302534103394]

[Epoch: 50 | Validation loss: 0.3773685693740845]

[Time elapsed for epoch: 8.710307121276855 seconds.]
```

1.0.6 Results

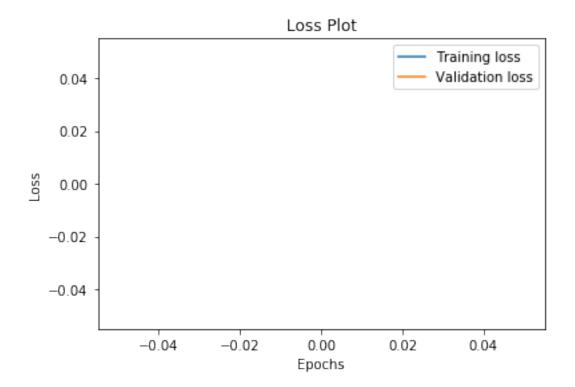
Below, we plot some examples taken from the test set, make a prediction and attempt to render the latex back into an image. Subjectively, we find that of the latex is invalid; a bracket is missing, or a character is in an invalid position. Nonetheless, when trained with enough data, the predictions often have significant overlap with the ground truth label. This is the nature of deep learning models – without a set of rules to govern the output, it all must be learned from data.

```
In [71]: validation_epoch_losses
```

```
Out[71]: [<tf.Tensor: id=430131, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=430251, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=430284, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=430317, shape=(), dtype=float32, numpy=inf>,
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          <tf.Tensor: id=430684, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=430717, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=430750, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=430783, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=430816, shape=(), dtype=float32, numpy=inf>,
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          <tf.Tensor: id=430962, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=430995, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=431028, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=431061, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=431174, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=431207, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=431240, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=431273, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=431306, shape=(), dtype=float32, numpy=inf>,
```

```
<tf.Tensor: id=431452, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=431485, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=431518, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=431551, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=431664, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=431697, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=431730, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=431763, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=431796, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=431909, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=431942, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=431975, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=432008, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=432041, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=432154, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=432187, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=432220, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=432253, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=432286, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=432399, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=432432, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=432465, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=432498, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=432531, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=432644, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=432677, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=432710, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=432743, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=432776, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=432889, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=432922, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=432955, shape=(), dtype=float32, numpy=inf>,
          <tf.Tensor: id=432988, shape=(), dtype=float32, numpy=inf>]
In [69]: import matplotlib.pyplot as plt
         plt.plot(train_epoch_losses)
         plt.plot(validation_epoch_losses)
         plt.xlabel('Epochs')
         plt.ylabel('Loss')
         plt.title('Loss Plot')
         plt.legend(["Training loss", "Validation loss"])
         plt.savefig(f"{figs_base_dir}/{datetime.datetime.now()}.png")
         plt.show()
```

<tf.Tensor: id=431419, shape=(), dtype=float32, numpy=inf>,



```
In [154]: import matplotlib.pyplot as plt
          def load_image(path):
              img_raw = tf.io.read_file(path)
              return tf.image.decode_png(img_raw)
          def plot_features(features):
              layer_count = features.shape[3]
              num rows = 16
              num_cols = int(layer_count / num_rows)
              fig, axes = plt.subplots(num_rows, num_cols, figsize=(32, 32))
              for i, ax in enumerate(axes.flat):
                  feat = features[0,:,:,i]
                  ax.imshow(feat)
                  ax.axis('off')
              plt.tight_layout()
              plt.show()
          def plot_attention(attn):
              layer_count = attn.shape[0]
```

```
num_rows = 16
   num_cols = math.floor(layer_count / num_rows)
    fig, axes = plt.subplots(num_rows, num_cols, figsize=(32, 20))
    for i, ax in enumerate(axes.flat):
        if i >= layer_count:
            break
        feat = attn[i,:,:]
        ax.imshow(feat)
        ax.axis('off')
   plt.tight_layout()
   plt.show()
def evaluate(img, max_formula_length):
    index_token_mapping = {v: k for k, v in vocab.token_index.items()}
   hidden = decoder.reset_state(batch_size=1)
    # Convert to grayscale so network can process it
    # and add a dimension at the start to simulate batch (size=1)
    image = tf.image.rgb_to_grayscale(img)
    temp_input = tf.expand_dims(image, 0)
    # Pass through encoder to obtain features
   features = encoder(temp_input)
    # Signal to the decoder that we are starting feeding in a new sequence
    decoder_input = tf.expand_dims(vocab.tokenize_formula(vocab.start), 1)
   result = []
   attention_plot = np.zeros((max_formula_length, features.shape[1], features.shape
   for i in range(max_formula_length):
        predictions, hidden, attention_weights = decoder(decoder_input, features, hid
        #attn weights: (1, feat_width * feat_height, 1)
        attention_plot[i] = tf.reshape(attention_weights, (features.shape[1], feature
        predicted_id = tf.argmax(predictions[0]).numpy()
        result.append(index_token_mapping[predicted_id])
        if index_token_mapping[predicted_id] == vocab.end:
            # Strip end token when returning
            return result[:-1], attention_plot, features
        decoder_input = tf.expand_dims([predicted_id], 0)
   return result, attention_plot, features
```

In []: import subprocess

```
def create_from_template(latex):
    '''Uses a simple template to create a valid latex document'''
    pre = """
    \documentclass[preview]{standalone}
    \\begin{document}
    \\begin{equation}
    0.000
   post = """
    \end{equation}
    \end{document}
    return pre + latex + post
def render_latex(latex):
    ''' Renders a latex string, creating a png'''
    # Write temp tex file
    latex_out_dir = f"{processed_data_path}latex/"
    temp_tex_filepath = f"{processed_data_path}latex/tmp.tex"
    temp_dvi_filepath = os.path.splitext(temp_tex_filepath)[0]+'.dvi'
    temp_png_filepath = os.path.splitext(temp_tex_filepath)[0]+'1.png'
    with open(temp_tex_filepath, 'w+') as f:
        f.seek(0)
        f.write(create_from_template(latex))
    # Render it
    cmd = ['latex', '-interaction=nonstopmode', '--halt-on-error', "-output-directory"
    output = subprocess.run(cmd, capture_output=True)
    if output.returncode != 0:
        print(f"Could not render latex (status code={output.returncode}. Output follows
        print(output.stdout)
        print(output.stderr)
        print("\n")
        return None
    render_png_cmd = ['dvipng','-D','300', "-o", temp_png_filepath, temp_dvi_filepath]
    output = subprocess.run(render_png_cmd, capture_output=True)
    if output.returncode != 0:
        print("Could not render .dvi file into .pdf! Output follows: \n")
        print(output.stdout)
        print(output.stderr)
        print("\n")
        return None
    return temp_png_filepath
```

```
def plot_image_clean(png):
            ''' plots an image without axes'''
            fig = plt.figure(figsize=(20,10))
            ax = fig.add_axes([0, 0, 1, 1])
            ax.imshow(plt.imread(out_file))
            ax.axis('off')
            plt.show()
        def process_latex(latex):
            return " ".join(latex)
        # Example params
        test_index = 5
        test_img = load_image(validation_images[test_index])
        # Make prediction
        result, attention_plot, features = evaluate(test_img, max_formula_length)
        # Plot original image
        plt.imshow(test_img)
        plt.show()
        # Render latex from the predicted formula
        latex = process_latex(result)
        out_file = render_latex(latex)
        if out_file is not None:
            plot_image_clean(out_file)
        print(f"Predicted formula: \n {result}")
        plot_attention(attention_plot)
        plot_features(features[:,:,:,0:64])
In [ ]: def search_for_valid_predictions(count, example_count, train_image_path = f"{processed
            ''' Search for predictions with latex that compiles'''
            success_count = 0
            index = 0
            success_indexes = []
            while success_count < count:</pre>
                if index >= example count:
                    return success_indexes
                # predict
                test_img = load_image(f"{train_image_path}/{index}.png")
                result, attention_plot, features = evaluate(test_img, max_formula_length)
                # attemp to render
                latex = process_latex(result)
```