

The GNFW profile gives  $P(r)$  as a shape function  $p(r)$  times a normalization  $P_{500}$  that is completely determined by  $M_{500}$ :

$$P(r) = 1.65 \times 10^{-3} h(z)^{8/3} \left[ \frac{M_{500}}{3 \times 10^{14} h_{70}^{-1} M_{\odot}} \right]^{2/3 + \alpha_P} \times p(r) h_{70}^2 \text{ keV cm}^{-3}, \quad (1)$$

For any radial model, the pressure can be integrated to give  $Y_{sph}(R)$ :

$$Y_{sph}(R) = \frac{\sigma_T}{m_e c^2} \int_0^R P(r) dV \quad (2)$$

and similarly  $M_{gas}(R)$ :

$$M_{gas}(R) = m_p \mu_e \left( \frac{m_e c^2}{k_B T_e} \right) \left( \frac{1}{\sigma_T} \right) Y_{sph}(R) \quad (3)$$

What I am doing is using the self-similarity arguments that go into determining  $P_{500}$  (and hence the normalization of  $P(r)$  above) to compute  $R_{500}$  from the input  $M_{500}$ :

$$M_{500} = 500 \rho_c(z) \frac{4\pi}{3} R_{500}^3 \quad (4)$$

and the characteristic temperature:

$$kT_{500} = \mu m_p \frac{GM_{500}}{2R_{500}} \quad (5)$$

and calculating  $M_{tot}(R_{500}) = \frac{1}{f_{gas}} M_{gas}(R_{500})$  via Eq 4.

This is what I'm comparing to the input  $M_{500}$  and determining that I have to apply that scale factor to make them agree.