

# Assignment 3, TTK4190

Shiv Jeet Rai  
Arne Selle  
Erik Liland

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# 1 Autopilot design

## 1.1 Heading autopilot

### Analysis of ship characteristics

To be able to model the ship in a good way we ran many simulations with different rudder angle and measured the steady-state yaw rate. We then made a  $\delta - r$  plot of the result. Since the ship was turning port while giving a positive rudder command, this plot the rest of the assignment is made with a fixed gain of -1 on  $\delta_c$ .

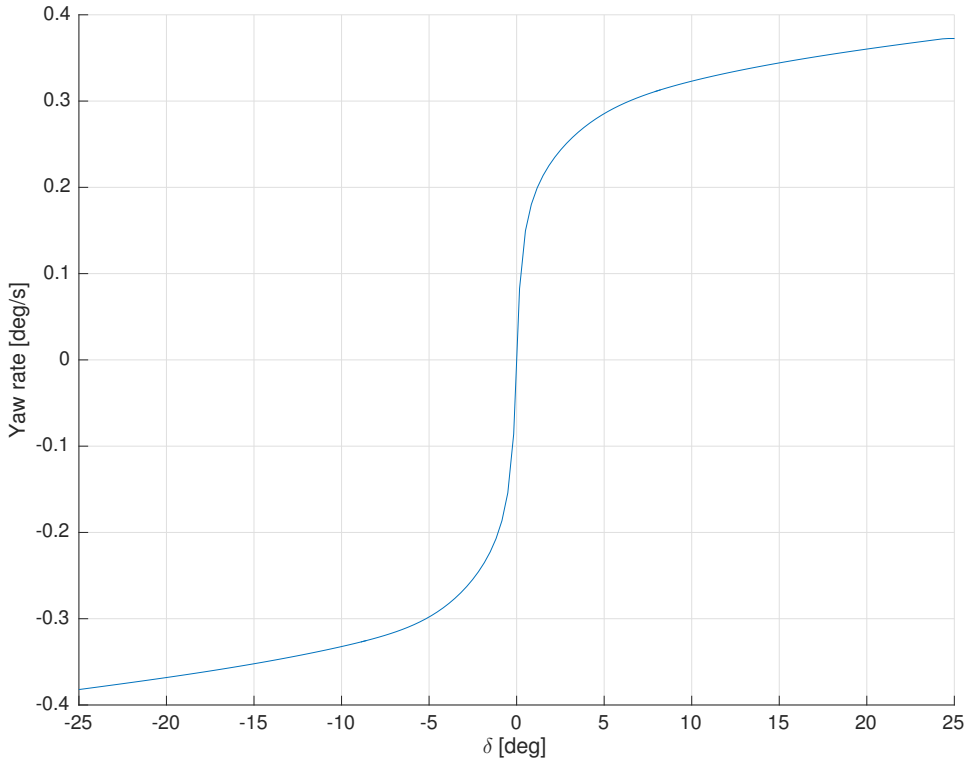


Figure 1:  $\delta - r$  plot

From figure 1 we clearly see the non-linear behavior of the ship. This motivates a 1-DOF heading model i.e. first- or second order Monoto model with non-linear extensions. To further investigate the effect of the non-linear characteristics of this ship, we compare the actual response with different models at different rudder angles. It should also be noticed that the ship has a constant drift to starboard with  $\delta_c = 0$ , as seen by the curve not passing through the origin. We compensate for this through the rest of the modeling part by adding a fixed rudder angle of  $0.52^\circ$  to the rudder input. We only need this correction while estimating the model parameters. In a closed loop, the integral effect will cancel both this

drift and drift caused by wind, current and waves.

### 1. order linear Nomoto

As expected the first order Nomoto model will only be accurate for small rudder angles, and is therefore not very good for modeling the non-linearities.

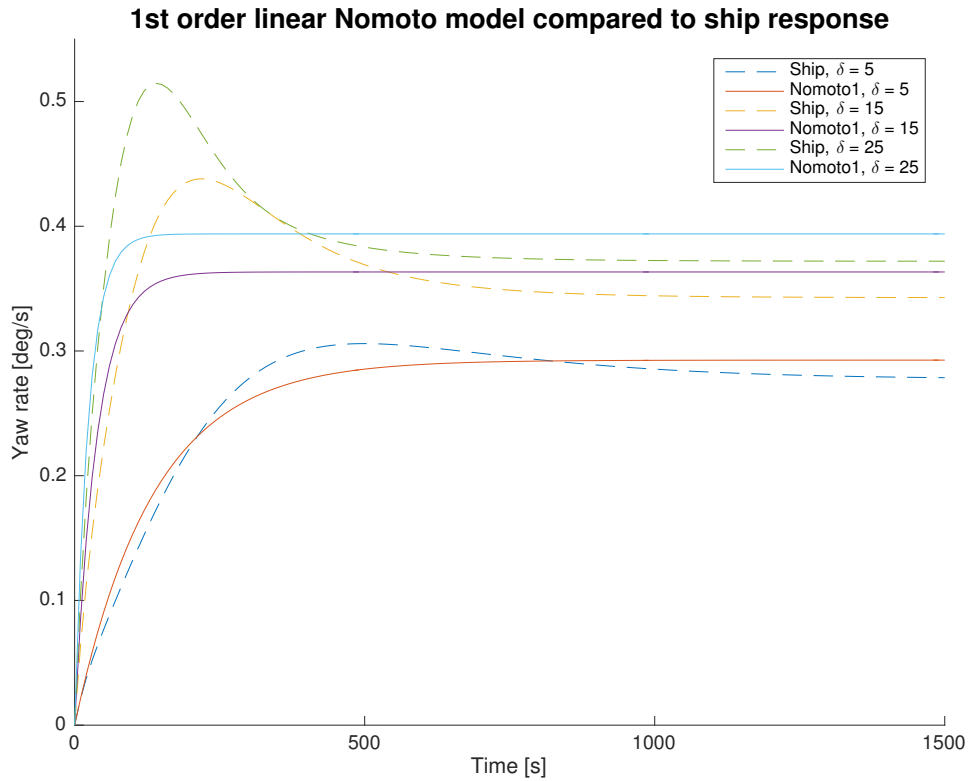


Figure 2: 1.order linear Nomoto model

### 2. order linear Nomoto

The second order Nomoto model follows the ships response much better, but...

We model the heading of MS Fartøystyring with a Norrbinn model

$$\begin{aligned} \dot{\Psi} &= r \\ T\dot{r} + n_3 r^3 + n_1 r &= K\delta \end{aligned} \tag{1}$$

### 1.2 Speed autopilot

To control the surge speed of MS Fartøystyring we suggest using a linearized model, where the surge speed is decoupled from the rest of the system. We are

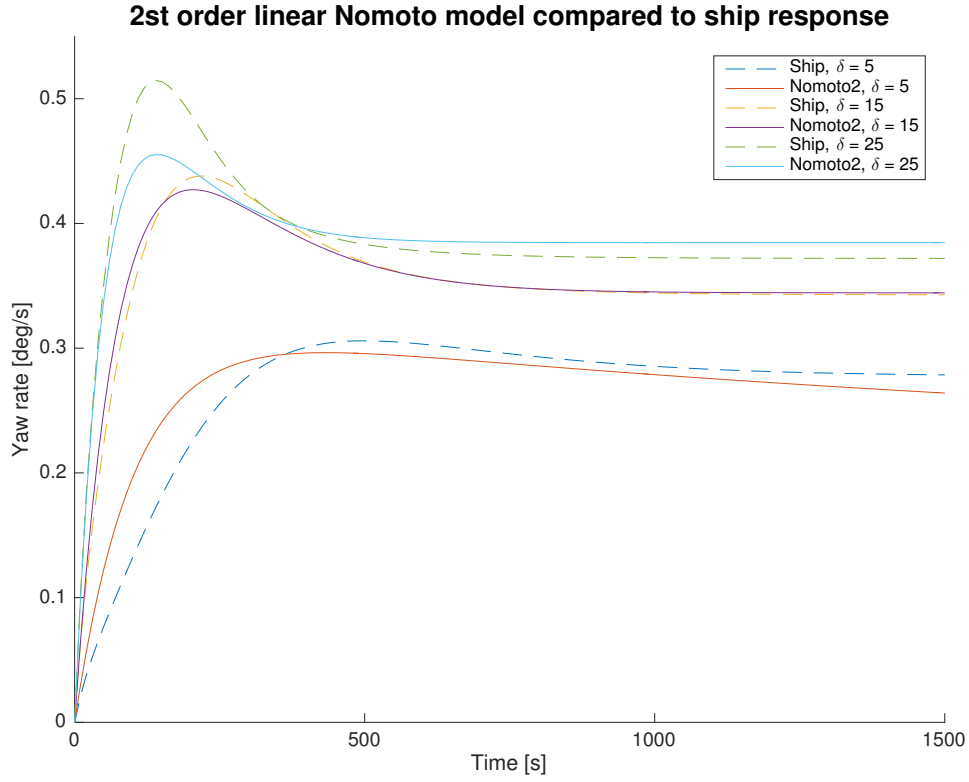


Figure 3: 2.order linear Nomoto model

assuming

$$u \gg v$$

which leads to the conclusion that

$$U = u$$

. We then use a first order linear speed model

$$(m + X_{\dot{u}})\dot{u} - X_u u_r - X_{|u|u}|u_r|u_r = \tau \quad (2)$$

which leads to

$$\dot{u} = \frac{\tau + X_{|u|u}|u_r|u_r + X_u u_r}{m - X_{\dot{u}}} = \frac{X_{|u|u}|u_r|u_r + X_u u_r}{m - X_{\dot{u}}} + \tau_{nl} \quad (3)$$

where

$$\tau_{nl} = \frac{\tau}{m - X_{\dot{u}}} \Rightarrow \tau = \tau_{nl}(m - X_{\dot{u}}) \quad (4)$$

## 2 Path following and Path tracking

### 2.1 Path Generation

Her skriver vi om Path generation

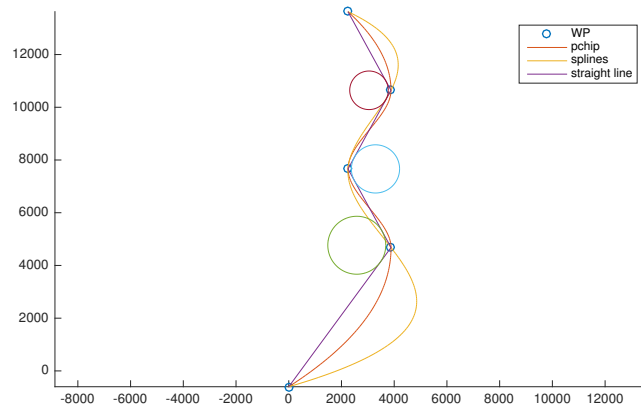


Figure 4: Different trajectories

### 2.2 Path following

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### 2.3 Path Tracking

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