4.2. SECOND ORDER 17

først har vi vores startligninger

$$\dot{\delta}^{(1)} = -\theta^{(1)} \quad \dot{\theta}^{(1)} = -\mathcal{H}\theta^{(1)} - \frac{3}{2} \frac{H_0^2 \Omega_M}{a} \delta_M^{(1)} - c_s^2 \nabla^2 \delta^{(1)}$$

$$\dot{\delta}_{\nu}^{(2)} = -2\partial_j \nabla^{-2} \theta^{(1)} \partial_j \delta^{(1)} - 2\delta^{(1)} \theta^{(1)} - \theta^{(2)}$$

$$(4.41)$$

$$\dot{\delta}_{\nu}^{(2)} = -2\partial_{i}\nabla^{-2}\theta^{(1)}\partial_{i}\delta^{(1)} - 2\delta^{(1)}\theta^{(1)} - \theta^{(2)} \tag{4.42}$$

$$\dot{\theta}^{(2)} = -\mathcal{H}\theta^{(2)} - 2\left(\partial_i\partial_j\nabla^{-2}\theta^{(1)}\partial_i\partial_j\theta^{(1)}\right) - 2\partial_j\nabla^{-2}\theta^{(1)}\partial_j\theta^{(1)}$$

$$\tag{4.43}$$

$$-\frac{3}{2}\frac{H_0^2\Omega_M}{a}\delta_M^{(2)} - c_s^2\nabla^2\delta^{(2)} \tag{4.44}$$

$$\ddot{\delta}^{(2)} = -2\partial_{j}\nabla^{-2}\theta^{(1)}\partial_{j}\delta^{(1)} - 2\partial_{j}\nabla^{-2}\dot{\theta}^{(1)}\partial_{j}\dot{\delta}^{(1)} - 2\dot{\delta}^{(1)}\theta^{(1)} - 2\delta^{(1)}\dot{\theta}^{(1)} - \dot{\theta}^{(2)}$$
(4.45)

$$\ddot{\delta}^{(2)} = -2\partial_j \nabla^{-2} \theta^{(1)} \partial_j \delta^{(1)} - 2\partial_j \nabla^{-2} \dot{\theta}^{(1)} \partial_j \dot{\delta}^{(1)} - 2\dot{\delta}^{(1)} \theta^{(1)} - 2\delta^{(1)} \dot{\theta}^{(1)}$$
 (4.46)

$$+\frac{3}{2}\frac{H_0^2\Omega_M}{a}\delta_M^{(2)} + c_s^2\nabla^2\delta^{(2)} + 2\left(\partial_i\partial_j\nabla^{-2}\theta^{(1)}\partial_i\partial_j\theta^{(1)}\right) + 2\partial_j\nabla^{-2}\theta^{(1)}\partial_j\theta^{(1)} + \mathcal{H}\theta^{(2)}$$
(4.47)

$$\ddot{\delta}^{(2)} = -2\partial_j \nabla^{-2} \theta^{(1)} \partial_j \delta^{(1)} - 2\partial_j \nabla^{-2} \dot{\theta}^{(1)} \partial_j \dot{\delta}^{(1)} - 2\dot{\delta}^{(1)} \theta^{(1)} - 2\delta^{(1)} \dot{\theta}^{(1)}$$
 (4.48)

$$+\frac{3}{2}\frac{H_0^2\Omega_M}{a}\delta_M^{(2)} + c_s^2\nabla^2\delta^{(2)} + 2\left(\partial_i\partial_j\nabla^{-2}\theta^{(1)}\partial_i\partial_j\theta^{(1)}\right) + 2\partial_j\nabla^{-2}\theta^{(1)}\partial_j\theta^{(1)}$$
(4.49)

$$+\mathcal{H}(-2\partial_{j}\nabla^{-2}\theta^{(1)}\partial_{j}\delta^{(1)} - 2\delta^{(1)}\theta^{(1)} - \dot{\delta}_{\nu}^{(2)}) \quad (4.50)$$

(4.51)

$$\ddot{\delta}^{(2)} = 2\partial_j \nabla^{-2} \delta^{(1)} \partial_j \delta^{(1)} + 2\partial_j \nabla^{-2} (\mathcal{H}\delta^{(1)} - \frac{3}{2} \frac{H_0^2 \Omega_M}{a} \delta_M^{(1)} - c_s^2 \nabla^2 \delta^{(1)})^{(1)} \partial_j \dot{\delta}^{(1)}$$
(4.52)

$$+2\dot{\delta}^{(1)}\dot{\delta}^{(1)} - 2\delta^{(1)}(\mathcal{H}\delta^{(1)} - \frac{3}{2}\frac{H_0^2\Omega_M}{a}\delta_M^{(1)} - c_s^2\nabla^2\delta^{(1)})$$
 (4.53)

$$+\frac{3}{2}\frac{H_0^2\Omega_M}{a}\delta_M^{(2)} + c_s^2\nabla^2\delta^{(2)} + 2\left(\partial_i\partial_j\nabla^{-2}\dot{\delta}^{(1)}\partial_i\partial_j\dot{\delta}^{(1)}\right) + 2\partial_j\nabla^{-2}\dot{\delta}^{(1)}\partial_j\dot{\delta}^{(1)}$$
(4.54)

$$+\mathcal{H}(2\partial_{i}\nabla^{-2}\dot{\delta}^{(1)}\partial_{i}\delta^{(1)} + 2\delta^{(1)}\dot{\delta}^{(1)} - \dot{\delta}^{(2)}) \tag{4.55}$$

bedre opskrivning

$$\ddot{\delta}^{(2)} + \mathcal{H}\dot{\delta}^{(2)} = \frac{3}{2} \frac{H_0^2}{a} \left(2\partial_j \nabla^{-2} \delta_M^{(1)} \partial_j \delta^{(1)} + 2\delta^{(1)} \delta_M^{(1)} + \delta_M^{(2)} \right) \tag{4.56}$$

$$+c_s^2 \left(2\partial_j \delta^{(1)} \partial_j \delta^{(1)} + 2\delta^{(1)} \nabla^2 \delta^{(1)} + \nabla^2 \delta^{(2)}\right)$$
 (4.57)

$$4\partial_{j}\nabla^{-2}\dot{\delta}^{(1)}\partial_{j}\dot{\delta}^{(1)} + 2\dot{\delta}^{(1)}\dot{\delta}^{(1)} + 2\partial_{i}\partial_{j}\nabla^{-2}\dot{\delta}^{(1)}\partial_{i}\partial_{j}\nabla^{-2}\dot{\delta}^{(1)}$$

$$(4.58)$$

$$\ddot{\delta}^{(2)} + \mathcal{H}\dot{\delta}^{(2)} = \frac{3}{2} \frac{H_0^2}{a} \left(2\partial_j \nabla^{-2} \delta_M^{(1)} \partial_j \delta^{(1)} + 2\delta^{(1)} \delta_M^{(1)} + \delta_M^{(2)} \right) \tag{4.59}$$

$$+4\partial_{i}\nabla^{-2}\dot{\delta}^{(1)}\partial_{i}\dot{\delta}^{(1)} + 2\dot{\delta}^{(1)}\dot{\delta}^{(1)} + 2\partial_{i}\partial_{j}\nabla^{-2}\dot{\delta}^{(1)}\partial_{i}\partial_{j}\nabla^{-2}\dot{\delta}^{(1)}$$

$$(4.60)$$

$$a = \frac{1}{4}H_0^2\tau^2 \quad \delta^{(1)} = D\tilde{\delta} \quad \delta_M = a\tilde{\delta}_M \quad \mathcal{H} = H_0/\sqrt{a} = \frac{2}{\tau}$$
 (4.61)

(4.62)

Vi indsætter og ser hvad der sker,

$$\ddot{\delta}^{(2)} + \frac{2}{\tau}\dot{\delta}^{(2)} - c_s^2\nabla^2\delta^{(2)} - \frac{6}{\tau^2}\delta_M^{(2)} = \frac{6}{\tau^2}\Big(2\partial_j\nabla^{-2}a\tilde{\delta}_M^{(1)}\partial_jD\tilde{\delta}^{(1)} + 2D\tilde{\delta}^{(1)}a\tilde{\delta}_M^{(1)}\Big) \eqno(4.63)$$

$$+4\dot{D}^2\partial_j\nabla^{-2}\tilde{\delta}^{(1)}\partial_j\tilde{\delta}^{(1)}+2\dot{D}^2\tilde{\delta}^{(1)}\tilde{\delta}^{(1)}+2\dot{D}^2\partial_i\partial_j\nabla^{-2}\tilde{\delta}^{(1)}\partial_i\partial_j\nabla^{-2}\tilde{\delta}^{(1)} \tag{4.64}$$

$$+c_s^2 \left(2\partial_j D\tilde{\delta}^{(1)}\partial_j D\tilde{\delta}^{(1)} + 2D\tilde{\delta}^{(1)}\nabla^2 D\tilde{\delta}^{(1)}\right) \tag{4.65}$$

reducere

$$\ddot{\delta}^{(2)} + \frac{2}{\tau}\dot{\delta}^{(2)} - c_s^2 \nabla^2 \delta^{(2)} - \frac{6}{\tau^2}\delta_M^{(2)} = aD\frac{6}{\tau^2} \left(2\partial_j \nabla^{-2}\tilde{\delta}_M^{(1)}\partial_j\tilde{\delta}^{(1)} + 2\tilde{\delta}^{(1)}\tilde{\delta}_M^{(1)}\right) \tag{4.66}$$

$$+4\dot{D}^{2}\left(\partial_{j}\nabla^{-2}\tilde{\delta}^{(1)}\partial_{j}\tilde{\delta}^{(1)}+2\tilde{\delta}^{(1)}\tilde{\delta}^{(1)}+2\partial_{i}\partial_{j}\nabla^{-2}\tilde{\delta}^{(1)}\partial_{i}\partial_{j}\nabla^{-2}\tilde{\delta}^{(1)}\right)$$
(4.67)

$$+c_s^2 D^2 \left(2\partial_j \tilde{\delta}^{(1)} \partial_j \tilde{\delta}^{(1)} + 2\tilde{\delta}^{(1)} \nabla^2 \tilde{\delta}^{(1)}\right) \tag{4.68}$$

$$\ddot{\delta}^{(2)} + \frac{2}{\tau}\dot{\delta}^{(2)} - c_s^2 \nabla^2 \delta^{(2)} - \frac{6}{\tau^2}\delta_M^{(2)} = D\frac{3}{2}H_0^2 \left(2\partial_j \nabla^{-2}\tilde{\delta}_M^{(1)}\partial_j\tilde{\delta}^{(1)} + 2\tilde{\delta}^{(1)}\tilde{\delta}_M^{(1)}\right) \tag{4.69}$$

$$+4\dot{D}^{2}\left(\partial_{j}\nabla^{-2}\tilde{\delta}^{(1)}\partial_{j}\tilde{\delta}^{(1)}+2\tilde{\delta}^{(1)}\tilde{\delta}^{(1)}+2\partial_{i}\partial_{j}\nabla^{-2}\tilde{\delta}^{(1)}\partial_{i}\partial_{j}\nabla^{-2}\tilde{\delta}^{(1)}\right) \tag{4.70}$$

$$+c_s^2 D^2 \Big(2\partial_j \tilde{\delta}^{(1)} \partial_j \tilde{\delta}^{(1)} + 2\tilde{\delta}^{(1)} \nabla^2 \tilde{\delta}^{(1)}\Big)$$
 (4.71)