

```
In [1]: library(boot)
library(glmnet)
```

```
Loading required package: Matrix
Loading required package: foreach
Loaded glmnet 2.0-16
```

```
In [2]: set.seed(2019)
```

```
In [3]: #TRAIN 1: ALL COVARIATES PLUS INTERACTION TERMS
train1 <- read.csv("trainC.csv")
test1 <- read.csv("testC.csv")
train1 <- subset(train1, select = -c(sessionDate, trialNum, timeSinceKetamine, animalName))
test1 <- subset(test1, select = -c(sessionDate, trialNum, timeSinceKetamine, animalName))

#TRAIN 2: ALL COVARIATES NO INTERACTION TERMS
train2 <- subset(train1, select = c(totalCellNum,gender,genotype,weight_g,ketamine_day,
correlationScore,lickAccuracy,lickNumber,avgFR,
avgSingleCellVariance,varianceFR,avgTrialSpeed,
varianceSpeed,medianCellDepth,ketBool))
test2 <- subset(test1, select = c(totalCellNum,gender,genotype,weight_g,ketamine_day,
correlationScore,lickAccuracy,lickNumber,avgFR,
avgSingleCellVariance,varianceFR,avgTrialSpeed,
varianceSpeed,medianCellDepth,ketBool))
```

Model Generation and Test Error Estimation

Basic Logistic Regression Model with Interaction Terms

```

In [4]: k = 10
n = length(train1[,1])
fsize = round(n/k)
rmse = rep(0,k)
zloss = rep(0,k)
for (i in 1:(k-1)){
  # Get train and validation sets
  df_train <- train1[-(((i-1)*fsize+1):(i*fsize)),]
  df_val <- train1[(((i-1)*fsize+1):(i*fsize)),]
  # Fit model on training and make predictions on validation
  model_cv <- glm(ketBool ~ ., data=df_train, family='binomial')
  lr_pred_lo <- predict(model_cv,df_val) # Lo : Log odds
  num_val = length(df_val$ketBool)
  lr_pred = rep(0,num_val)
  actual = rep(0,num_val)
  for (j in 1:num_val){
    if (lr_pred_lo[j]>0){
      lr_pred[j]=1
    }
    actual[j] = df_val$ketBool[j]
  }
  # Compute 0-1 Loss for each observation
  lr_loss = abs(lr_pred-actual) # loss is 0 if NB_pred=actual, 1 otherwise
  # Compute mean 0-1 loss on the val set
  zoloss[i] = mean(lr_loss)
}
df_train <- train1[-(((k-1)*fsize+1):n),]
df_val <- train1[(((k-1)*fsize+1):n),]
# Fit model on training and make predictions on validation
model_cv <- glm(ketBool ~ ., data=df_train, family='binomial')
lr_pred_lo <- predict(model_cv,df_val) # Lo : Log odds
num_val = length(df_val$ketBool)
lr_pred = rep(0,num_val)
actual = rep(0,num_val)
for (j in 1:num_val){
  if (lr_pred_lo[j]>0){
    lr_pred[j]=1
  }
  actual[j] = df_val$ketBool[j]
}
lr_loss = abs(lr_pred-actual)
zoloss[k] = mean(lr_loss)
test_error_est = mean(zoloss)

cat("=====\n")
cat("Logistic Regression Model with Interaction Terms\n\n")
cat("Zero-One Loss (10-fold Cross-Validation Average):",test_error_est,"\n")
cat("Accuracy (10-fold Cross-Validation Average):",1-test_error_est,"\n")
cat("=====\n")

# Train now on entire training set to get model for prediction
model1 <- glm(ketBool ~ ., data=train1, family='binomial')

```

```

=====
Logistic Regression Model with Interaction Terms

Zero-One Loss (10-fold Cross-Validation Average): 0.09182746
Accuracy (10-fold Cross-Validation Average): 0.9081725
=====

```

Basic Logistic Regression without Interaction Terms

```

In [5]: k = 10
n = length(train2[,1])
fsize = round(n/k)
rmse = rep(0,k)
zoloss = rep(0,k)
for (i in 1:(k-1)){
  # Get train and validation sets
  df_train <- train2[-(((i-1)*fsize+1):(i*fsize)),]
  df_val <- train2[(((i-1)*fsize+1):(i*fsize)),]
  # Fit model on training and make predictions on validation
  model_cv <- glm(ketBool ~ ., data=df_train, family='binomial')
  lr_pred_lo <- predict(model_cv,df_val) # Lo : Log odds
  num_val = length(df_val$ketBool)
  lr_pred = rep(0,num_val)
  actual = rep(0,num_val)
  for (j in 1:num_val){
    if (lr_pred_lo[j]>0){
      lr_pred[j]=1
    }
    actual[j] = df_val$ketBool[j]
  }
  # Compute 0-1 Loss for each observation
  lr_loss = abs(lr_pred-actual) # loss is 0 if NB_pred=actual, 1 otherwise
  # Compute mean 0-1 loss on the val set
  zoloss[i] = mean(lr_loss)
}
df_train <- train2[-(((k-1)*fsize+1):n),]
df_val <- train2[(((k-1)*fsize+1):n),]
# Fit model on training and make predictions on validation
model_cv <- glm(ketBool ~ ., data=df_train, family='binomial')
lr_pred_lo <- predict(model_cv,df_val) # Lo : Log odds
num_val = length(df_val$ketBool)
lr_pred = rep(0,num_val)
actual = rep(0,num_val)
for (j in 1:num_val){
  if (lr_pred_lo[j]>0){
    lr_pred[j]=1
  }
  actual[j] = df_val$ketBool[j]
}
lr_loss = abs(lr_pred-actual)
zoloss[k] = mean(lr_loss)
test_error_est = mean(zoloss)

cat("=====\n")
cat("Logistic Regression Model without Interaction Terms\n\n")
cat("Zero-One Loss (10-fold Cross-Validation Average):",test_error_est,"\n")
cat("Accuracy (10-fold Cross-Validation Average):",1-test_error_est,"\n")
cat("=====\n")

# Train now on entire training set to get model for prediction
model2 <- glm(ketBool ~ ., data=train2, family='binomial')

```

```

=====
Logistic Regression Model without Interaction Terms

Zero-One Loss (10-fold Cross-Validation Average): 0.1413709
Accuracy (10-fold Cross-Validation Average): 0.8586291
=====

```

Look at Coefficients on TRAIN

Model 1 (including interaction terms) Summary

```
In [6]: summary(model1)
```

```
Call:
glm(formula = ketBool ~ ., family = "binomial", data = train1)
```

Deviance Residuals:

Min	1Q	Median	3Q	Max
-2.9532	-0.2677	0.0100	0.2355	5.0333

Coefficients:

	Estimate	Std. Error	z value	Pr(> z)	
(Intercept)	-3.07543	0.84032	-3.660	0.000252	***
totalCellNum	1.48468	0.36237	4.097	4.18e-05	***
gender	5.27077	0.80163	6.575	4.86e-11	***
genotype	4.70327	0.73513	6.398	1.58e-10	***
weight_g	0.12584	0.35738	0.352	0.724760	
ketamine_day	-0.71834	0.25786	-2.786	0.005340	**
correlationScore	-2.30386	0.96069	-2.398	0.016479	*
lickAccuracy	-2.59838	0.62801	-4.137	3.51e-05	***
lickNumber	-0.51051	0.76272	-0.669	0.503289	
avgFR	4.72545	1.78614	2.646	0.008154	**
avgSingleCellVariance	7.85496	2.25356	3.486	0.000491	***
varianceFR	1.58919	1.02274	1.554	0.120216	
avgTrialSpeed	-0.91611	0.73195	-1.252	0.210715	
varianceSpeed	1.67179	1.06811	1.565	0.117539	
medianCellDepth	1.26773	0.30867	4.107	4.01e-05	***
totalCellNumxCorrelationScore	-2.45892	0.29758	-8.263	< 2e-16	***
totalCellNumxLickAccuracy	0.24686	0.16550	1.492	0.135803	
totalCellNumxLickNumber	0.08498	0.19849	0.428	0.668571	
totalCellNumxAvgFR	1.43740	0.56874	2.527	0.011493	*
totalCellNumxAvgSingleCellVariance	-0.67645	0.40254	-1.680	0.092871	.
totalCellNumxVarianceFR	-0.86265	0.16684	-5.171	2.33e-07	***
totalCellNumxAvgTrialSpeed	-0.94312	0.24154	-3.905	9.44e-05	***
totalCellNumxVarianceSpeed	0.75321	0.28168	2.674	0.007495	**
genderxCorrelationScore	-0.08490	0.24236	-0.350	0.726094	
genderxLickAccuracy	0.28144	0.12668	2.222	0.026304	*
genderxLickNumber	-0.14458	0.10581	-1.366	0.171828	
genderxAvgFR	-2.35801	0.80157	-2.942	0.003264	**
genderxAvgSingleCellVariance	0.54791	0.54906	0.998	0.318326	
genderxVarianceFR	0.08090	0.30108	0.269	0.788160	
genderxAvgTrialSpeed	-1.05481	0.29317	-3.598	0.000321	***
genderxVarianceSpeed	-1.15447	0.38986	-2.961	0.003064	**
genotypexCorrelationScore	-0.33733	0.22293	-1.513	0.130233	
genotypexLickAccuracy	0.56838	0.16717	3.400	0.000674	***
genotypexLickNumber	-0.52894	0.14448	-3.661	0.000251	***
genotypexAvgFR	0.92673	0.72838	1.272	0.203262	
genotypexAvgSingleCellVariance	-5.99671	0.85149	-7.043	1.89e-12	***
genotypexVarianceFR	-0.22840	0.33708	-0.678	0.498033	
genotypexAvgTrialSpeed	-0.49684	0.32787	-1.515	0.129686	
genotypexVarianceSpeed	-0.61546	0.44262	-1.391	0.164377	
weight_gxCorrelationScore	3.16988	0.79975	3.964	7.38e-05	***
weight_gxLickAccuracy	0.94502	0.50304	1.879	0.060297	.
weight_gxLickNumber	0.04100	0.56794	0.072	0.942451	
weight_gxAvgFR	-1.81136	1.68183	-1.077	0.281473	
weight_gxAvgSingleCellVariance	-1.28619	1.45427	-0.884	0.376470	
weight_gxVarianceFR	-0.93719	0.97722	-0.959	0.337537	
weight_gxAvgTrialSpeed	0.54390	0.57514	0.946	0.344310	
weight_gxVarianceSpeed	-2.35374	0.78367	-3.003	0.002669	**
ketamine_dayxCorrelationScore	0.41956	0.33708	1.245	0.213237	
ketamine_dayxLickAccuracy	-0.20682	0.20144	-1.027	0.304539	
ketamine_dayxLickNumber	0.45125	0.22458	2.009	0.044502	*
ketamine_dayxAvgFR	1.44940	0.96651	1.500	0.133715	
ketamine_dayxAvgSingleCellVariance	-0.92388	0.94597	-0.977	0.328747	
ketamine_dayxVarianceFR	-0.76557	0.45440	-1.685	0.092027	.
ketamine_dayxAvgTrialSpeed	0.24416	0.32816	0.744	0.456857	
ketamine_dayxVarianceSpeed	1.47173	0.38611	3.812	0.000138	***
medianCellDepthxCorrelationScore	-1.44980	0.32376	-4.478	7.53e-06	***
medianCellDepthxLickAccuracy	0.36188	0.22533	1.606	0.108280	
medianCellDepthxLickNumber	-0.08501	0.26385	-0.322	0.747295	
medianCellDepthxAvgFR	-2.05059	0.75163	-2.728	0.006368	**
medianCellDepthxAvgSingleCellVariance	-2.85366	0.94725	-3.013	0.002590	**
medianCellDepthxVarianceFR	0.20696	0.27064	0.765	0.444430	
medianCellDepthxAvgTrialSpeed	1.63901	0.31478	5.207	1.92e-07	***
medianCellDepthxVarianceSpeed	-1.95645	0.45961	-4.257	2.07e-05	***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for binomial family taken to be 1)

Null deviance: 5538.9 on 3996 degrees of freedom
Residual deviance: 1794.6 on 3934 degrees of freedom
AIC: 1920.6

Number of Fisher Scoring iterations: 7

Model 2 (not including interaction terms) Summary

```
In [7]: summary(model2)

Call:
glm(formula = ketBool ~ ., family = "binomial", data = train2)

Deviance Residuals:
    Min       1Q   Median       3Q      Max
-3.1024  -0.4780   0.0845   0.4688   3.8002

Coefficients:
              Estimate Std. Error z value Pr(>|z|)
(Intercept)   -0.64251    0.15630  -4.111 3.94e-05 ***
totalCellNum  -0.03728    0.06442  -0.579 0.562759
gender         0.46578    0.13882   3.355 0.000793 ***
genotype       0.05546    0.11283   0.492 0.623009
weight_g      -0.46373    0.06503  -7.131 9.94e-13 ***
ketamine_day   0.16121    0.04486   3.594 0.000326 ***
correlationScore -1.50123    0.07377 -20.351 < 2e-16 ***
lickAccuracy   -0.80960    0.05888 -13.750 < 2e-16 ***
lickNumber     -0.60947    0.06549  -9.306 < 2e-16 ***
avgFR          1.77153    0.12885  13.749 < 2e-16 ***
avgSingleCellVariance -1.32595    0.11463 -11.567 < 2e-16 ***
varianceFR     -0.23810    0.05966  -3.991 6.58e-05 ***
avgTrialSpeed  -0.18518    0.05614  -3.298 0.000973 ***
varianceSpeed  -0.99420    0.07504 -13.249 < 2e-16 ***
medianCellDepth -0.04057    0.05383  -0.754 0.451108
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for binomial family taken to be 1)

    Null deviance: 5538.9  on 3996  degrees of freedom
Residual deviance: 2741.0  on 3982  degrees of freedom
AIC: 2771

Number of Fisher Scoring iterations: 6
```

Test Performance

```
In [8]: lr_pred_lo <- predict(model1,test1) # Lo : Log odds
num_val = length(test1$ketBool)
lr_pred = rep(0,num_val)
actual = rep(0,num_val)
for (j in 1:num_val){
  if (lr_pred_lo[j]>0){
    lr_pred[j]=1
  }
  actual[j] = test1$ketBool[j]
}
lr_loss = abs(lr_pred-actual)
zolooss[k] = mean(lr_loss)
test_error_est = mean(zolooss)

cat("=====\n")
cat("Logistic Regression Model with Interaction Terms\n\n")
cat("Zero-One Loss (Test Set):",test_error_est,"\n")
cat("Accuracy (Test Set):",1-test_error_est,"\n")
cat("=====\n")

=====  
Logistic Regression Model with Interaction Terms  
  
Zero-One Loss (Test Set): 0.13475  
Accuracy (Test Set): 0.86525  
=====
```

```

In [9]: lr_pred_lo <- predict(model2,test2) # Lo : Log odds
num_val = length(test2$ketBool)
lr_pred = rep(0,num_val)
actual = rep(0,num_val)
for (j in 1:num_val){
  if (lr_pred_lo[j]>0){
    lr_pred[j]=1
  }
  actual[j] = test2$ketBool[j]
}
lr_loss = abs(lr_pred-actual)
zoloss[k] = mean(lr_loss)
test_error_est = mean(zoloss)

cat("=====\n")
cat("Logistic Regression Model without Interaction Terms\n\n")
cat("Zero-One Loss (Test Set):",test_error_est,"\n")
cat("Accuracy (Test Set):",1-test_error_est,"\n")
cat("=====\n")

```

```

=====
Logistic Regression Model without Interaction Terms

Zero-One Loss (Test Set): 0.14175
Accuracy (Test Set): 0.85825
=====

```

Look at Coefficients on TEST

With Interaction Terms

```
In [10]: model1_test <- glm(ketBool ~ ., data=test1, family='binomial')
summary(model1_test)
```


Warning message:
"glm.fit: fitted probabilities numerically 0 or 1 occurred"

```
Call:
glm(formula = ketBool ~ ., family = "binomial", data = test1)
```

Deviance Residuals:

Min	1Q	Median	3Q	Max
-3.0289	-0.1986	0.0016	0.1849	2.9694

Coefficients:

	Estimate	Std. Error	z value	Pr(> z)	
(Intercept)	-3.65227	2.05234	-1.780	0.075147	.
totalCellNum	0.26300	0.88535	0.297	0.766426	.
gender	7.81598	1.83003	4.271	1.95e-05	***
genotype	7.42112	1.86461	3.980	6.89e-05	***
weight_g	1.15238	0.83398	1.382	0.167037	.
ketamine_day	-1.58289	0.63604	-2.489	0.012823	*
correlationScore	-2.20880	2.19214	-1.008	0.313647	.
lickAccuracy	-2.24522	1.44600	-1.553	0.120494	.
lickNumber	0.33636	1.85504	0.181	0.856112	.
avgFR	4.23584	3.76048	1.126	0.259992	.
avgSingleCellVariance	9.97080	5.09635	1.956	0.050411	.
varianceFR	3.36081	2.66836	1.260	0.207848	.
avgTrialSpeed	0.29209	1.81798	0.161	0.872356	.
varianceSpeed	3.03594	2.45716	1.236	0.216627	.
medianCellDepth	1.65360	0.72813	2.271	0.023146	*
totalCellNumxCorrelationScore	-3.01461	0.66719	-4.518	6.23e-06	***
totalCellNumxLickAccuracy	-0.01844	0.42563	-0.043	0.965452	.
totalCellNumxLickNumber	0.85883	0.46080	1.864	0.062355	.
totalCellNumxAvgFR	-0.72389	1.28868	-0.562	0.574299	.
totalCellNumxAvgSingleCellVariance	2.13417	1.06527	2.003	0.045134	*
totalCellNumxVarianceFR	-1.20751	0.36359	-3.321	0.000897	***
totalCellNumxAvgTrialSpeed	-1.15633	0.56101	-2.061	0.039289	*
totalCellNumxVarianceSpeed	2.58590	0.57912	4.465	8.00e-06	***
genderxCorrelationScore	-0.49791	0.55891	-0.891	0.373005	.
genderxLickAccuracy	0.08964	0.28202	0.318	0.750598	.
genderxLickNumber	0.50079	0.34721	1.442	0.149218	.
genderxAvgFR	-4.79261	1.83800	-2.608	0.009120	**
genderxAvgSingleCellVariance	2.02599	1.25764	1.611	0.107191	.
genderxVarianceFR	0.60497	0.64171	0.943	0.345811	.
genderxAvgTrialSpeed	-1.38870	0.69665	-1.993	0.046219	*
genderxVarianceSpeed	-2.08394	1.04008	-2.004	0.045109	*
genotypexCorrelationScore	-0.65555	0.55225	-1.187	0.235209	.
genotypexLickAccuracy	0.28092	0.36612	0.767	0.442899	.
genotypexLickNumber	-0.37848	0.60850	-0.622	0.533948	.
genotypexAvgFR	-1.08513	1.96100	-0.553	0.580020	.
genotypexAvgSingleCellVariance	-6.50830	2.23454	-2.913	0.003585	**
genotypexVarianceFR	-0.04429	0.81545	-0.054	0.956689	.
genotypexAvgTrialSpeed	-0.48904	0.76063	-0.643	0.520263	.
genotypexVarianceSpeed	-0.02729	1.12641	-0.024	0.980672	.
weight_gxCorrelationScore	4.20517	1.80688	2.327	0.019949	*
weight_gxLickAccuracy	0.53872	1.01541	0.531	0.595730	.
weight_gxLickNumber	-2.76258	1.46563	-1.885	0.059443	.
weight_gxAvgFR	3.28156	3.49283	0.940	0.347467	.
weight_gxAvgSingleCellVariance	-5.86363	3.35396	-1.748	0.080417	.
weight_gxVarianceFR	-4.58480	1.94465	-2.358	0.018391	*
weight_gxAvgTrialSpeed	-0.06083	1.38059	-0.044	0.964858	.
weight_gxVarianceSpeed	-5.94149	1.73747	-3.420	0.000627	***
ketamine_dayxCorrelationScore	-0.10723	0.80114	-0.134	0.893524	.
ketamine_dayxLickAccuracy	0.31969	0.45310	0.706	0.480469	.
ketamine_dayxLickNumber	0.37617	0.53723	0.700	0.483798	.
ketamine_dayxAvgFR	3.33903	2.03621	1.640	0.101042	.
ketamine_dayxAvgSingleCellVariance	-0.31757	2.03221	-0.156	0.875822	.
ketamine_dayxVarianceFR	-0.62787	1.00364	-0.626	0.531581	.
ketamine_dayxAvgTrialSpeed	0.07342	0.73297	0.100	0.920208	.
ketamine_dayxVarianceSpeed	1.03936	0.87252	1.191	0.233567	.
medianCellDepthxCorrelationScore	-1.59720	0.70336	-2.271	0.023158	*
medianCellDepthxLickAccuracy	0.32039	0.49388	0.649	0.516519	.
medianCellDepthxLickNumber	1.08690	0.77763	1.398	0.162200	.
medianCellDepthxAvgFR	-4.70330	1.56983	-2.996	0.002735	**
medianCellDepthxAvgSingleCellVariance	-2.55433	2.04819	-1.247	0.212353	.
medianCellDepthxVarianceFR	0.90155	0.98434	0.916	0.359726	.
medianCellDepthxAvgTrialSpeed	1.31766	0.76205	1.729	0.083792	.
medianCellDepthxVarianceSpeed	-1.42238	1.01890	-1.396	0.162715	.

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for binomial family taken to be 1)

Null deviance: 1386.19 on 999 degrees of freedom
Residual deviance: 399.57 on 937 degrees of freedom
AIC: 525.57

Number of Fisher Scoring iterations: 8

Without Interaction Terms

```
In [11]: model2_test <- glm(ketBool ~ ., data=test2, family='binomial')
summary(model2_test)
```

Call:

```
glm(formula = ketBool ~ ., family = "binomial", data = test2)
```

Deviance Residuals:

Min	1Q	Median	3Q	Max
-2.52524	-0.51562	0.05817	0.49094	3.03239

Coefficients:

	Estimate	Std. Error	z value	Pr(> z)
(Intercept)	-0.11054	0.29360	-0.377	0.706540
totalCellNum	-0.20103	0.12503	-1.608	0.107873
gender	0.38001	0.26237	1.448	0.147507
genotype	0.28291	0.21514	1.315	0.188518
weight_g	-0.21089	0.13190	-1.599	0.109851
ketamine_day	-0.07733	0.08284	-0.934	0.350543
correlationScore	-1.27870	0.13062	-9.789	< 2e-16 ***
lickAccuracy	-0.77094	0.10958	-7.035	1.99e-12 ***
lickNumber	-0.69481	0.14704	-4.725	2.30e-06 ***
avgFR	1.96396	0.25970	7.562	3.96e-14 ***
avgSingleCellVariance	-1.21420	0.22392	-5.423	5.88e-08 ***
varianceFR	-0.54385	0.14694	-3.701	0.000215 ***
avgTrialSpeed	-0.22271	0.11054	-2.015	0.043934 *
varianceSpeed	-0.79791	0.14073	-5.670	1.43e-08 ***
medianCellDepth	-0.14587	0.10636	-1.371	0.170241

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for binomial family taken to be 1)

Null deviance: 1386.19 on 999 degrees of freedom
Residual deviance: 712.67 on 985 degrees of freedom
AIC: 742.67

Number of Fisher Scoring iterations: 6

BOOTSTRAP

```
In [16]: df = train1
coef.boot = function(data, indices) {
  fm = glm(data = data[indices,], ketBool ~ ., family='binomial')
  return(coef(fm))
}
```

Warning message:

"glm.fit: fitted probabilities numerically 0 or 1 occurred"

5000 iterations for speed

```
In [19]: boot.out5000 = boot(df, coef.boot, 5000)
boot.out5000
```

ORDINARY NONPARAMETRIC BOOTSTRAP

Call:
boot(data = df, statistic = coef.boot, R = 5000)

```
Bootstrap Statistics :
      original      bias    std. error
t1*  -3.07542785 -0.163512021  0.8860557
t2*   1.48468157  0.112356796  0.3982214
t3*   5.27077347  0.159548420  0.9726796
t4*   4.70326862  0.313296250  0.8355723
t5*   0.12583501  0.117775884  0.4392267
t6*  -0.71834083 -0.039675563  0.2893456
t7*  -2.30385934 -0.161958413  1.0846243
t8*  -2.59837684 -0.142450055  0.8149587
t9*  -0.51050792  0.305620053  1.0697160
t10*  4.72544849  0.406416640  2.0435735
t11*  7.85495894  0.347478652  2.6492854
t12*  1.58919458  0.327730785  1.2905950
t13* -0.91610950  0.046432168  0.7747884
t14*  1.67179140  0.069693668  1.5398312
t15*  1.26773118  0.064050586  0.3727106
t16* -2.45892080 -0.136245023  0.3385636
t17*  0.24686052  0.021494625  0.1872190
t18*  0.08497568 -0.062724044  0.2535600
t19*  1.43740112  0.004117731  0.6191387
t20* -0.67644636 -0.031402824  0.4553493
t21* -0.86265381 -0.039073363  0.1912735
t22* -0.94312277 -0.044831936  0.2822165
t23*  0.75320836  0.041489704  0.3633940
t24* -0.08490350 -0.028799448  0.2833826
t25*  0.28144194 -0.014737391  0.1484569
t26* -0.14457774  0.078944184  0.1897451
t27* -2.35801119 -0.041716782  0.9129283
t28*  0.54791051  0.005038970  0.6220143
t29*  0.08089907 -0.056589037  0.3140653
t30* -1.05480872 -0.044183591  0.3112202
t31* -1.15446519 -0.022564232  0.4463352
t32* -0.33733429 -0.007568054  0.2366915
t33*  0.56837745  0.019828235  0.1873987
t34* -0.52894342 -0.097652598  0.2350277
t35*  0.92672514  0.097335353  0.7967583
t36* -5.99671390 -0.421273083  1.0111801
t37* -0.22840376 -0.016616648  0.3633037
t38* -0.49683573 -0.068480186  0.3682878
t39* -0.61546156  0.016337821  0.5350772
t40*  3.16987809  0.223434175  0.9385362
t41*  0.94502026  0.090436758  0.6523454
t42*  0.04099947 -0.343765445  0.8609804
t43* -1.81136124 -0.262571263  1.9759017
t44* -1.28618684  0.044050764  1.6340870
t45* -0.93719327 -0.209127921  1.2355809
t46*  0.54390075 -0.065604833  0.6128631
t47* -2.35374381 -0.158873696  1.0950737
t48*  0.41956403 -0.008785576  0.3909710
t49* -0.20682497 -0.009121904  0.2201788
t50*  0.45125095  0.037531456  0.2569805
t51*  1.44939647  0.129445071  1.3169700
t52* -0.92387593 -0.056870319  1.2501330
t53* -0.76557467 -0.049875559  0.4766562
t54*  0.24416101  0.013699044  0.3461907
t55*  1.47172660  0.036047186  0.5656592
t56* -1.44980365 -0.055473346  0.3799927
t57*  0.36187921  0.005246599  0.2684968
t58* -0.08501437  0.035774747  0.3051450
t59* -2.05058738 -0.137705414  0.7560627
t60* -2.85366214 -0.116652223  0.9145253
t61*  0.20696415 -0.096952072  0.4191914
t62*  1.63900578  0.104593900  0.3455519
t63* -1.95645257 -0.070477153  0.7176047
```

50000 iterations (full)

```
boot.out50000 = boot(df, coef.boot, 50000)
```

```
Warning message:  
"glm.fit: fitted probabilities numerically 0 or 1 occurred"  
Warning message:  
"glm.fit: fitted probabilities numerically 0 or 1 occurred"  
Warning message:  
"glm.fit: fitted probabilities numerically 0 or 1 occurred"  
Warning message:  
"glm.fit: fitted probabilities numerically 0 or 1 occurred"  
Warning message:  
"glm.fit: fitted probabilities numerically 0 or 1 occurred"
```

[illegible]

```
In [22]: boot.out50000
```

ORDINARY NONPARAMETRIC BOOTSTRAP

Call:

```
boot(data = df, statistic = coef.boot, R = 50000)
```

Bootstrap Statistics :

	original	bias	std. error
t1*	-3.07542785	-1.871698e-01	0.8792577
t2*	1.48468157	1.127601e-01	0.3967608
t3*	5.27077347	1.731006e-01	0.9561716
t4*	4.70326862	3.296524e-01	0.8346279
t5*	0.12583501	1.142588e-01	0.4338361
t6*	-0.71834083	-3.709430e-02	0.2928084
t7*	-2.30385934	-1.744887e-01	1.0945069
t8*	-2.59837684	-1.208257e-01	0.8054944
t9*	-0.51050792	2.811960e-01	1.0476530
t10*	4.72544849	4.244491e-01	2.0446802
t11*	7.85495894	3.091727e-01	2.6725212
t12*	1.58919458	3.292959e-01	1.3055680
t13*	-0.91610950	4.970261e-02	0.7872574
t14*	1.67179140	8.618482e-02	1.5495920
t15*	1.26773118	6.642372e-02	0.3741739
t16*	-2.45892080	-1.319045e-01	0.3378930
t17*	0.24686052	2.255831e-02	0.1870262
t18*	0.08497568	-5.883696e-02	0.2532629
t19*	1.43740112	-3.469021e-03	0.6104196
t20*	-0.67644636	-2.216683e-02	0.4512524
t21*	-0.86265381	-3.982182e-02	0.1930281
t22*	-0.94312277	-4.960241e-02	0.2765598
t23*	0.75320836	4.067542e-02	0.3610569
t24*	-0.08490350	-2.945468e-02	0.2793542
t25*	0.28144194	-1.442663e-02	0.1481560
t26*	-0.14457774	7.825786e-02	0.1887436
t27*	-2.35801119	-3.853824e-02	0.9099176
t28*	0.54791051	5.621079e-05	0.6256602
t29*	0.08089907	-5.525108e-02	0.3122576
t30*	-1.05480872	-5.268672e-02	0.3140202
t31*	-1.15446519	-1.871115e-02	0.4537412
t32*	-0.33733429	-6.219927e-03	0.2404171
t33*	0.56837745	1.509976e-02	0.1889228
t34*	-0.52894342	-9.971533e-02	0.2349638
t35*	0.92672514	9.796381e-02	0.8023645
t36*	-5.99671390	-4.181811e-01	1.0309204
t37*	-0.22840376	-1.718045e-02	0.3631185
t38*	-0.49683573	-7.915667e-02	0.3755853
t39*	-0.61546156	1.768040e-02	0.5437601
t40*	3.16987809	2.345893e-01	0.9468469
t41*	0.94502026	7.590176e-02	0.6448561
t42*	0.04099947	-3.273368e-01	0.8450051
t43*	-1.81136124	-2.787316e-01	1.9578292
t44*	-1.28618684	6.494018e-02	1.6463267
t45*	-0.93719327	-2.009340e-01	1.2391201
t46*	0.54390075	-5.728862e-02	0.6157488
t47*	-2.35374381	-1.757830e-01	1.0874152
t48*	0.41956403	-6.743100e-03	0.3943418
t49*	-0.20682497	-8.665752e-03	0.2227302
t50*	0.45125095	4.128976e-02	0.2580814
t51*	1.44939647	1.304988e-01	1.3308724
t52*	-0.92387593	-5.375926e-02	1.2543304
t53*	-0.76557467	-5.990636e-02	0.4783992
t54*	0.24416101	8.613222e-03	0.3482670
t55*	1.47172660	4.227326e-02	0.5596560
t56*	-1.44980365	-5.973846e-02	0.3787705
t57*	0.36187921	-1.288271e-04	0.2660305
t58*	-0.08501437	3.944570e-02	0.3031622
t59*	-2.05058738	-1.362395e-01	0.7685607
t60*	-2.85366214	-1.131885e-01	0.9198808
t61*	0.20696415	-9.772077e-02	0.4144050
t62*	1.63900578	1.068083e-01	0.3462285
t63*	-1.95645257	-8.045814e-02	0.7253150

```
In [ ]:
```