

## 15.1 - Key terms

- Performance & response time
- Execution time
- Average CPI

## 15.2 - Factors affecting performance

- Compiler
- Hardware implementation

## 15.3 - Amdahl's law

## 15.1 - Key terms Performance & response time

### Performance: **Definitions**

$$\text{Performance} = \frac{1}{\text{ResponseTime}}$$

#### Performance

- "units of things-per-second"
- Bigger is better

#### Response time

- "number of seconds"
- Smaller is better

Speedup  $n$ , between  $x$  and  $y$  is

$$\text{Speedup} = \frac{\text{Performance}_x}{\text{Performance}_y} = \frac{\text{ResponseTime}_y}{\text{ResponseTime}_x}$$

## Execution time

- We define execution time to focus on **User CPU Time**:
  - Time spent executing the lines of code in the program
  - Excluding time spent on input / output, task switching etc

$$CPU\ Time = \frac{Seconds}{Program}$$



$$CPU\ Time = \frac{Cycles}{Program} \times \frac{Seconds}{Cycle}$$



$$CPU\ Time = \frac{Instructions}{Program} \times \frac{Cycles}{Instruction} \times \frac{Seconds}{Cycle}$$

## Average CPI

$$CPU\ Time = \frac{Instructions}{Program} \times \frac{Cycles}{Instruction} \times \frac{Seconds}{Cycle}$$

- Average **Cycle Per Instruction (CPI)**

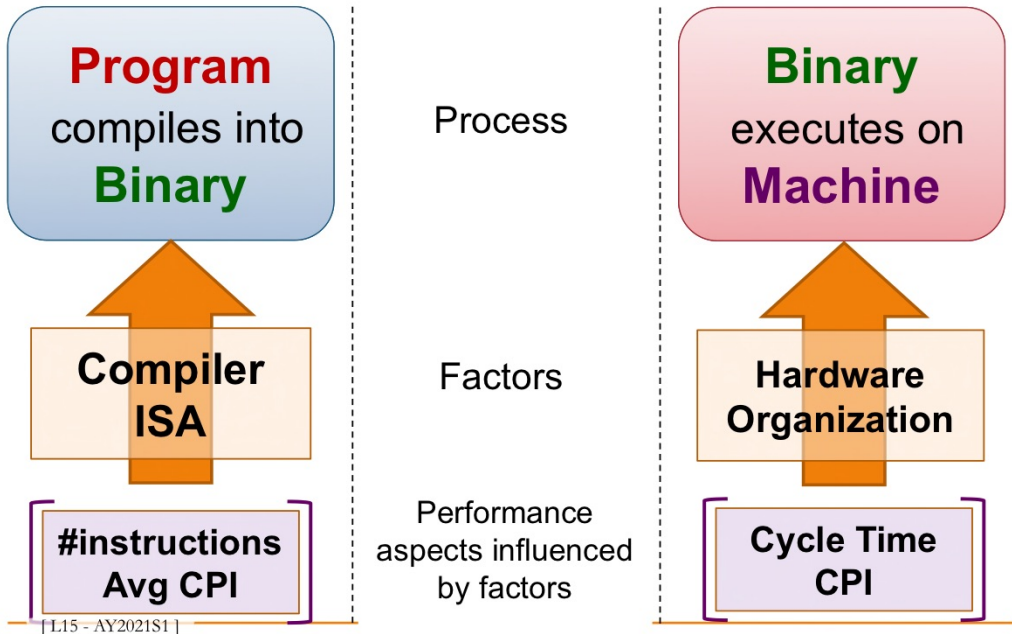
$$\begin{aligned} CPI &= (CPU\ time \times Clock\ rate) / Instruction\ count \\ &= Clock\ cycles / Instruction\ count \end{aligned}$$

$$CPI = \sum_{k=1}^n CPI_k \times F_k \quad \text{where} \quad F_k = \frac{I_k}{\text{Instruction count}}$$

$I_k$  = Instruction frequency

## 15.2 - Factors affecting performance

### Performance: **Influencing Factors**



Factors : program → binary (Compiler)

### ■ Compiler:

- ❑ Different compiler may generate different binary
  - e.g. gnu vs intel c/c++ compiler
- ❑ Different optimization may generate different binary
  - e.g. different optimization level in *gnu c compiler*

### ■ Instruction Set Architecture:

- ❑ The same high level statement can be translated differently depending on the ISA
  - e.g. same C program under *Intel* machine vs *Sunfire* server

Factors : execution of binary (Hardware implementation)

### ■ Machine

- ❑ More accurately the hardware implementation
- ❑ Determine **cycle time** and **cycle per instruction**

### ■ Cycle Time:

- ❑ Different clock frequency (e.g. 2ghz vs 3.6ghz)

### ■ Cycle Per Instruction:

- ❑ Design of internal mechanism (e.g. specific accelerator to improve floating point performance)

## Summary: **Key Concepts**

- Performance is specific to a particular program on a specific machine
  - Total execution time is a consistent summary of performance
- For a given architecture, performance increase comes from:
  - Increase in clock rate (without adverse CPI effects)
  - Improvement in processor organization that lowers CPI
  - Compiler enhancement that lowers CPI and/or instruction count

### **Pitfall:**

Expecting improvement in one aspect of a machine's performance to affect the total performance.

## Amdahl's Law: Definition

### Amdahl's Law

Performance is limited to the non-speedup portion of the program

Original  
Execution Time

$$(1 - P) \times T$$

$$P \times T$$

Improved  
Execution Time

$$(1 - P) \times T$$

$$\frac{P \times T}{S}$$

**P** = Proportion of program  
that can be sped up  
**T** = Execution Time  
**S** = Speedup

### Amdahl's Law Corollary

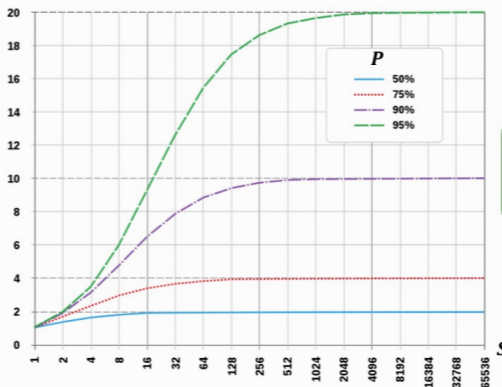
Optimize the common case first!

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## Amdahl's Law: Definition

- The proportion of **non-affected portion (1-P)** effectively place an upper limit of overall speedup:

Speedup



$$\text{Speedup} = \frac{1}{(1 - P) + \frac{P}{S}}$$

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