

moony-15

Goal :

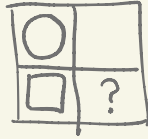
$$1+2+3+\dots+n$$

$$\approx \frac{n}{2} (n+1)$$

$$\approx \frac{n^2}{2}$$

$$= O(n^2)$$

moony-1 :  
(?)

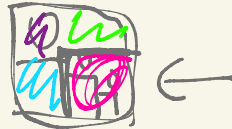
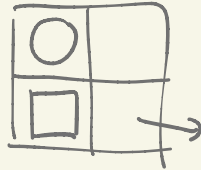


Wishful thinking

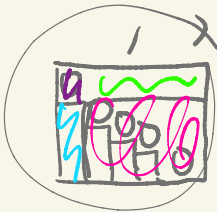
↳ base case

↳ inductive step:  
 $f(n-1) \rightarrow f(n)$

moony-2 :  
(n)



moony-3 :



$$sf\left(\frac{1}{n}, bf\left(\frac{1}{n}, \square, \square\right),\right.$$

$$\left. bf\left(\frac{1}{n}, \blacksquare, \text{moony-2}(n-1)\right)\right)$$



$n$



$\frac{n}{2}$



$\frac{n}{4}$



$\frac{1}{2}$



$n$

$f_n$  cone (n, rune) {

$f_n$  cone\_helper (n, rune, max) {

↳ n == 1

? rune

: overlay\_f (  $\frac{1}{n}$ ,  $1 - \frac{n-1}{\text{max}}$   
scale (  $\frac{1}{n}$ , rune ), max  
cone\_helper (n-1, rune<sub>1</sub>) );

↳ cone\_helper ( n, rune, n );

}

$\left(\frac{1}{4}\right) \quad \frac{1}{3} \quad \frac{1}{2} \quad \frac{1}{1}$

↳  $\frac{1}{4} \quad \frac{2}{4} \quad \frac{3}{4} \quad \frac{4}{4}$

$f(n)$



beside- $f$ ,  
...

$f(n-1)$

① Base case ( $n=1$ )

② Inductive step

$\text{cone}(n)$  {

↳  $n == 1$

? 0

:

$\text{cone}(n-1)$

$t \Rightarrow \text{make\_point}(0.5, t)$

