Homework 5 – Graph

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Deadline: 2018 Dec.11, 11:59pm

1. Objective
   - ☐ Find the minimal cost spanning tree by using Kruskal's algorithm
   - ☐ Find the minimal cost spanning tree by using Prim's algorithm
   - ☐ Find the cost of the shortest path between two specified vertices by using Dijkstra's algorithm

2. Descriptions

   You should use an **adjacency matrix** to implement the program.
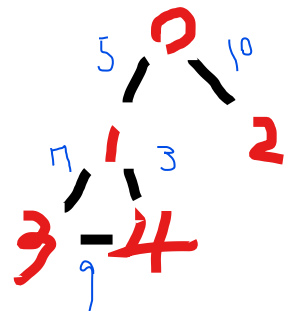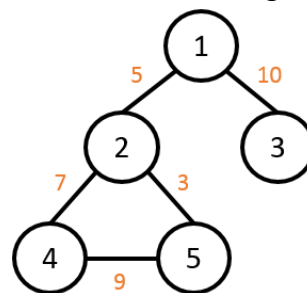
2.1 Kruskal's algorithm
   - ➤ Function details:

     Your program should read the standard input file that stores a graph and print out **each edge** of the minimum cost spanning tree according the processing order.
   - ➤ Input format:
     - ▪ A text file includes the information of the weighted undirected graph.
     - ▪ The first line of the input file is *n* representing the number of vertices. The vertex No. starts from 1 and ends at n, that is, V={1, 2, …, n}.
     - ▪ The second line to the last line of the input file represent an adjacency matrix.
     - ▪ The following is a sample input file for the below graph:
       ```
       5
       0  5  10  0  0
       5  0  0  7  3
       10 0  0  0  0
       0  7  0  0  9
       0  3  0  9  0
       ```


   - ➤ Output format:
     - ▪ The output consists of the starting node and the ending node of an edge with its corresponding cost.
     - ▪ The following is a sample output:

```
The edges of Minimum Cost Spanning Tree are

Edge 1:(2 5) cost:3
Edge 2:(1 2) cost:5
Edge 3:(2 4) cost:7
Edge 4:(1 3) cost:10
Minimum cost = 25
```

2.2 Prim's algorithm

➢ Function details:

Your program should read the standard input file and print out **each edge** of the minimum cost spanning tree according the processing order.

➢ Input format:

▪ A text file includes the information of the weighted undirected graph.

▪ The first line of the input file is n representing the number of vertices.

▪ The second line to the (n+1) line of the input file represent an adjacency matrix. The vertex No. starts from 1 and ends at n, that is, V={1, 2, …, n}.

▪ The last line is the specified vertex as the source vertex.

▪ The following are two sample input files for the below graph:

```
5                    5
0 5 10 0 0           0 5 10 0 0
5 0 0 7 3            5 0 0 7 3
10 0 0 0 0           10 0 0 0 0
0 7 0 0 9            0 7 0 0 9
0 3 0 9 0            0 3 0 9 0
2                    3
```
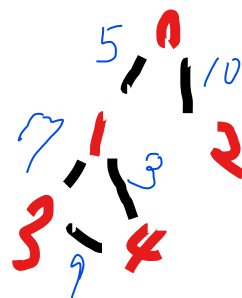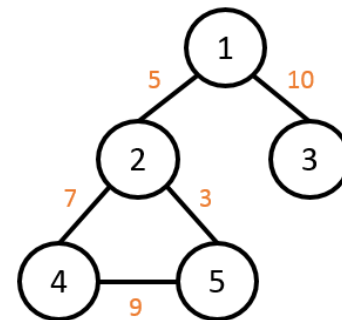

➢ Output format:

▪ The output consists of the starting node and the ending node of an edge with its corresponding cost.

▪ The following are the corresponding sample outputs:

```
The output is              The output is

Edge 1:(2 5) cost:3        Edge 1:(3 1) cost:10
Edge 2:(2 1) cost:5        Edge 2:(1 2) cost:5
Edge 3:(2 4) cost:7        Edge 3:(2 5) cost:3
Edge 4:(1 3) cost:10       Edge 4:(2 4) cost:7
Minimum cost=25            Minimum cost=25
```

## 2.3 Dijkstra's algorithm

➢ Function details:

Your program should read the standard input file and two variables from a

user. Show the cost of the shortest path between two specified vertices in the weighted **directed** graph.

➢ Input format:

▪ A text file includes the information of the weighted undirected graph.

▪ The first line of the input file is *n* representing the number of vertices. The vertex No. starts from 1 and ends at n, that is, V={1, 2, …, n}.

▪ The second line to the last line of the input file represent an adjacency matrix.

▪ Read two variables from a user as the source and destination nodes, respectively.

▪ The following is a sample input file for the below graph:

```
7
0 3 6 9 0 0 0
0 0 2 0 4 0 0
0 0 0 0 0 7 0
0 0 0 0 0 8 0
0 0 1 0 0 0 0
0 0 0 0 0 0 0
0 0 0 5 0 0 0
```
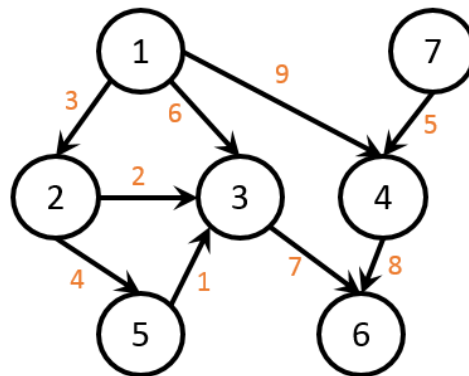
➢ Output format:

▪ Print the cost of the shortest path between the two vertices entered by a user. If the vertex can't reach another one, print -1.

▪ The following is a sample output:

```
Enter two vertices(start end):1 6
The cost from 1 to 6 is : 12
Enter two vertices(start end):1 7
The cost from 1 to 7 is : -1
Enter two vertices(start end):2 6
The cost from 2 to 6 is : 9
```

3. Grade policies

10%- Readme file, code style, and comments in the source code

To keep source code maintainable and readable, you should **add English comments to your source code**. For this assignment, please also compose a small "**README.txt**" which contains a **brief** explanation of **how to compile your program** and **what problem you met**.

30%- Implement the Kruskal's algorithm function

See 2.1, and if you didn't use Kruskal's algorithm, you will get 0%.

30%- Implement the Prim's algorithm function

   See 2.2, and if you didn't use Prim's algorithm, you will get 0%.

30%- Implement the Dijkstra's algorithm function

   See 2.3, and if you didn't use Dijkstra's algorithm, you will get 0%.

Notice that if your homework is copied from your classmate, **you** and **your classmate** will get **0%** in this homework!

4. Summit
   ➢ Turn in
      ● System
         ○ To submit your files electronically, enter the following command from the csie workstation: turnin DS_I_2018.hw5 [your files…]
         ○ To check the files you turnin, enter the following command from the csie workstation: turnin –ls DS_I_2018
         ○ You can see other description about turnin from following link: https://www.cs.ccu.edu.tw/lab401/doku.php?id=turninhowto
         ○ This source code will be compiled and tested on the workstation
      ● Source code
         ○ Source code with appropriate comments
      ● Report
         ○ A document named "readme.txt". You should describe the details of your project in your readme file