Control and Optimization



Example Design Goals

- Prevent overheating
- Meet deadlines
- Save energy

Design Goals

- Prevent overheating
- Meet deadlines
- Save energy

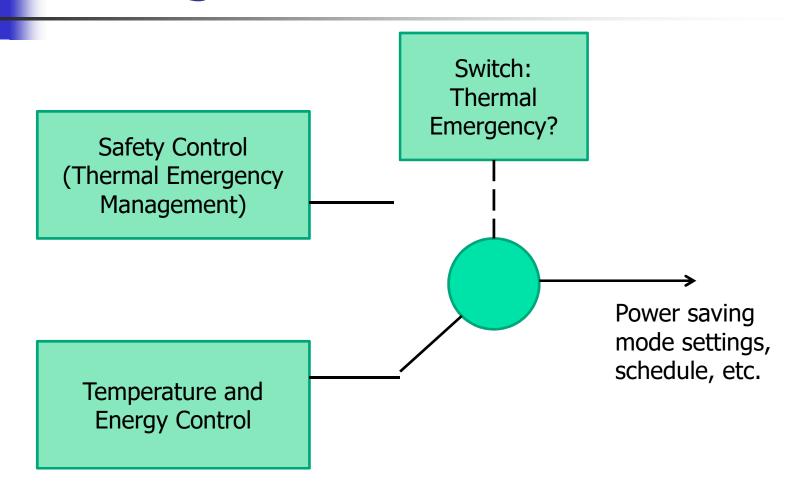
• Question: what the safety, mission, and performance requirements here?



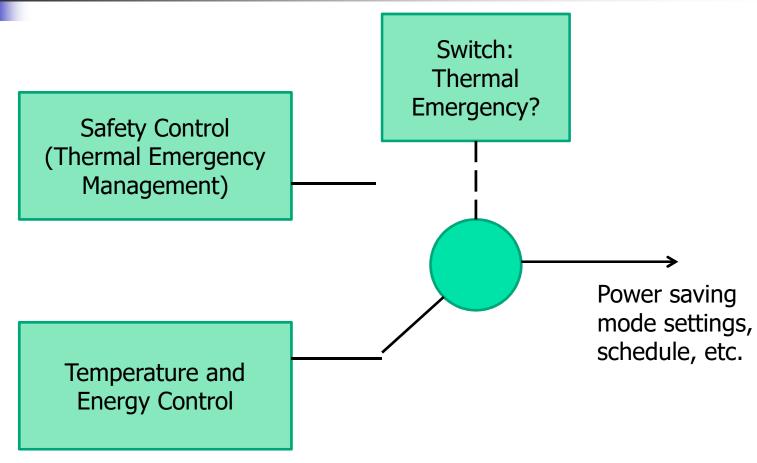
- Prevent overheating (safety requirement)
- Meet deadlines (Mission requirement)
- Save energy (Performance requirement)

• Question: what the safety, mission, and performance requirements here?

Thermal and Energy Management



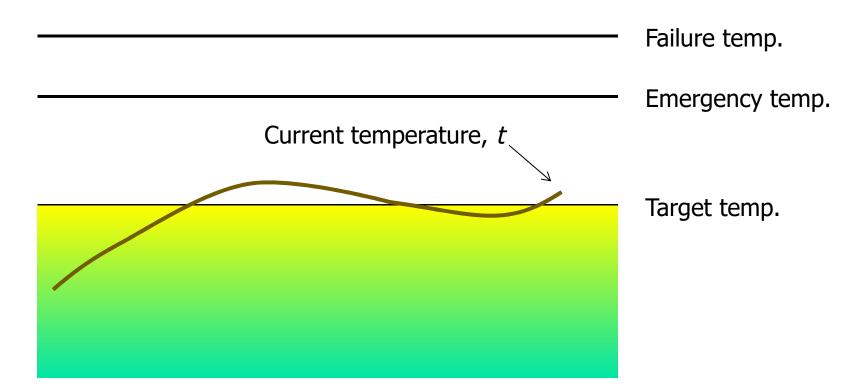
Thermal and Energy Management



Operate as close to the thermal limit as is safe, but without exceeding it

Thermal and Energy Management

Target temperature, emergency temperature, and meltdown temperature:



Relation of Temperature and Energy

 The rate of change of temperature is proportional to the difference between input power and output power (via cooling)

$$\frac{dT}{dt} = P_{in} - P_{out}$$

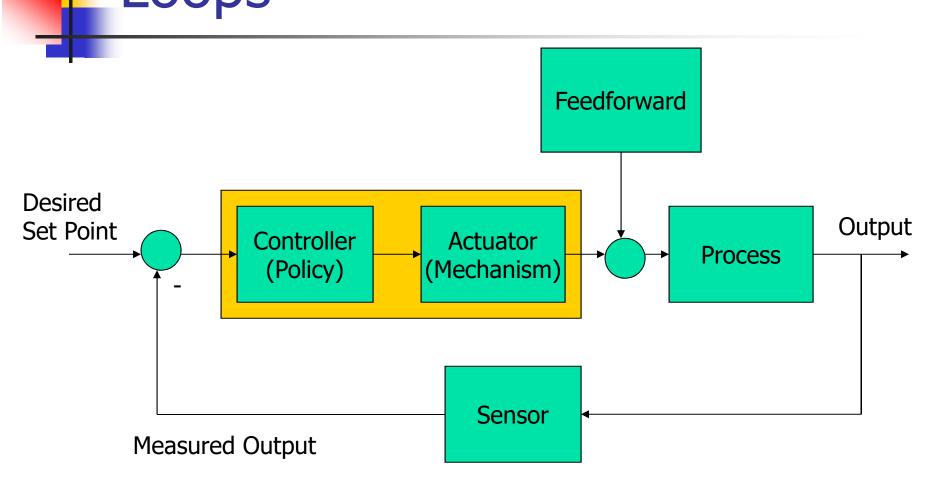
$$P_{in} = f(DVS, sleep)$$

$$P_{out} = g(T)$$

Scheduling and Feedback Control

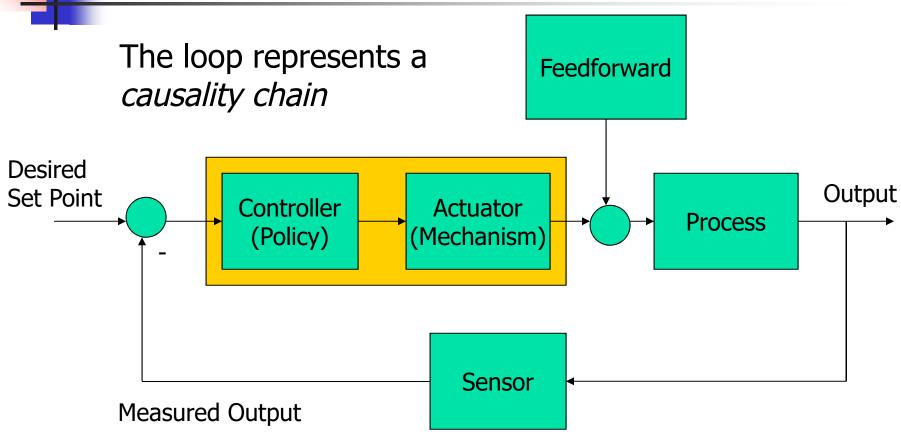
- Feedback control corrects quality deviations or performance deviations in the physical world
- Feedback control loops sample the environment, determine how far it is from "desired state" then actuate in a direction that approaches desired state

Classical Feedback Control Loops

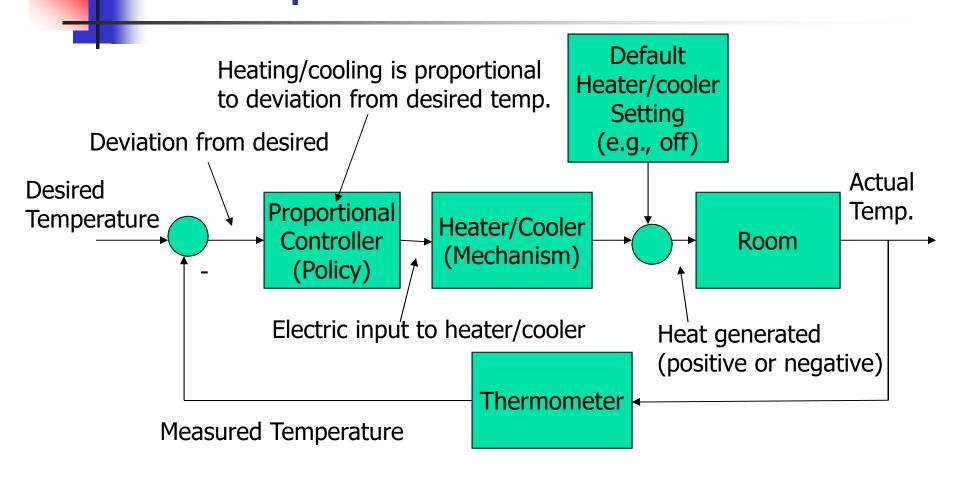




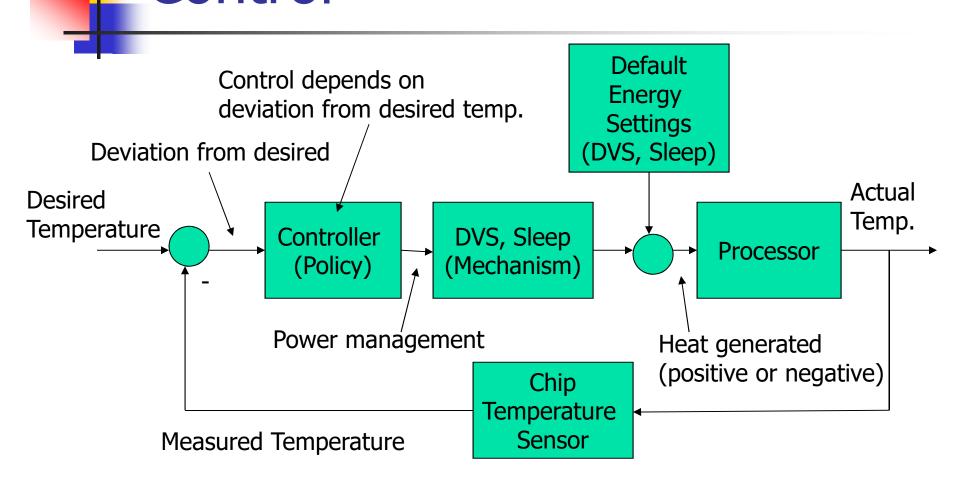
Feedback Control



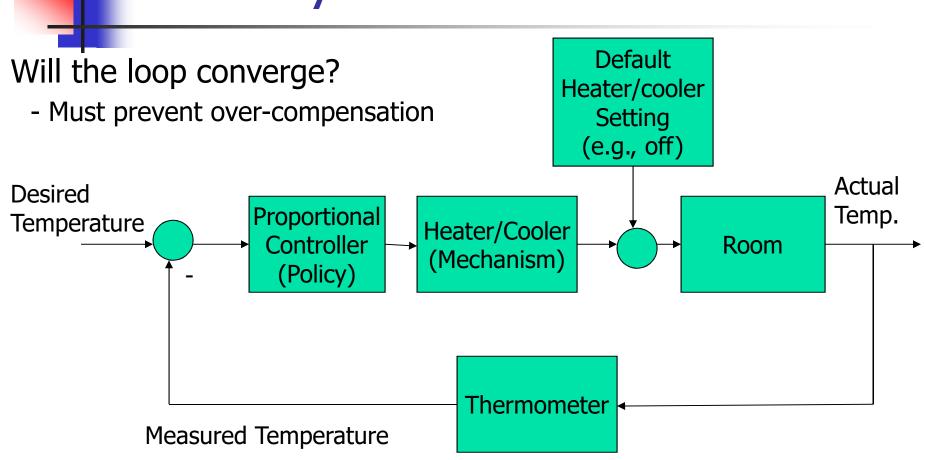
Non-CS Feedback Control Example



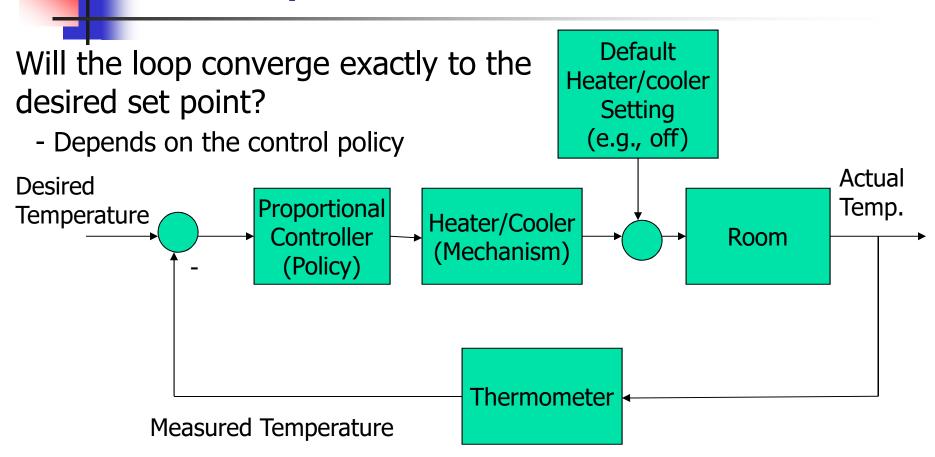
Chip Temperature Feedback Control

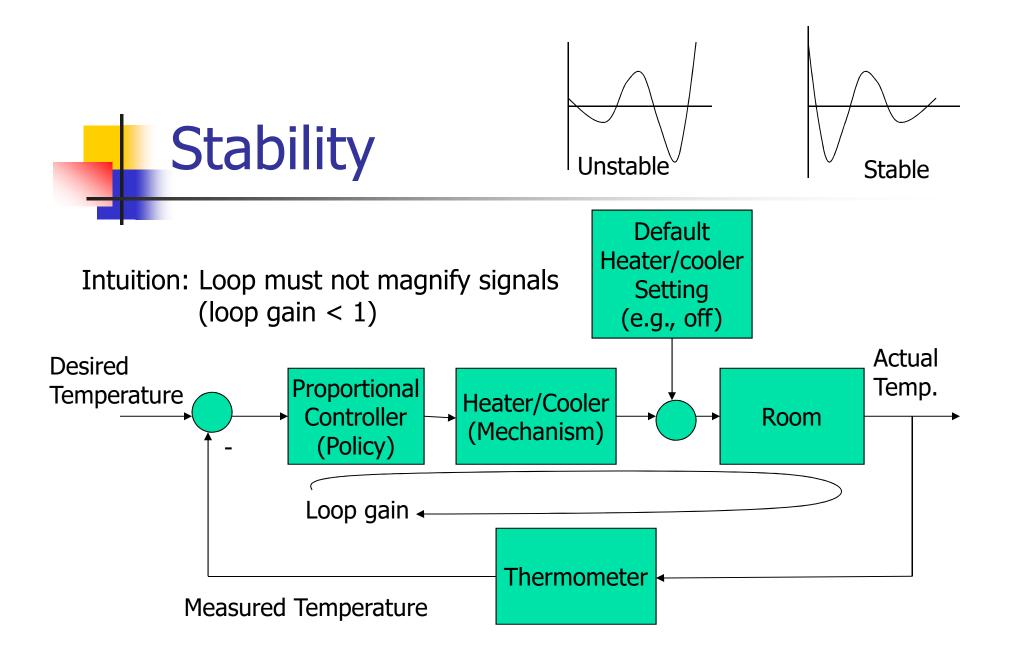


Feedback Design Concern #1: Stability



Feedback Design Concern #2: Steady State Error

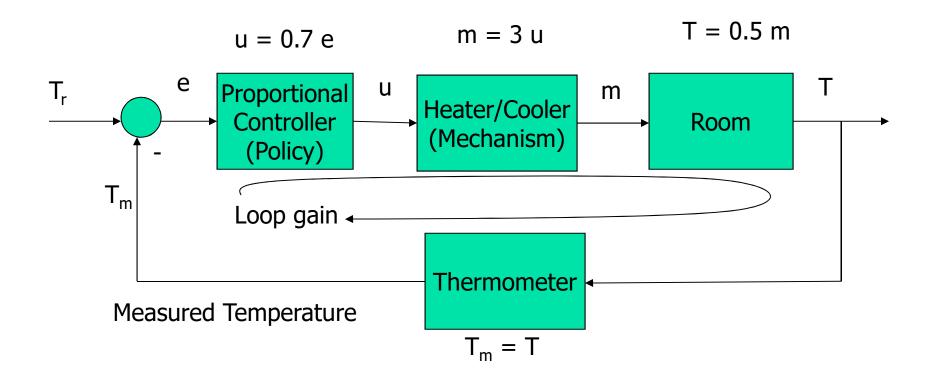




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Stability Example

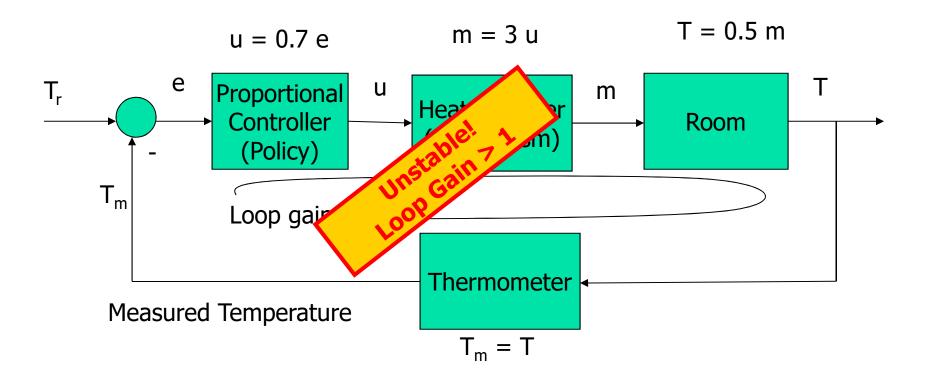
Is the loop below stable?



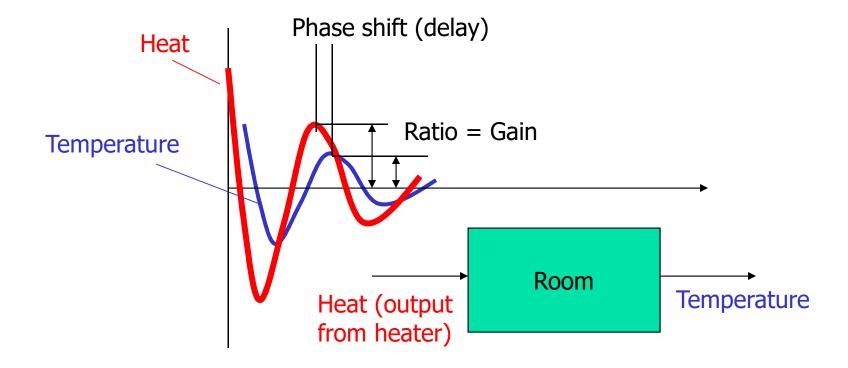
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Stability Example

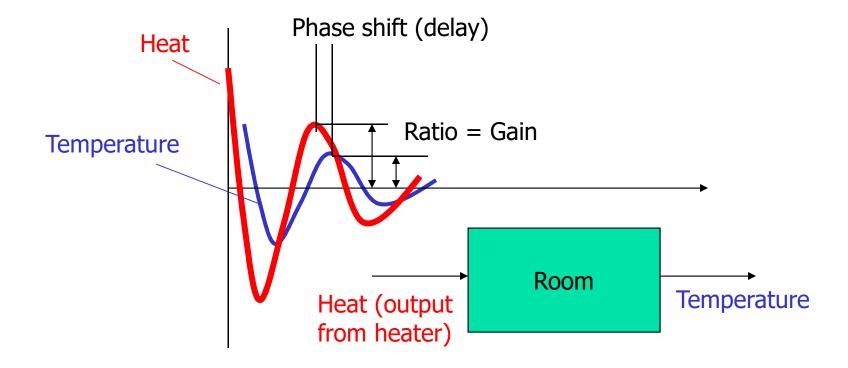
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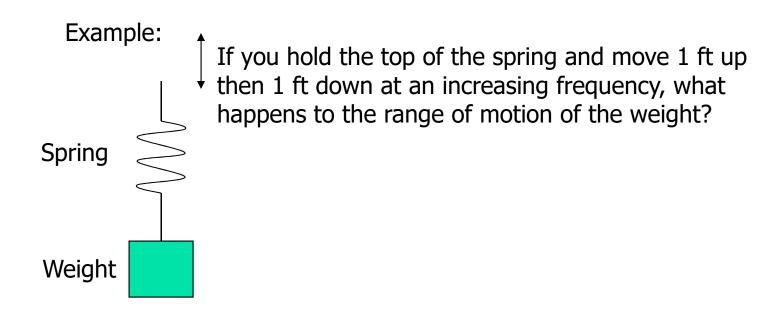
Fact 1: Most reactions are not instantaneous



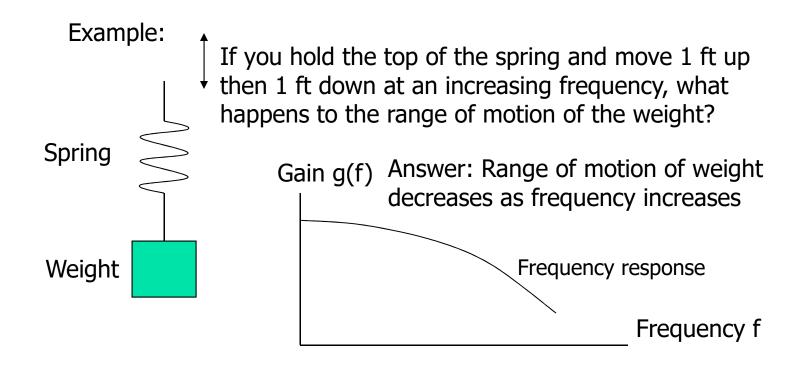
Fact 2: Gain and phase shift depend on frequency



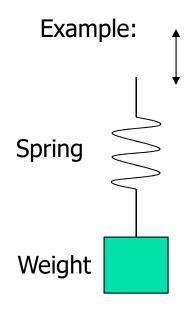
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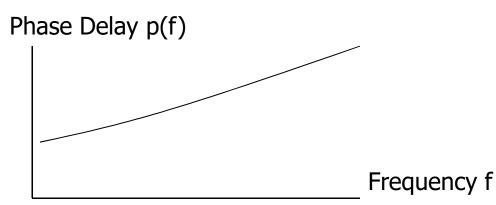
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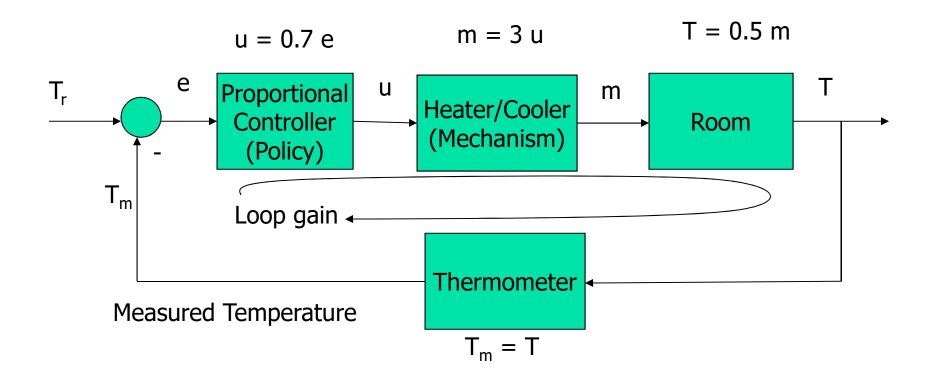


Also, the weight grows more "out of sync" with you (lags behind). That is to say, phase shift increases



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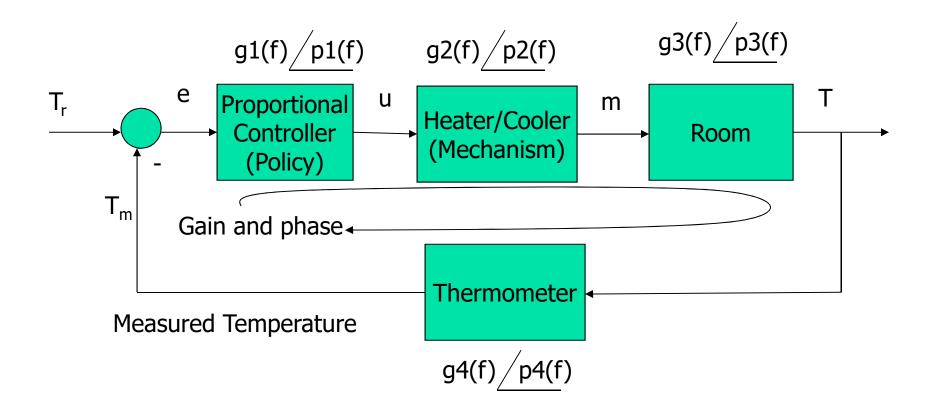
Stability Example Revisited



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Stability Example Revisited

Which frequency f to consider?

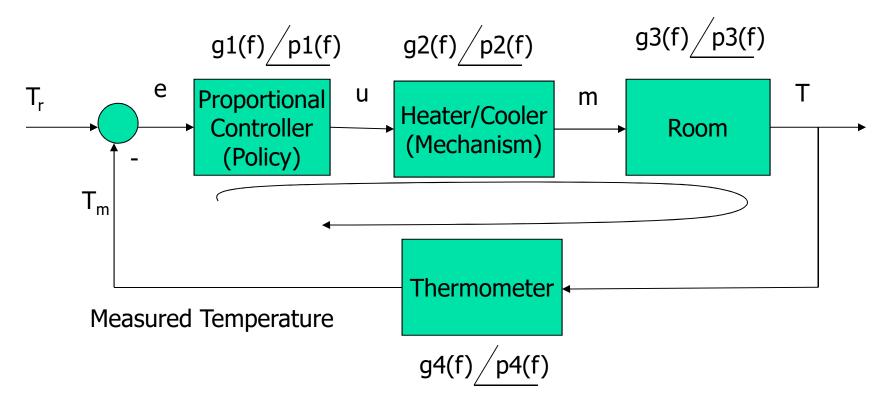


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Stability Example Revisited

Which frequency f to consider?

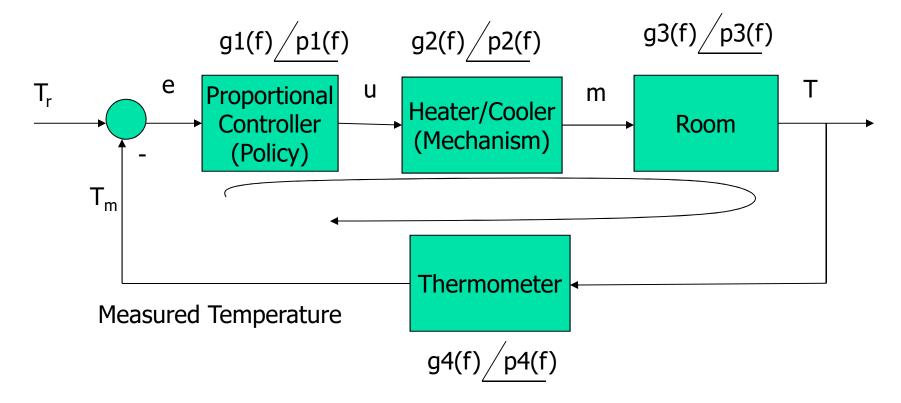
Answer: The one that makes the sum of $p_i(f) = 180^{\circ}$ (why?)



Stability Example Revisited

Phase equation: $\Sigma_i p_i(f) = \pi$ f is obtained

Gain equation: Π_i $g_i(f)$ must be less than 1 for stability



Example 1: Find gain and phase of an integrator? Hint: substitute for input with sin (wt), and compute output, then determine gain and phase shift.

Example 1: Find gain and phase of an integrator?

- Observation: The integral of sin (wt) is
 - -cos (wt) / w
 - Gain = 1/w
 - Phase = -90°

Example 2: Find gain and phase of a differentiator?

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- Observation: The derivative of sin (wt) is w cos (wt)
 - Gain = w
 - Phase = 90°

Example 3: Find gain and phase of a pure delay element?

- Example 3: Find gain and phase of a pure time-delay element?
- Observation: Delay does not magnify signal. Phase shift is equal to proportional to frequency and delay
 - Gain = 1
 - Phase = w D

Example 4: Find gain and phase of an element given by the first order differential equation below?

$$Output + \tau \frac{dOutput}{dt} = K Input$$

- Observation:
 - Gain = ?
 - Phase = ?

Example 4: Find gain and phase of an element given by the first order differential equation below?

$$Output + \tau \frac{dOutput}{dt} = K Input$$

Observation:

Gain = K

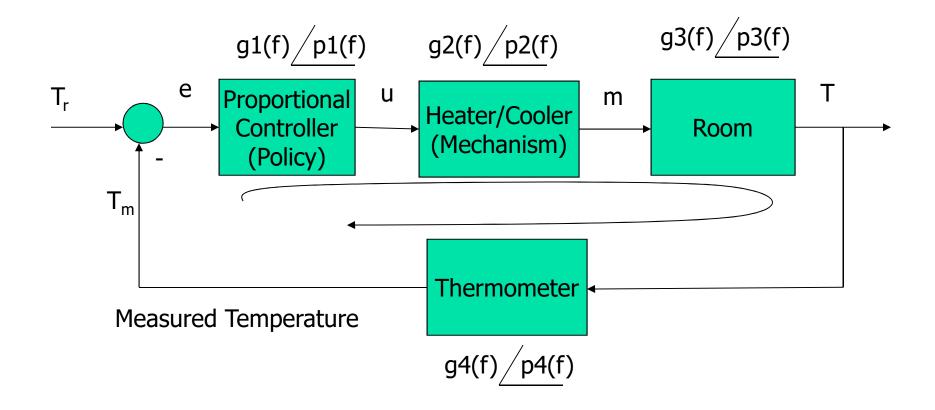
Phase = - $tan^{-1} w \tau$

Note: This element is called "first order lag". τ is called a time constant.

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Steady State Error

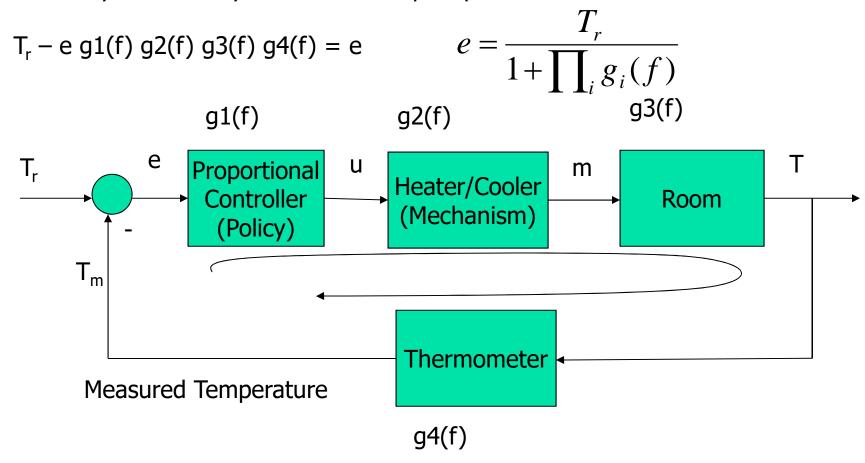
Loop must contain an integrator for the steady state error to be zero. (Why?)



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Steady State Error

At steady state the system "catches up" – phase shift is zero.





Summary of Basic Elements

Input = sin(wt)

Element	Gain	Phase
Integrator	1/w	-π/2
Differentiator	W	π/2
Pure delay element (Delay = D)	1	- w D
First order lag (time constant = τ)	K/ sqrt $(1 + (\tau w)^2)$	- tan ⁻¹ (w τ)
Pure gain (Gain = K)	K	0

Note:

 $w = 2 \pi f_{osc}$

Where f_{osc} is the loop frequency of oscillation

• A robot has a side sensor that can measure distance from a wall when the robot is traveling roughly parallel to it (a short distance away). The operator can control the wheels to turn the robot towards or away from the wall. Design a control loop that keeps the robot traveling along the wall a constant distance away (without bumping into it and without straying away). Wall can be a curved surface.

• When a processor executes a task, its temperature increases with normalized frequency, f, with a time constant = 1 minute. An increase of 0.1 in f causes a temperature increase of 3 degrees. An on-chip sensor reports temperature with a 10 second delay. Design a frequency controller such that processor temperature stays at or around 80 degrees.

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- Does your control loop ensure zero steady state error? If not, redesign.

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- Does your control loop ensure zero steady state error? If not, redesign.
- What is the effect of sensor delay on frequency of oscillation?