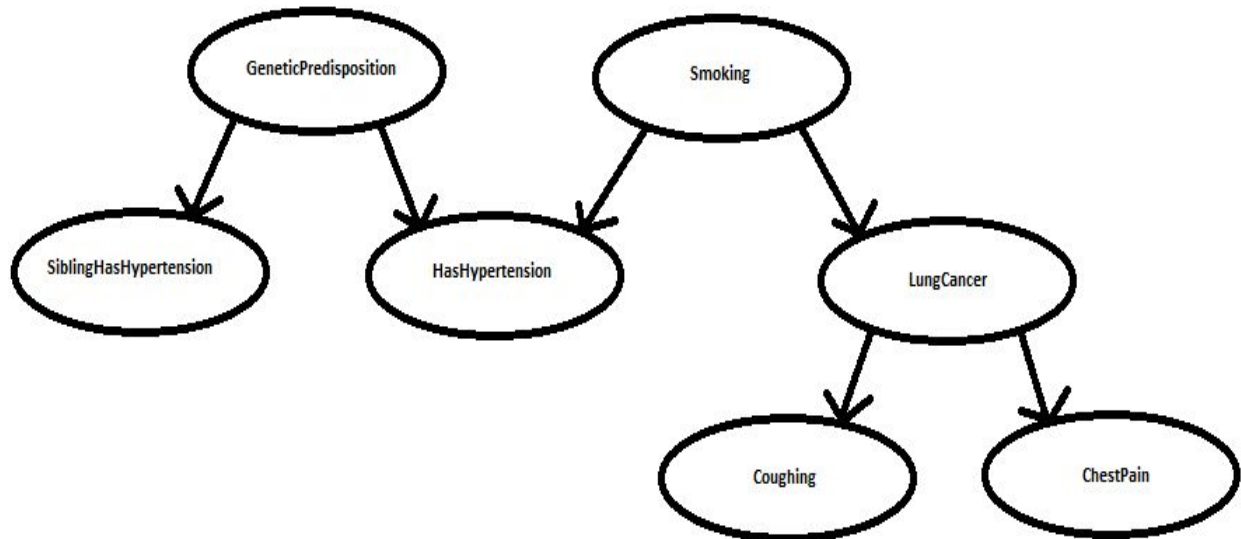


## HW5

### Problem 1

a.)



b.)

14 parameters needed for bayes net

c.)

127 parameters needed for full joint probability distribution  
( $2^7 - 1$ )

d.)

A = GenticPredisposition

B = Smoking

C = SiblingHasHypertension

D = HasHypertension

E = LungCancer

F = Coughing

G = ChestPain

$P(b|d) + P(b|g)$

$P(b|d) = P(d|b) \cdot P(b) / P(d) = P(d|b) \cdot P(b)$

$P(d|b) = P(d|a,b) \cdot P(a) + P(d|\neg a,b) \cdot P(\neg a)$

$P(b|e) = P(e|b) \cdot P(b) / P(e)$

$P(e|g) = P(g|e) \cdot P(e) / P(g) = P(g|e) \cdot P(e)$

$P(b|g) = P(e|b) \cdot P(b) \cdot P(g|e)$

Answer =  $(P(d|a,b) \cdot P(a) + P(d|\neg a,b) \cdot P(\neg a)) \cdot P(b) + P(e|b) \cdot P(b) \cdot P(g|e)$

## Problem 2

a.)

$$a = 0.3$$

$$b = 0.6$$

$$c = 0.3$$

$$d = 0.5$$

$$e = 0.4$$

$$f = 0.7$$

$$g = 0.5$$

$$h = 0.4$$

b.)

The sum of the four ways to that D = true while A = false

$$P(C=T \mid A=F, B=F)$$

$$P(C=T \mid A=F, B=T)$$

$$P(C=F \mid A=F, B=F)$$

$$P(C=F \mid A=F, B=T)$$

$$b \cdot e \cdot g + (1-b) \cdot f \cdot g + b \cdot (1-e) \cdot h + (1-b) \cdot (1-f) \cdot h$$

c.)

d.)

$$0.6 \cdot 0.4 \cdot 0.5 + 0.4 \cdot 0.7 \cdot 0.5 + 0.6 \cdot 0.6 \cdot 0.4 + 0.4 \cdot 0.3 \cdot 0.4$$

$$\text{Answer} = 0.452$$

## Problem 3

a.)

$$BN1 - BN6 = NaNbNcNdNeNf$$

b.)

$$BN1 = (1-Na) + Na(1-Nc) + Nc(1-Ne) + (1-Nb) + Nb(1-Nd) + Nd(1-Nf)$$

$$BN2 = (1-Na) + Na(1-Nc) + Nc(1-Ne) + (1-Nb) + Nb(1-Nd) + NcNd(1-Nf)$$

$$BN3 = (1-Na) + Na(1-Nc) + Nc(1-Ne) + (1-Nb) + NaNb(1-Nd) + Nd(1-Nf)$$

$$BN4 = (1-Na) + Na(1-Nc) + Nc(1-Ne) + (1-Nb) + NbNc(1-Nd) + NcNd(1-Nf)$$

$$BN5 = (1-Na) + NaNb(1-Nc) + Nc(1-Ne) + (1-Nb) + NaNb(1-Nd) + Nd(1-Nf)$$

$$BN6 = (1-Na) + NaNb(1-Nc) + Nc(1-Ne) + (1-Nb) + NaNb(1-Nd) + NcNd(1-Nf)$$