# Digital Filter Design

(Subject Code - EET 3134)

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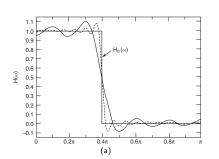
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# **Equiripple Linear Phase FIR Filter** or **Optimal FIR Filters**



### Fundamental Difference



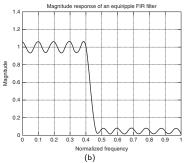


Figure: (b) Equiripple or Chebyshev response

 This method minimizes the maximum error in the passband and stopband, so called "minimax design" or the "Equiripple design"



# Optimal FIR Filter Design

 Allow an unconstrained optimization of the filter coefficients to minimize a cost function. The cost function generally defined as:

$$J(\omega) = W(\omega) \left[ H_d(\omega) - H(\omega) \right]$$

- $H_d(\omega)$  is the desired frequency response normally specified over subinterval of  $0 \le \omega \le \pi$ .
- $W(\omega)$  is a weighting function chosen by the designer to emphasize relative magnitude of the error over different subintervals.
- One approach is to determine the h(n) such that the maximum weighted value of  $J(\omega)$  is minimized.





# Optimal FIR Filter Design

• It has been shown that when this minimum value is achieved, the frequency response exhibits an equiripple behaviour.

$$\min_{\{h_n\}} \quad \left\{ \max_{\{\omega\}} \quad |W(\omega) \left[ H_d(\omega) - H(\omega) \right] | \right\} \tag{1}$$

where  $\{\omega\}$  is used to denote the union of the disjoint frequency band in  $0 \le \omega \le \pi$ .

• Parks & McClellen solved this minimizing the maximum absolute value of the error function  $J(\omega)$  using the theory of Chebyshev approximation & developed an algorithm to implement it by using scheme called Remez exchange algorithm.



## Optimal FIR Filter Design in MATLAB

- For the optimum design filter method it is necessary to first estimate the number of coefficients required.
- The empirical formula to calculate number of coefficients

$$\widehat{N} = \frac{2}{3} \frac{1}{\Delta F} \log_{10} \left[ \frac{1}{10 \delta_p \delta_s} \right] \tag{2}$$

- The values of the coefficients are then determined using suitable DSP simulation package (e.g. REMEZ in matlab). Using these coefficient values, the frequency response is compared with that required; if it is outside the original specification then the value of N is increased, and the design process repeated.
- The advantage of this technique over the window-based method is that a smaller value can be specified for  $\delta_s$  than for  $\delta_p$ , and this can lead to a significant saving in the number of coefficients required.



# Digital Filter Design Lab



#### Assignment 1

• Design a low-pass filter using FIR windowing technique that satisfies the specification of  $\omega_p=0.4\pi$  and  $\omega_s=0.6\pi$  and exhibits a minimum attenuation greater than 50dB in the stop-band.



#### Assignment 1

• Design a low-pass filter using FIR windowing technique that satisfies the specification of  $\omega_p=0.4\pi$  and  $\omega_s=0.6\pi$  and exhibits a minimum attenuation greater than 50dB in the stop-band.

#### Assignment 2

- A FIR low-pass filter is required to have the following specifications:
  - Pass-band edge frequency  $f_p = 2kHz$
  - Transition band  $\Delta f = 200 Hz$
  - Pass-band ripple  $A_p = 0.1dB$
  - Minimum stop-band attenuation  $A_s = 50dB$
  - Sampling frequency of  $f_s = 10kHz$

Using the window method, determine an appropriate window function and calculate the required number of filter coefficients to design this filter. Furthermore, ascertain the corresponding filter coefficient values h[n] for  $-10 \le n \le 10$ .



#### Assignment 3

- Design an FIR filter using windowing method that need to adhere to the following specifications.
  - Passband 8-12 kHz
  - Stopband ripple 0.001
  - Peak passband ripple 0.01
  - Sampling frequency 44.14 kHz
  - Transition width 3 kHz





#### Assignment 3

- Design an FIR filter using windowing method that need to adhere to the following specifications.
  - Passband 8-12 kHz
  - Stopband ripple 0.001
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  - Sampling frequency 44.14 kHz
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#### Assignment 4

 Design an optimal FIR filter for the same specifications of Assignment 3 and compare the performances of both.





