

# Robust Representation and Efficient Feature Selection Allows for Effective Clustering of SARS-CoV-2 Variants: Paper Reproduction dan Improvements

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The COVID-19 pandemic has led to an abundance of genomic data on the SARS-CoV-2 virus, presenting a unique opportunity for detailed analysis. This research benefits biologists, policymakers, and authorities in making informed decisions to control virus spread and prepares for future pandemics. Despite the challenge posed by the virus's diverse variants and mutations, this paper focuses on clustering spike protein sequences, crucial for understanding variant behavior. Utilizing a  $k$ -mers based approach, the original author of the paper create a fixed-length feature vector for spike sequences. The proposed feature selection method enables efficient clustering of spike sequences, demonstrating higher F1 scores for clusters in both hard and soft clustering methods.

Keywords: COVID-19; SARS-CoV-2; Spike Protein Sequences; Clustering Analysis; Feature Selection;  $k$ -mers

## I. INTRODUCTION

The SARS-CoV-2 virus, responsible for COVID-19, has a rapidly spreading genomic sequence worldwide. This genetic information is crucial for understanding outbreak dynamics, designing analyses, drugs, and vaccines, and monitoring changes in viral effectiveness over time. The virus's spike protein, particularly its S region, plays a key role in infection and exhibits significant genomic variation. To efficiently analyze this variation, the original author of the paper propose a focus on amino acid sequences encoded by the spike region using machine learning and clustering methods<sup>1</sup>. By converting these sequences into numeric vectors through  $k$ -mers, the original author of the paper aim to reduce data dimensionality and enhance analysis efficiency. The proposed approach integrates feature selection and clustering to gain insights into the virus's evolutionary dynamics, overcoming challenges posed by the vast number of available genomic sequences. The significance of the S protein makes it a potential target for therapeutic interventions and vaccine development. The methodology proposed ensures meaningful analytics, laying the foundation for effective strategies to combat the COVID-19 pandemic.

## II. ALGORITHMS

In this section, the proposed algorithm is discussed in detail. The discussion start with the description of  $k$ -mers generation from the spike sequences. Then, the generation of feature vector representation from the  $k$ -mers information will be described. After that, discussion on different feature selection methods will be given in detail. Finally, the detail of the application of clustering approaches on the final feature vector representation will be explained.

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### A. k-mers Generation

Given a spike sequence, the first step is to compute all possible  $k$ -mers. The total number of  $k$ -mers that can be generated for a spike sequence are described as follows.

$$N - k + 1 \quad (1)$$

where  $N$  is the length of the spike sequence ( $N = 1274$  for this paper dataset). The variable  $k$  is a user-defined parameter ( $k = 3$  is chosen using standard validation set approach<sup>2</sup>).

### B. Fixed-Length Feature Vector Generation

Since most of the Machine Learning (ML) models work with a fixed-length feature vector representation, the  $k$ -mers information is needed to be converted into the vectors. For this purpose, a feature vector  $\Phi_k$  is generated for a given spike sequence  $a$  (i.e.,  $\Phi_k(a)$ ). Given an alphabet  $\Sigma$  (characters representing amino acids in the spike sequences), the length of  $\Phi_k(a)$  will be equal to the number of possible  $k$ -mers of  $a$ . More formally,

$$\Phi_k(a) = |\Sigma|^k \quad (2)$$

Since there are 21 unique characters in  $\Sigma$  (namely  $ACDEFGHIKLMNPQRSTVWXY$ ), the length of each frequency vector is  $21^3 = 9261$ .

### C. Low Dimensional Representation

Since the dimensionality of data is high after getting the fixed length feature vector representation, different supervised and unsupervised methods is applied to obtain a low dimensional representation of data to avoid the problem of the *curse of dimensionality*<sup>3,4</sup>. Each of the methods for obtaining a low dimensional representation of data is discussed below:

#### 1. Random Fourier Features

The first method that is used is an approximate kernel method called Random Fourier Features (RFF)<sup>5</sup>. It is an unsupervised approach, which maps the input data to a randomized low dimensional feature space (euclidean inner product space) to get an approximate representation of data in lower dimensions  $D$  from the original dimensions  $d$ . More formally:

$$z : \mathbb{R}^d \rightarrow \mathbb{R}^D \quad (3)$$

In this way, the inner product between a pair of transformed points is approximated. More formally:

$$f(x, y) = \langle \phi(x), \phi(y) \rangle \approx z(x)'z(y) \quad (4)$$

In Equation 4,  $z$  is low dimensional (unlike the lifting  $\phi$ ). Now,  $z$  acts as the approximate low dimensional embedding for the original data. Then,  $z$  can be used as an input for different ML tasks like clustering and classification.

#### 2. Least Absolute Shrinkage and Selection Operator (Lasso) Regression

Lasso regression is a supervised method that can be used for efficient feature selection. It is a type of regularized linear regression variants. It is a specific case of the penalized

least squares regression with an  $L_1$  penalty function. By combining the good qualities of ridge regression<sup>6,7</sup> and subset selection, Lasso can improve both model interpretability and prediction accuracy<sup>8</sup>. Lasso regression tries to minimize the following objective function:

$$\min(\text{Sum of square residuals} + \alpha \times |\text{slope}|) \quad (5)$$

where  $\alpha \times |\text{slope}|$  is the penalty term. In Lasso regression, the absolute value of the slope is chosen in the penalty term rather than the square (as in ridge regression<sup>7</sup>). This helps to reduce the slope of useless variables exactly equal to zero.

### 3. Boruta

The last feature selection method that is used is Boruta. It is a supervised method that is made all around the random forest (RF) classification algorithm. It works by creating shadow features so that the features do not compete among themselves but rather they compete with a randomized version of them<sup>9</sup>. It captures the non-linear relationships and interactions using the RF algorithm. It then extract the importance of each feature (corresponding to the class label) and only keep the features that are above a specific threshold of importance. The threshold is defined as the highest feature importance recorded among the shadow features.

### D. Clustering Methods

Dalam artikel penelitian yang direproduksi hasilnya ini, digunakan lima metode *clustering* yang berbeda (baik *hard* maupun *soft clustering*) yaitu *k-means*<sup>10</sup>, *k-modes*<sup>11</sup>, *Fuzzy c-means*<sup>12,13</sup>, *agglomerative hierarchical clustering*, dan *spatial clustering* pada penerapan dengan *noise* berbasis *Hierarchical density* (HDBSCAN)<sup>14,15</sup> (dicatat bahwa metode ini merupakan *soft clustering*). Untuk *k-means* dan *k-modes*, parameter *default* digunakan. Untuk *Fuzzy c-means*, kriteria *clustering* yang digunakan untuk mengagregat subset adalah fungsi objektif *generalized least-squares*. Untuk *agglomerative hierarchical clustering*, pendekatan *bottom-up* diterapkan, yang mana diakui sebagai metode *agglomerative*. Oleh karena prosedur *bottom-up* dimulai dari manapun di titik pusat dari hierarki dan bagian bawah hierarki dikembangkan dengan metode yang lebih ringan seperti *partitional clustering*, biaya komputasi dapat ditekan.

HDBSCAN tidak hanya *spatial clustering* pada aplikasi dengan *noise* berbasis *density* tetapi memindahkannya pada algoritma *hierarchical clustering* dan kemudian diperoleh *flat clustering* berdasarkan kepadatan *cluster*. HDBSCAN tidak banyak dipengaruhi oleh pemilihan parameter dan dapat menemukan *cluster* dari kerapatan yang berbeda<sup>15</sup>.

## III. EXPERIMENTAL SETUP AND DATA PREPARATION

Dalam reproduksi artikel ilmiah ini, penulis hanya menerapkan empat metode clustering yaitu *k-means*, *k-modes*, *Fuzzy c-means*, dan HDBSCAN. *Agglomerative hierarchical clustering* tidak dilakukan karena program dalam bahasa pemrograman python yang saat ini tersedia tidak didukung dengan kemampuan paralelisasi yang mengakibatkan waktu eksekusi metode yang sangat lama, terutama pada ukuran data berdimensi tinggi, contohnya sekuens genom maupun *fixed-length feature vector representation*. Selain *k-means*, pada metode *clustering* lainnya hanya diberikan *low dimensional representation* dari data asli mengingat dimensi data input yang tinggi yang mengakibatkan eksekusi metode dijalankan sangat lama.  $F_1$  score digunakan untuk mengukur kualitas algoritma *clustering*. Eksperimen dilakukan pada sistem Core i7 dengan sistem operasi MacOS, memori 16GB, dan prosesor 1.7 GHz. Implementasi algoritma dilakukan dalam Python, dan kode tersedia di <https://github.com/erland-ramadhan/sars-cov2-variants-results-reproduction.git>.

#### IV. HASIL PENELITIAN DAN PEMBAHASAN

#### V. KESIMPULAN

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