t ... + 2f(xm) + 4f(xm-1) + f(xm))

C Shell finne politicus fil
$$197 = x^{2} + \frac{1}{2}x^{2} - \frac{1}{2}x - \frac{1}{2}$$

Vi vel at en av politicus av $x = -\frac{1}{2}$

Ufforer polynomia vision

$$(x^{3} + \frac{1}{2}x^{2} - \frac{3}{2}x - \frac{11}{20}) : (x + \frac{1}{2}) = x^{2} + x - \frac{11}{10}$$

$$-(x^{3} + \frac{1}{2}x^{2})$$

$$x^{2} - \frac{1}{2}x$$

$$-(x^{2} + \frac{1}{2}x)$$

$$-$$

$$\frac{d}{dx} = \frac{(x - x_2)(x - x_3)}{(x_0 - x_3)(x_0 - x_3)}$$

$$\frac{d}{dx} = \frac{(x - x_1)(x_0 - x_3)}{(x_1 - x_1)(x_2 - x_3)}$$

$$\frac{d}{dx} = \frac{(x - x_1)(x_2 - x_3)}{(x_2 - x_1)(x_2 - x_3)}$$

$$\frac{d}{dx} = \frac{(x - x_1)(x_2 - x_3)}{(x_2 - x_1)(x_2 - x_2)}$$

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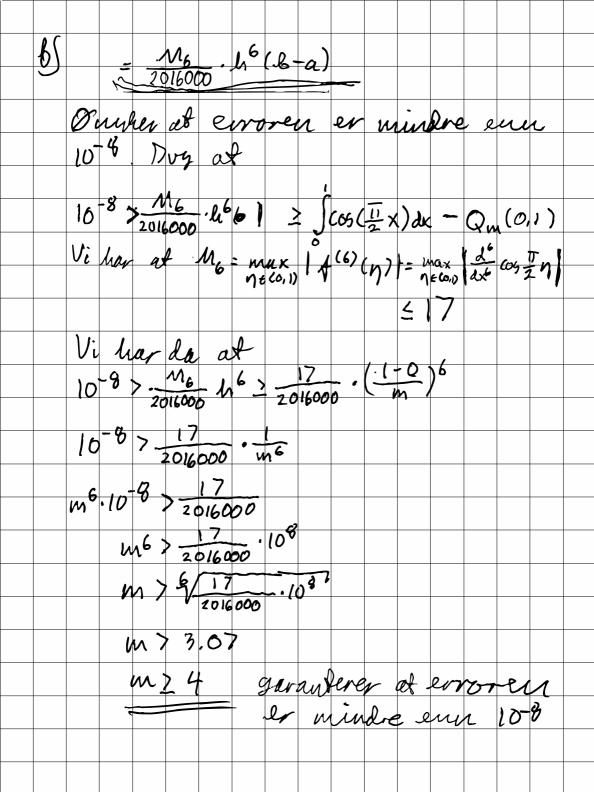
$$\frac{d}{dx} = \frac{(x - x_1)(x_2 - x_3)}{(x_3 - x_1)(x_3 - x_2)}$$

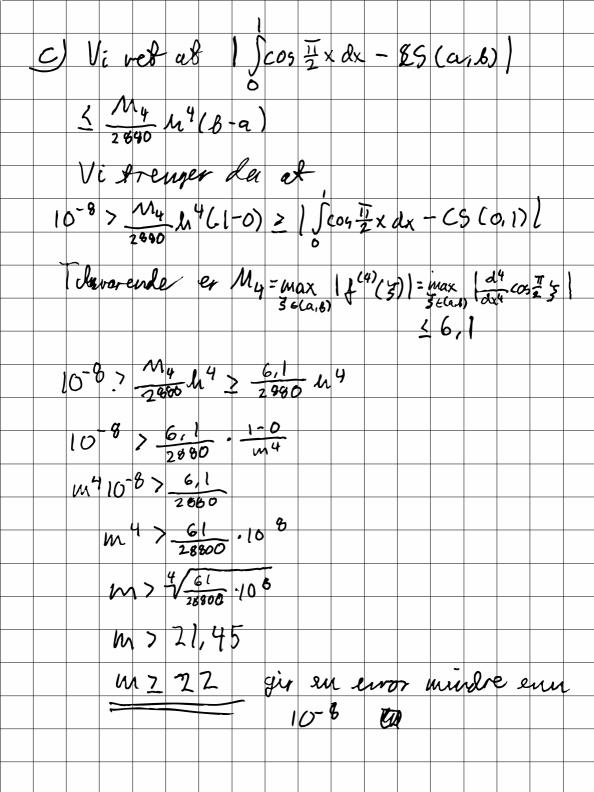
$$\frac{d}{dx} = \frac{(x - x_1)(x_2 - x_3)}{(x_3 - x_1)(x_3 - x_2)}$$

$$\frac{d}{dx} = \frac{dx}{(x_3 - x_1)(x_3 - x_2)}$$

$$\frac{d}{dx} = \frac{dx}{(x_$$

 $S = \frac{1}{2} = \frac{1}{2} = -\sqrt{3} \cdot \frac{3}{2} - \frac{1}{2}$ $=\frac{-1-\sqrt{27}}{2}=\times_2$ $\frac{1}{X}$, = $\frac{1}{X}$, $\frac{3}{2}$ - $\frac{1}{2}$ = 0 $\frac{3}{2}$ - $\frac{1}{2}$ = $-\frac{1}{2}$ = \times $\sqrt{2} = \sqrt{2} \cdot \frac{3}{2} - \frac{1}{2} = \sqrt{3} \cdot \frac{3}{2} - \frac{1}{2} = \frac{-1+\sqrt{3}}{2} \times 3$ Grennet mellom minuhe og skombe verde i £ 4, £ 5 3 er 2 Spennet i Eg, 5, 5 er 1 Må da skalere det sinte mengelen med faltor 3 silen 3.3 = 1 Derette må vi fersligve ved å telike fra lige Ril en honstært, Idette tilfellet er det O. Ganger er [5 , 5 , 7 3 mal 3 tou v 54, 5 5 3 your alemner med det ur fant i a-2.





Oving2_matte4

September 19, 2021

```
[1]: %matplotlib inline
      from numpy import *
      from matplotlib.pyplot import *
      from math import factorial
      import matplotlib.pyplot as plt
      newparams = {'figure.figsize': (8.0, 4.0), 'axes.grid': True,
      'lines.markersize': 8, 'lines.linewidth': 2,
      'font.size': 14}
      plt.rcParams.update(newparams)
 [9]: # composite simpsons rule
      def CSR(function, a, b, n):
          h = (b-a)/n
          x = linspace(a, b, n+1)
          result = 0
          for i in range(1, n+1):
              result += function(x[i-1]) + 4*function((x[i-1] + x[i])/2) +
       \rightarrowfunction(x[i])
          result = result * h/6
          return result
 [3]: def f(x):
          return tan((pi/4)*x)
[13]: for i in range(2, 7):
          m = 2**i
          print("m =", m,":", CSR(f, 0, 1, m))
     m = 4 : 0.441280049596664
     m = 8 : 0.4412717695321729
     m = 16 : 0.44127123615003055
     m = 32 : 0.4412712025498551
     m = 64 : 0.4412712004456543
[23]: answer = 2 * log(2)/pi
      errors = []
      steps = []
```

```
tabulate = []

for i in range(2, 7):
    m = 2**i
    h = 2**(-i)
    steps.append(h)
    errors.append(abs(answer - CSR(f, 0, 1, m)))
    row = [h, m, errors[i-2]]
    tabulate.append(row)

print(tabulate)
```

[[0.25, 4, 8.849291360801814e-06], [0.125, 8, 5.692268696955161e-07], [0.0625, 16, 3.5844727352962735e-08], [0.03125, 32, 2.2445518776947893e-09], [0.015625, 64, 1.4035111961518965e-10]]

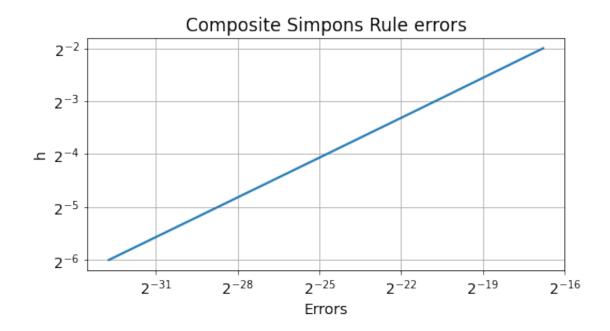
```
[32]: plt.title("Composite Simpons Rule errors")
   plt.xlabel("Errors")
   plt.ylabel("h")
   plt.plot(errors, steps)
   plt.loglog(basex=2, basey=2)
   plt.show()
```

/tmp/ipykernel_161719/2022188119.py:5: MatplotlibDeprecationWarning: The 'basex' parameter of __init__() has been renamed 'base' since Matplotlib 3.3; support for the old name will be dropped two minor releases later.

plt.loglog(basex=2, basey=2)

/tmp/ipykernel_161719/2022188119.py:5: MatplotlibDeprecationWarning: The 'basey' parameter of __init__() has been renamed 'base' since Matplotlib 3.3; support for the old name will be dropped two minor releases later.

plt.loglog(basex=2, basey=2)



 $log_2 - log_2$ plottet har ca stigningstall 4, som tyder på at konvergensen er av grad 4

```
[41]: def g(x):
          return sqrt(1-x**2)
[43]: for i in range(2, 7):
          m = 2**i
          print("m =", m,":", CSR(g, 0, 1, m))
     m = 4 : 0.7802972924438545
     m = 8 : 0.7835994172461493
     m = 16 : 0.7847630544733984
     m = 32 : 0.7851737690201337
     m = 64 : 0.7853188547338977
[47]: answer = pi/4
      errors = []
      steps = []
      tabulate = []
      for i in range(2, 7):
          m = 2**i
          h = 2**(-i)
          steps.append(h)
          errors.append(abs(answer - CSR(g, 0, 1, m)))
          row = [h, m, errors[i-2]]
          tabulate.append(row)
```

```
print(tabulate)
```

[[0.25, 4, 0.005100870953593795], [0.125, 8, 0.0017987461512989356], [0.0625, 16, 0.000635108924049832], [0.03125, 32, 0.00022439437731458511], [0.015625, 64, 7.9308663550548e-05]]

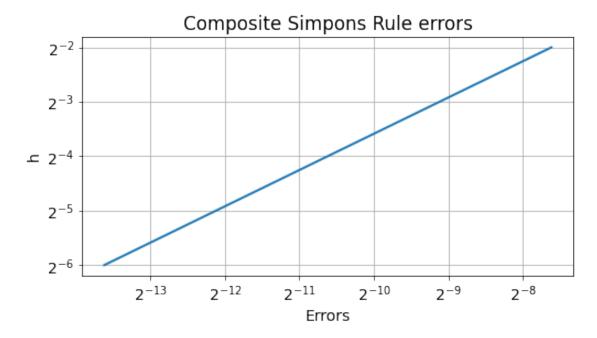
```
[48]: plt.title("Composite Simpons Rule errors")
   plt.xlabel("Errors")
   plt.ylabel("h")
   plt.plot(errors, steps)
   plt.loglog(basex=2, basey=2)
   plt.show()
```

/tmp/ipykernel_161719/2022188119.py:5: MatplotlibDeprecationWarning: The 'basex' parameter of __init__() has been renamed 'base' since Matplotlib 3.3; support for the old name will be dropped two minor releases later.

plt.loglog(basex=2, basey=2)

/tmp/ipykernel_161719/2022188119.py:5: MatplotlibDeprecationWarning: The 'basey' parameter of __init__() has been renamed 'base' since Matplotlib 3.3; support for the old name will be dropped two minor releases later.

plt.loglog(basex=2, basey=2)



Stigningstallet er mye lavere enn i b). Dette kommer nok av at i nærheten av 1 går den deriverte av funksjonen mot uendelig.

[]:

[]:[

Oving2_oppg2

September 19, 2021

1 Oppgave 2

```
[2]: from sympy.abc import x
from sympy import integrate
a=-2
b=1
#Define the inner poduct
def scp(p,q):
    return integrate(p*q, (x, a, b))
#Define polynomials
p0 = 1
phi1 = x
#Calculate the inner product and print it.
print(scp(p0,phi1))
```

-3/2

```
[34]: p1 = x + 1.0/2
phi2 = x**2
p2 = x**2 + x - 1.0/2
phi3 = x**3
p3 = x**3 + 3.0/2 * x**2 - 3.0/5 * x - 11.0/20
tr = 10**(-10)

print(0 if scp(p0, p1)
```

0

0

0

0