

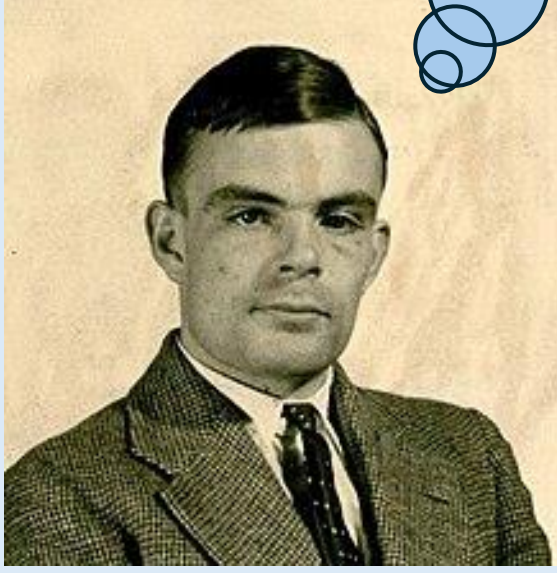
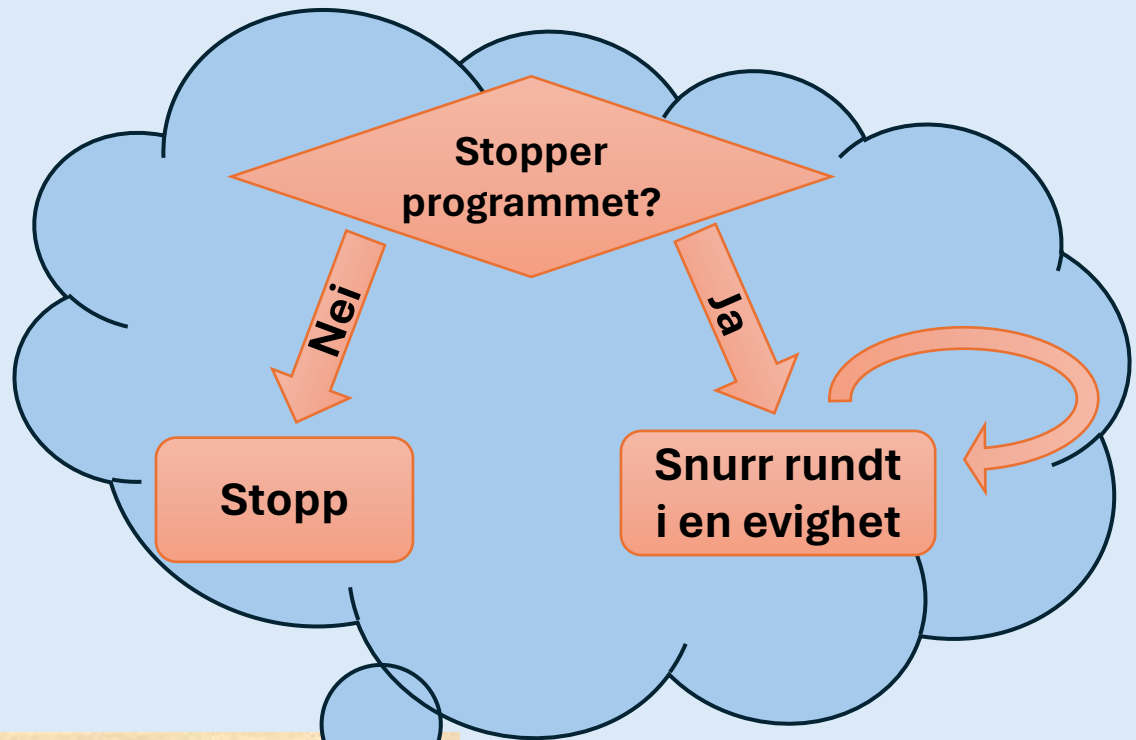


Parameteriserte algoritmer: Løser vanskelige problemer raskt



Høgskulen
på Vestlandet

UMULIG ELLER VANSKELIG?



STOPPEPROBLEMET
Q: Kan vi lage et program som sjekker om et annet program stopper opp?
A: Nei!

<- Bevis av Alan Turing

TRE TYPER PROBLEMER

P: Lett å finne en løsning.

NP: Lett å sjekke at en løsning stemmer.

NP-KOMPLETT: Lett å løse bare dersom $P = NP$.

Clay Mathematics Institute
About Programs & Awards People The Millennium Problems

Home - Millennium Problems - P vs NP
Unsolved
P vs NP

Following the decision of the Scientific Advisory Board, the Board of Directors of CMI designated a \$7 million prize fund for the solutions to these problems, with \$1 million allocated to the solution of each problem.

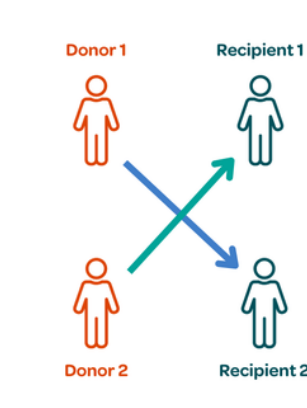
\$1 million



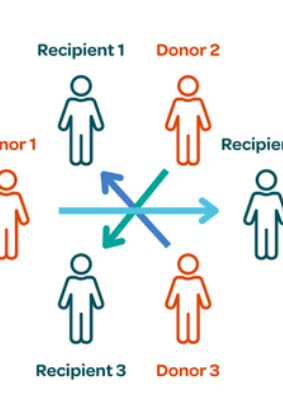
NOEN NP-KOMPLETTE PROBLEM



Two-way exchange (paired exchange)



Three-way exchange (pooled donation)



ER DETTE NYTTIG? JA!

Her kan du miste jobben...



Dette klarer du (sannsynligvis) ikke...



Men dette kan du få til!



"I can't find an efficient algorithm, I guess I'm just too dumb." "I can't find an efficient algorithm, because no such algorithm is possible!" "I can't find an efficient algorithm, but neither can all these famous people."

HVORDAN BEVISE A NOE ER NP-KOMPLETT?

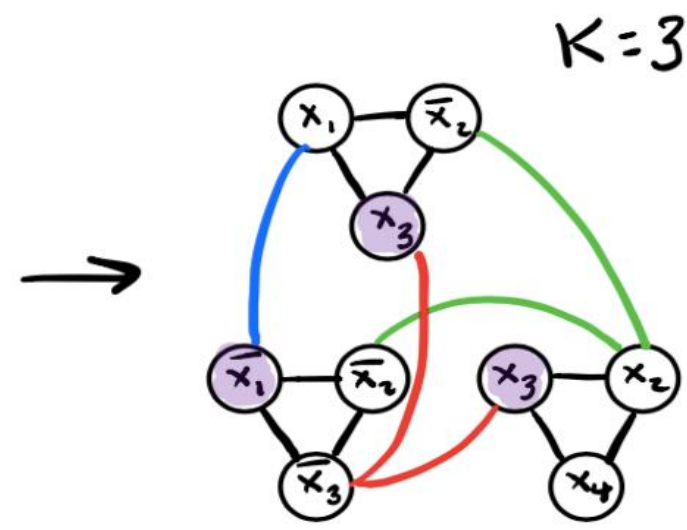
Andre ganger er det mye arbeid...

IDE:

Vi vet at problemet «3SAT» er NP-komplett. Dersom vi koder 3SAT som et annet problem er vi i mål!

3SAT

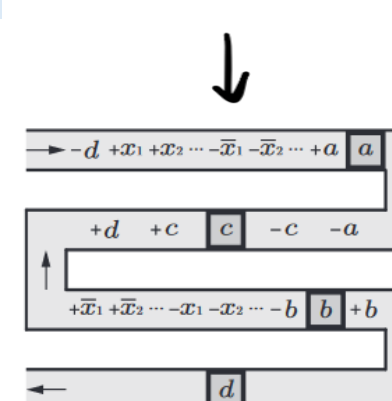
$(x_1 \vee \bar{x}_2 \vee x_3) \wedge$
 $(\bar{x}_1 \vee \bar{x}_2 \vee \bar{x}_3) \wedge$
 $(x_4 \vee x_2 \vee x_3)$



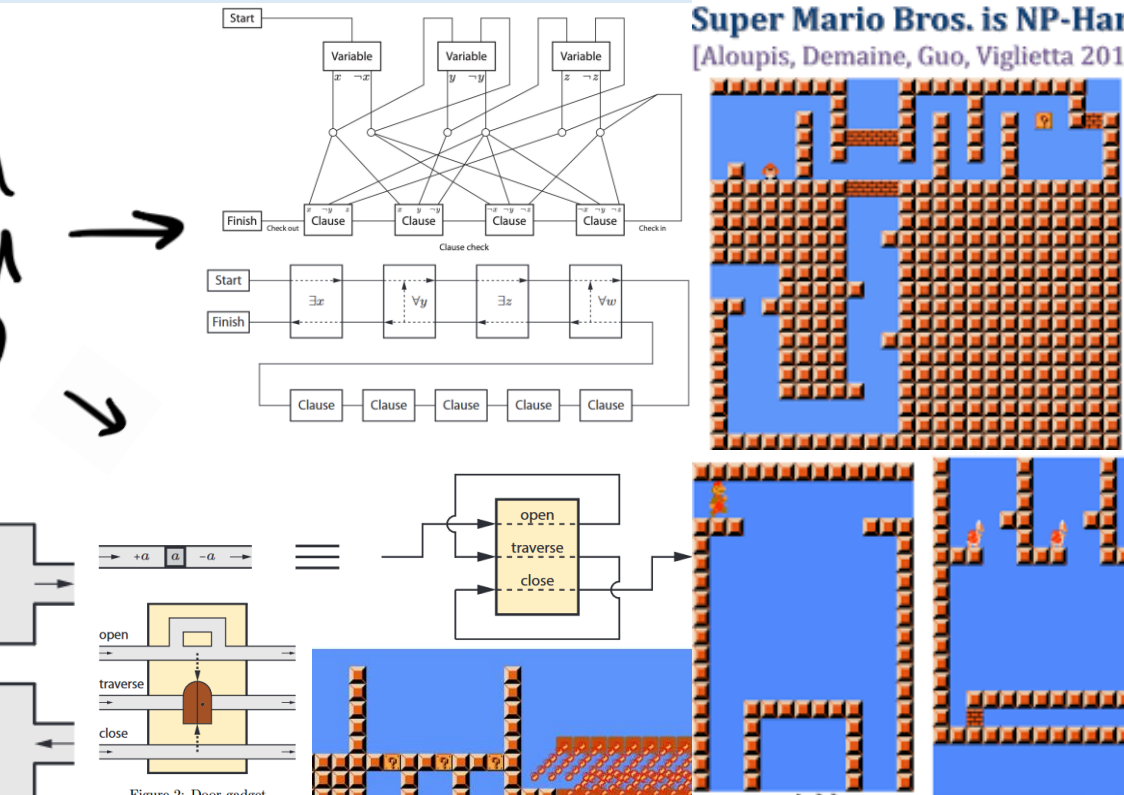
Noen ganger er dette (ganske) enkelt...

3SAT

$(x_1 \vee \bar{x}_2 \vee x_3) \wedge$
 $(\bar{x}_1 \vee \bar{x}_2 \vee \bar{x}_3) \wedge$
 $(x_4 \vee x_2 \vee x_3)$

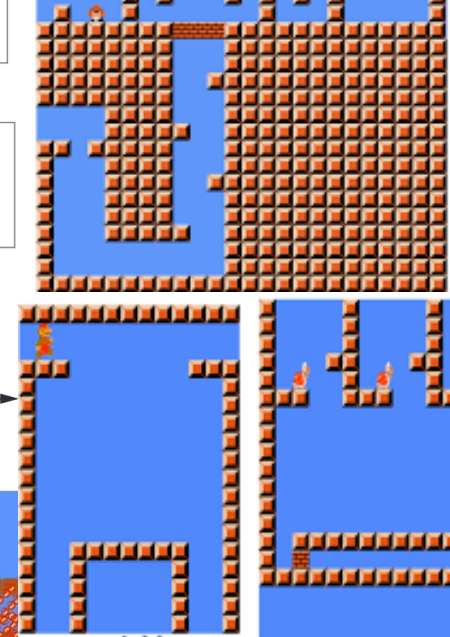


Ofte er jobben alt gjort av noen andre!



Super Mario Bros. is NP-Hard

[Aloupis, Demaine, Guo, Viglietta 2014]

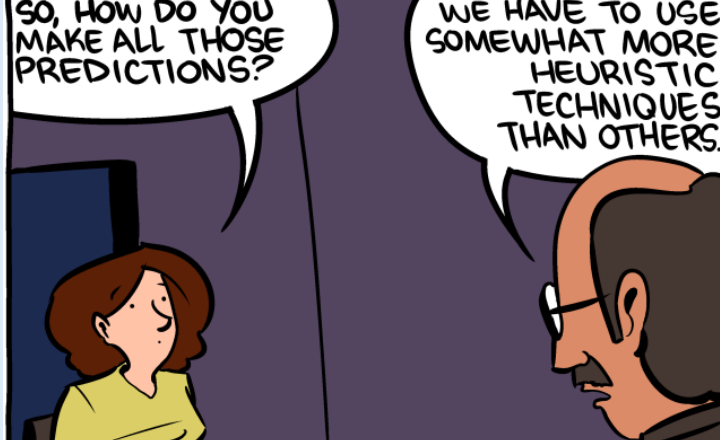
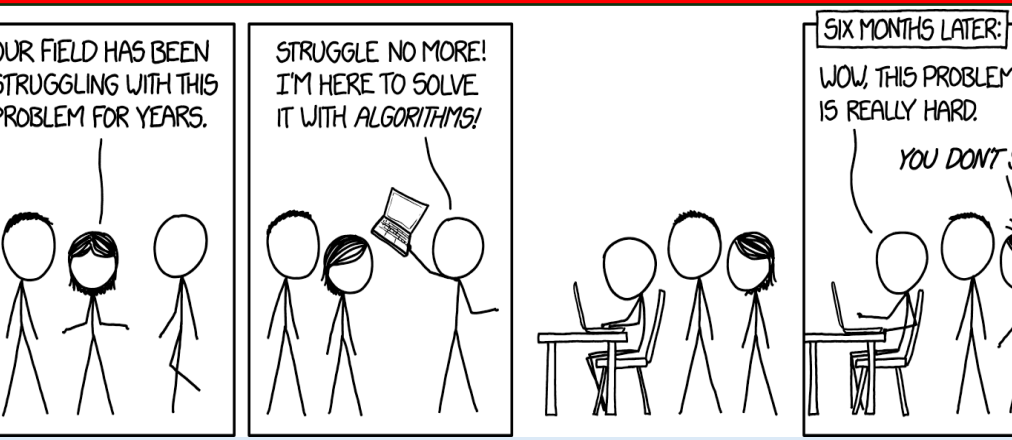


V E I E N V I D E R E ->

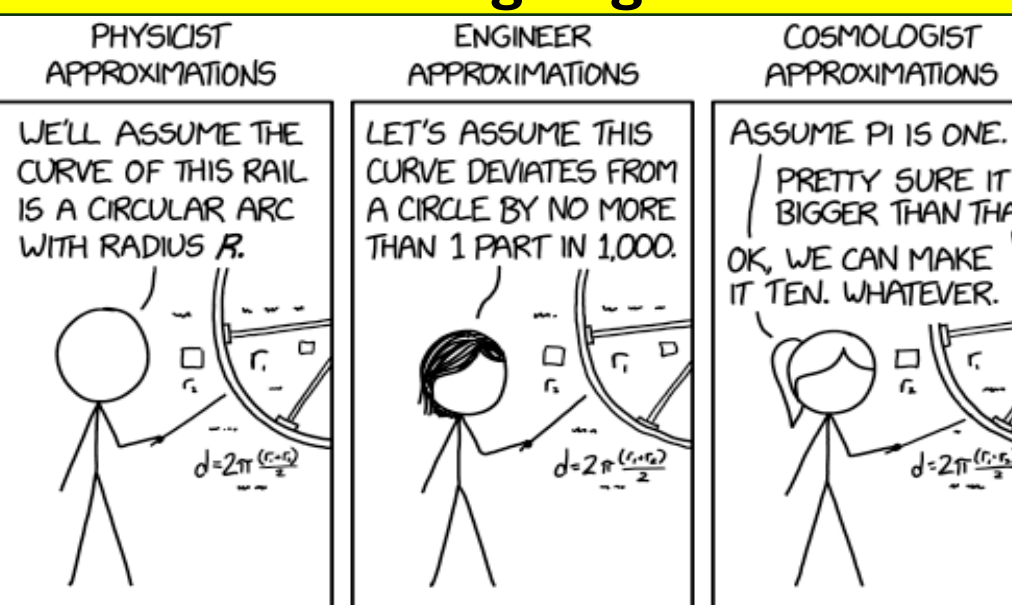
HVORDAN LØSE VANSKEelige PROBLEM?

Ingen quick fix, men vi kan bruke...

Heuristikker



Tilnærmingsalgoritmer



Restriksjoner



Randomisering

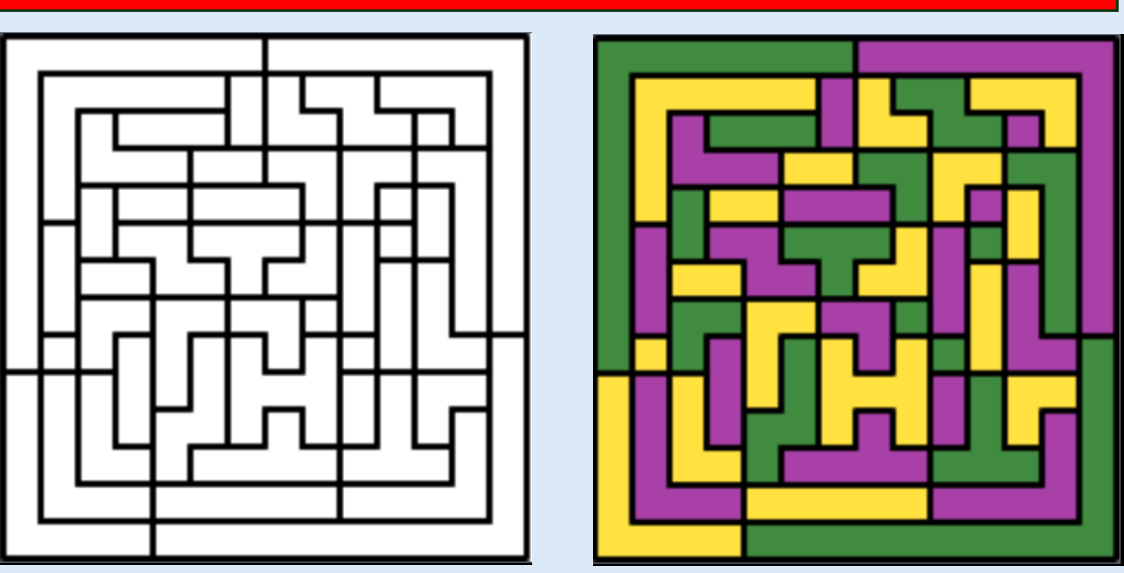
```
int getRandomNumber()  
{  
    return 4; // chosen by fair dice roll.  
    // guaranteed to be random.  
}
```

ELLER...

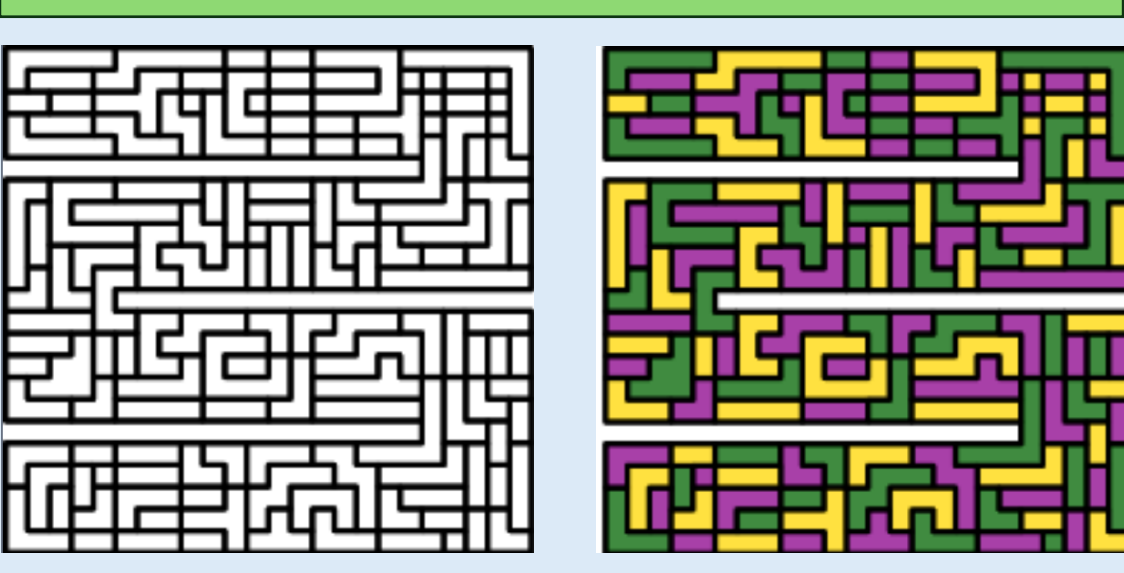
PARAMETERISERTE ALGORITMER!

IDE: Å utnytte «strukturer» i problemet til å finne løsninger som er effektive i praksis.

Vanskelig



Enkelt



Parameterisert kompleksitetsteori
For å «bevise» at parameteriserte algoritmer ikke kan hjelpe oss.

