# Dependency Parsing

Gabriele A. Musillo Fall 2014

Thanks to Joakim Nivre and Ryan McDonald for sharing their slides.

#### Overview

- Dependency Syntax
- Transition-based Parsing

```
Configuration: (S, B, A)

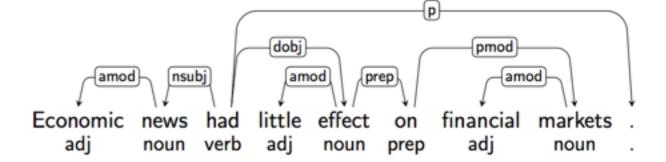
Initial: ([], [0, 1, ..., n], \{])

Terminal: (S, [], A)

Shift: (S, i|B, A) \Rightarrow (S|i, B, A) \iff
```

Reduce:  $(S|i,B,A) \Rightarrow (S,B,A)$ Right-Arc(k):  $(S|i,j|B,A) \Rightarrow (S|i|j,B,A \cup \{(i,j,k)\})$ 

Left-Arc(k):  $(S|i,j|B,A) \Rightarrow (S,j|B,A \cup \{(j,i,k)\})$ 



## Dependency Syntax

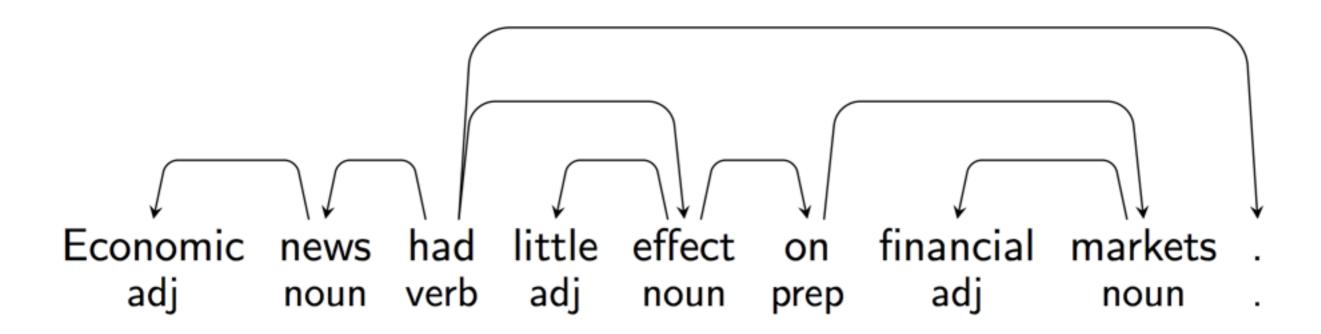
- The basic idea:
  - Syntactic structure consists of lexical items, linked by binary asymmetric relations called dependencies.
- In the words of Lucien Tesnière [Tesnière 1959]:
  - La phrase est un ensemble organisé dont les éléments constituants sont les mots. [1.2] Tout mot qui fait partie d'une phrase cesse par lui-même d'être isolé comme dans le dictionnaire. Entre lui et ses voisins, l'esprit aperçoit des connexions, dont l'ensemble forme la charpente de la phrase. [1.3] Les connexions structurales établissent entre les mots des rapports de dépendance. Chaque connexion unit en principe un terme supérieur à un terme inférieur. [2.1] Le terme supérieur reçoit le nom de régissant. Le terme inférieur reçoit le nom de subordonné. Ainsi dans la phrase Alfred parle [...], parle est le régissant et Alfred le subordonné. [2.2]

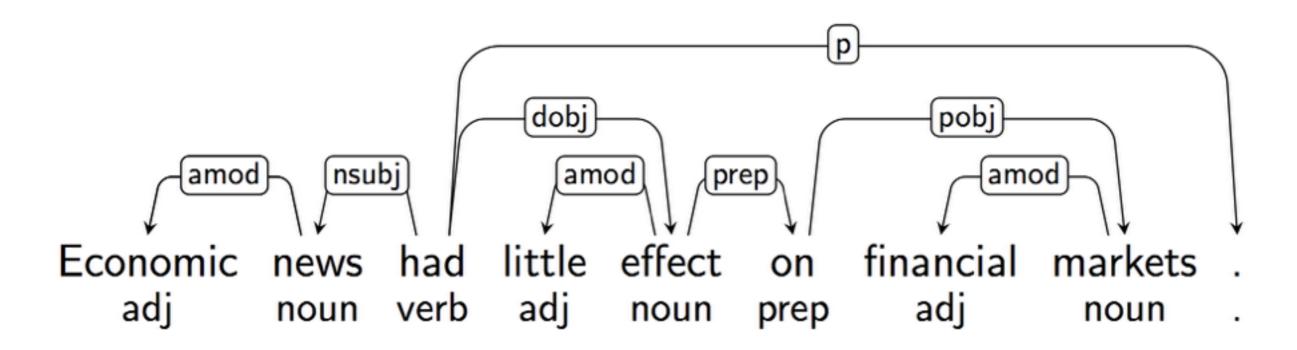
```
Economic news had little effect on financial markets . adj noun verb adj noun prep adj noun .
```

```
Economic news had little effect on financial markets adj noun verb adj noun prep adj noun
```

```
Economic news had little effect on financial markets adj noun verb adj noun prep adj noun
```

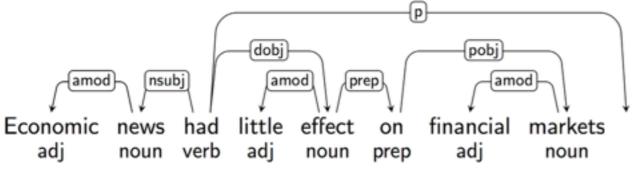
```
Economic news had little effect on financial markets adj noun verb adj noun prep adj noun
```



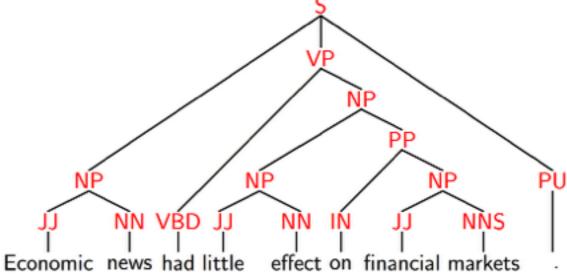


# Dependency vs. Constituency Syntax

- head-dependent relations (directed arcs),
- functional categories (arc labels),
- possibly some structural categories (parts-of-speech)



- phrases (nonterminal nodes),
- structural categories (nonterminal labels),
- possibly some functional categories (grammatical functions)



## Dependency Graphs

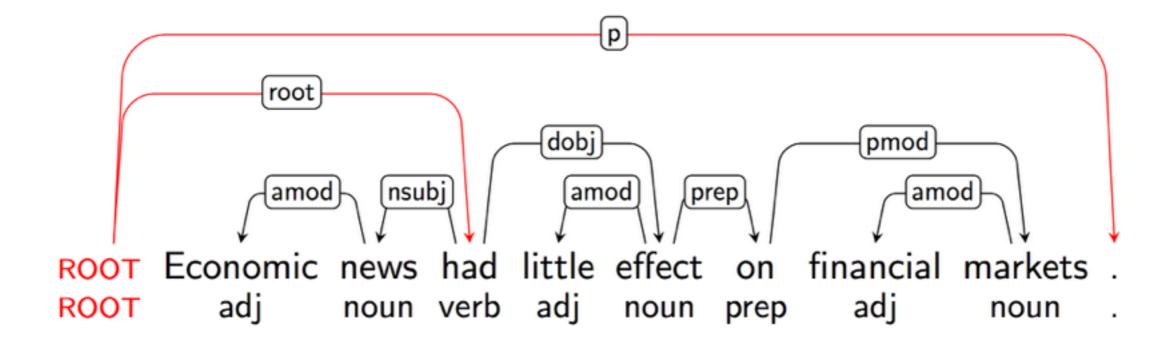
- A dependency structure can be defined as a directed graph G, consisting of
  - a set V of nodes (vertices),
  - a set A of arcs (directed edges),
  - a linear precedence order < on V (word order).</p>
- Labeled graphs:
  - Nodes in V are labeled with word forms (and annotation).
  - Arcs in A are labeled with dependency types:
    - ▶  $L = \{l_1, ..., l_{|L|}\}$  is the set of permissible arc labels.
    - Every arc in A is a triple (i, j, k), representing a dependency from  $w_i$  to  $w_j$  with label  $I_k$ .

# Formal Properties of Dependency Graphs

- For a dependency graph G = (V, A)
- ▶ With label set  $L = \{l_1, \dots, l_{|L|}\}$ ▶  $i \to j \equiv \exists k : (i, j, k) \in A$ ▶  $i \leftrightarrow j \equiv i \to j \lor j \to i$ ▶  $i \to^* j \equiv i = j \lor \exists i' : i \to i', i' \to^* j$ ▶  $i \leftrightarrow^* j \equiv i = j \lor \exists i' : i \leftrightarrow i', i' \leftrightarrow^* j$
- ► *G* is (weakly) connected:
  - ▶ If  $i, j \in V$ ,  $i \leftrightarrow^* j$ .
- ► *G* is acyclic:
  - ▶ If  $i \rightarrow j$ , then not  $j \rightarrow^* i$ .
- G obeys the single-head constraint:
  - ▶ If  $i \rightarrow j$ , then not  $i' \rightarrow j$ , for any  $i' \neq i$ .
- ► *G* is projective:
  - ▶ If  $i \rightarrow j$ , then  $i \rightarrow^* i'$ , for any i' such that i < i' < j or j < i' < i.

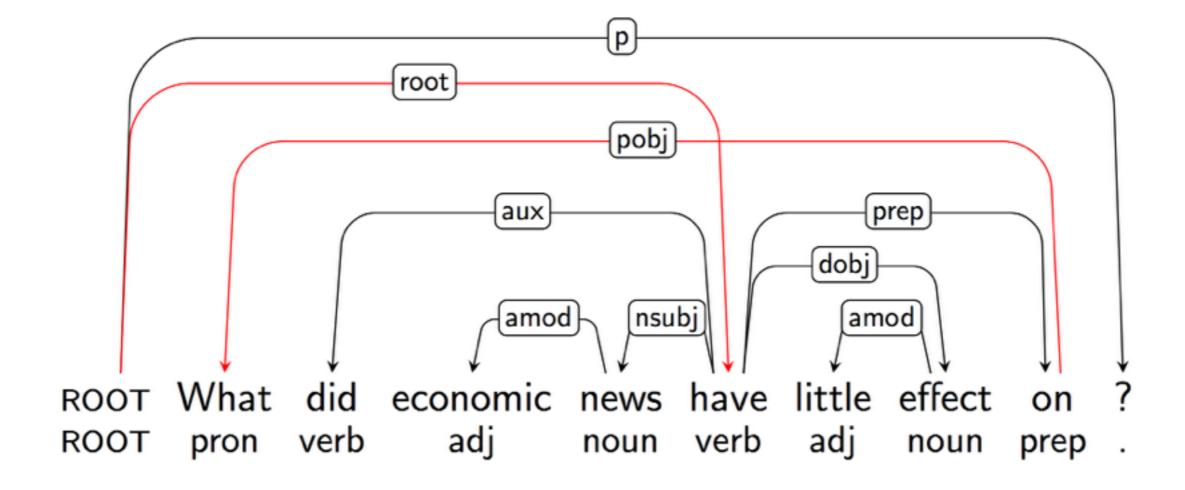
## Projective Dependency Trees

- Single-Headedness
- Acyclicity
- Connectedness (by adding a special root node)
- Projective



## Non-Projective Dependency Trees

- Long-Distance Dependencies
- Free Word Order



# Dependency Parsing

- ► The problem:
  - ▶ Input: Sentence  $x = w_0, w_1, \dots, w_n$  with  $w_0 = ROOT$
  - ▶ Output: Dependency graph G = (V, A) for x where:
    - $V = \{0, 1, \dots, n\}$  is the vertex set,
    - ▶ A is the arc set, i.e.,  $(i, j, k) \in A$  represents a dependency from  $w_i$  to  $w_j$  with label  $I_k \in L$
- Two main approaches:
  - Grammar-based parsing
    - Context-free dependency grammar
    - Lexicalized context-free grammars
    - Constraint dependency grammar
  - Data-driven parsing
    - Graph-based models
    - Transition-based models
    - Easy-first parsing
    - Hybrids: grammar+data-driven, ensembles, etc.

#### Transition-Based Models

- Define a transition system for dependency parsing
- Learn a model for scoring possible transitions
- Parse by searching for the optimal transition sequence

```
Configuration: (S, B, A)

Initial: ([], [0, 1, ..., n], \{ \})

Terminal: (S, [], A)

Shift: (S, i|B, A) \Rightarrow (S|i, B, A)

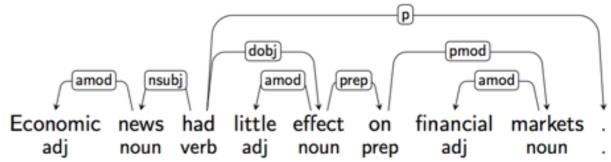
Reduce: (S|i, B, A) \Rightarrow (S, B, A)

Right-Arc(k): (S|i, j|B, A) \Rightarrow (S|i|j, B, A \cup \{(i, j, k)\})

Economic news adj noun
```

 $(S|i,j|B,A) \Rightarrow (S,j|B,A \cup \{(j,i,k)\})$ 

Left-Arc(k):



#### Arc-Eager Transition System

**Configuration:** (S, B, A) [S = Stack, B = Buffer, A = Arcs]

Initial:  $([], [0, 1, ..., n], \{])$ 

Terminal: (S, [], A)

**Shift:**  $(S, i|B, A) \Rightarrow (S|i, B, A)$ 

**Reduce:**  $(S|i,B,A) \Rightarrow (S,B,A)$  h(i,A)

Right-Arc(k):  $(S|i,j|B,A) \Rightarrow (S|i|j,B,A \cup \{(i,j,k)\})$ 

**Left-Arc(k):**  $(S|i,j|B,A) \Rightarrow (S,j|B,A \cup \{(j,i,k)\}) \neg h(i,A) \land i \neq 0$ 

Notation: S|i = stack with top i and remainder S

j|B =buffer with head j and remainder B

h(i, A) = i has a head in A

#### Shift

[] ROOT, Economic, news, had, little, effect, on, financial, markets, .]

[ROOT] [Economic, news, had, little, effect, on, financial, markets, .]

ROOT Economic news had little effect on financial markets adj noun verb adj noun prep adj noun

#### Shift

Economic, news, had, little, effect, on, financial, markets, .] ROOT

ROOT, Economic news, had, little, effect, on, financial, markets, .

ROOT Economic news had little effect on financial markets noun verb adj noun adj adj prep noun

## Left-Arc(amod)

ROOT, Economic news, had, little, effect, on, financial, markets, .

news, had, little, effect, on, financial, markets, . ROOT

```
amod
ROOT Economic news had little effect
                                      on financial markets
                                            adj
        adj
               noun verb adj
                                     prep
                               noun
                                                    noun
```

#### Shift

[ROOT] [news, had, little, effect, on, financial, markets, .]

ROOT, news

had, little, effect, on, financial, markets, .

ROOT Economic news had little effect on financial markets adj noun verb adj noun prep adj noun

## Left-Arc(nsubj)

ROOT, news had, little, effect, on, financial, markets, .

ROOT

had, little, effect, on, financial, markets, .

```
amod
```

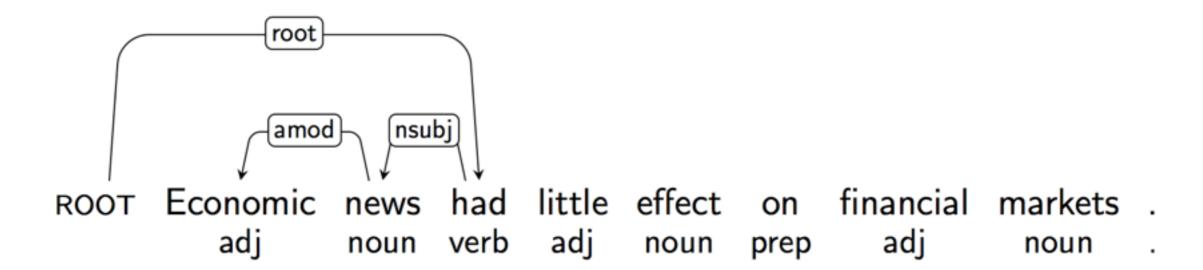
ROOT Economic news had little effect on financial markets noun verb adj noun adj adj prep noun

# Right-Arc(root)

[ROOT] [had, little, effect, on, financial, markets, .]

ROOT, had

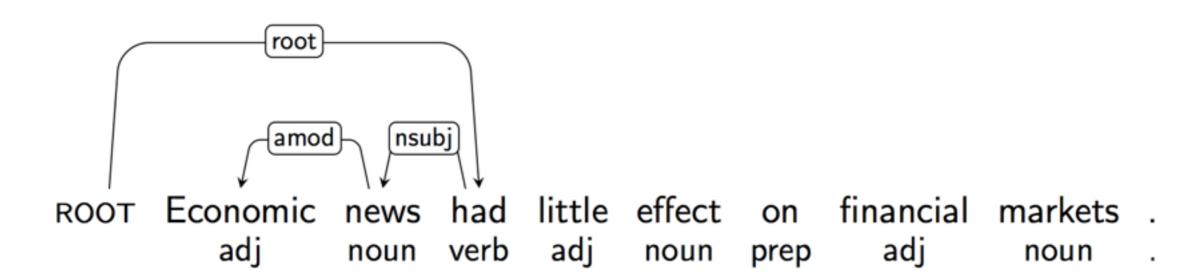
little, effect, on, financial, markets, .]



#### Shift

[ROOT, had] [little, effect, on, financial, markets, .]

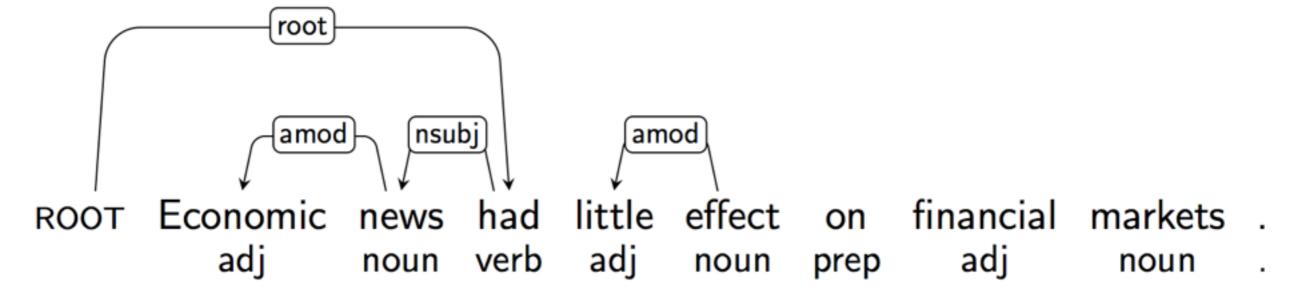
ROOT, had, little [effect, on, financial, markets, .]



## Left-Arc(amod)

[ROOT, had, little] [effect, on, financial, markets, .]

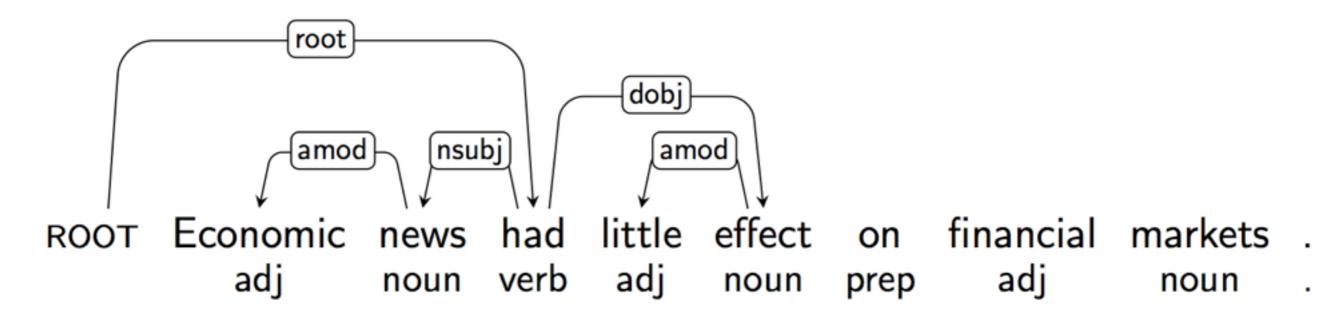
[ROOT, had] [effect, on, financial, markets, .]



# Right-Arc(dobj)

ROOT, had effect, on, financial, markets, .

ROOT, had, effect on, financial, markets, .

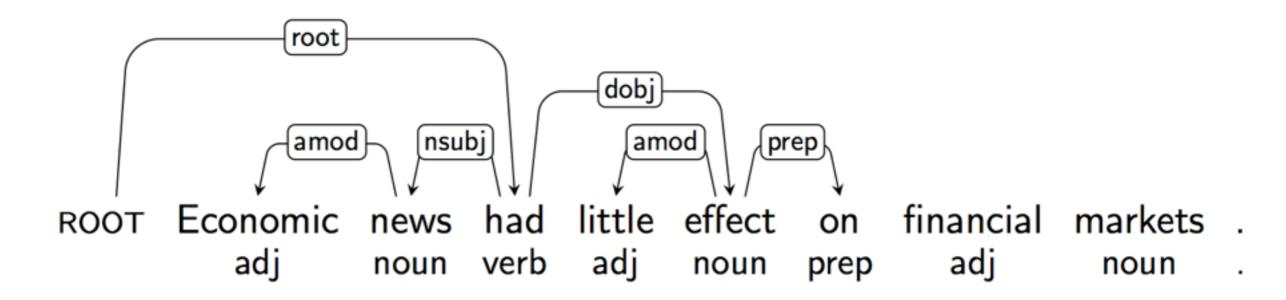


# Right-Arc(prep)

ROOT, had, effect on, financial, markets, .

ROOT, had, effect, on

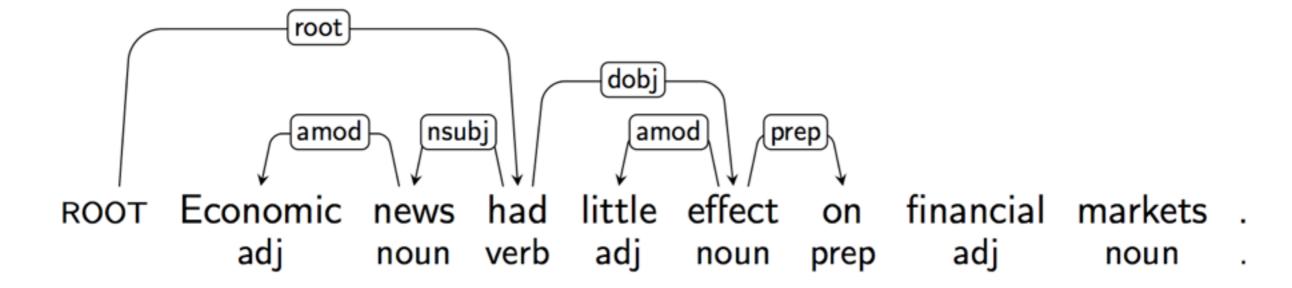
financial, markets, .



#### Shift

[ROOT, had, effect, on] [financial, markets, .]

[ROOT, had, effect, on, financial] [markets, .]

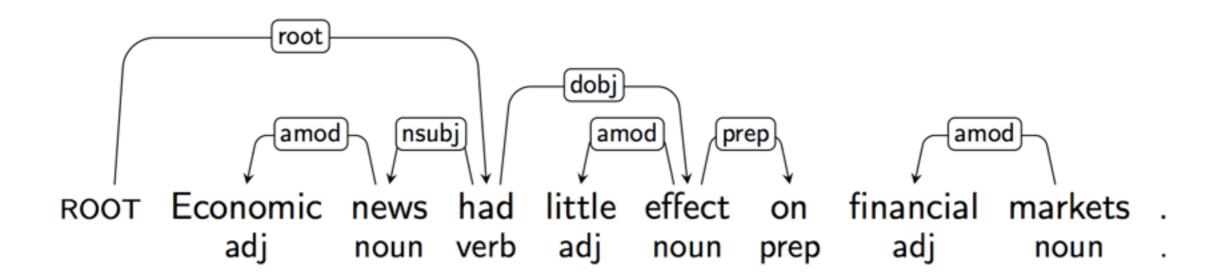


## Left-Arc(amod)

ROOT, had, effect, on, financial markets, .]

ROOT, had, effect, on

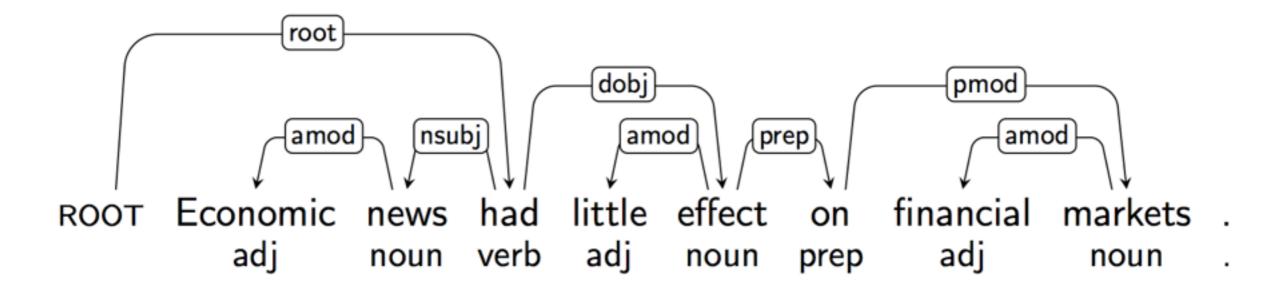
markets, .



# Right-Arc(pmod)

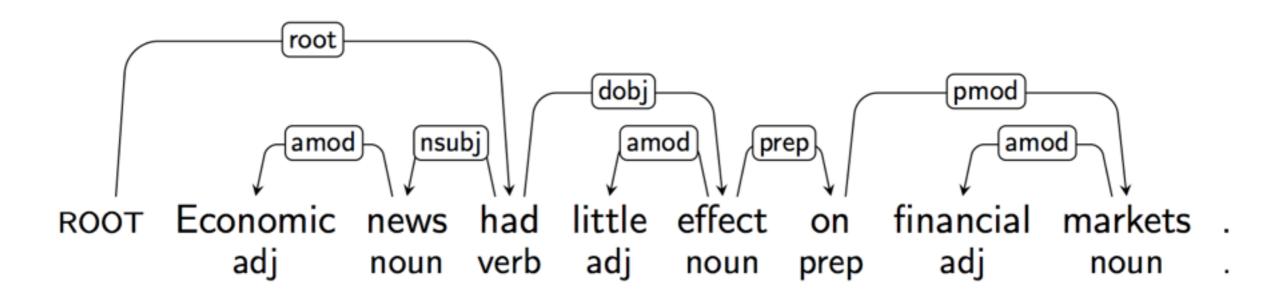
ROOT, had, effect, on markets, .]

ROOT, had, effect, on, markets



#### Reduce

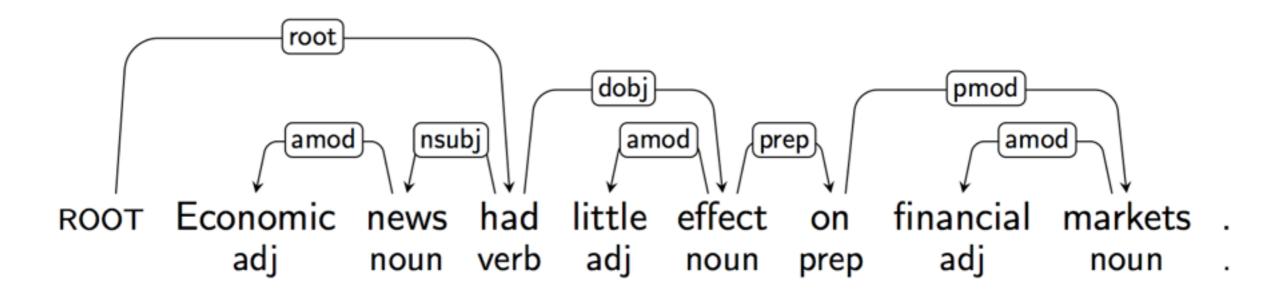
```
ROOT, had, effect, on, markets [.]
```



#### Reduce

```
ROOT, had, effect, on [.]

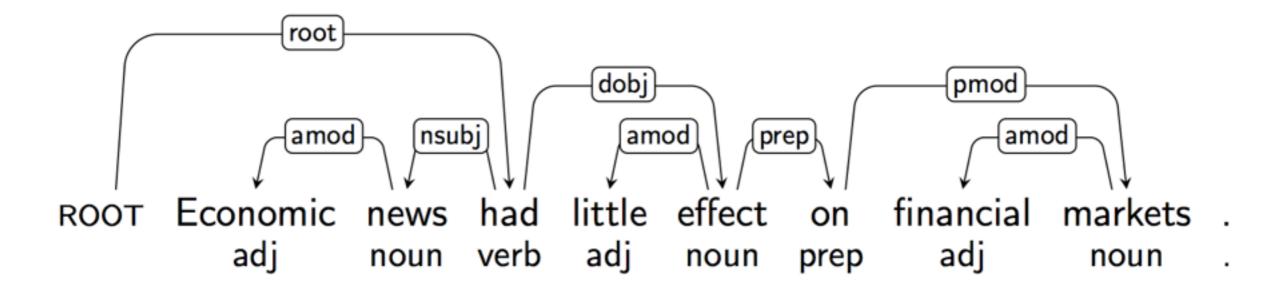
ROOT, had, effect [.]
```



#### Reduce

```
[ROOT, had, effect] [.]

[ROOT, had] [.]
```



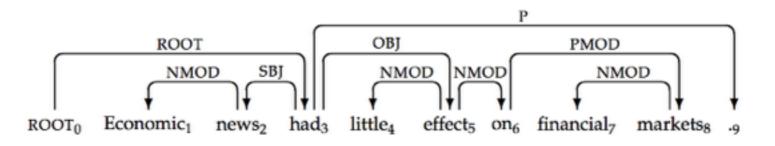
## Right-Arc(p)

```
[ROOT, had] [.]

ROOT, had, .]
```

```
p
        root
                            dobj
                                                   pmod
                nsubj
                              amod
                                       prep
        amod
                                                       amod
Economic
                           little effect
                                               financial
                                                          markets
            news
                    had
                                          on
                    verb
                           adj
                                                  adj
     adj
             noun
                                  noun
                                         prep
                                                            noun
```

## Arc-Eager Transition Sequence



```
Transition
                               Configuration
                                    [0],
                                                   [1, \ldots, 9],
                                                    [2, \ldots, 9],
                                   [0,1],
              SHIFT \Longrightarrow
                                                    [2,...,9], A_1 = \{(2, NMOD, 1)\}
 LEFT-ARC_{NMOD} \Longrightarrow ([0],
                                                    [3, \ldots, 9],
              SHIFT \Longrightarrow ([0,2],
                                                                   A_1
                                                   [3,\ldots,9], A_2=A_1\cup\{(3,SBJ,2)\}
     Left-Arc_{SBI} \Longrightarrow ([0],
RIGHT-ARC<sup>e</sup><sub>ROOT</sub> \Longrightarrow ( [0,3],
                                                   [4,\ldots,9], A_3 = A_2 \cup \{(0,ROOT,3)\}
              SHIFT \Longrightarrow ( [0,3,4],
                                                   [5, \ldots, 9],
                                                                  A_3
                                                   [5,\ldots,9], A_4 = A_3 \cup \{(5, NMOD, 4)\}
 Left-Arc_{NMOD} \Longrightarrow ([0,3],
  RIGHT-ARC<sup>e</sup><sub>OBJ</sub> \Longrightarrow ( [0,3,5], [6,...,9], A_5 = A_4 \cup \{(3,OBJ,5)\}
RIGHT-ARC<sup>e</sup><sub>NMOD</sub> \Longrightarrow ( [0,...,6], [7,8,9],
                                                                   A_6 = A_5 \cup \{(5, NMOD, 6)\}
              SHIFT \Longrightarrow ([0,...,7], [8,9],
                                                                   A_6
 Left-Arc_{NMOD} \Longrightarrow ([0,...6],
                                                                   A_7 = A_6 \cup \{(8, \text{NMOD}, 7)\}
                                                   [8,9],
RIGHT-ARC<sup>e</sup><sub>PMOD</sub> \Longrightarrow ( [0,...,8], [9],
                                                                   A_8 = A_7 \cup \{(6, PMOD, 8)\}
                                   [0, \ldots, 6],
          Reduce \Longrightarrow (
                                                   [9],
                                                                   A_8
                                                    [9],
          Reduce \Longrightarrow (
                                   [0,3,5],
                                                                   A_8
          Reduce \Longrightarrow
                                   [0,3],
                                                    [9],
                                                                   A_8
    RIGHT-ARC_{P}^{e} \Longrightarrow
                                                    [],
                                                                   A_9 = A_8 \cup \{(3, P, 9)\}
                                    [0,3,9],
```

### Oracle Transition Sequence

```
Algorithm 1 Oracle-Parser (x = (w_1, \dots, w_n), h, d)

1: c = c_0 {initial configuration}

2: T = \emptyset {initial empty transition sequence}

3: while c = (\sigma, \tau, h, d) is not terminal do

4: if \sigma = \epsilon then

5: t = SHIFT

6: else

7: t = Oracle(\sigma, \tau, h, d) {oracle transition}

8: T = T + t {update transition sequence with transition t}

9: c = t(c) {configuration resulting from transition t}

10: return T
```

#### **Algorithm 2** Oracle $(c = (\sigma|i, j|\tau, h, d))$

```
1: if h(i) = j then

2: return Left-Arc(d(i))

3: else if h(j) = i then

4: return Right-Arc(d(j))

5: else if \exists k \in \sigma(h(j) = k \lor h(k) = j) then

6: return Reduce

7: else

8: return Shift
```

### Transition-Based Models

- Define a transition system for dependency parsing
- Learn a model for scoring possible transitions
- Parse by searching for the optimal transition sequence

```
Configuration: (S, B, A)

Initial: ([], [0, 1, ..., n], \{ \})

Terminal: (S, [], A)

Shift: (S, i|B, A) \Rightarrow (S|i, B, A)

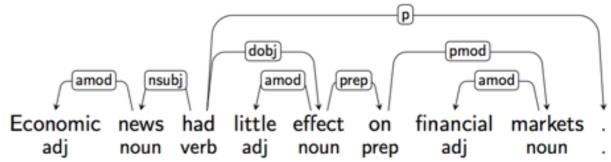
Reduce: (S|i, B, A) \Rightarrow (S, B, A)

Right-Arc(k): (S|i, j|B, A) \Rightarrow (S|i|j, B, A \cup \{(i, j, k)\})

Economic news adj noun
```

 $(S|i,j|B,A) \Rightarrow (S,j|B,A \cup \{(j,i,k)\})$ 

Left-Arc(k):



## Learning Oracle Transitions

► An oracle can be approximated by a (linear) classifier:

$$o(c) = \underset{t}{\operatorname{argmax}} \mathbf{w} \cdot \mathbf{f}(c, t)$$

- ▶ History-based feature representation  $\mathbf{f}(c, t)$
- Weight vector w learned from treebank data

## Learning Oracle Transitions

- Given a treebank:
  - Reconstruct oracle transition sequence for each sentence
  - ▶ Construct training data set  $D = \{(c, t) | o(c) = t\}$
  - ▶ Maximize accuracy of local predictions o(c) = t
- Any (unstructured) classifier will do (SVMs are popular)
- Training is local and restricted to oracle configurations

# Greedy Parsing

```
Parse(w_1, ..., w_n)

1 c \leftarrow ([]_S, [0, 1, ..., n]_B, \{])

2 while B_c \neq []

3 t \leftarrow o(c)

4 c \leftarrow t(c)

5 return G = (\{0, 1, ..., n\}, A_c)
```

- Complexity given by upper bound on number of transitions
- ightharpoonup Parsing in O(n) time for the arc-eager transition system

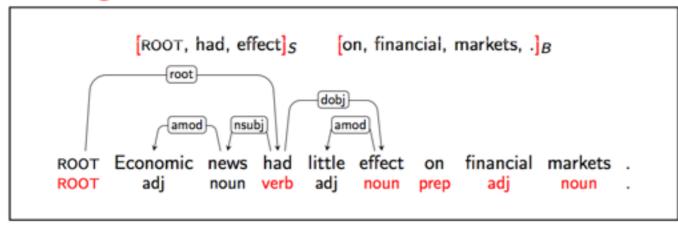
# Linear-Time Transition-Based Parsing

- o(c) and t(c) can be computed in constant time
- PUSH transitions: Shift and Right-Arc
- POP transitions: Left-Arc and Reduce
- at most *n* PUSH transitions to reach a terminal configuration from the initial one
- POP transitions bounded by PUSH transitions

### Static PoS Features

► Features over input tokens relative to S and B

### Configuration



#### **Features**

```
pos(S_2) = ROOT

pos(S_1) = verb

pos(S_0) = noun

pos(B_0) = prep

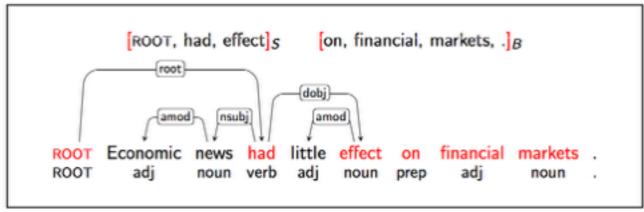
pos(B_1) = adj

pos(B_2) = noun
```

### Static Lexical Features

► Features over input tokens relative to S and B

### Configuration



#### **Features**

```
word(S_2) = ROOT

word(S_1) = had

word(S_0) = effect

word(B_0) = on

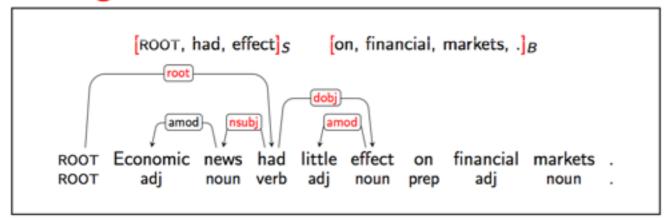
word(B_1) = financial

word(B_2) = markets
```

### Dynamic Syntactic Features

- Features over input tokens relative to S and B
- Features over the (partial) dependency graph defined by A

### Configuration



#### **Features**

```
dep(S_1) = root

dep(lc(S_1)) = nsubj

dep(rc(S_1)) = dobj

dep(S_0) = dobj

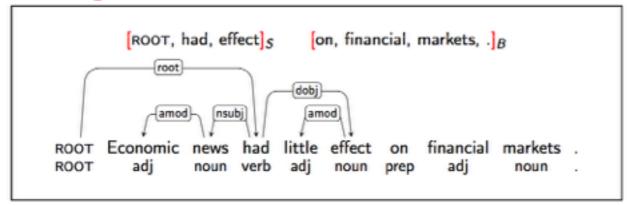
dep(lc(S_0)) = amod

dep(rc(S_0)) = NIL
```

### Dynamic Historical Features

- Features over input tokens relative to S and B
- Features over the (partial) dependency graph defined by A
- Features over the (partial) transition sequence

### Configuration



#### **Features**

```
t_{i-1} = \text{Right-Arc(dobj)}

t_{i-2} = \text{Left-Arc(amod)}

t_{i-3} = \text{Shift}

t_{i-4} = \text{Right-Arc(root)}

t_{i-5} = \text{Left-Arc(nsubj)}

t_{i-6} = \text{Shift}
```

Feature representation unconstrained by parsing algorithm

# Greedy Local Transition-Based Parsing

### Advantages:

- Highly efficient parsing linear time complexity with constant time oracles and transitions
- Rich history-based feature representations no rigid constraints from inference algorithm

#### Drawback:

- Sensitive to search errors and error propagation due to greedy inference and local learning
- The major question in transition-based parsing has been how to improve learning and inference, while maintaining high efficiency and rich feature models

### Evaluation Metrics

- Standard setup:
  - ► Test set  $\mathcal{E} = \{(x_1, G_1), (x_2, G_2), \dots, (x_n, G_n)\}$
  - ▶ Parser predictions  $P = \{(x_1, G'_1), (x_2, G'_2), ..., (x_n, G'_n)\}$
- Evaluation on the word (arc) level:
  - Labeled attachment score (LAS) = head and label
  - Unlabeled attachment score (UAS) = head
  - Label accuracy (LA) = label
- Evaluation on the sentence (graph) level:
  - Exact match (labeled or unlabeled) = complete graph
- ▶ NB: Evaluation metrics may or may not include punctuation

# Multilingual Dependency Parsing

Parsing accuracy for 7 parsers on 13 languages, measured by labeled attachment score (LAS), unlabeled attachment score (UAS) and label accuracy (LA). NP-L = non-projective list-based; P-L = projective list-based; P-E = projective arc-eager stack-based; P-E = projective arc-eager stack-based; P-S = projective arc-standard stack-based; PP-S = pseudo-projective arc-standard stack-based; McD = McDonald, Lerman and Pereira (2006); Niv = Nivre et al. (2006).

	Labeled Attachment Score (LAS)								
Language	NP-L	P-L	PP-L	P-E	PP-E	P-S	PP-S	McD	Niv
Arabic	63.25	63.19	63.13	64.93	64.95	65.79	66.05	66.91	66.71
Bulgarian	87.79	87.75	87.39	87.75	87.41	86.42	86.71	87.57	87.41
Chinese	85.77	85.96	85.96	85.96	85.96	86.00	86.00	85.90	86.92
Czech	78.12	76.24	78.04	76.34	77.46	78.18	80.12	80.18	78.42
Danish	84.59	84.15	84.35	84.25	84.45	84.17	84.15	84.79	84.77
Dutch	77.41	74.71	76.95	74.79	76.89	73.27	74.79	79.19	78.59
German	84.42	84.21	84.38	84.23	84.46	84.58	84.58	87.34	85.82
Japanese	90.97	90.57	90.53	90.83	90.89	90.59	90.63	90.71	91.65
Portuguese	86.70	85.91	86.20	85.83	86.12	85.39	86.09	86.82	87.60
Slovene	70.06	69.88	70.12	69.50	70.22	72.00	71.88	73.44	70.30
Spanish	80.18	79.80	79.60	79.84	79.60	78.70	78.42	82.25	81.29
Swedish	83.03	82.63	82.41	82.63	82.41	82.12	81.54	82.55	84.58
Turkish	64.69	64.49	64.37	64.37	64.43	64.67	64.73	63.19	65.68
Average	79.77	79.19	79.49	79.33	79.63	79.38	79.67	80.83	80.75