



High-speed video analysis of forward and backward spattered blood droplets



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ABSTRACT

High-speed videos of blood spatter due to a gunshot taken by the Ames Laboratory Midwest Forensics Resource Center (MFRC) [1] are analyzed. The videos used in this analysis were focused on a variety of targets hit by a bullet which caused either forward, backward, or both types of blood spatter. The analysis process utilized particle image velocimetry (PIV) and particle analysis software to measure drop velocities as well as the distributions of the number of droplets and their respective side view area. The results of this analysis revealed that the maximal velocity in the forward spatter can be about 47 ± 5 m/s and for the backward spatter – about 24 ± 8 m/s. Moreover, our measurements indicate that the number of droplets produced is larger in forward spatter than it is in backward spatter. In the forward and backward spatter the droplet area in the side-view images is approximately the same. The upper angles of the close-to-cone domain in which droplets are issued in forward and backward spatter are, $27 \pm 9^\circ$ and $57 \pm 7^\circ$, respectively, whereas the lower angles of the close-to-cone domain are $28 \pm 12^\circ$ and $30 \pm 18^\circ$, respectively. The inclination angle of the bullet as it penetrates the target is seen to play a large role in the directional preference of the spattered blood. Also, muzzle gases, bullet impact angle, as well as the aerodynamic wake of the bullet are seen to greatly influence the flight of the droplets. The intent of this investigation is to provide a quantitative basis for current and future research on bloodstain pattern analysis (BPA) of either forward or backward blood spatter due to a gunshot.

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1. Introduction

Working for project No. 06-S-02 for the Midwest Forensics Resource Center (MFRC), T.L. Laber, B.P. Epstein, and M.C. Taylor took a series of over 500 high-speed videos of common bloodletting mechanisms [2]. The set of videos includes blood spatter formation due to a gunshot, blood spatter due to a blunt object such as a hammer, or blood drop formation from a single droplet and is located on the MFRC website [1]. In literature, the videos have been referred to before [3–5], and are routinely used in bloodstain pattern analysis (BPA) presentation and training classes. However, a quantitative analysis of this dataset is still unavailable, especially for the scenario of blood spatter due to a gunshot. Accordingly, the aim of the present work is in quantitative analysis of blood spatter induced by a gunshot to facilitate the BPA community tools for scientific analysis of a crime scene event.

Blood is a complex non-Newtonian fluid which is shear-thinning [6–8], exhibits viscoelastic behavior [8–11] and possesses a yield stress [12]. It is an aqueous suspension which contains plasma and particles such as white and red blood cells, and platelets. Blood starts to coagulate when it leaves the body or under conditions of increased shear stress [13]. The rheology of blood could affect the atomization process [14–16] which is of fundamental importance for BPA because it determines the distribution of drop sizes and velocities [17], thus the resulting blood spatter. The atomization is diminished by the effects of viscoelasticity [18–20], and the resulting size of the impacting droplets can be heavily influenced by viscosity and elasticity of liquid [21–26]. Therefore, an accurate crime scene reconstruction from any crime involving blood spatter must account for the rheological behavior of blood.

The uncertainties of different BPA techniques can be significant, up to a 50% overestimation of the height of the origin of a blood spatter [5]. A better understanding of the mechanisms of blood droplet formation and flight is required. The first theoretical steps in this direction are already available [27]. Such efforts would be significantly facilitated by a thorough analysis of the available

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experimental data, e.g. high-speed videos [4]. It should be emphasized that some experimental simplifications do not necessarily reflect the real crime scene situations. For example, oftentimes, human blood is substituted for swine blood for safety reasons, and because of expected similarities in size and concentration of blood cells, and in rheology [5,27], albeit it is definitely not a perfect substitute [28]. Moreover, blood spatter found in some crime scenes could be affected by the dynamic effect of muzzle gases from a firearm which are significant, especially when the gun is close to its target [29]. Crime scene reconstruction after a gunshot is often simplified by neglecting gravity and air drag, resulting in what is called a straight-line assumption, or the method of strings [30–34]. Unsurprisingly, this assumption can be quite inaccurate [5,35,36] and as a result, there is a permanent drive for more realistic models [17,27,37–39]. Accordingly, in BPA research, it is imperative to analyze all available sources of data. The MFRC videos are a treasure trove of valuable information for numerous situations. As a result of their untapped nature, they have gone relatively undetected as many groups have attempted their own high-speed video analysis for their specific problems at hand. This has the consequence of building solutions which might work only for a limited set of problems. To avoid such limitations, a general pattern must be analyzed, which is the goal of the present work.

2. Experimental video analysis

The MFRC videos were produced from experiments performed primarily at the Minnesota Bureau of Criminal Apprehension Forensic Science Laboratory, in Minnesota, USA, with some performed at the Christchurch Laboratory of the Institute of Environmental Science and Research, in Christchurch, New Zealand [2]. The camera used to record the experiments was a Photron Fastcam-SA1 High-Speed Digital Video camera with most videos using either a Tamron 90 mm macro lens, Micro Nikkor 55 mm, or Micro Nikkor 105 mm lens. Proper lighting was specific to each experiment which resulted in a variety of apertures and shutter speeds used to produce the highest quality videos possible. Room temperature human blood with an anti-coagulant was used within 72 h of the draw date for every experiment.

Of the series of over 500 videos, over 200 are posted on the MFRC Blood Pattern Analysis Videos webpage, 19 of them are directly related to blood spatter due to a gunshot, and four of those show different muzzle discharges [1]. The targets consisted of a blood soaked sponge, fabric covering the sponge, tape encompassing the entire sponge, and a silicone-encased sponge. The targets were placed at distances in the 1–182 cm range from the muzzle of the gun. Of the 19 videos available for blood spatter induced by a gunshot, five were chosen for a quantitative analysis with particle image velocimetry (PIV) in the present work because they either contained both forward and backward spatter, or, their spatter pattern was resolved enough (in time and space) for an accurate analysis. The five experiments used in this analysis are described in Table 1.

Each frame of the high-speed videos were taken at time intervals of 0.1 ms. In the present work, PIV analysis was conducted to characterize the motion of the blood droplets. The PIV method

relies on recording the positions of fluid particles (here droplets) for two time instances in quick succession of the order of a millisecond. Statistical correlation of the two images with the position of the particles allows for the determination of the velocity field that is the spatial distribution of velocities. Here, PIV is conducted from approximately the time the bullet impacted the sponge to two milliseconds in each experiment. The program used for PIV was PIVlab 1.41 which is an application built for the numerical computing language MATLAB [40]. The analysis was done with a Fast Fourier Transform (FFT) algorithm with four interrogation passes from 64, 32, 16, and finally 8 square pixels. A linear interpolator was used with a Gauss 2×3 -point sub-pixel estimator and the contrast of each image was automatically locally enhanced before processing. A region of interest mask of 100×200 pixels was drawn about a centimeter from the target for back spatter, and half a centimeter from the target for forward spatter. The dimensions for the region of interest were chosen so that it would be sufficiently large enough to capture the created spray of blood droplets, yet not too large as to increase the likelihood of a false reading by including phantom vectors. The location of the region of interest away from the target was dictated by the distance at which droplets became recognizable, as it was centered about the splash of blood droplets. Post-processing vector validation was performed, in which physically impossible vectors were deleted as outliers.

Each experiment was also analyzed for the area of each droplet, measured as the area of the droplet in flight as seen directly from frames of the high-speed videos, and the number of droplets located within a region of interest. This was done using ImageJ [41], utilizing the particle analysis toolset. A rectangular region of interest, 100×200 pixels large, was placed at approximately the same respective location as done in the PIV tests. Each experiment was analyzed at approximately 2 ms, a time which was chosen because the droplets became very easily distinguishable from the background. Automatic local thresholding was performed on each image following the method of Phansalkar et al. [42] with a thresholding radius of 15 pixels, $k=0.25$, and $r=0.5$. This converted each image into a binary image which was then analyzed with the particles toolset. There were no pixel-size limiting or circularity-based restrictions imposed on the analysis.

3. Results and discussion

The PIV technique described in Section 2 was employed to find the velocity magnitude at the midplane of the region of interest, parallel to the target face. For each time interval between the frames of interest, the velocity magnitude along this midplane was averaged and then these velocities were plotted against the time reckoned from the bullet impact on the target. For the bare sponge experiments number 7Aa1 and 7Ab1 from Table 1, this process results in Fig. 1. These two experiments are directly comparable with one another because they differ only in the caliber of bullet used and both experiments resulted in forward and backward spatter.

Fig. 1 shows that the larger caliber bullet used in experiment 7Ab1 results in an overall larger average velocity for both

Table 1

Experiments from the MFRC used in this analysis. The experiment number corresponds to a part of the title of a particular video on the MFRC website.

Experiment number	Bullet caliber	Target type	Target distance [cm]
7Aa1	.22	Bare sponge	182
7Ab1	.44	Bare sponge	182
7Cb3	.44	Tape-covered sponge	182
7Db1	.44	Silicone-covered sponge	182
7Db2	.44	Silicone-covered sponge	182

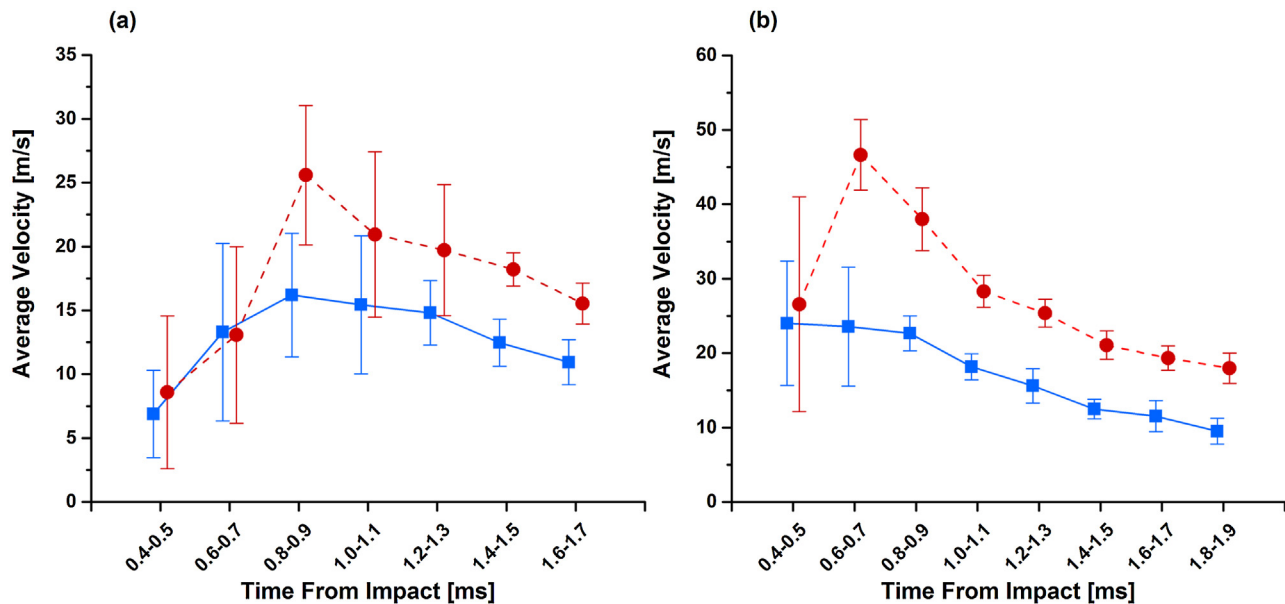


Fig. 1. PIV results for experiment 7Aa1 are shown in panel (a), and for experiment 7Ab1 in panel (b). The red dashed line with circular data points represents the results from forward spatter, and the solid blue line with square data points is for backward spatter. The error bars are the standard deviations of the sets of data. Note that the data points are slightly offset from their corresponding time reckoned from the bullet impact moment in order to more easily distinguish the error bars. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

forward and backward spattered droplets. The difference is apparent from the first data point of the analysis at a time from the bullet impact in the 0.4–0.5 ms range, all the way to the end of the experiment. For either caliber, the forward spattered velocity is larger than that of the backward spattered velocity, even though in Fig. 1a, the velocity gap is only noticeable starting at the 0.8–0.9 ms mark from the bullet impact time, which may be due to a large number of droplets difficult to resolve. A larger forward spatter velocity makes physical sense due to the entraining effect of the bullet traveling in the direction of the blood spatter. It is also interesting to note that as the time from the bullet impact increases, the standard deviation of the data, as indicated by the error bars, decreases due to a more uniform flow field in the corresponding part of the region of interest. The trend of the steep gradient upward and steady decrease in average velocity (cf. Fig. 1) indicates that at the onset of the analysis which was at 0.4 ms after the bullet impact, the blood droplets are accelerated. This means (from the second law of Newton applied to an individual droplet) that droplets analyzed at the onset of the PIV analysis practically do not experience air drag but on the contrary, are pulled forward by the aerodynamic wake of the fast moving, small-sized, preceding droplets from the initial splash. This is similar to the aerodynamic interaction of birds flying in V formation [43]. After about 0.6–0.9 ms, the blood droplets finally begin to slow down due air drag, since at the later stage droplets have already sufficiently separated and their mutual aerodynamic interaction has been diminished. It should be emphasized that not only in forward spatter droplets are initially accelerated but also in the backward spatter (cf. Fig. 1). Therefore, this acceleration cannot be attributed to the aerodynamic effect of bullet preceding droplets in forward spatter but to the mutual entrainment of droplets described above.

The tape-covered sponge of experiment 7Cb3 only produced forward spattered droplets and the results from the PIV analysis are shown in Fig. 2. Since the same bullet caliber and shooting distance as in experiment 7Ab1 were used, the results in Fig. 2 can be directly compared to the forward spatter case of Fig. 1b.

Covering the sponge with tape prevents the onset of backward spatter. Due to the spread of the error bars, an accelerated droplet

motion due to the aerodynamic wake of the preceding droplets is still plausible, however, it is not directly seen in Fig. 2. The magnitude of the average velocity is approximately that of the forward spattered case shown in Fig. 1b. The trend of a decrease in the error bar spread at longer time is still seen, albeit to a lesser extent.

The two experiments with silicone-covered sponges, 7Db1 and 7Db2, were conducted using the same caliber of bullet and the same shooting distance. The results for the 7Db1 and 7Db2 experiments are presented in Fig. 3.

Even though experiments 7Db1 and 7Db2 were conducted under exactly the same conditions as indicated in Table 1, 7Db1 only resulted in forward spatter, whereas 7Db2 revealed both forward and backward spatter. This sheds light on the complexity of performing repeatable BPA experiments: it means that for this set of

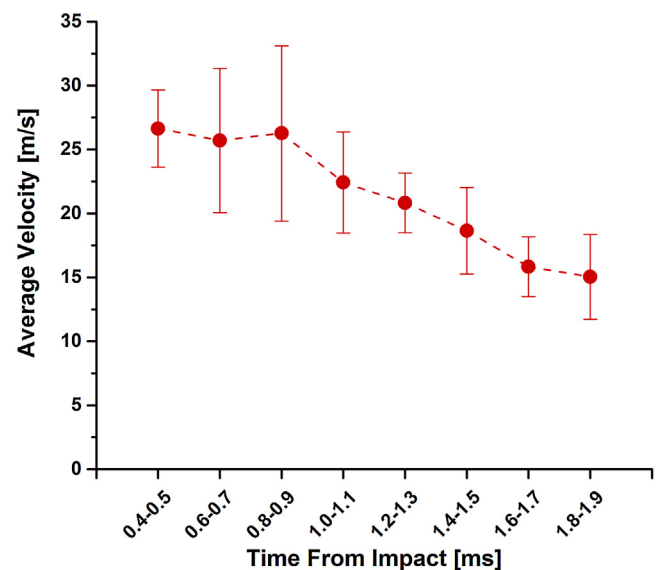


Fig. 2. PIV result for the forward spattered blood data of experiment 7Cb3. The error bars are the standard deviation of the set of data.

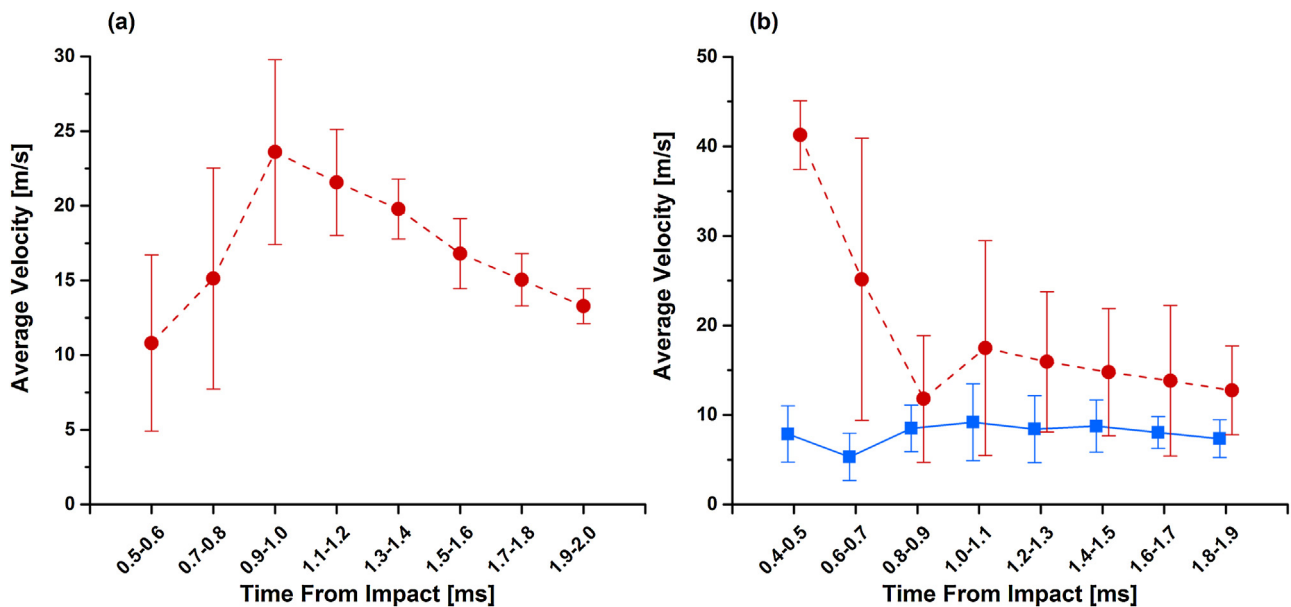


Fig. 3. Droplet velocities for experiment 7Db1 shown in panel (a), and 7Db2 shown in panel (b). The red dashed lines with circular data points represent the results for forward spatter, and the solid blue line with square data points is for backward spatter. The error bars are the standard deviations of the set of data. Note that the data points are once again slightly offset from their corresponding time from impact value in order to more easily distinguish the error bars. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

experiments, there are some uncontrolled factors which result in two very different outcomes. Upon careful inspection of the high-speed videos, it seems that the silicone-encased sponge in experiment 7Db2 held more blood. Even more critically, the blood seems to have pooled to the backside of the target where backward spatter would form. Therefore, the presence of backward spatter in only one of these trials could simply be explained by the undocumented blood filling process of the silicone-encased sponge, or by gravity-driven transport of blood. Regardless of this deficiency, Fig. 3b still reveals the important result of a faster average blood velocity for forward scattered droplets versus backward scattered droplets.

It should be emphasized that the PIV results shown in Figs. 1–3 do not contain data with the initial velocities of the droplets. All data points were taken starting at 0.4 ms after the bullet impacted the target (except for experiment 7Db1 where data started at 0.5 ms due to the inability to accurately resolve the droplets at an earlier moment of time – the early frames are completely blurry). The analysis was only conducted for the time interval when the droplets became clear enough to get accurate results. Droplets were formed before 0.4 ms, but with the current high-speed videos, PIV cannot be utilized to measure their velocity. The high-speed videos seem to show at least two regimes of the expulsion of droplets, the first of which has not been measured by PIV here. The first regime is a very fast moving spray which occurs almost instantaneously after the impact. After about 0.4 ms, the second regime begins to take place where the web of blood issued from the target consists of recognizable droplets moving at a much slower pace. An example of these two regimes can be seen in Fig. 4 which is a frame taken from the high-speed video of experiment 7Aa1.

As described in Section 2, the number of droplets was counted with the particle analysis toolset of ImageJ within a region of interest replicating the one used in the PIV analysis. The results for the number of droplets in each experiment are shown in Fig. 5.

For the three experiments which contained both forward and backward scattered droplets, there were always more forward scattered droplets. In comparing experiments 7Aa1 and 7Ab1, which differ only in the caliber of the bullet, experiment 7Ab1,

corresponding to the larger caliber, produced more droplets in both forward and backward spatter. It also seems as if the experiments with an open-faced bare sponge produce more droplets overall when accounting for the experimental inconsistencies of 7Db1 and 7Db2.

Using the particle analysis toolset of ImageJ, the side view area of each individual droplet can also be determined. An average of all these values in each experiment is shown in Fig. 6

For the experiments which revealed both forward and backward scattered droplets, there is an insignificant difference between the average side view area of droplets in the case of a bare sponge. The silicone-covered sponge in experiment of 7Db2 resulted in much larger backward scattered droplets, albeit

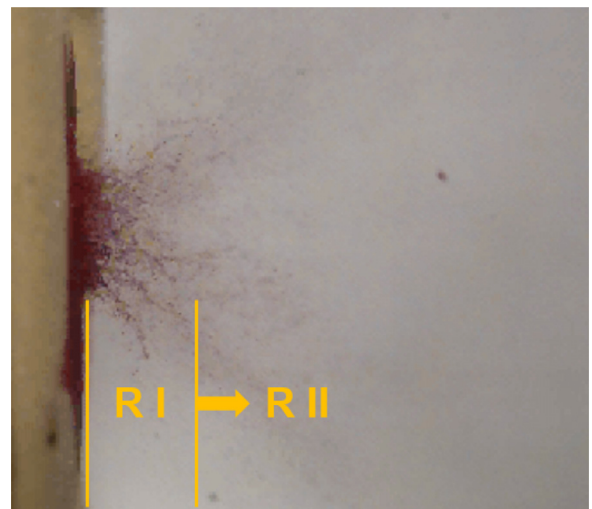


Fig. 4. Cropped image of the backward spatter region of experiment 7Aa1 at 0.1 ms after the bullet impact [1]. The two labels, R I and R II, represent the two regimes found. The first regime, R I, is where recognizable droplets which are relatively large and travel relatively slowly begin to form; they were analyzed by PIV. Note, that as time goes on, the boundary between R I and R II moves towards the right of the image and at about 0.4 ms, individual droplets in R I are easy to resolve.

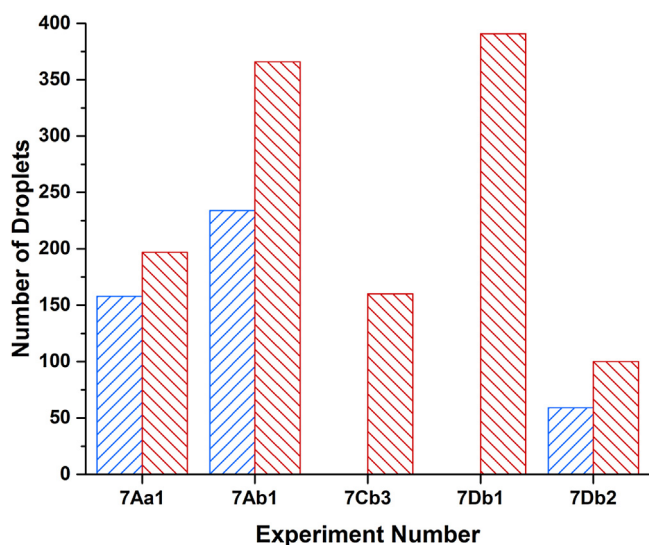


Fig. 5. The number of droplets in the PIV region of interest for each experiment. The red bars with negatively sloped crosshatching are for the forward spatter and the blue bars with positively sloped crosshatching are for backward spatter. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

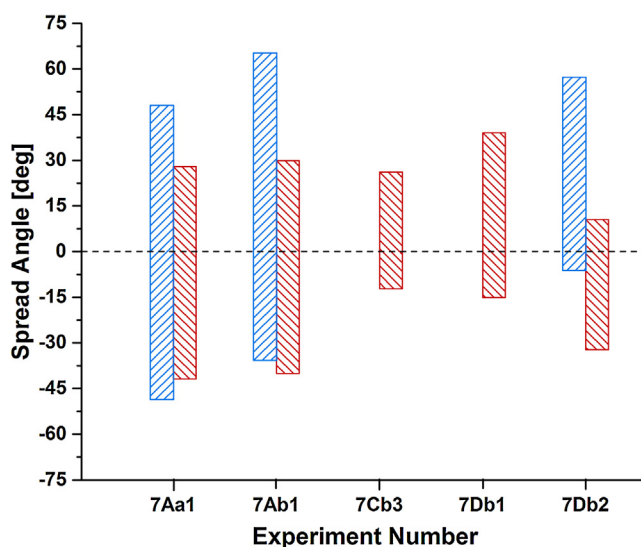


Fig. 7. Spread angles of the close-to-cone domain in which droplet clouds are issued at 0.5 ms. The dashed line is the axis of symmetry of the bullet, the red bars correspond to the forward spatter and the blue bars to the backward spatter. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

that might be due to the blood pooling towards that direction in the sponge as discussed above.

Using the data from the high-speed videos of each experiment at 0.5 ms after the bullet impact, the maximum angular spread of the forward and backward spatter was established by drawing tangents to the issued drop clouds near the target faces and reckoning their angles from the bullet axis. This resulted in the average upper angles of the close-to-cone domain in which droplets are issued for the forward and backward spatter of $27 \pm 9^\circ$ and $57 \pm 7^\circ$, respectively, whereas the lower angles of the close-to-cone domain are $28 \pm 12^\circ$ and $30 \pm 18^\circ$, respectively. The detailed information on these angles is given in Fig. 7, with the lower semi-angles shown as negative.

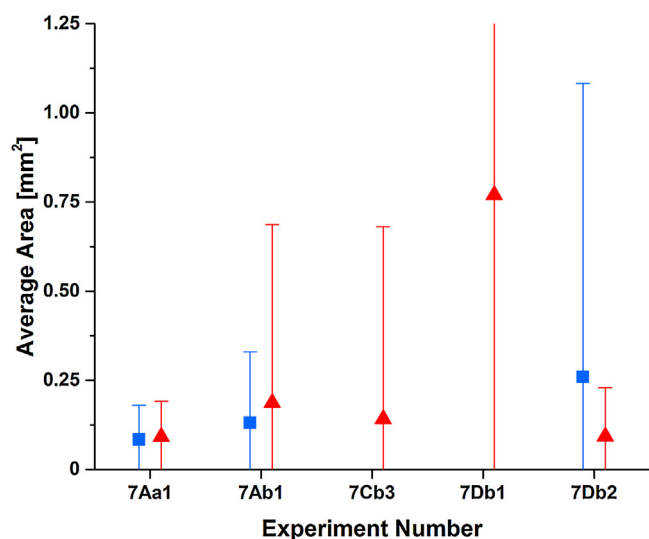


Fig. 6. Average side view area of the droplets in all experimental cases. The red triangles represent forward spattered droplets and the blue squares represent the backward spattered ones. The error bars show the standard deviation. For experiment 7Db1, the error bar for the area about 0.75 mm^2 is too wide to be included in full in this frame. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

Fig. 7 shows that backward spattered droplets have a wider spread angle than the forward spattered ones. The bare sponge experiments 7Aa1 and 7Ab1 revealed an almost symmetric upper and lower angles of the spatter domains in forward and backward spatter. Such symmetry is less prominent in the other experiments which indicates that covering a sponge with silicone or tape results in an uneven distribution of droplets. This is important because the initial droplet cloud significantly determines their further trajectories and shows that the effect of victim's clothes may be crucial for crime scene reconstruction. It should be emphasized that blood droplets were seen to form from the target periphery not penetrated by the bullet and continued to be formed long after the bullet left the target. The above-mentioned angles correspond to 0.5 ms after the bullet impact. However, they vary in time, albeit not too much, i.e. staying close to the values shown in Fig. 7.

The effect of muzzle gases on the blood spattered droplets is more pronounced in experiments where the distance between the muzzle of the gun and target was short. An example of this is shown in a high-speed video not analyzed above, whose experiment number was 7Aa7 which was a .22 cal bullet impacting a blood-impregnated sponge at 50 cm. Several frames of this video are shown in Fig. 8.

While the motion of the muzzle gases is difficult to discern in the still images, it is clearly visible in the video. The effect of the muzzle gases is the following: as time progresses, the droplets do not only move outward from the surface of the sponge, but are also entrained by muzzle gases impinging onto the sponge and turn towards the left, which is against gravity and against backward spatter motion. This phenomena has been discussed in literature before [29], and clearly should not be ignored.

Two more observations worth noting were made when viewing the selection of MFRC videos. Both of them are revealed in the forward spattered section of experiment 7Db2, of which a series of four video frames are shown in Fig. 9.

First, note that the angle of the bullet coming out of the target is not normal to the target face. The forward spattered droplets seem to follow the axis of penetration and as a result, they travel at a downward angle of inclination. Note that this trend is opposite to what is seen for backward spattered droplets in Fig. 8. For that

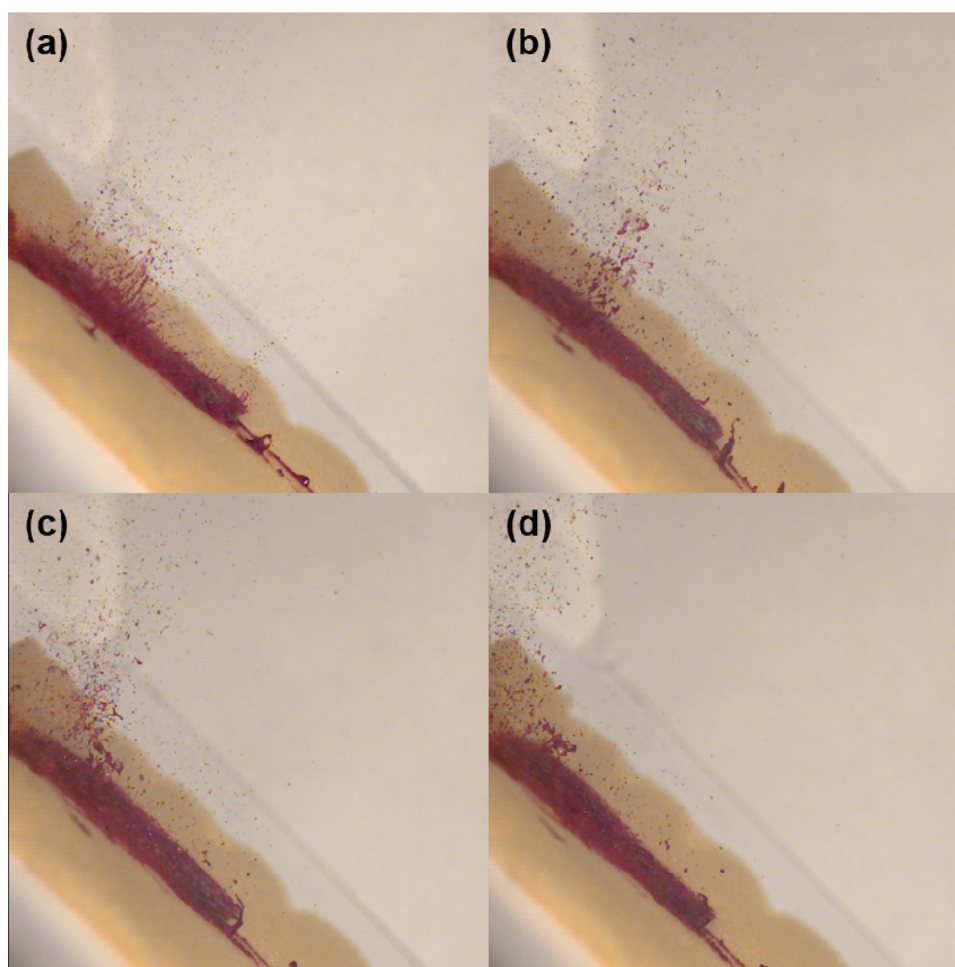


Fig. 8. Frames from experiment 7Aa7 where panel (a) corresponds to 2.4 ms, (b) 6.4 ms, (c) 7.9 ms, and (d) 9.4 ms after the horizontally traveling bullet impacted the inclined sponge [1].

experiment, the bullet traveled horizontally, parallel to the floor, and therefore impacted the sponge target at an angle. The backward spattered droplets are then issued normally to the face of the target, not in preference with the axis of the bullet as seen in forward spatter in Fig. 9.

The final important observation in Fig. 9 is that the issued blood droplets do not continue to travel as their initial trajectory would tend to suggest. For example, looking at the top grouping of droplets in Fig. 9b, notice that they move downward towards the centerline of where the bullet was in Fig. 9c, and then they continue to move in that direction as indicated in Fig. 9d. The same phenomena happen with the bottom grouping of droplets in Fig. 9b, except in reverse. This means that the droplets initially traveling upwards, end up projected downwards, and vice versa for the group initially traveling downwards. The process may be difficult to visualize with only four frames of experiment 7Db2, but it is clearly visible in the MFRC video online. This phenomena can occur because of two possibilities. First, it might be that the aerodynamic wake forming behind the bullet is causing the droplets to spiral about the axis of penetration, a process which would be very difficult to see from this viewpoint and might manifest itself as this artifact. Second, the low pressure zone within the wake of the bullet may be causing the droplets to travel opposite to their initial direction. With the current set of MFRC videos, it is impossible to accurately deduce a reason. It should be emphasized that in the other videos used in this analysis which

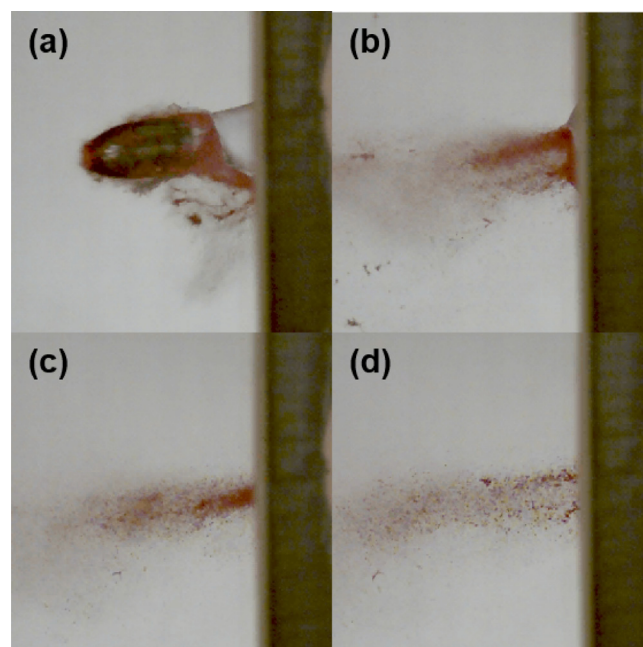


Fig. 9. Frames from the forward spattered portion of experiment 7Db2 [1]. Panel (a) is 0.2 ms, (b) 0.8 ms, (c) 1.1 ms, and (d) 1.5 ms after the bullet impacted the silicon-encased sponge target.

contained forward spatter, this phenomena were only observed in experiment 7Db2.

4. Conclusion

Five different videos from the MFRC were quantitatively analyzed with PIV and droplet detection software. The videos are freely available to the public [1] as well as the droplet detection software used which was ImageJ. A toolset called analyze particles was used after the image was converted to binary with the use of a standard, automatic local thresholding method. The PIV software was PIVlab 1.41 which is a free application that works within the MATLAB environment [40]. The average velocity of both forward spattered and backward spattered droplets, number of droplets, and average side view area were found.

When comparing experiment numbers 7Aa1 and 7Ab1, it was observed that a larger caliber bullet results in more, faster, and larger droplets in both forward and backward spatter. Covering the blood-impregnated sponge target with tape, as was done in experiment 7Cb3, reduced the amount of droplets created, and only produced forward spatter. These droplets were of about the same size as in the experiment with a comparable bullet size, 7Ab1. The average spread angles of the close-to-cone domain of the droplet cloud in the forward and backward spatter for the upper domain were measured as $27 \pm 9^\circ$ and $57 \pm 7^\circ$, respectively, whereas for the lower domain they were $28 \pm 12^\circ$ and $30 \pm 18^\circ$, respectively. Encasing the sponge in silicone produced mixed results which may be attributed to the blood filling process of the sponge. It was also noted that the blood spatter experiments clearly produced two regimes of spatter. In one of the regimes, a fine mist which traveled rapidly and was created immediately after the bullet impacted the target. In another regime larger droplets propagated much slower, and within this regime the analysis contained in this work was performed. The inclination angle of the spattered blood droplets was seen to be influenced by the impact angle of the bullet which is not the case for backward spattered droplets. Additionally, the effect of muzzle gas was prominent and the aerodynamic wake of the bullet may influence the trajectory of the blood spatter.

It was found that in both forward and backward spatter, the droplets analyzed with PIV were moving with an acceleration. This is because those droplets which constitute a dense cloud practically do not experience air drag, and on the contrary are pulled forward by the aerodynamic wake of the preceding droplets spattered initially, at earlier time moments. This effect is similar to the aerodynamic interaction of birds flying in V formation. Only at the later stage when droplets are sufficiently separated, their mutual aerodynamic interaction has been diminished and they started to experience aerodynamic drag and decelerate. The MFRC video database, despite its limits in space and time resolution, contain an immense information that can facilitate the development of BPA models.

Note that the videos analyzed were chosen from the entire MFRC database because they were of high enough quality to extract reliable information on the physical mechanisms of backward and forward blood spatter. It should be emphasized that there is no known recording of the volume of blood which was used in each experiment. From viewing the videos, however, it is clear that a sufficient amount of blood was soaked into the sponge target because blood stains several times larger than the impacting bullet are clearly visible. Nevertheless, in this work we showed that even with such limited accompanying information, the database is a rich source for the exploration of the physical mechanisms of blood spatter aimed in the present work.

The physical aspects of the process which we were able to establish in this work facilitate and confirm the foundations of the detailed numerical models recently developed in Ref. [27], which

describe in detail velocities, sizes and trajectories of blood drops formed in back spatter after a gunshot, as well as their impact angles and velocities, and the stain size they form.

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