

Matt Mazur

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About

Hey there! I'm the founder of [Preceden](#), a web-based timeline maker, and a data analyst consultant. I also built [Lean Domain Search](#) and [many other software products](#) over the years.



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A Step by Step Backpropagation Example

Background

Backpropagation is a common method for training a neural network. There is [no shortage of papers](#) online that attempt to explain how backpropagation works, but few that include an example with actual numbers. This post is my attempt to explain how it works with a concrete example that folks can compare their own calculations to in order to ensure they understand backpropagation correctly.

If this kind of thing interests you, you should [sign up for my newsletter](#) where I post about AI-related projects that I'm working on.

Backpropagation in Python

You can play around with a Python script that I wrote that implements the backpropagation algorithm in [this Github repo](#).

Backpropagation Visualization

For an interactive visualization showing a neural network as it learns, check out my [Neural Network visualization](#).

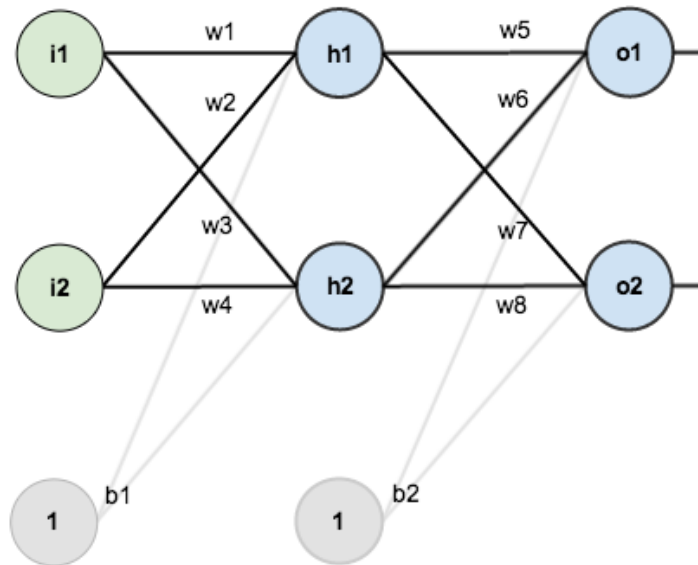
Additional Resources

If you find this tutorial useful and want to continue learning about neural networks, machine learning, and deep learning, I highly recommend checking out Adrian Rosebrock's new book, [Deep Learning for Computer Vision with Python](#). I really enjoyed the book and will have a full review up soon.

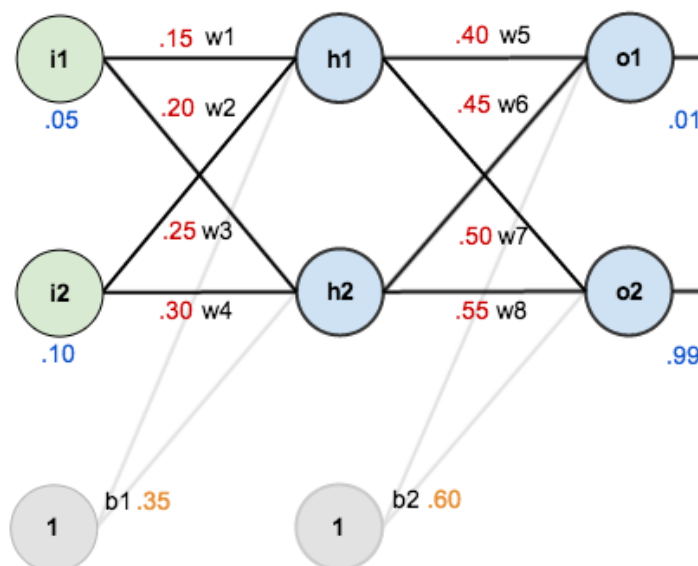
Overview

For this tutorial, we're going to use a neural network with two inputs, two hidden neurons, two output neurons. Additionally, the hidden and output neurons will include a bias.

Here's the basic structure:



In order to have some numbers to work with, here are the **initial weights**, the **biases**, and **training inputs/outputs**:



The goal of backpropagation is to optimize the weights so that the neural network can learn how to correctly map arbitrary inputs to outputs.

For the rest of this tutorial we're going to work with a single training set: given inputs 0.05 and 0.10, we want the neural network to output 0.01 and 0.99.

The Forward Pass

To begin, let's see what the neural network currently predicts given the weights and biases above and inputs of 0.05 and 0.10. To do this we'll feed those inputs forward through the network.

We figure out the *total net input* to each hidden layer neuron, *squash* the total net input using an *activation function* (here we use the *logistic function*), then

repeat the process with the output layer neurons.

Total net input is also referred to as just *net input* by [some sources](#).

Here's how we calculate the total net input for h_1 :

$$net_{h1} = w_1 * i_1 + w_2 * i_2 + b_1 * 1$$

$$net_{h1} = 0.15 * 0.05 + 0.2 * 0.1 + 0.35 * 1 = 0.3775$$

We then squash it using the logistic function to get the output of h_1 :

$$out_{h1} = \frac{1}{1+e^{-net_{h1}}} = \frac{1}{1+e^{-0.3775}} = 0.593269992$$

Carrying out the same process for h_2 we get:

$$out_{h2} = 0.596884378$$

We repeat this process for the output layer neurons, using the output from the hidden layer neurons as inputs.

Here's the output for o_1 :

$$net_{o1} = w_5 * out_{h1} + w_6 * out_{h2} + b_2 * 1$$

$$net_{o1} = 0.4 * 0.593269992 + 0.45 * 0.596884378 + 0.6 * 1 = 1.105905967$$

$$out_{o1} = \frac{1}{1+e^{-net_{o1}}} = \frac{1}{1+e^{-1.105905967}} = 0.75136507$$

And carrying out the same process for o_2 we get:

$$out_{o2} = 0.772928465$$

Calculating the Total Error

We can now calculate the error for each output neuron using the [squared error function](#) and sum them to get the total error:

$$E_{total} = \sum \frac{1}{2}(target - output)^2$$

[Some sources](#) refer to the target as the *ideal* and the output as the *actual*.

The $\frac{1}{2}$ is included so that exponent is cancelled when we differentiate later on. The result is eventually multiplied by a learning rate anyway so it doesn't matter that we introduce a constant here [1].

For example, the target output for o_1 is 0.01 but the neural network output 0.75136507, therefore its error is:

$$E_{o1} = \frac{1}{2}(\text{target}_{o1} - \text{out}_{o1})^2 = \frac{1}{2}(0.01 - 0.75136507)^2 = 0.274811083$$

Repeating this process for o_2 (remembering that the target is 0.99) we get:

$$E_{o2} = 0.023560026$$

The total error for the neural network is the sum of these errors:

$$E_{total} = E_{o1} + E_{o2} = 0.274811083 + 0.023560026 = 0.298371109$$

The Backwards Pass

Our goal with backpropagation is to update each of the weights in the network so that they cause the actual output to be closer the target output, thereby minimizing the error for each output neuron and the network as a whole.

Output Layer

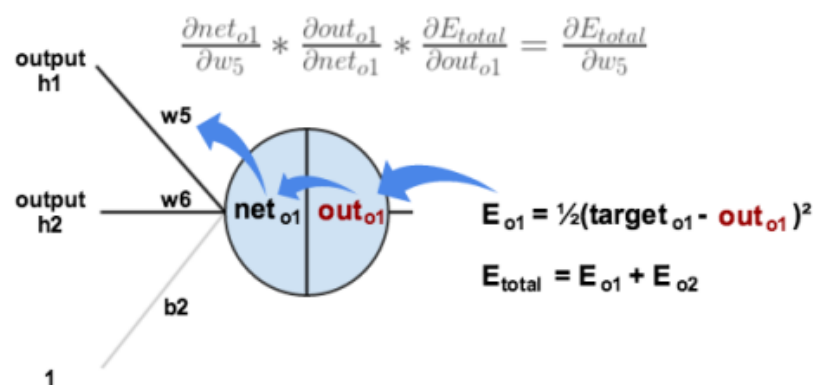
Consider w_5 . We want to know how much a change in w_5 affects the total error, aka $\frac{\partial E_{total}}{\partial w_5}$.

$\frac{\partial E_{total}}{\partial w_5}$ is read as “the partial derivative of E_{total} with respect to w_5 ”. You can also say “the gradient with respect to w_5 ”.

By applying the [chain rule](#) we know that:

$$\frac{\partial E_{total}}{\partial w_5} = \frac{\partial E_{total}}{\partial \text{out}_{o1}} * \frac{\partial \text{out}_{o1}}{\partial \text{net}_{o1}} * \frac{\partial \text{net}_{o1}}{\partial w_5}$$

Visually, here's what we're doing:



We need to figure out each piece in this equation.

First, how much does the total error change with respect to the output?

$$E_{total} = \frac{1}{2}(\text{target}_{o1} - \text{out}_{o1})^2 + \frac{1}{2}(\text{target}_{o2} - \text{out}_{o2})^2$$

$$\frac{\partial E_{total}}{\partial \text{out}_{o1}} = 2 * \frac{1}{2}(\text{target}_{o1} - \text{out}_{o1})^{2-1} * -1 + 0$$

$$\frac{\partial E_{total}}{\partial out_{o1}} = -(target_{o1} - out_{o1}) = -(0.01 - 0.75136507) = 0.74136507$$

$-(target - out)$ is sometimes expressed as $out - target$

When we take the partial derivative of the total error with respect to out_{o1} , the quantity $\frac{1}{2}(target_{o2} - out_{o2})^2$ becomes zero because out_{o1} does not affect it which means we're taking the derivative of a constant which is zero.

Next, how much does the output of o_1 change with respect to its total net input?

The partial [derivative of the logistic function](#) is the output multiplied by 1 minus the output:

$$out_{o1} = \frac{1}{1 + e^{-net_{o1}}}$$

$$\frac{\partial out_{o1}}{\partial net_{o1}} = out_{o1}(1 - out_{o1}) = 0.75136507(1 - 0.75136507) = 0.186815602$$

Finally, how much does the total net input of o_1 change with respect to w_5 ?

$$net_{o1} = w_5 * out_{h1} + w_6 * out_{h2} + b_2 * 1$$

$$\frac{\partial net_{o1}}{\partial w_5} = 1 * out_{h1} * w_5^{(1-1)} + 0 + 0 = out_{h1} = 0.593269992$$

Putting it all together:

$$\frac{\partial E_{total}}{\partial w_5} = \frac{\partial E_{total}}{\partial out_{o1}} * \frac{\partial out_{o1}}{\partial net_{o1}} * \frac{\partial net_{o1}}{\partial w_5}$$

$$\frac{\partial E_{total}}{\partial w_5} = 0.74136507 * 0.186815602 * 0.593269992 = 0.082167041$$

You'll often see this calculation combined in the form of the [delta rule](#):

$$\frac{\partial E_{total}}{\partial w_5} = -(target_{o1} - out_{o1}) * out_{o1}(1 - out_{o1}) * out_{h1}$$

Alternatively, we have $\frac{\partial E_{total}}{\partial out_{o1}}$ and $\frac{\partial out_{o1}}{\partial net_{o1}}$ which can be written as $\frac{\partial E_{total}}{\partial net_{o1}}$, aka δ_{o1} (the Greek letter delta) aka the *node delta*. We can use this to rewrite the calculation above:

$$\delta_{o1} = \frac{\partial E_{total}}{\partial out_{o1}} * \frac{\partial out_{o1}}{\partial net_{o1}} = \frac{\partial E_{total}}{\partial net_{o1}}$$

$$\delta_{o1} = -(target_{o1} - out_{o1}) * out_{o1}(1 - out_{o1})$$

Therefore:

$$\frac{\partial E_{total}}{\partial w_5} = \delta_{o1} out_{h1}$$

Some sources extract the negative sign from δ so it would be written as:

$$\frac{\partial E_{total}}{\partial w_5} = -\delta_{o1} out_{h1}$$

To decrease the error, we then subtract this value from the current weight (optionally multiplied by some learning rate, eta, which we'll set to 0.5):

$$w_5^+ = w_5 - \eta * \frac{\partial E_{total}}{\partial w_5} = 0.4 - 0.5 * 0.082167041 = 0.35891648$$

[Some sources](#) use α (alpha) to represent the learning rate, [others use \$\eta\$](#) (eta), and [others](#) even use ϵ (epsilon).

We can repeat this process to get the new weights w_6 , w_7 , and w_8 :

$$w_6^+ = 0.408666186$$

$$w_7^+ = 0.511301270$$

$$w_8^+ = 0.561370121$$

We perform the actual updates in the neural network *after* we have the new weights leading into the hidden layer neurons (ie, we use the original weights, not the updated weights, when we continue the backpropagation algorithm below).

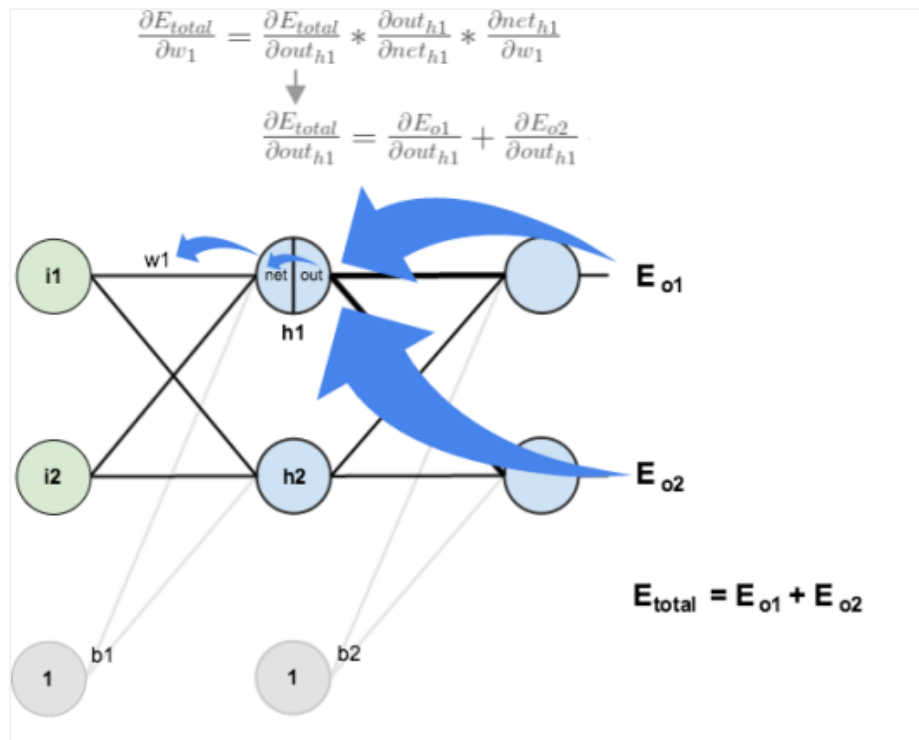
Hidden Layer

Next, we'll continue the backwards pass by calculating new values for w_1 , w_2 , w_3 , and w_4 .

Big picture, here's what we need to figure out:

$$\frac{\partial E_{total}}{\partial w_1} = \frac{\partial E_{total}}{\partial out_{h1}} * \frac{\partial out_{h1}}{\partial net_{h1}} * \frac{\partial net_{h1}}{\partial w_1}$$

Visually:



We're going to use a similar process as we did for the output layer, but slightly different to account for the fact that the output of each hidden layer neuron contributes to the output (and therefore error) of multiple output neurons. We know that out_{h1} affects both out_{o1} and out_{o2} therefore the $\frac{\partial E_{total}}{\partial out_{h1}}$ needs to take into consideration its effect on the both output neurons:

$$\frac{\partial E_{total}}{\partial out_{h1}} = \frac{\partial E_{o1}}{\partial out_{h1}} + \frac{\partial E_{o2}}{\partial out_{h1}}$$

Starting with $\frac{\partial E_{o1}}{\partial out_{h1}}$:

$$\frac{\partial E_{o1}}{\partial out_{h1}} = \frac{\partial E_{o1}}{\partial net_{o1}} * \frac{\partial net_{o1}}{\partial out_{h1}}$$

We can calculate $\frac{\partial E_{o1}}{\partial net_{o1}}$ using values we calculated earlier:

$$\frac{\partial E_{o1}}{\partial net_{o1}} = \frac{\partial E_{o1}}{\partial out_{o1}} * \frac{\partial out_{o1}}{\partial net_{o1}} = 0.74136507 * 0.186815602 = 0.138498562$$

And $\frac{\partial net_{o1}}{\partial out_{h1}}$ is equal to w_5 :

$$net_{o1} = w_5 * out_{h1} + w_6 * out_{h2} + b_2 * 1$$

$$\frac{\partial net_{o1}}{\partial out_{h1}} = w_5 = 0.40$$

Plugging them in:

$$\frac{\partial E_{o1}}{\partial out_{h1}} = \frac{\partial E_{o1}}{\partial net_{o1}} * \frac{\partial net_{o1}}{\partial out_{h1}} = 0.138498562 * 0.40 = 0.055399425$$

Following the same process for $\frac{\partial E_{o2}}{\partial out_{h1}}$, we get:

$$\frac{\partial E_{o2}}{\partial out_{h1}} = -0.019049119$$

Therefore:

$$\frac{\partial E_{total}}{\partial out_{h1}} = \frac{\partial E_{o1}}{\partial out_{h1}} + \frac{\partial E_{o2}}{\partial out_{h1}} = 0.055399425 + -0.019049119 = 0.036350306$$

Now that we have $\frac{\partial E_{total}}{\partial out_{h1}}$, we need to figure out $\frac{\partial out_{h1}}{\partial net_{h1}}$ and then $\frac{\partial net_{h1}}{\partial w}$ for each weight:

$$out_{h1} = \frac{1}{1 + e^{-net_{h1}}}$$

$$\frac{\partial out_{h1}}{\partial net_{h1}} = out_{h1}(1 - out_{h1}) = 0.59326999(1 - 0.59326999) = 0.241300709$$

We calculate the partial derivative of the total net input to h_1 with respect to w_1 the same as we did for the output neuron:

$$net_{h1} = w_1 * i_1 + w_3 * i_2 + b_1 * 1$$

$$\frac{\partial net_{h1}}{\partial w_1} = i_1 = 0.05$$

Putting it all together:

$$\frac{\partial E_{total}}{\partial w_1} = \frac{\partial E_{total}}{\partial out_{h1}} * \frac{\partial out_{h1}}{\partial net_{h1}} * \frac{\partial net_{h1}}{\partial w_1}$$

$$\frac{\partial E_{total}}{\partial w_1} = 0.036350306 * 0.241300709 * 0.05 = 0.000438568$$

You might also see this written as:

$$\frac{\partial E_{total}}{\partial w_1} = \left(\sum_o \frac{\partial E_{total}}{\partial out_o} * \frac{\partial out_o}{\partial net_o} * \frac{\partial net_o}{\partial out_{h1}} \right) * \frac{\partial out_{h1}}{\partial net_{h1}} * \frac{\partial net_{h1}}{\partial w_1}$$

$$\frac{\partial E_{total}}{\partial w_1} = \left(\sum_o \delta_o * w_{ho} \right) * out_{h1}(1 - out_{h1}) * i_1$$

$$\frac{\partial E_{total}}{\partial w_1} = \delta_{h1} i_1$$

We can now update w_1 :

$$w_1^+ = w_1 - \eta * \frac{\partial E_{total}}{\partial w_1} = 0.15 - 0.5 * 0.000438568 = 0.149780716$$

Repeating this for w_2 , w_3 , and w_4

$$w_2^+ = 0.19956143$$

$$w_3^+ = 0.24975114$$

$$w_4^+ = 0.29950229$$

Finally, we've updated all of our weights! When we fed forward the 0.05 and 0.1 inputs originally, the error on the network was 0.298371109. After this first round of backpropagation, the total error is now down to 0.291027924. It might not seem like much, but after repeating this process 10,000 times, for example, the error plummets to 0.0000351085. At this point, when we feed forward 0.05 and

0.1, the two outputs neurons generate 0.015912196 (vs 0.01 target) and 0.984065734 (vs 0.99 target).









If you’ve made it this far and found any errors in any of the above or can think of any ways to make it clearer for future readers, don’t hesitate to [drop me a note](#). Thanks!

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Nikesh

— April 22, 2019 at 5:11 am

Superb Explanation

[Reply](#)



krishna

— December 18, 2019 at 1:45 am

I m not getting if same inputs need to regenerate why we are putting hidden layers ,whats is the purpose?

[Reply](#)

**Chaitra**

— April 23, 2019 at 10:51 am

just awesome explanation....!!

[Reply](#)**Mattie**

— April 26, 2019 at 2:34 pm

Took a pen and paper and really enjoyed this. Thanks!

[Reply](#)**Cat**

— April 29, 2019 at 11:51 am

This is simply the best explanation I have found for back propagation
Love how you broke everything down!!

[Reply](#)**Saheli Mahapatra**

— April 29, 2019 at 10:33 pm

Here is another very nice tutorial with step by step Mathematical explanation and full coding.

<http://www.adeveloperdiary.com/data-science/machine-learning/understand-and-implement-the-backpropagation-algorithm-from-scratch-in-python/>

[Reply](#)**Syed Mohsin Bukhari**

— July 15, 2019 at 7:00 am

This link has awesome description of backprop. Thanks!

[Reply](#)**Charles Yin**

— April 30, 2019 at 2:20 pm

This is the best tutorial on neural work! All textbooks should be written like this. Thank you very much!

[Reply](#)**Ava Trimble**

— May 2, 2019 at 12:20 pm

This really was the greatest explanation! Love it. Thanks

[Reply](#)



Andrew Bannerman

— May 7, 2019 at 10:26 pm

Great! Thanks for the walk through! When using different activation functions.... during back propogation we just need to use the derivative of the activation function yes?

[Reply](#)



Tony

— May 8, 2019 at 2:28 am

Teaching is an art! Good Post!

[Reply](#)

Nūr Al-Dīn

— June 10, 2019 at 1:54 pm

Thank you very very very useful topic

[Reply](#)



Ashutosh Nayak

— June 19, 2019 at 4:07 pm

Best explanation for back propagation with clear steps..thanks a lot...

[Reply](#)



Anthony

— July 19, 2019 at 3:50 pm

This is a gem! Thanks so much, Matt! You made me understand in an hour what a semester in grad school failed to do!

[Reply](#)



Dont want to give

— July 23, 2019 at 9:57 am

Such a wonderful and simple explanation

[Reply](#)



Jagan Mohan

— August 8, 2019 at 4:53 pm

Goshhhh..... I am so happy I came across this post. Such a clean way of explanation. Thanks Matt.

[Reply](#)



amaury L

— August 11, 2019 at 3:36 pm

Amazing article, can't recommend enough ! Not ashamed to cover the math step by step which I am sure not every teacher is always willing to do. Understand it once and the rest will come with it.

[Reply](#)



yolix

— August 27, 2019 at 3:21 am

Thank you very much, you are artist on deep learning !

[Reply](#)

Partha Sarathi

— September 3, 2019 at 7:31 am

Was looking for exactly this kind of a blog! Thanks!!!

[Reply](#)



ryan reza fadillah

— September 12, 2019 at 5:04 am

wow its amazing

[Reply](#)



Mykel Stone

— September 13, 2019 at 4:43 pm

I just wanted to comment that this blog post has served me well for the last 4 years. I mess with neural networks as a hobby and while I mainly create art pieces that use the chaotic dynamics inherent in these networks, sometimes I like to play around with making something that can learn and this is my go-to read for remembering how to do backpropagation. It saves me so much time! So I'd just like to personally say thank you.

[Reply](#)



Mazur

— September 13, 2019 at 9:00 pm

Appreciate you saying so!

[Reply](#)**Leo**

— September 16, 2019 at 6:01 am

Excellent explanation !

[Reply](#)**dikibhuyan**

— September 26, 2019 at 12:04 pm

Don't you think the hidden nodes should have different bias values? You're using the same values for hidden nodes on the same layer.

[Reply](#)**Aryan**

— December 5, 2019 at 7:23 am

I have the same doubt! It's a pity the author isn't replying. I suppose he must've done it for the sake of simplicity but that would defeat the purpose of the article, wouldn't it? Maybe as an empirical rule the biases for a layer are to be initialized as the same value?

[Reply](#)**Noah**

— January 6, 2020 at 8:17 pm

I'm betting you just use the chain rule that he uses throughout and the summation that he uses for the hidden layers. Modifying what he says: "We know that b_2 affects both out_{o1} and out_{o2} therefore the $\frac{\partial E_{total}}{\partial b_2}$ needs to take into consideration its effect on the both output neurons"

[Reply](#)**Carlos**

— October 30, 2019 at 3:50 am

What about bias values?

[Reply](#)**Arun M**

— October 30, 2019 at 1:35 pm

Great material! Thank you so much for your effort! Your idea of plugging numbers into the equation was a great aid in developing understanding and intuition behind this. Will read this many times over until required.

[Reply](#)**ANJANA**

— November 7, 2019 at 5:40 am

Thank you sir !!

[Reply](#)**Hannah Her.**

— November 7, 2019 at 6:25 am

This is an awesome tutorial, thank you very much. I only struggle at one point, namely the Backward Pass, Output Layer. You write

$$E_Total = 1/2 (target_o1 - out_o1)^2 + 1/2 (target_o1 - out_o2)^2$$

That is clear to me. But then the next line reads:

$\phi E_Total / \phi out_o1 = 2 * 1/2 (target_o1 - out_o1)^2 - 1 * -1 + 0$ <<- Where is the '-1' coming from? I spend an hour trying to understand it, but I just don't. Any help would be greatly appreciated.

Hannah

[Reply](#)**MinimalArchitect**

— December 21, 2019 at 6:15 pm

If you use the correct partial-derivative without the -1, you would need to add the new weight onto the old one (not subtract them), so it's a unexplained side-product that everyone seems to use.

[Reply](#)**Afer Ventus**

— December 29, 2019 at 1:59 am

$$1/2 (target_o1 - out_o1)^2$$

the derivative of this function states that:

a) the exponent becomes the multiplier, so:

$$1/2 (target_o1 - out_o1)^2$$

becomes

$$2 * 1/2 (target_o1 - out_o1)^2$$

b) subtract 1 from the exponent, so:

$$2 * 1/2 (target_o1 - out_o1)^2$$

becomes

$$2 * 1/2 (target_o1 - out_o1)^{2-1}$$

c) the inner function $g(x) = out_o1$, so:

$$2 * 1/2 (target_o1 - x)^{2-1}$$

d) the "x" has 1 as exponent. The derivative states that it should be subtracted by 1, so:

$$2 * 1/2 (target_o1 - x^{*1-1})^2-1$$

which results in

$$2 * 1/2 (target_o1 - x^0)^2-1$$

e) every number powered by zero becomes 1, so:

$$2 * 1/2 (target_o1 - 1)^2-1$$

f) it is a composite function, so applying the chain rule:

$$f'(g(x)) \cdot g'(x)$$

$$g'(x) = -1$$

the -1 is $g'(x)$. The remaining before it is $f'(g(x))$

[Reply](#)



Martti

— November 13, 2019 at 9:07 am

Excellent story about backpropagation. I tried to make a C++ implementation. I managed to do the same numeric values for the weights. However there is no lines about the bias adjusting. Can biases b1 and b2 adjusted like weights, where the inputs always 1.0 ?
Thanks

[Reply](#)



MANUEL OMAR OLGUIN HERNANDEZ

— November 19, 2019 at 12:08 pm

Thanks for your explanation, is good, however, I can't see how Bias could adjust. could you help us. Tks

[Reply](#)



gg1101

— November 20, 2019 at 6:40 pm

PLEASE, answer me, the term $d(E_{o2})/d(out_{h1})$ should be -0.0222903640721166...
check pleaseeee

Anyway, best explanation on internet

[Reply](#)



Ravi

— December 4, 2019 at 11:41 am

This is a really nice explanation. Good job.

[Reply](#)



asdf

— December 6, 2019 at 11:00 pm

Bless your heart... Thank you.

[Reply](#)



James

— January 2, 2020 at 10:28 pm

Excellent explanation! Would love to see the calculations followed through for the biases too.

[Reply](#)



Ishan Dindorkar

— January 6, 2020 at 4:48 am

Thank you so much for writing this awesome blog. I greatly appreciate your efforts

[Reply](#)



vinay

— January 9, 2020 at 9:55 pm

I am unable to understand $net_{o1} = w_5 * out_{h1} + w_6 * out_{h2} + b_2 * 1$. how does the derivative translate into $1 * out_{h1} * w_5^{(1-1)} + 0 + 0 = out_{h1} = 0.593269992$, from where did $w_5^{(1-1)}$ come from shouldnt it just be $1 * out_{h1} * w_5^{(1-1)}$

[Reply](#)



Vinay Vernekar

— January 9, 2020 at 10:47 pm

I am unable to understand $net_{o1} = w_5 * out_{h1} + w_6 * out_{h2} + b_2 * 1$. how does the derivative translate into $1 * out_{h1} * w_5^{(1-1)} + 0 + 0 = out_{h1} = 0.593269992$, from where did $w_5^{(1-1)}$ come from shouldnt it just be $1 * out_{h1} * w_5^{(1-1)}$

[Reply](#)



cthulhuu

— January 30, 2020 at 5:02 am

Best explanation i've ever seen.

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