

Problem 2

(5 points): Find $\partial w / \partial v$ when $u = -1$, $v = 2$ if $w = xy + \ln z$, $x = v^2/u$, $y = u + v$, $z = \cos u$.

$$\begin{aligned}w &= xy + \ln z \\&= \left(\frac{v^2}{u} (u+v)\right) + \ln(\cos u) \\&= v^2 + \frac{v^3}{u} + \ln(\cos u) \\\frac{\partial w}{\partial v} &= \frac{\partial}{\partial v} \left(v^2 + \frac{v^3}{u} + \ln(\cos u) \right) \\&= 2v + \frac{3v^2}{u} + 0 \\&= 2v + \frac{3v^2}{u} \\&= 2 \cdot 2 + \frac{3(2^2)}{-1} \\&= 4 + \frac{12}{-1} \\&= 4 - 12 \\&= \boxed{-8}\end{aligned}$$