## What I've understood so far

- Argumentation Framework (AF) is a pair of a set of arguments (AR) and attacks.
- A set S is conflict-free if there are no pairs of arguments in S that attack each other
- An argument A is acceptable within S if for any attacks(B, A) there is a B' in S such that attacks(B', B) holds.
- S is admissible if it is conflict-free and every argument within A is acceptable.
- IDEA: When a human mind tries to develop a reasonment what it does is developing an admissible set that makes every conclusion it reaches acceptable
- A preferred extension is a maximal admissible set of AF (wrt set inclusion).
- Admissible sets can be constructed inductively. For example, if A be acceptable within S, then  $S' = S \cup A$  is admissible
- Admissible sets constitute a complete partial ordering wrt set inclusion. That implies that the preferred extension always exist (i.e. the sequence of admissible sets has an upper bound)

## Stable extensions

- A set S is a stable extension if it is conflict free and "spartan" i.e. attacks everything not in S
- Can be proven that they can be constructed inductively by simply taking every argument that makes S conflict-free.
- As we cannot extend a stable extension anymore, it must be a preferred extension.

The idea is: a matching problem usually involves finding stable extensions.

## **Fixpoints**

We need to introduce skeptical semantics

- The characteristic function:
  - Maps subsets of ARs to subsets of ARs
  - $F AF(S) = \{A \mid A \text{ is acceptable wrt } S\}$
- Why? Given S for granted, we want to "expand" our knowledgebase with arguments that can be defended by the KB.
- In fact, it can be proven that S is always a subset of F(S) iff S is admissible.

- Sketch: Every element in S is always acceptable within S by definition of admissibility. Besides, if S is conflict-free then F(S) is conflict-free. Suppose not, then there would exist a B in F(S) such that B attacks A, A in F(S), hence there is a B' that attacks B, but S was admissible!
- F is monotonic wrt set inclusion, so we can expand our knowledge safely
- The maximal we can reach is called **Grounded extension**