

$$(1) P\left(+ \mid \begin{matrix} A_1=T \\ A_2=F \\ A_3=T \end{matrix}\right) = \frac{P\left(\begin{matrix} A_1=T \\ A_2=F \\ A_3=T \end{matrix} \mid +\right) * P(+)}{P\left(\begin{matrix} A_1=T \\ A_2=F \\ A_3=T \end{matrix}\right)}$$

Based on Bayes theorem only one may be known and the probability of other ~~nots~~ may not be estimated mathematically - To address the scenario we create a complement of the above scenario or a negative - And compare which is bigger based on a Naive Bayes learning which ever is bigger in value of the positive or negative is valid.

$$P\left(+ \mid \begin{matrix} A_1=T \\ A_2=F \\ A_3=T \end{matrix}\right), \quad P\left(- \mid \begin{matrix} A_1=T \\ A_2=F \\ A_3=T \end{matrix}\right)$$

Using Naive Bayes learning assumption all the descriptive are Independent

$$P(E_1 E_2 E_3) = P(E_1) * P(E_2) * P(E_3) \dots * P(E_n)$$

$$\propto P(A_1=T|+) * P(A_2=F|+) * P(A_3=T|+)$$

$$0/2 * 1/2 * 1/2 * 2/6 \quad \text{Applying Laplace smoothing}$$

$$\frac{0+1}{2+3} * \frac{1+1}{2+3} * \frac{1+1}{2+3} = 1/5 * 2/5 * 2/5 = \frac{2}{125} * 2/6$$

$$\propto P(A_2=T|-) * P(A_2=F|-) * P(A_3=T|-) * \frac{n(-)}{n(+)}$$

$$2/4 * 2/4 * 1/3 * 4/6 = 1/2 * 1/2 * 1/3 * 4/6 =$$

$$\text{Valid} - P\left(- \mid \begin{matrix} A_1=T \\ A_2=F \\ A_3=T \end{matrix}\right) > P\left(+ \mid \begin{matrix} A_1=T \\ A_2=F \\ A_3=T \end{matrix}\right)$$