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- Module UpdateCluster
EXTENDS Integers, FiniteSets
CONSTANTS
    \_Requests,
                  the requests sent by the user
    _{-}Workers,
                  the pool of workers
    NULL
VARIABLES
    last VOK, last successfully applied version
    toApply,
                  the version to apply (last requets that passed the initial tests)
    cluster,
                  cluster state
    requests,
                  the state of all requests
    workers, the state of all workers
    lock damn, I used a lock...
VARIABLES
     these variables are tla + details
    confOK, are we able to get a valid conf?
    reqCounter just to keep track of the order of submissions
vars \triangleq \langle confOK, reqCounter, lastVOK, toApply, cluster, requests, workers, lock \rangle
TypeInvariants \triangleq
    \land confOK \in BOOLEAN won't change for a specific behavior
    \land lock \in BOOLEAN
    \land cluster.st \in \{
        "idle",
        "starting",
         "partial",
         "failed"
     \land \, \forall \, r \in \_Requests : requests[r].st \in \{
        "waiting", the request (req) hasn't been submitted yet
        \hbox{``submitted''}\,,\quad \hbox{req has been submitted}
        "rejected", reg has been rejected (auth problem)
        "valid" auth etc passed
     \land \forall \, w \in \_Workers : workers[w].st \in \{
        "waiting",
        "starting",
        "working"
```

Initial State

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Init \stackrel{\triangle}{=}
      \land requests = [r \in \_Requests \mapsto [st \mapsto "waiting", v \mapsto NULL]]
     \land workers = [w \in \_Workers \mapsto [st \mapsto "waiting", v \mapsto NULL]]
      \wedge cluster = [v \mapsto 0, st \mapsto \text{``idle''}]
      \wedge lastVOK = 0
      \land \mathit{reqCounter} = 0
     \wedge toApply = 0
      \land confOK \in BOOLEAN
      \wedge lock = false
Actions
     pmit(r) \stackrel{\triangle}{=} \text{ update request received from the user}

LET newV \stackrel{\triangle}{=} reqCounter + 1IN
Submit(r) \triangleq
     \land requests[r].st = "waiting"
     \land regCounter' = newV
     \land \mathit{requests'} = [\mathit{requests} \ \mathtt{EXCEPT} \ ![r].\mathit{st} = \text{``submitted''}, \ ![r].v = \mathit{newV}]
      \land UNCHANGED \langle confOK, lastVOK, toApply, cluster, workers, lock <math>\rangle
Initialcheck(r) \stackrel{\Delta}{=} request validation (auth, quotas...)
      \land requests[r].st = "submitted"
     \wedge \exists ok \in BOOLEAN :
          IF ok
                THEN
                    requests' = [requests \ EXCEPT \ ![r].st = "valid"]
                    requests' = [requests \ EXCEPT \ ![r].st = "rejected"]
      \land UNCHANGED \langle confOK, reqCounter, lastVOK, toApply, cluster, workers, lock <math>\rangle
PushToPending(r) \stackrel{\Delta}{=} the request is pushed to queue
      \land requests[r].st = "valid"
      \land IF toApply < requests[r].v
           THEN \wedge toApply' = requests[r].v
                    \land UNCHANGED \langle confOK, regCounter, lastVOK, cluster, requests, workers, lock <math>\rangle
           ELSE \land requests' = [requests \ EXCEPT \ ![r].st = "rejected"]
                    \land UNCHANGED \langle confOK, reqCounter, lastVOK, toApply, cluster, workers, lock <math>\rangle
SpawnWorker(w) \stackrel{\Delta}{=} spawns a new worker
      \land workers[w].st = "waiting"
      \land toApply \neq lastVOK
      \wedge lock = FALSE
      \land \lor cluster.st = "idle"
          \lor cluster.st = "failed"
      \land workers' = [workers \ EXCEPT \ ![w].v = toApply, \ ![w].st = "starting"]
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\wedge lock' = TRUE
    \land UNCHANGED \langle confOK, reqCounter, lastVOK, toApply, requests, cluster <math>\rangle
ApplyStart(w) \stackrel{\Delta}{=} the cluster starts to be modified
    \land workers[w].st = "starting"
    \land IF workers[w].v \ge toApply
         THEN
            IF confOK
                  THEN
                      \land cluster' = [v \mapsto workers[w].v, st \mapsto "partial"]
                      \land workers' = [workers \ EXCEPT \ ![w].st = "working"]
                      \land UNCHANGED \langle confOK, reqCounter, lastVOK, toApply, requests, lock <math>\rangle
                  ELSE
                      \wedge lock' = false
                      \land workers' = [workers \ EXCEPT \ ![w].st = "waiting", ![w].v = NULL]
                      \land UNCHANGED \langle confOK, reqCounter, lastVOK, toApply, cluster, requests <math>\rangle
                 a new version has been submitted, no need to apply this one
             \land workers' = [workers \ EXCEPT \ ![w].st = "waiting", ![w].v = NULL]
             \wedge lock' = FALSE
             \land UNCHANGED \langle confOK, regCounter, lastVOK, toApply, cluster, requests <math>\rangle
RollbackVersion \triangleq
     to differenciate it from the original last VOK
    lastVOK + 10
ApplyFinish(w) \stackrel{\triangle}{=} the cluster update finishes
    \land workers[w].st = "working"
    \wedge lock' = false
    \wedge \exists ok \in BOOLEAN :
        IF ok \lor workers[w].v = RollbackVersion rollback always works
             THEN
                 \land cluster' = [cluster \ EXCEPT \ !.st = "idle"]
                 \wedge lastVOK' = workers[w].v
                 \land workers' = [workers \ EXCEPT \ ![w].st = "waiting", ![w].v = NULL]
                 \land UNCHANGED \langle confOK, reqCounter, toApply, requests <math>\rangle
                 \land cluster' = [cluster \ EXCEPT \ !.st = "failed"]
                 \land workers' = [workers \ EXCEPT \ ![w].st = "waiting", ![w].v = NULL]
                 \land IF workers[w].v < toApply
                      THEN a newer version has been submitted
                          \land UNCHANGED \langle confOK, regCounter, lastVOK, toApply, requests <math>\rangle
                      ELSE let's trigger a rollback
                          \wedge toApply' = RollbackVersion
                          \land UNCHANGED \langle confOK, regCounter, lastVOK, requests <math>\rangle
```

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Requirements
NoConcurrentUpdate \triangleq
     \Box(Cardinality(\{r \in DOMAIN \ requests : requests[r].st = "working"\}) < 2)
NoPartialUpdateTermination \triangleq
                                                 we don't want the cluster to end up in a partially update st
     \Diamond \Box (cluster.st = "idle")
EveryReqIsProcessed \triangleq
     \Diamond \Box (\neg \exists \ r \in \_Requests : requests[r].st = "waiting")
Spec
Next \triangleq
     \vee \, \exists \, r \in \_Requests :
             \vee Submit(r)
             \vee Initialcheck(r)
             \vee PushToPending(r)
     \vee \exists w \in \_Workers:
              \vee SpawnWorker(w)
              \lor ApplyStart(w)
              \vee ApplyFinish(w)
\textit{Fairness} \ \stackrel{\triangle}{=} \ \forall \, r \in \_\textit{Requests}, \, w \in \_\textit{Workers}:
                      \wedge \operatorname{WF}_{vars}(Submit(r))
                      \wedge \operatorname{WF}_{vars}(Initial check(r))
                       \wedge \operatorname{WF}_{vars}(\operatorname{PushToPending}(r))
                       \wedge \operatorname{WF}_{vars}(SpawnWorker(w))
                       \wedge WF_{vars}(ApplyStart(w))
                       \wedge \operatorname{WF}_{vars}(ApplyFinish(w))
Spec \triangleq
   \land Init
   \wedge \Box [Next]_{vars}
   \land Fairness
THEOREM Spec \Rightarrow \Box(TypeInvariants)
Theorem Spec \Rightarrow NoPartialUpdateTermination
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