$\hbox{``rolledback''} \quad \hbox{the req has been } {\it rolledback}$

 $\land \forall \, w \in _Workers : workers[w].st \in \{$

"waiting",
"starting",
"working"

```
Initial State
Init \triangleq
     \land requests = [r \in \_Requests \mapsto [st \mapsto "waiting", v \mapsto NULL]]
     \land workers = [w \in \_Workers \mapsto [st \mapsto "waiting", v \mapsto NULL]]
     \wedge cluster = [v \mapsto 0, st \mapsto \text{``idle''}]
     \wedge lastVOK = 0
     \wedge lastVSubmitted = 0
     \wedge toApply = 0
     \land confOK \in BOOLEAN
     \wedge lock = false
Actions
Submit(r) \triangleq
                   update request received from the user
    Let newV \triangleq lastVSubmitted + 1in
     \land requests[r].st = "waiting"
     \wedge lastVSubmitted' = newV
     \land requests' = [requests \ EXCEPT \ ![r].st = "submitted", \ ![r].v = newV]
     \land UNCHANGED \langle confOK, lastVOK, toApply, cluster, workers, lock <math>\rangle
Initialcheck(r) \stackrel{\Delta}{=} request validation (auth, quotas...)
     \land requests[r].st = "submitted"
     \wedge \exists ok \in BOOLEAN:
        IF ok
                  requests' = [requests \ EXCEPT \ ![r].st = "valid"]
              ELSE
                  requests' = [requests \ EXCEPT \ ![r].st = "rejected"]
     \land UNCHANGED \langle confOK, lastVSubmitted, lastVOK, toApply, cluster, workers, lock <math>\rangle
PushToPending(r) \stackrel{\Delta}{=} the request is pushed to queue
     \land reguests[r].st = "valid"
     \land IF toApply < requests[r].v
          THEN \wedge toApply' = requests[r].v
                  \land UNCHANGED \langle confOK, lastVSubmitted, lastVOK, cluster, requests, workers, lock <math>\rangle
          ELSE \land requests' = [requests \ EXCEPT \ ![r].st = "rejected"]
                  \land UNCHANGED \langle confOK, lastVSubmitted, lastVOK, to Apply, cluster, workers, lock <math>\rangle
```

}

 $SpawnWorker(w) \triangleq$

 $\land workers[w].st = "waiting"$

spawns a new worker

```
\wedge lock = false
    \land \lor cluster.st = "idle"
         \lor cluster.st = "failed"
    \wedge IF cluster.st = "idle"
         THEN
             \land workers' = [workers \ EXCEPT \ ![w].v = toApply, \ ![w].st = "starting"]
         ELSE
             \land workers' = [workers \ EXCEPT \ ![w].v = lastVOK, \ ![w].st = "starting"]
    \wedge lock' = TRUE
    \land UNCHANGED \langle confOK, lastVSubmitted, lastVOK, to Apply, requests, cluster <math>\rangle
ApplyStart(w) \stackrel{\Delta}{=} the cluster starts to be modified
    \land workers[w].st = "starting"
    \land \text{ if } \lor workers[w].v = lastVSubmitted
           \vee workers[w].v = lastVOK rollingback
         THEN
            IF confOK
                  THEN
                      \land cluster' = [v \mapsto workers[w].v, st \mapsto "partial"]
                      \land workers' = [workers \ EXCEPT \ ![w].st = "working"]
                      \land UNCHANGED \langle confOK, lastVSubmitted, lastVOK, toApply, requests, lock <math>\rangle
                  ELSE
                      \wedge lock' = false
                      \land workers' = [workers \ EXCEPT \ ![w].st = "waiting", ![w].v = NULL]
                      \land UNCHANGED \langle confOK, lastVSubmitted, lastVOK, toApply, cluster, requests <math>\rangle
         ELSE
             \land workers' = [workers \ EXCEPT \ ![w].st = "waiting", \ ![w].v = NULL]
             \land UNCHANGED \langle confOK, lastVSubmitted, lastVOK, toApply, cluster, requests, lock <math>\rangle
ApplyFinish(w) \stackrel{\triangle}{=} the cluster update finishes
    \land workers[w].st = "working"
    \wedge lock' = false
    \wedge \exists ok \in BOOLEAN :
        IF ok \lor workers[w].v = lastVOK rollback always works
                  \land cluster' = [cluster \ EXCEPT \ !.st = "idle"]
                  \wedge lastVOK' = workers[w].v
                  \land workers' = [workers \ EXCEPT \ ![w].st = "waiting", ![w].v = NULL]
                  \land UNCHANGED \langle confOK, lastVSubmitted, toApply, requests <math>\rangle
             ELSE
                  \land cluster' = [cluster \ EXCEPT \ !.st = "failed"]
                  \land workers' = [workers \ \texttt{EXCEPT} \ ![w].st = "waiting", ![w].v = NULL]
                  \land UNCHANGED \langle confOK, lastVSubmitted, lastVOK, toApply, requests <math>\rangle
```

```
Requirements
NoConcurrentUpdate \triangleq
     \Box(Cardinality(\{r \in DOMAIN \ requests : requests[r].st = "working"\}) < 2)
NoPartialUpdateTermination \triangleq
                                                we don't want the cluster to end up in a partially update st
     \Diamond \Box (cluster.st = "idle")
EveryReqIsProcessed \triangleq
     \Diamond \Box (\neg \exists \ r \in \_Requests : requests[r].st = "waiting")
Spec
Next \triangleq
      \vee \exists r \in \_Requests :
             \vee Submit(r)
             \vee Initialcheck(r)
             \vee PushToPending(r)
     \vee \, \exists \, w \in \_Workers :
              \vee SpawnWorker(w)
              \vee ApplyStart(w)
              \vee ApplyFinish(w)
Fairness \stackrel{\triangle}{=} \forall r \in \_Requests, w \in \_Workers :
                      \wedge \operatorname{WF}_{vars}(Submit(r))
                      \wedge \operatorname{WF}_{vars}(Initialcheck(r))
                      \wedge \operatorname{WF}_{vars}(\operatorname{PushToPending}(r))
                      \wedge \operatorname{WF}_{vars}(SpawnWorker(w))
                      \wedge \operatorname{WF}_{vars}(ApplyStart(w))
                      \wedge \operatorname{WF}_{vars}(ApplyFinish(w))
Spec \triangleq
   \wedge Init
   \wedge \Box [Next]_{vars}
   \land \textit{Fairness}
THEOREM Spec \Rightarrow \Box(TypeInvariants)
Theorem Spec \Rightarrow NoPartialUpdateTermination
 THEOREM Spec \Rightarrow NoApplicationOfOutdatedReq
 Theorem Spec \Rightarrow EveryReqInQueueIsProcessed
```