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MODULE *UpdateCluster*

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EXTENDS *Integers, FiniteSets*

CONSTANTS

*\_Requests*, the requests sent by the user  
*\_Workers*, the pool of workers  
*NULL*

VARIABLES

*lastVOK*, last successfully applied version  
*toApply*, the version to apply (last request that passed the initial tests)  
*cluster*, cluster state  
*requests*, the state of all requests  
*workers*, the state of all workers  
*clusterUpdating* damn, I use a lock...

VARIABLES

these variables are *tla* + details  
*confOK*, are we able to get a valid conf?  
*reqCounter* just to keep track of the order of submissions

vars  $\triangleq \langle \textit{confOK}, \textit{reqCounter}, \textit{lastVOK}, \textit{toApply}, \textit{cluster}, \textit{requests}, \textit{workers}, \textit{clusterUpdating} \rangle$

TypeInvariants  $\triangleq$

$\wedge \textit{confOK} \in \text{BOOLEAN}$  won't change for a specific behavior  
 $\wedge \textit{clusterUpdating} \in \text{BOOLEAN}$   
 $\wedge \textit{cluster.st} \in \{$   
     "idle",  
     "starting",  
     "partial",  
     "failed"  
   }  
 $\wedge \forall r \in \textit{\_Requests} : \textit{requests}[r].\textit{st} \in \{$   
     "waiting", the request (req) hasn't been submitted yet  
     "submitted", req has been submitted  
     "rejected", req has been rejected (auth problem)  
     "valid" auth etc passed  
   }  
 $\wedge \forall w \in \textit{\_Workers} : \textit{workers}[w].\textit{st} \in \{$   
     "waiting",  
     "starting",  
     "working"  
   }

Initial State

$Init \triangleq$   
 $\wedge requests = [r \in \_Requests \mapsto [st \mapsto \text{"waiting"}, v \mapsto NULL]]$   
 $\wedge workers = [w \in \_Workers \mapsto [st \mapsto \text{"waiting"}, v \mapsto NULL]]$   
 $\wedge cluster = [v \mapsto 0, st \mapsto \text{"idle"}]$   
 $\wedge lastVOK = 0$   
 $\wedge reqCounter = 0$   
 $\wedge toApply = 0$   
 $\wedge confOK \in \text{BOOLEAN}$   
 $\wedge clusterUpdating = \text{FALSE}$

#### Actions

$Submit(r) \triangleq$   
 update request received from the user  
 $LET\ newV \triangleq reqCounter + 1\ IN$   
 $\wedge requests[r].st = \text{"waiting"}$   
 $\wedge reqCounter' = newV$   
 $\wedge requests' = [requests\ EXCEPT\ ![r].st = \text{"submitted"}, ![r].v = newV]$   
 $\wedge UNCHANGED\ \langle confOK, lastVOK, toApply, cluster, workers, clusterUpdating \rangle$

$PushToPending(r) \triangleq$   
 the request is pushed to queue  
 $\wedge requests[r].st = \text{"submitted"}$   
 $\wedge IF\ toApply < requests[r].v$   
     THEN  $\wedge requests' = [requests\ EXCEPT\ ![r].st = \text{"valid"}]$   
          $\wedge toApply' = requests[r].v$   
          $\wedge UNCHANGED\ \langle confOK, reqCounter, lastVOK, cluster, workers, clusterUpdating \rangle$   
     ELSE  $\wedge requests' = [requests\ EXCEPT\ ![r].st = \text{"rejected"}]$   
          $\wedge UNCHANGED\ \langle confOK, reqCounter, lastVOK, toApply, cluster, workers, clusterUpdating \rangle$

$SpawnWorker(w) \triangleq$   
 spawns a new worker  
 $\wedge workers[w].st = \text{"waiting"}$   
 $\wedge toApply \neq lastVOK$   
 $\wedge clusterUpdating = \text{FALSE}$   
 $\wedge \vee cluster.st = \text{"idle"}$   
      $\vee cluster.st = \text{"failed"}$   
 $\wedge workers' = [workers\ EXCEPT\ ![w].v = toApply, ![w].st = \text{"starting"}]$   
 $\wedge clusterUpdating' = \text{TRUE}$   
 $\wedge UNCHANGED\ \langle confOK, reqCounter, lastVOK, toApply, requests, cluster \rangle$

$ApplyStart(w) \triangleq$   
 the cluster starts to be modified

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 $\wedge workers[w].st = \text{"starting"}$ 
 $\wedge \text{IF } workers[w].v \geq toApply$ 
  THEN
    IF confOK
      THEN
         $\wedge cluster' = [v \mapsto workers[w].v, st \mapsto \text{"partial"}]$ 
         $\wedge workers' = [workers \text{ EXCEPT } ![w].st = \text{"working"}]$ 
         $\wedge \text{UNCHANGED } \langle confOK, reqCounter, lastVOK, toApply, requests, clusterUpdating \rangle$ 
      ELSE
         $\wedge clusterUpdating' = \text{FALSE}$ 
         $\wedge workers' = [workers \text{ EXCEPT } ![w].st = \text{"waiting"}, ![w].v = NULL]$ 
         $\wedge \text{UNCHANGED } \langle confOK, reqCounter, lastVOK, toApply, cluster, requests \rangle$ 
    ELSE
      a new version has been submitted, no need to apply this one
       $\wedge workers' = [workers \text{ EXCEPT } ![w].st = \text{"waiting"}, ![w].v = NULL]$ 
       $\wedge clusterUpdating' = \text{FALSE}$ 
       $\wedge \text{UNCHANGED } \langle confOK, reqCounter, lastVOK, toApply, cluster, requests \rangle$ 

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*RollbackVersion*  $\triangleq$

to differentiate it from the original last *VOK* (in realworld, could be *conf* + timestamp)  
 $lastVOK + 10$

*ApplyFinish*(*w*)  $\triangleq$

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the cluster update finishes
 $\wedge workers[w].st = \text{"working"}$ 
 $\wedge clusterUpdating' = \text{FALSE}$ 
 $\wedge \exists ok \in \text{BOOLEAN} :$ 
  IF  $ok \vee workers[w].v = RollbackVersion$  rollback always works
    THEN
       $\wedge cluster' = [cluster \text{ EXCEPT } !.st = \text{"idle"}]$ 
       $\wedge lastVOK' = workers[w].v$ 
       $\wedge workers' = [workers \text{ EXCEPT } ![w].st = \text{"waiting"}, ![w].v = NULL]$ 
       $\wedge \text{UNCHANGED } \langle confOK, reqCounter, toApply, requests \rangle$ 
    ELSE
       $\wedge cluster' = [cluster \text{ EXCEPT } !.st = \text{"failed"}]$ 
       $\wedge workers' = [workers \text{ EXCEPT } ![w].st = \text{"waiting"}, ![w].v = NULL]$ 
       $\wedge \text{IF } workers[w].v < toApply$ 
        THEN a newer version has been submitted
           $\wedge \text{UNCHANGED } \langle confOK, reqCounter, lastVOK, toApply, requests \rangle$ 
        ELSE let's trigger a rollback
           $\wedge toApply' = RollbackVersion$ 
           $\wedge \text{UNCHANGED } \langle confOK, reqCounter, lastVOK, requests \rangle$ 

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Spec

$$\begin{aligned}
Next &\triangleq \\
&\vee \exists r \in \_Requests : \\
&\quad \vee Submit(r) \\
&\quad \vee PushToPending(r) \\
&\vee \exists w \in \_Workers : \\
&\quad \vee SpawnWorker(w) \\
&\quad \vee ApplyStart(w) \\
&\quad \vee ApplyFinish(w)
\end{aligned}$$

$$\begin{aligned}
Fairness &\triangleq \forall r \in \_Requests, w \in \_Workers : \\
&\quad \wedge WF_{vars}(Submit(r)) \\
&\quad \wedge WF_{vars}(PushToPending(r)) \\
&\quad \wedge WF_{vars}(SpawnWorker(w)) \\
&\quad \wedge WF_{vars}(ApplyStart(w)) \\
&\quad \wedge WF_{vars}(ApplyFinish(w))
\end{aligned}$$

$$\begin{aligned}
Spec &\triangleq \\
&\wedge Init \\
&\wedge \Box[Next]_{vars} \\
&\wedge Fairness
\end{aligned}$$

#### Expectations

$$\begin{aligned}
NoConcurrentUpdate &\triangleq \\
&\Box(Cardinality(\{w \in DOMAIN workers : workers[w].st = \text{"working"}\}) < 2)
\end{aligned}$$

$$\begin{aligned}
NoPartialUpdateTermination &\triangleq \\
&\text{we don't want the cluster to end up in a partially update state} \\
&\Diamond\Box(cluster.st = \text{"idle"})
\end{aligned}$$

$$\begin{aligned}
EveryReqIsProcessed &\triangleq \\
&\Diamond\Box(\neg\exists r \in \_Requests : requests[r].st = \text{"waiting"})
\end{aligned}$$

THEOREM  $Spec \Rightarrow \Box(TypeInvariants)$

THEOREM  $Spec \Rightarrow NoConcurrentUpdate$

THEOREM  $Spec \Rightarrow NoPartialUpdateTermination$

THEOREM  $Spec \Rightarrow EveryReqIsProcessed$