

# Causal Inference in Algorithmic Fairness

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# What is the problem?

- Algorithms are now used set parole, give loans, and set insurance premiums
- Back when humans made these decisions, biases such as racism influenced how individuals from different groups were treated
- Algorithms tend to exhibit similar prejudices

# Preliminaries & Notation

- Causal model defined with triplet  $(U, V, F)$ 
  - $U$ : unobservable variables
  - $V$ : observable variables
  - $F$ : set of structural assignments in a Structural Causal Model
- A Fairness Problem
  - $Y$  is the real outcome,  $\hat{Y}$  the predicted outcome
  - $A$  is the protected attribute,  $X$  are the rest of the features
- Intervention:  $P(Y | do(X = x))$ , Counterfactual:  $V_i(v_j, u)$

# Case Study: COMPAS

- COMPAS predicts whether defendants will commit crimes after release
- Judges use COMPAS score to set bail and parole terms
- ProPublica reported that COMPAS was significantly biased against black individuals
- In reality, black and white individuals with similar background reoffend at the same rates

# Fairness Criteria

- **Equalized odds:** Predict the the real outcome with the same probability for all values of  $A$ 
  - $P(\hat{Y} = y | A = a, Y = y) = P(\hat{Y} = y | A = a', Y = y)$
  - In other words:  $\hat{Y} \perp\!\!\!\perp A | Y$
- **Calibration:** For a predicted outcome, the probability of that outcome being true should be the same for all values of  $A$ 
  - $P(Y = y | A = a, \hat{Y} = y) = P(Y = y | A = a', \hat{Y} = y)$
  - In other words:  $Y \perp\!\!\!\perp A | \hat{Y}$

# Incompatibility of Fairness Measures

- COMPAS used *calibration* as a fairness criterion
- ProPublica considered COMPAS to be unfair, using *equalised odds* as a measure
- Both measures are reasonable to some extent
- Kleinberg et al. showed that these two constraints cannot be simultaneously satisfied

# Fairness Criteria for Populations & Individuals

- **Demographic Parity/Disparate Impact**

- $P(\hat{Y} = y | A = a) = P(\hat{Y} = y | A = a')$  **Or**  $\hat{Y} \perp\!\!\!\perp A$

- It can cause discrimination, undermines calibration and equalized odds

- **Individual Fairness**

$$P(\hat{Y}^{(i)} = y | X^{(i)}, A^{(i)}) \approx P(\hat{Y}^{(j)} = y | X^{(j)}, A^{(j)}) \approx , \text{ if } d(i, j) \approx 0$$

- $d(\cdot, \cdot)$  is a task-specific similarity metric between individuals
  - Fixes DP's discrimination, but choosing  $d(\cdot, \cdot)$  is a hard problem

# Why does Causality matter in Fairness?

- Many ideas and statements in ethics and law are causal in nature
  - Agency & Egalitarianism in Justice
- Unfairness: Experiencing different outcomes due to caused by factors that are out of one's control
- Causal Inference is the superior platform for dealing with confounders and inherent biases



# Shortcomings of Conventional Fairness Measures

- If  $A$  and  $Y$  are not independent, true outcomes are biased themselves
  - The judges may be prejudiced toward minorities
- Both calibration and equalized odds fail to mitigate inherent bias in the data
- This is a problem that Causal Inference can solve

# Inherent Bias: Gender Bias & Simpson's Paradox

- Berkeley Admissions: a lower percentage of women were accepted to graduate programs compared to men
- If we control for department of choice, unfairness disappears.
- Women applied to the most selective programs
- Bickel et al. concluded that socialization caused women to apply to more crowded, less funded departments
- Pearl extensively analyzes this example from a causal standpoint

# Counterfactual Fairness

- A predictor  $\hat{Y}$  satisfies *counterfactual fairness (CF)* if:

$$P(\hat{Y}(a, U) = y \mid X = x, A = a) = P(\hat{Y}(a', U) = y \mid X = x, A = a)$$

- "...other things being equal, our prediction would not have changed in the parallel world where only  $A$  would have changed."
- "...we purposely avoid making use of any information concerning the structural equation for  $Y$  in model. This is motivated by the fact that  $Y$  must not make use of  $\hat{Y}$  at test time.

# Counterfactual Fairness vs. Conventional Fairness Criteria

- CF satisfies Demographic Parity if the predictor is independent of  $A$  and a function of  $U$  and  $X$
- Two different individuals can be compared as counterfactual version of each other
- "...the counterfactual version of individual  $i$  ... is in reality an observed case  $j$  in a sample of controls, such that  $i$  and  $j$  are close..."
- "close" is the similarity metric used in Individual Fairness
- But here the fairness condition only holds for matched pairs

# Counterfactual Fairness vs. Conventional Fairness Criteria

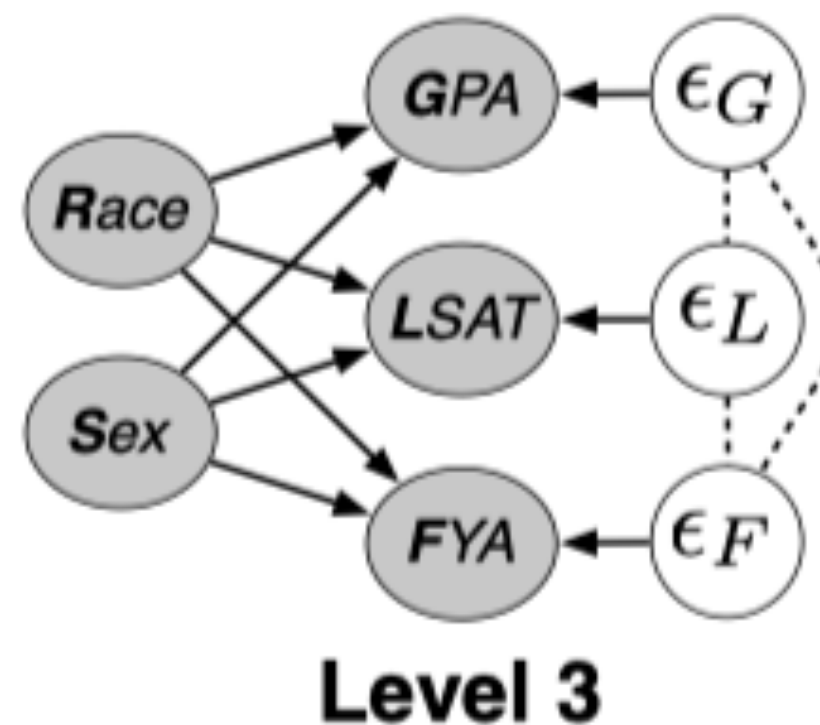
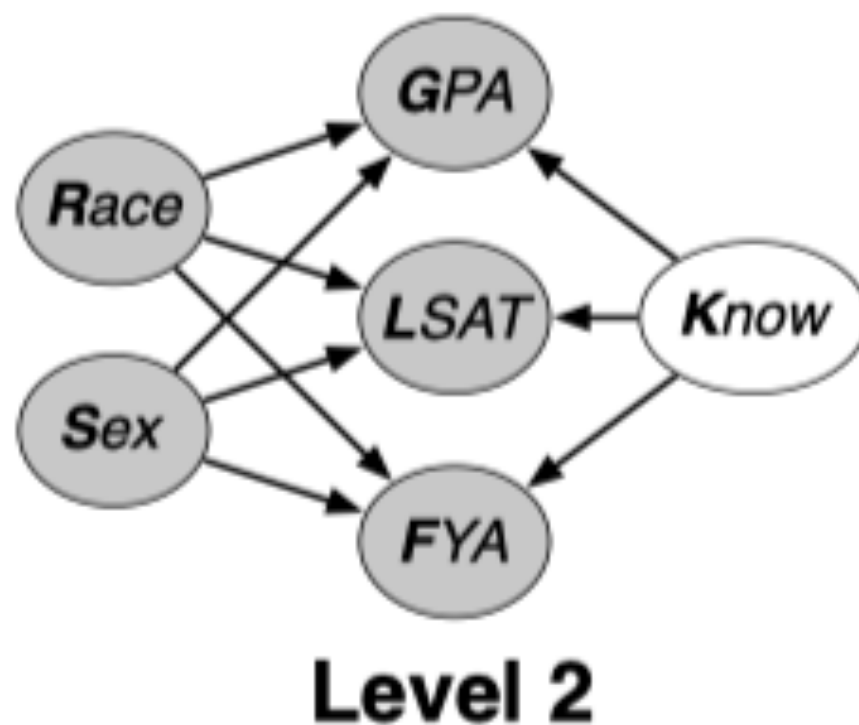
- $Y$  and  $A$  are independent if there are no causal paths exist between them
- Consider a counterfactually fair predictor, only trained with non-descendants of  $A$ 
  - It can be shown that it will respect both Equalized Odds & Calibration

# Counterfactual Fairness: Three levels of Causal Modeling

- Three levels of assumptions of increasing strength
- Level 1: Build predictor using only the observable non-descendants of A
- Level 2: Latent variables that act as non-deterministic causes of observable variables
- Level 3: Fully deterministic model with latents
  - Treat  $P(V_i|pa_i)$  as an additive error model,  $V_i = f_i(pa_i) + e_i$
  - $e_i$  as an input to  $\hat{Y}$

# Counterfactual Fairness: Applications

	Full	Unaware	Fair $K$	Fair Add
RMSE	0.873	0.894	0.929	0.918



# $\tau$ -Controlled Counterfactual Privilege

- Our goal is to assign (binary) interventions  $\mathbf{z}$  to maximize the sum of expected outcomes over individuals subject to a maximum budget  $B$

$$\mathbf{z}^* \equiv \operatorname{argmax}_{\mathbf{z}} \sum_{i=1}^n \mathbb{E}[Y_i(\mathbf{z}) \mid A_i = a_i, X_i = x_i],$$

$$s.t., \sum_{i=1}^n z_i \leq B$$

$$\underbrace{\mathbb{E}_{\mathcal{M}^{\prec}}[Y_i(a_i, \mathbf{z}) \mid A_i = a_i, X_i^{\prec} = x_i^{\prec}] - \mathbb{E}_{\mathcal{M}^{\prec}}[Y_i(a', \mathbf{z}) \mid A_i = a_i, X_i^{\prec} = x_i^{\prec}]}_{G_{ia'}} < \tau,$$

$X_i^{\prec}$  is the subset of  $X_i$  that are non-descendants of  $A_i$  in the causal graph, and  $\mathcal{M}^{\prec}$  is a causal model that excludes all observed non-descendants of  $A$  but  $Y$

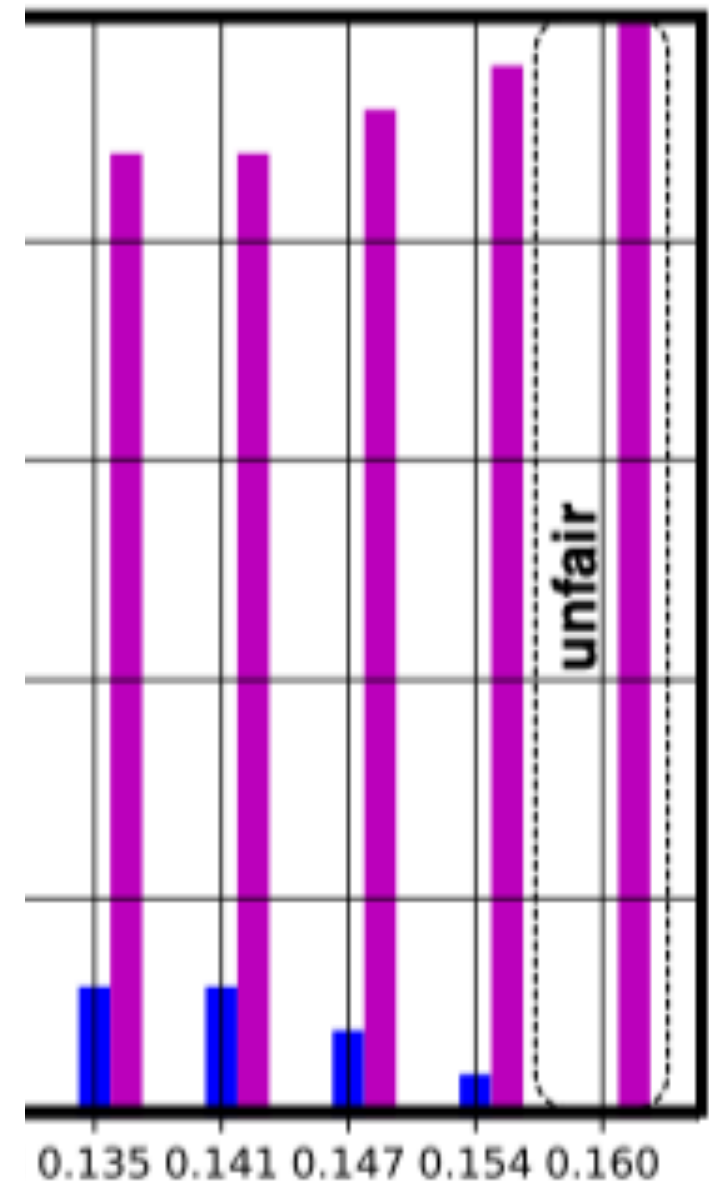
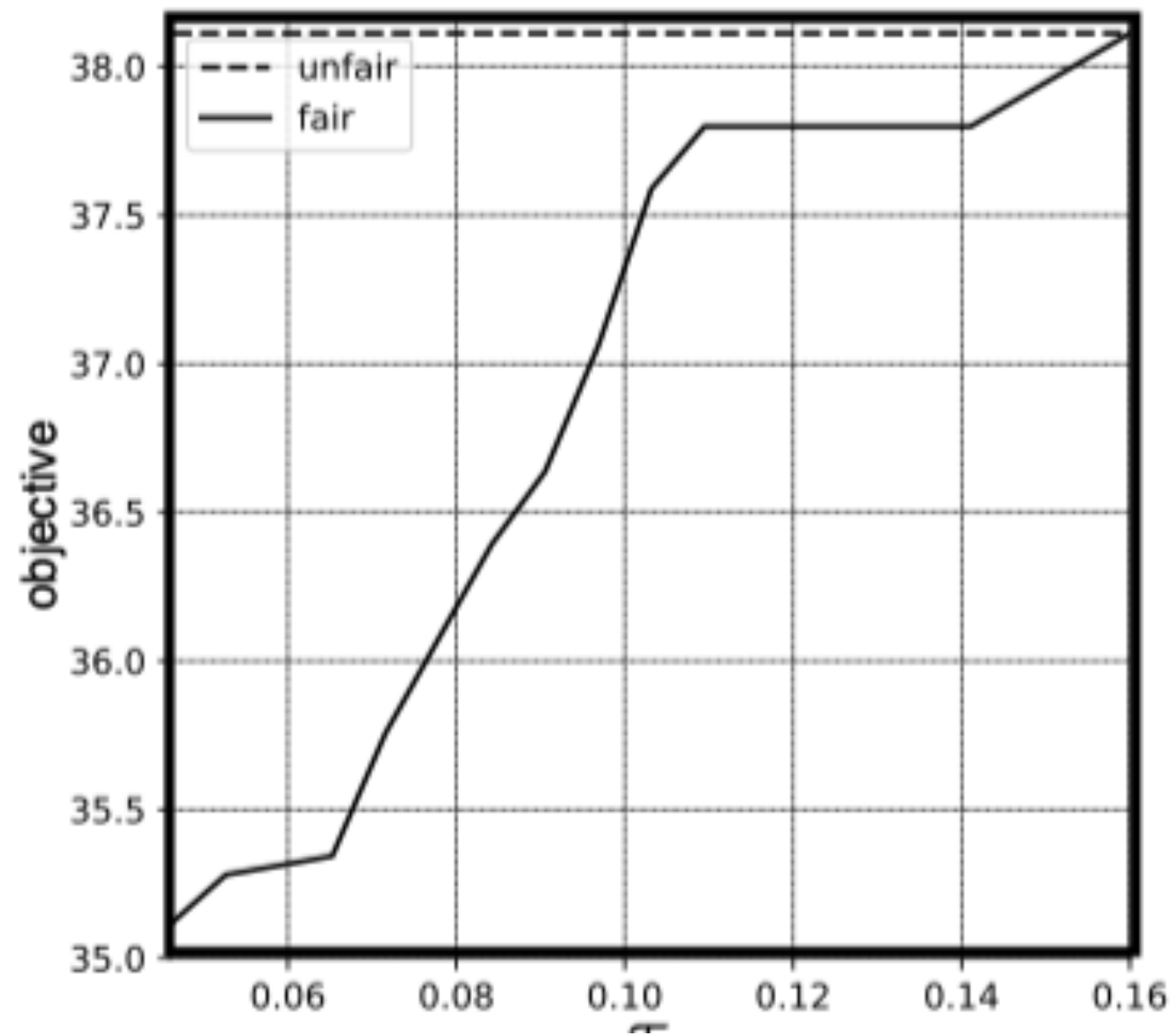
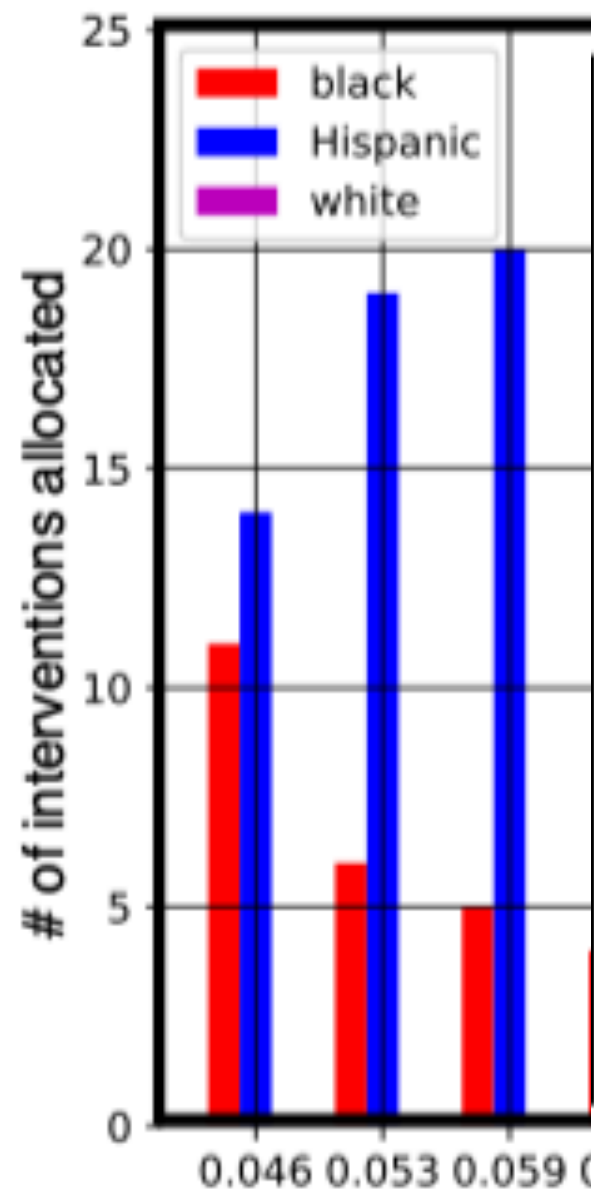


# The Fair Optimization Problem

- Formulated as a mixed-integer-linear-program
- Also a set of neighbors are considered for spillover effect

$$\begin{aligned} & \max_{z_1, \dots, z_n} \sum_{i=1}^n \mathbb{E}[Y_i(\mathbf{z}) \mid A_i = a_i, X_i = x_i] \\ & s.t., \sum_{i=1}^n z_i \leq B \\ & \quad G_{ia'} \leq \tau \quad \forall a' \in \mathcal{A}, i \in \{1, \dots, n\}, \end{aligned}$$

# Counterfactual Fairness: Applications



Kusner, M.J. (2018)

# Causal Fairness: Interventions

- Enforcing fairness by constraining interventional distributions

$$P(\hat{Y} | do(A = a)) = P(\hat{Y} | do(A = a'))$$

- A family of causal models are created as to minimize total effect of  $A$  on  $\hat{Y}$

# Kilbertus et al. on Counterfactual Fairness

- "It requires modeling counterfactuals on a per individual level, which is a delicate task..."
- "...Even determining the effect of race at the group level is difficult."
- An interesting argument among Causality researchers:
  - "Can we estimate causal effects for causes that we cannot understand in the real world?"

**Pearl, J. (2018). "Does Obesity Shorten Life? Or is it the Soda? On Non-manipulable Causes". [https://ftp.cs.ucla.edu/pub/stat\\_ser/r483-reprint.pdf](https://ftp.cs.ucla.edu/pub/stat_ser/r483-reprint.pdf)**



**Judea Pearl** @yudapearl · 15 Dec 2018

5/n

that DEFINES potential outcomes. This explains why @\_MiguelHernan depicts it as black magic when I assert that an ideal intervention is defined as a property of one's model. This conceptual barrier continues to impede communication until ..(YES)... a metamorphosis occurs...



2



13



**Miguel Hernán**

@\_MiguelHernan

Following

Replying to @yudapearl

No, not black magic. Just magic.

Black magic is evil. Your magical thinking is simply extrascientific.

By the way, your belief that hopelessly ill-defined causal questions can bring us the answer to life, the universe, and everything reminds me of this:

[https://twitter.com/\\_MiguelHernan/status/1074164493419200512](https://twitter.com/_MiguelHernan/status/1074164493419200512)

## Does Obesity Shorten Life? Or is it the Soda? On Non-manipulable Causes



**Miguel Hernán** @\_MiguelHernan · 16 May 2018

We cannot estimate "the causal effect of obesity" because we don't know what that means.

For the causal effect of A to be well defined, we need a common understanding of the interventions that we would use to change A. Otherwise, the effect is undefined.



**Miguel Hernán**  
@\_MiguelHernan

Following

Pearl believes that any causal effect we can name must also exist.

To him, the meaning of "the causal effect of A on death" is self-evident. He says we can quantify, say, the causal effect of race or the causal effect of obesity.

I don't think we can.

[https://twitter.com/\\_MiguelHernan/status/996876145953050624](https://twitter.com/_MiguelHernan/status/996876145953050624)

# Loftus et al. on Kilbertus et al.

- On the criterion: "...not realistic if  $X$  is a descendant of  $A$  in the causal graph, since in this case no single individual will keep  $X$  at a fixed level as  $A$  hypothetically varies."
- "...it is perfectly possible that  $\hat{Y}$  is highly discriminatory in a counterfactual sense and yet satisfies the purely interventional criterion..."
- Example: consider structural assignment  $Y = f(A, U_Y)$  such that:

$$P(U_Y = 0) = P(U_Y = 1) = \frac{1}{2} \text{ and } f(a, 1) = 1, f(a, 0) = 1 - a \text{ for } a \in \{0, 1\}$$

- Then:  $P(Y = 1 \mid do(A = 1)) = P(Y = 1 \mid do(A = 0)) = \frac{1}{2}$
- Even though for every individual:  $Y(a, u_Y) = 1 - Y(1 - a, u_Y)$

# The Causal Explanation Formula

- Explain discrimination by breaking up causal effects to 3 categories
- Partition discrimination to direct and indirect
- Alternative notions of causal unfairness
  - Zhang et al. consider  $A \leftarrow X \rightarrow \hat{Y}$  as spurious discrimination
  - But Loftus et al. believe that then  $X$  is protected too



# The Causal Explanation Formula

- Direct discrimination/Disparate treatment
  - Enforces procedural fairness
  - "...The equality of treatments that prohibits the use of the protected attribute in the decision process."
- Indirect discrimination/Disparate impact
  - Enforces outcome fairness
  - "...the equality of outcomes among protected groups."
  - "...occurs if a facially neutral practice has an adverse impact..."

# The Causal Explanation Formula

- Direct discrimination  $A \rightarrow Y$
- Indirect discrimination
  - Indirect causal discrimination  $A \rightarrow M \rightarrow Y$
  - Indirect spurious discrimination  $A \leftarrow Z \rightarrow Y$
- Zhang et al. argue that none of the existing measures are capable of detecting all three types of discrimination

# The Causal Explanation Formula

- Recap: Demographic parity:  $P(\hat{Y} = y | A = a) = P(\hat{Y} | A = a')$
- Total Variation  $TV_{a,a'}(y) = P(\hat{Y} = y | A = a) - P(\hat{Y} = y | A = a')$
- Recap: Counterfactual fairness:

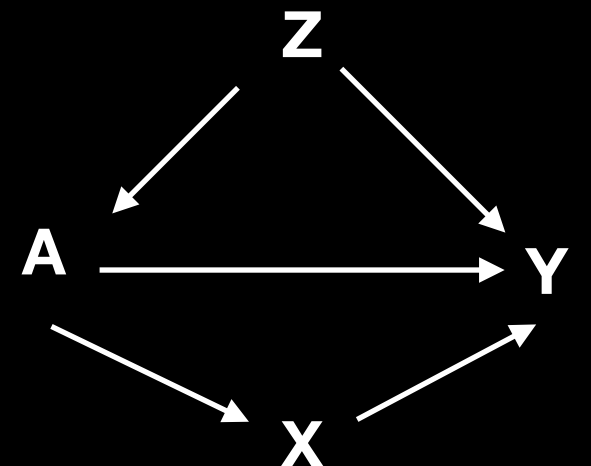
$$P(\hat{Y}(a, U) = y | X = x, A = a) = P(\hat{Y}(a', U) = y | X = x, A = a)$$

- Effect of Treatment on the Treated

$$ETT_{a,a'}(y) = P(\hat{Y}(a, U) = y | X = x, A = a) - P(\hat{Y}(a', U) = y | X = x, A = a)$$

# Toy Example: Hiring

- Y: Hiring decision, 1 for hired and 0 for not hired
- A: Religious belief, 1 for believer and 0 for non-believer
- Z: Educational background, 1 for high, 0 for low
- X: Location of the applicant, 1 for close to religious institutes, 0 for distant
- Assume Z has a negative effect on A
- Assume Z has a positive effect on X



# Toy Example: Hiring

- An applicant sues the company for discrimination
- The court notices that  $TV_{a,a'}(y) = 1$  where  $Y = 1$
- The company argues the disparity is mainly caused by  $Z$
- How can we verify this claim?
- Neither ETT, nor TE will show any unfairness
  - These two along, other measures, only account for direct and indirect effects

# Decomposing TV to Counterfactual Measures

- Counterfactual Direct Effect (Ctf-DE)

$$DE_{a,a'}(y | A) = P(Y(a', U), X(a, U)) - P(Y(a, U) | A)$$

- $DE_{a,a'}(y | A)$  captures existence of disparate treatment
- It is proved that if  $DE_{a,a'}(y | A) \neq 0$ , there is a direct path connecting A and Y

# Decomposing TV to Counterfactual Measures

- Counterfactual Indirect Effect (Ctf-IE)

$$IE_{a,a'}(y | A) = P(Y(a, U), X(a', U)) - P(Y(a, U) | A)$$

- "For  $A = a$ ,  $IE_{a,a'}(y | A = a)$  measures changes in the probability of the outcome  $Y$  would be  $y$  had  $A$  been  $a$ , while changing  $X$  to whatever level it would have obtained had  $A$  been  $a'$ , in particular, for the individuals that (naturally) have  $A = a$ ."
- It is proved that if  $IE_{a,a'}(y | A) \neq 0$ , there is a indirect path connecting  $A$  and  $Y$

# Decomposing TV to Counterfactual Measures

- Counterfactual Spurious Effect (Ctf-SE)

$$SE_{a,a'}(y) = P(Y(a, U) | A = a') - P(y | A = a)$$

- "  $SE_{a,a'}(y)$  measures the difference in outcome  $Y = y$  had  $A$  been  $a$  for the individuals that would naturally choose  $A$  to be  $a$  versus  $a'$ .
- It is proved that if  $SE_{a,a'}(y) \neq 0$ , there is a back-door path connecting  $A$  and  $Y$



# Decomposing TV to Counterfactual Measures

- Total disparity (TV) experienced by the individuals naturally attaining  $a'$  relative to the ones attaining  $a$  equals to the disparity experienced due to the spurious discrimination minus the advantage the ones attaining  $a'$  would have gained had they been  $a$

$$TV_{a,a'}(y) = SE_{a,a'}(y) - ETT_{a,a'}(y)$$

$$TV_{a,a'}(y) = ETT_{a',a}(y) - SE_{a',a}(y)$$

$$ETT_{a,a'}(y) = DE_{a,a'}(y | A = a) - IE_{a',a}(y | A = a)$$

# Causal Explanation Formula

- Total disparity experienced by the individuals who have naturally attained  $a'$  (relative to  $a$ ) equals to the disparity experienced associated with spurious discrimination, plus the advantage it lost due to indirect discrimination, minus the advantage it would have gained without direct discrimination

$$TV_{a,a'}(y) = SE_{a,a'}(y) + IE_{a,a'}(y | A = a') - DE_{a',a}(y | A = a')$$

$$TV_{a,a'}(y) = DE_{a,a'}(y | A = a) - SE_{a',a}(y) + IE_{a',a}(y | A = a)$$

# Causal Explanation Formula for Linear Models

$$IE_{a,a'}(Y|A = \alpha) = \gamma_{yx.\alpha z}\gamma_{x\alpha.z}(a' - a)$$

$$DE_{a,a'}(Y|A = \alpha) = \gamma_{ya.zx}(a' - a)$$

$$SE_{a,a'}(Y|A) = \gamma_{\alpha z}(\gamma_{yz.\alpha x} + \gamma_{yx.\alpha z}\gamma_{xz.\alpha})(a' - a)$$

- $\gamma$  are the corresponding (partial) regression coefficient.

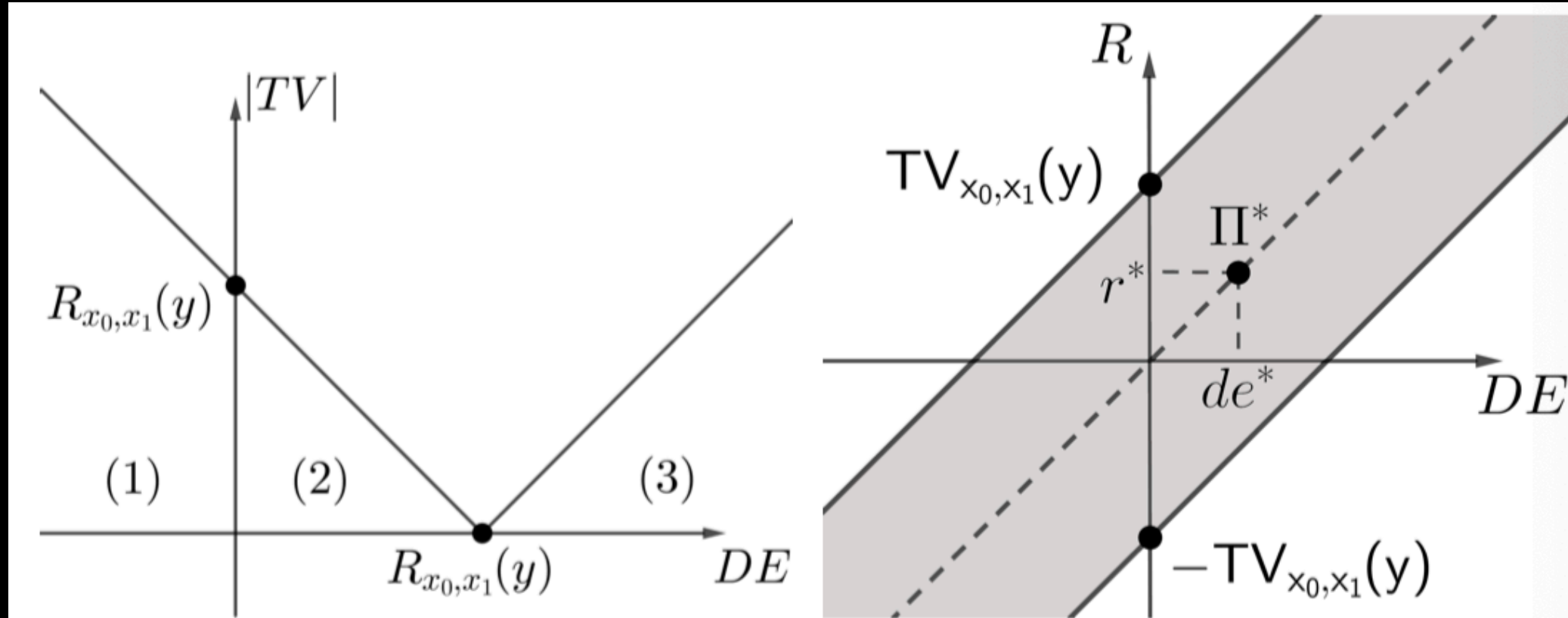
$$TV_{a,a'}(Y) = SE_{a,a'}(Y) + IE_{a,a'}(Y|A = \alpha) + DE_{a,a'}(Y|A = \alpha)$$

# Applications: Designing Reparatory Policies

- Companies and universities are required to fix unfairness if outcome disparity persists
- Affirmative action: Compensate previous discrimination by providing opportunities for members of the protected group
- A trade-off between Procedural and Outcome fairness
- Zhang et al. advocate for “narrowly tailoring” of affirmative action, to not introduce *reverse discrimination*

# Applications: Designing Reparatory Policies

- Residual disparity:  $R_{a,a'}(y) = SE_{a,a'}(y) + IE_{a,a'}(y | a')$
- Fix positive  $R_{a,a'}(y)$  and manipulate  $DE_{a',a}(y)$  so as to minimize total disparity  $|TV_{a,a'}(y)| = |R_{a,a'}(y) - DE_{a',a}(y | a')|$



- Narrow tailoring is satisfied only if:  $DE_{a',a}(y | A = a') \in [0, R_{a,a'}(y)]$

# What is Next?

- A paradigm for composition of causal measures of fairness
- Formalizing Interventions as a tool in policy-making
- Manipulating the non-manipulable causes

- Racial Bias and In-group Bias in Judicial Decisions: Evidence from Virtual Reality Courtrooms. Samantha Bielen, Wim Marneffe, Naci H. Mocan. December 2018
- "We shot videos of criminal trials using 3D Virtual Reality (VR) technology, prosecuted by actual prosecutors and defended by actual defense attorneys in an actual courtroom."
- "...allows us to replace white defendants in the courtroom with individuals who have Middle Eastern or North African descent in a real-life environment. We alter only the race of the defendants in these trials, holding all activity in the courtroom constant".
- "...significant overall racial bias in conviction decisions against minorities"

**<https://www.semanticscholar.org/paper/Racial-Bias-and-In-group-Bias-in-Judicial-Evidence-Bielen-Mocan/4aad052ab688a8b8e829caaeeede59ee05493b9e>**

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