

Types of Data:

BMI \rightarrow Numerical (~~Interval~~)

Smoking \rightarrow Categorical (~~Nominal~~)

Physical Health \rightarrow Numerical

Race \rightarrow Categorical

Age Category \rightarrow Numerical

Skin Cancer \rightarrow Categorical

Calculating Entropy

For BMI, we can make data intervals:

$$x < 20 \rightarrow 1$$

$$20 < x < 25 \rightarrow 22$$

$$25 < x < 30 \rightarrow 39$$

$$30 < x < 35 \rightarrow 25$$

$$35 < x < 40 \rightarrow 5$$

$$x > 40 \rightarrow 8$$

$$\begin{aligned}\therefore \text{Entropy (BMI)} &= -\frac{1}{100} \log_2 \left(\frac{1}{100} \right) - \frac{22}{100} \log_2 \left(\frac{22}{100} \right) \\ &\quad - \frac{39}{100} \log_2 \left(\frac{39}{100} \right) - \frac{25}{100} \log_2 \left(\frac{25}{100} \right) \\ &\quad - \frac{5}{100} \log_2 \left(\frac{5}{100} \right) - \frac{8}{100} \log_2 \left(\frac{8}{100} \right) \\ &= 2.08441\end{aligned}$$

Smoking:

$$0 \rightarrow 53$$

$$1 \rightarrow 47$$

$$\begin{aligned}\therefore \text{Entropy (Smoking)} &= -\frac{53}{100} \log_2 \left(\frac{53}{100} \right) - \frac{47}{100} \log_2 \left(\frac{47}{100} \right) \\ &= 0.9974\end{aligned}$$

Physical Health:

$$x < 5 \rightarrow 31$$

$$5 < x < 10 \rightarrow 31$$

$$10 < x < 20 \rightarrow 11$$

$$x > 20 \rightarrow 27$$

$$\begin{aligned}\therefore \text{Entropy (Physical Health)} &= -\frac{31}{106} \log_2 \left(\frac{31}{106} \right) - \frac{31}{100} \log_2 \left(\frac{31}{100} \right) \\ &\quad - \frac{11}{100} \log_2 \left(\frac{11}{100} \right) - \frac{27}{100} \log_2 \left(\frac{27}{100} \right) \\ &= 1.90789\end{aligned}$$

Race:

0 \rightarrow 1

1 \rightarrow 20

2 \rightarrow 1

3 \rightarrow 78

$$\begin{aligned}\text{Entropy (Race)} &= -\frac{1}{100} \log_2 \left(\frac{1}{100} \right) - \frac{20}{100} \log_2 \left(\frac{20}{100} \right) \\ &\quad - \frac{1}{100} \log_2 \left(\frac{1}{100} \right) - \frac{78}{100} \log_2 \left(\frac{78}{100} \right) \\ &= 0.87685\end{aligned}$$

Age Category :

$x < 30 \rightarrow 1$

$31 < x < 50 \rightarrow 5$

$51 < x < 70 \rightarrow 44$

$71 < x < 90 \rightarrow 50$

Entropy (Age Category) =

$$= -\frac{1}{100} \log_2 \left(\frac{1}{100} \right) - \frac{5}{100} \log_2 \left(\frac{5}{100} \right)$$

$$- \frac{44}{100} \log_2 \left(\frac{44}{100} \right) - \frac{50}{100} \log_2 \left(\frac{50}{100} \right)$$

$$= 1.30368$$

Skin Cancer :

$$0 \rightarrow 78$$

$$1 \rightarrow 22$$

$$\text{Entropy (Skin Cancer)} = -\frac{78}{100} \log_2 \left(\frac{78}{100} \right) - \frac{22}{100} \log_2 \left(\frac{22}{100} \right)$$

$$= 0.76016$$