

# 05\_Analysis\_of\_characters

March 29, 2020

## 1 Analysis of similarity of measured data

Computational notebook 05 for **Morphological tessellation as a way of partitioning space: Improving consistency in urban morphology at the plot scale.**

Fleischmann, M., Feliciotti, A., Romice, O. and Porta, S. (2020) *'Morphological tessellation as a way of partitioning space: Improving consistency in urban morphology at the plot scale'*, Computers, Environment and Urban Systems, 80, p. 101441. doi: [10.1016/j.compenvurbsys.2019.101441](https://doi.org/10.1016/j.compenvurbsys.2019.101441).

Contact: martin@martinfleischmann.net

Date: 29/03/2020

Note: notebook has been cleaned and released retroactively. It is likely that different versions of packages were initially used, but we made sure that the results remained unaltered.

### Data

The source of the data used within the research is the Amtliche Vermessung dataset accessible from the Zurich municipal GIS open data portal (<https://maps.zh.ch>). From it can be extracted the cadastral layer (`Liegenschaften_Liegenschaft_Area`) and the layer of buildings (all features named `Gebäude`). All data are licensed under CC-BY 4.0.

Source data: Vektor-Übersichtsplan des Kantons Zürich, 13.03.2018, Amt für Raumentwicklung Geoinformation / GIS-Produkte, Kanton Zürich, <https://opendata.swiss/de/dataset/vektor-ubersichtsplan1>

—

Data structure:

data/

single\_uids.csv - IDs of buildings being alone on a single plot (QGIS generated)

cadastre/

blg\_cadvals.shp - Cadastral values spatially joined to buildings

tessellation/

{k}\_tessellation.shp - tessellation layers

```
[1]: import numpy as np
import pandas as pd
import seaborn as sns
```

```

import matplotlib.pyplot as plt
from scipy import stats
import geopandas as gpd
from tqdm import tqdm
from sklearn.metrics import mean_squared_error
import math
import scipy.stats as sp
import matplotlib

```

```
[2]: path = 'data/'
```

```

[ ]: # set default seaborn style
sns.set()

cadastre = gpd.read_file(path + 'cadastre/blg_cadvals.shp')
tess10 = gpd.read_file(path + 'tessellation/10_tessellation.shp')
tess15 = gpd.read_file(path + 'tessellation/15_tessellation.shp')
tess20 = gpd.read_file(path + 'tessellation/20_tessellation.shp')
tess25 = gpd.read_file(path + 'tessellation/25_tessellation.shp')
tess30 = gpd.read_file(path + 'tessellation/30_tessellation.shp')
tess40 = gpd.read_file(path + 'tessellation/40_tessellation.shp')
tess50 = gpd.read_file(path + 'tessellation/50_tessellation.shp')
tess60 = gpd.read_file(path + 'tessellation/60_tessellation.shp')
tess70 = gpd.read_file(path + 'tessellation/70_tessellation.shp')
tess80 = gpd.read_file(path + 'tessellation/80_tessellation.shp')
tess90 = gpd.read_file(path + 'tessellation/90_tessellation.shp')
tess100 = gpd.read_file(path + 'tessellation/100_tessellation.shp')
tess150 = gpd.read_file(path + 'tessellation/150_tessellation.shp')
tess200 = gpd.read_file(path + 'tessellation/200_tessellation.shp')
tess300 = gpd.read_file(path + 'tessellation/300_tessellation.shp')

```

```

[ ]: characters = ['area', 'lal', 'circom', 'shapeix', 'rectan', 'fractal',
                  'orient', 'freq', 'car', 'gini_area', 'gini_car', 'Reach']

```

```

[ ]: buffers = {10: tess10, 15: tess15, 20: tess20, 25: tess25, 30: tess30, 40:
→tess40, 50: tess50, 60: tess60, 70: tess70, 80: tess80, 90: tess90,
            100: tess100, 150: tess150, 200: tess200, 300: tess300}
keys = [10, 15, 20, 25, 30, 40, 50, 60, 70, 80, 90, 100, 150, 200, 300]

```

```

[ ]: cadastre.rename(index=str, columns={'uID_left': 'uID'}, inplace=True)

```

```

[ ]: singleuids = pd.read_csv('data/single_uids.csv')
singles = singleuids['2'].to_list()

```

## 1.1 normality test

```
[ ]: for ch in characters:
    k2, p = sp.normaltest(cadastre[ch])
    alpha = 1e-3
    print("p = {:.g}".format(p))

    if p < alpha: # null hypothesis: x comes from a normal distribution
        print(ch + ": The null hypothesis can be rejected (non-normal_
↪distribution)")
    else:
        print(ch + ": The null hypothesis cannot be rejected")
```

## 1.2 root mean squared deviation

#tes = tes.loc[tes['uID'].isin(singles)] can be used to generate analysis for single/multi building plots individually

```
[ ]: df1 = pd.DataFrame(keys, columns=['buffer'])
rmsde = df1
for ch in characters:
    for b in buffers:
        try:
            key = '{b}_{ch}'.format(b=b, ch=ch)
            tes = buffers[b]
            #tes = tes.loc[tes['uID'].isin(singles)]
            true = tes[ch]
            cad = cadastre
            #cad = cad.loc[cad['uID'].isin(singles)]
            prediction = cad[ch]
            min = true.min() if true.min() < prediction.min() else prediction.
↪min()
            max = true.max() if true.max() > prediction.max() else prediction.
↪max()

            # iqr = stats.iqr(true) if stats.iqr(true) > stats.iqr(prediction)
↪else stats.iqr(prediction)
            value = math.sqrt(mean_squared_error(true, prediction)) / (max -
↪min) # normalised
        except Exception:
            value = np.nan
        if b == 10:
            list = pd.Series(value, index=[b])
        else:
            list = list.append(pd.Series(value, index=[b]))

    rmsde[ch] = list.values
#rmsde.to_csv('Results_all_rsmd.csv')
```

```
[ ]: sns.set_style('ticks', {'xtick.bottom': False, 'ytick.left': True})
sns.set_context(context='paper', font_scale=1, rc=None)
colors = [(72,129,185), (123,173,210), (115,109,170), (158,155,196),
↳(188,189,217), (218,218,234), (224,131,173), (197,57,51), (230,156,155),
      (85,160,92), (135,187,125), (142,60,33), (201,102,45), (231,155,71),
↳(248,218,152), (252,248,216)]

# create a color palette
# palette = plt.get_cmap('tab20')
for index, col in enumerate(colors):
    list = []
    for idx, rgb in enumerate(col):
        rgb = rgb / 255
        list.append(rgb)
    colors[index] = tuple(list)
palette = matplotlib.colors.ListedColormap(colors, name='from_list', N=None)
# multiple line plot
num = 0
for column in rmsde.drop(['buffer'], axis=1):
    plt.plot(rmsde['buffer'], rmsde[column].fillna(method='ffill'), marker='',
↳color=palette(num), linewidth=1, alpha=0.9, label=column)
    num += 1
sns.despine(offset=10, trim=False, left=True, bottom=True)
plt.xlim(1, 300)
plt.axvline(x=100, color='r', linestyle='--', lw=1)

# Add legend
lgd = plt.legend(bbox_to_anchor=(1.05, 1), loc=2, ncol=1,)
plt.grid(True, which='major', axis='x')
plt.ylabel("Normalised RMSD")
plt.xlabel("Buffer distance")
plt.title("Normalised root squared mean deviation")
new_labels = ['area', 'longest axis length', 'circular compactness', 'shape',
↳index', 'rectangularity', 'fractal dimension',
      'orientation', 'CAR', 'frequency', 'Gini of area', 'Gini of CAR',
↳'Reach']
for t, l in zip(lgd.texts, new_labels):
    t.set_text(l)
#plt.savefig(path + 'Results_multi_rsmd.png',
#           dpi=300, bbox_extra_artists=(lgd,), bbox_inches='tight')
plt.gcf().clear()
```

### 1.3 spearman rho

#tes = tes.loc[tes['uID'].isin(singles)] can be used to generate analysis for single/multi building plots individually

```
[ ]: # correlation spearman rho
df1 = pd.DataFrame(keys, columns=['buffer'])
spearman_rho = df1
for ch in characters:

    for b in buffers:
        try:
            key = '{b}_{ch}'.format(b=b, ch=ch)
            tes = buffers[b]
            #tes = tes.loc[~tes['uID'].isin(singles)]
            cad = cadastre
            #cad = cad.loc[~cad['uID'].isin(singles)]
            value = sp.spearmanr(cad[ch], tes[ch])[0] # get correlation
            ↪coefficient r
            p = sp.spearmanr(cad[ch], tes[ch])[1]
        except Exception:
            value = np.nan
            p = np.nan

        if b == 10:
            list = pd.Series(value, index=[b])
            p_list = pd.Series(p, index=[b])
        else:
            list = list.append(pd.Series(value, index=[b]))
            p_list = p_list.append(pd.Series(p, index=[b]))

    p_column = 'p_{ch}'.format(ch=ch)
    spearman_rho[ch] = list.values
    # spearman_rho[p_column] = p_list.values

#spearman_rho.to_csv('Results_multi_spearman.csv')
```

```
[ ]: # plot
# style
sns.set_style('ticks', {'xtick.bottom': False, 'ytick.left': True,})
sns.set_context(context='paper', font_scale=1, rc=None)
colors = [(72,129,185), (123,173,210), (115,109,170), (158,155,196), ↵
            ↪(188,189,217), (218,218,234), (224,131,173), (197,57,51), (230,156,155),
            (85,160,92), (135,187,125), (142,60,33), (201,102,45), (231,155,71), ↵
            ↪(248,218,152), (252,248,216)]

# create a color palette
# palette = plt.get_cmap('tab20')
for index, col in enumerate(colors):
    list = []
    for idx, rgb in enumerate(col):
        rgb = rgb / 255
```

```

        list.append(rgb)
    colors[index] = tuple(list)
palette = matplotlib.colors.ListedColormap(colors, name='from_list', N=None)

# multiple line plot
num = 0
for column in spearman_rho.drop(['buffer'], axis=1):
    plt.plot(spearman_rho['buffer'], spearman_rho[column].
        ↪ fillna(method='ffill'), marker='', color=palette(num), linewidth=1, alpha=0.
        ↪ 9, label=column)
    num += 1
sns.despine(offset=10, trim=False, left=True, bottom=True)
plt.xlim(1, 300)
plt.axvline(x=100, color='r', linestyle='--', lw=1)

# Add legend
lgd = plt.legend(bbox_to_anchor=(1.05, 1), loc=2, ncol=1,)
plt.grid(True, which='major', axis='x')
plt.ylim(0, 1.05)
# plt.xlim(10)
plt.ylabel("Spearman's rho")
plt.xlabel("Buffer distance")
plt.title("Correlations")
new_labels = ['area', 'longest axis length', 'circular compactness', 'shape_
    ↪ index', 'rectangularity', 'fractal dimension',
                'orientation', 'CAR', 'frequency', 'Gini of area', 'Gini of CAR',
    ↪ 'Reach']
for t, l in zip(lgd.texts, new_labels):
    t.set_text(l)

# plt.savefig(path + 'Results_multi_spearman.png', dpi=300,
    ↪ bbox_extra_artists=(lgd,), bbox_inches='tight')
plt.gcf().clear()

```

#### 1.4 moran deviation

#tes = tes.loc[tes['uID'].isin(singles)] can be used to generate analysis for single/multi building plots individually

```

[ ]: files = [
    tess10,
    tess15,
    tess20,
    tess25,
    tess30,
    tess40,

```

```

tess50,
tess60,
tess70,
tess80,
tess90,
tess100,
tess150,
tess200,
tess300,
cadastre,
]

for f in files:
    f.rename(
        index=str,
        columns={"m_gini_are": "m_gini_area", "p_gini_are": "p_gini_area"},
        inplace=True,
    )

```

```

[ ]: # moran deviation
moran = pd.DataFrame(keys, columns=["buffer"])
for ch in tqdm(characters):
    max = 0
    cadlist = []
    rch = "p_{}".format(ch)
    mch = "m_{}".format(ch)
    for idx, row in cadastre.iterrows():
        if row[rch] <= 0.01:
            max = max + 1
            cadlist.append(row[mch])
        else:
            cadlist.append(None)
    cadastre["Moran_sig"] = cadlist
    for b in tqdm(buffers):
        try:
            buflist = []
            for idx, row in buffers[b].iterrows():
                if row[rch] <= 0.01:
                    buflist.append(row[mch])
                else:
                    buflist.append(None)
            buffers[b]["Moran_sig"] = buflist

            compare = cadastre["Moran_sig"] == buffers[b]["Moran_sig"]
            value = sum(compare) / max
        except Exception:
            value = np.nan

```

```

        if b == 10:
            list = pd.Series(value, index=[b])
        else:
            list = list.append(pd.Series(value, index=[b]))

    moran[ch] = list.values
#moran.to_csv(
#    "Results2_all_accu.csv"
#)

```

```

[ ]: #cad_s = cadastre.loc[~cadastre["uID_left"].isin(singles)] # used to filter
      ↳analysis for single-building, multt-building and all plots
for ch in tqdm(characters):
    max = 0
    cadlist = []
    rch = "p_{}".format(ch)
    mch = "m_{}".format(ch)
    for idx, row in cad_s.iterrows():
        if row[rch] <= 0.01:
            max = max + 1
            cadlist.append(row[mch])
        else:
            cadlist.append(None)
    cad_s["Moran_sig"] = cadlist
    for b in tqdm(buffers):
        try:
            buflist = []
            tes = buffers[b]
            tes_s = tes.loc[~tes["uID"].isin(singles)]
            for idx, row in tes_s.iterrows():
                if row[rch] <= 0.01:
                    buflist.append(row[mch])
                else:
                    buflist.append(None)
            tes_s["Moran_sig"] = buflist

            compare = cad_s["Moran_sig"] == tes_s["Moran_sig"]
            value = sum(compare) / max
        except Exception:
            value = np.nan
    if b == 10:
        list = pd.Series(value, index=[b])
    else:
        list = list.append(pd.Series(value, index=[b]))

    moran[ch] = list.values
#moran.to_csv(

```



```
# "Results2_m_accu.csv"
#)
```

```
[ ]: sns.set_style("ticks", {"xtick.bottom": False, "ytick.left": True})
sns.set_context(context="paper", font_scale=1, rc=None)
colors = [
    (72, 129, 185),
    (123, 173, 210),
    (115, 109, 170),
    (158, 155, 196),
    (188, 189, 217),
    (218, 218, 234),
    (224, 131, 173),
    (197, 57, 51),
    (230, 156, 155),
    (85, 160, 92),
    (135, 187, 125),
    (142, 60, 33),
    (201, 102, 45),
    (231, 155, 71),
    (248, 218, 152),
    (252, 248, 216),
]

# create a color palette
# palette = plt.get_cmap('tab20')
for index, col in enumerate(colors):
    list = []
    for idx, rgb in enumerate(col):
        rgb = rgb / 255
        list.append(rgb)
    colors[index] = tuple(list)
palette = matplotlib.colors.ListedColormap(colors, name="from_list", N=None)

# multiple line plot
num = 0
# moran[[col for col in moran.columns if '_m' in col]]
for column in moran.drop(["buffer"], axis=1):
    plt.plot(
        moran["buffer"],
        moran[column].fillna(method="ffill"),
        marker="",
        color=palette(num),
        linewidth=1,
        alpha=0.9,
        label=column,
```

```

    )
    num += 1
# Add legend
lgd = plt.legend(bbox_to_anchor=(1.05, 1), loc=2, ncol=1)
plt.grid(True, which='major', axis='x')
sns.despine(offset=10, trim=False, left=True, bottom=True)
plt.xlim(1, 300)
plt.ylim(0, 1.05)
plt.axvline(x=100, color="r", linestyle="--", lw=1)

plt.ylabel("Accuracy score")
plt.xlabel("Buffer distance")
plt.title("Local spatial autocorrelation accuracy")
new_labels = [
    "area",
    "longest axis length",
    "circular compactness",
    "shape index",
    "rectangularity",
    "fractal dimension",
    "orientation",
    "CAR",
    "frequency",
    "Gini of area",
    "Gini of CAR",
    "Reach",
]
for t, l in zip(lgd.texts, new_labels):
    t.set_text(l)
plt.savefig(
    path + "Results2_m_accu.png",
    dpi=300,
    bbox_extra_artists=(lgd,),
    bbox_inches="tight",
)
plt.gcf().clear()

```

[ ]: