

$$\begin{aligned} \textcircled{1} \quad F(x, y, z) &= xy + x'z + yz + (x \cdot x') \\ &\equiv (x' + y) + xy + (x \cdot x') \\ &\equiv (x' + y) + x(x' + y) \\ &\Rightarrow (x + z) \cdot (x' + y) \end{aligned}$$

$$\begin{aligned} \textcircled{2} \quad (x+y)(x'+z)(y+z) &= (x+y)(x'+z) \\ &\quad (x+y)(x'+z)(y+z+x \cdot x') \\ &\quad (x+y)(x'+z) \quad (x+y+z) \uparrow (x'+y+z) \\ &\quad (x+y) \underbrace{(1+z)}_{1} \quad (x'+z) \underbrace{(1+y)}_{1} \\ &\Rightarrow (x+y)(x'+z) \end{aligned}$$

a)

	A	B	C	D	$B'D$	$A'D$	BD	F	
0	0	0	0	0	0	0	0	0	m_0
0	0	0	1	1	1	0	1	$\rightarrow a'b'c'd$	m_1
0	0	1	0	0	0	0	0	0	m_2
0	0	1	1	1	1	0	1	$\rightarrow a'b'cd$	m_3
0	1	0	0	0	0	0	0	0	m_4
0	1	0	1	0	1	1	1	$\rightarrow a'bc'd$	m_5
0	1	1	0	0	0	0	0	0	m_6
0	1	1	1	0	1	1	1	$\rightarrow a'bcd$	m_7
1	0	0	0	0	0	0	0	0	m_8
1	0	0	1	1	0	0	1	$\rightarrow ab'cd$	m_9
1	0	1	0	0	0	0	0	0	m_{10}
1	0	1	1	1	0	0	1	$\rightarrow ab'c'd$	m_{11}
1	1	0	0	0	0	0	0	0	m_{12}
1	1	0	1	0	0	1	1	$\rightarrow abc'd$	m_{13}
1	1	1	0	0	0	0	0	0	m_{14}
1	1	1	1	0	0	1	1	$\rightarrow abc'd$	m_{15}

Sum of minterms $\Sigma(1, 3, 5, 7, 9, 11, 13, 15)$ Product of maxterm $\Pi(0, 2, 4, 6, 8, 10, 12, 14)$

$$\begin{aligned} A+A' &= 1 \\ A'+A &= 1 \end{aligned}$$

$$F(A, B, C, D) = B'D + A'D + BD$$

$$D(B' + A' + B) = D \underbrace{(1 + A')}_{1} - D$$