

Ege University
Department of Computer Engineering
Automata Theory
2020-2021 Fall
HOMEWORK-1

Date Given: 20.11.2020

Due Date: 26.11.2020

QUESTIONS

1. $S=\{ab,bb\}$ and $T=\{ab,bb,bbb\}$ is given.

i) Write the set S^* .

ii) Write the set T^* .

iii) Is the word **bbbbababbb** an element of S^* ? Show your answer.

iv) Is the word **bbbaab** an element of T^* ? Show your answer.

v) Show (by giving examples) that $S^* \neq T^*$

vi) Show (by giving examples) that $S^* \subseteq T^*$

2. Give recursive definitions for the following languages over the alphabet $\Sigma=\{a,b\}$

i) Give a recursive definition for the language L_{AA} of all words containing the substring aa . (The alphabet $\Sigma=\{a,b\}$ and $NULL$ is **not** an element in L_{AA} .) Then, prove that **baabb** is a word in the language L_{AA} .

ii) Give a recursive definition for the language L_{NOTAA} of all words not containing the substring aa . (The alphabet $\Sigma=\{a,b\}$ and $NULL$ is an element in L_{NOTAA}). Then, prove that **babab** is a word in the language L_{NOTAA} .

3. Construct a regular expression for each of the languages given below (The alphabet $\Sigma=\{a,b\}$).

i) All words in which a appears tripled, if at all. This means that every clump of a 's contains 3 or 6 or 9 or 12 . . . a 's.

ii) All words that contain exactly two b 's or exactly three b 's, not more.

iii) All strings in which any b 's that occur are found in clumps of an odd number at a time, such as **abaabbbab**.

iv) Describe in English phrases the language defined by the regular expression
 $(a + b)^*a(\Lambda + bbbb)$

v) Describe in English phrases the language defined by the regular expression
 $b^*ab^*(ab^*ab^*)^*$

Evaluation : Q1)30 pts Q2)20 pts Q3)50 pts