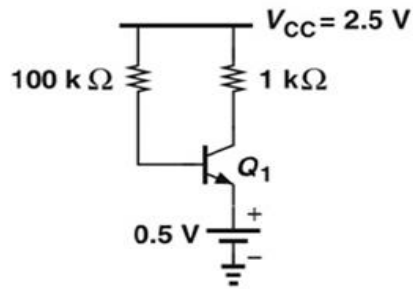


EE 101 Tutorial -4 BJT Amplifier (Solution)

1.
Sol



$$V_{CC} - I_B(100 \text{ k}\Omega) = V_{BE} + 0.5 \text{ V}$$

$$V_{CC} - \frac{1}{\beta} I_C(100 \text{ k}\Omega) = V_T \ln(I_C/I_S) + 0.5 \text{ V}$$

$$I_C = \boxed{1.262 \text{ mA}}$$

$$V_{BE} = \boxed{738 \text{ mV}}$$

$$V_{CE} = V_{CC} - I_C(1 \text{ k}\Omega) - 0.5 \text{ V} \\ = \boxed{738 \text{ mV}}$$

Q_1 is operating at the edge of saturation.

2. Sol.

(a)

$V_{CE} \geq V_{BE}$ (in order to guarantee operation in the active mode)

$$V_{CC} - I_C(2 \text{ k}\Omega) \geq V_{BE}$$

$$V_{CC} - I_C(2 \text{ k}\Omega) \geq V_T \ln(I_C/I_S)$$

$$I_C \leq 886 \text{ }\mu\text{A}$$

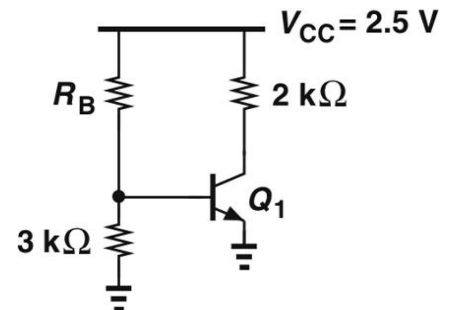
$$\frac{V_{CC} - V_{BE}}{R_B} - \frac{V_{BE}}{3 \text{ k}\Omega} = I_B = \frac{I_C}{\beta}$$

$$\frac{V_{CC} - V_T \ln(I_C/I_S)}{R_B} - \frac{V_T \ln(I_C/I_S)}{3 \text{ k}\Omega} = \frac{I_C}{\beta}$$

$$R_B \left(\frac{I_C}{\beta} + \frac{V_T \ln(I_C/I_S)}{3 \text{ k}\Omega} \right) = V_{CC} - V_T \ln(I_C/I_S)$$

$$R_B = \frac{V_{CC} - V_T \ln(I_C/I_S)}{\frac{I_C}{\beta} + \frac{V_T \ln(I_C/I_S)}{3 \text{ k}\Omega}}$$

$$R_B \geq \boxed{7.04 \text{ k}\Omega}$$



(b)

$$\frac{V_{CC} - V_{BE}}{R_B} - \frac{V_{BE}}{3 \text{ k}\Omega} = I_B = \frac{I_C}{\beta}$$

$$I_C = \beta \frac{V_{CC} - V_T \ln(I_C/I_S)}{R_B} - \beta \frac{V_T \ln(I_C/I_S)}{3 \text{ k}\Omega}$$

$$I_C = 1.14 \text{ mA}$$

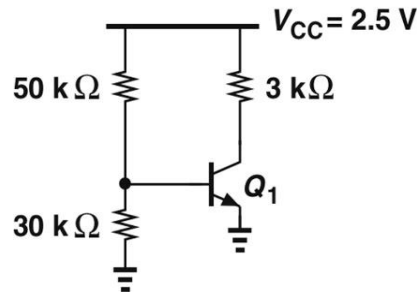
$$V_{BE} = 735 \text{ mV}$$

$$V_{CE} = V_{CC} - I_C(2 \text{ k}\Omega) = 215 \text{ mV}$$

$$V_{BC} = V_{BE} - V_{CE} = \boxed{520 \text{ mV}}$$

3.

Sol.



Q.3. Sol.
 Given, $I_C = 0.5 \text{ mA}$
 $\beta = 100$
 Find I_S
 $\rightarrow I_C = \beta I_B$
 $\Rightarrow I_B = 0.005 \text{ mA}$
 $\rightarrow \frac{(V_{th} - V_{BE})}{R_{th}} = I_B \times R_{th}$
 $0.9375 - V_{BE} = 0.5 \times 10^{-5} \times 18.75 \times 10^3$
 $\boxed{V_{BE} = 0.84375 \text{ V}}$
 \Rightarrow
 $\rightarrow R_{th} = 30 \text{ k} \parallel 50 \text{ k}$
 $= \left(\frac{30 \times 50}{80} \right) \text{ k} = \boxed{18.75 \text{ k}}$
 $\rightarrow V_{th} = \left(\frac{30}{30+50} \right) \times 2.5 = \boxed{0.9375}$
 $\Rightarrow I_C = I_S \left(e^{V_{BE}/V_T} \right)$
 $\Rightarrow I_S = \frac{I_C}{e^{(V_{BE}/V_T)}}$
 $= \frac{0.5 \times 10^{-3}}{e^{(0.84375/0.025)}}$
 $I_S = 4.03 \times 10^{-15} \text{ mA}$

(b) At the edge of saturation — $V_{CE} = V_{CE}$ (Left saturation not allowed.)

$$V_{CE} = 2.5 - I_C (3 \text{ k})$$

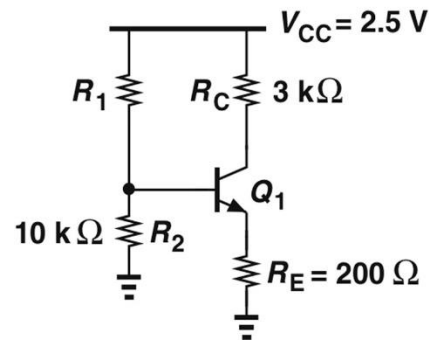
$$I_C = \beta I_B = \beta \left(\frac{V_{th} - V_{BE}}{R_{th}} \right)$$

$$V_{BE} = 2.5 - \beta \left(\frac{V_{th} - V_{BE}}{R_{th}} \right) \times (3 \text{ k})$$

$$\Rightarrow \boxed{V_{BE} = 0.83 \text{ V}}$$

$$I_S = \frac{I_C}{e^{(V_{BE}/V_T)}} = 7.84 \times 10^{-15} \text{ mA}$$

4.



Sol. (a)

$$\begin{aligned}
 I_C &= 0.25\text{ mA} \\
 V_{BE} &= 696\text{ mV} \\
 \frac{V_{CC} - V_{BE} - I_E R_E}{R_1} - \frac{V_{BE} + I_E R_E}{R_2} &= I_B = \frac{I_C}{\beta} \\
 R_1 &= \frac{V_{CC} - V_{BE} - \frac{1+\beta}{\beta} I_C R_E}{\frac{I_C}{\beta} + \frac{V_{BE} + \frac{1+\beta}{\beta} I_C R_E}{R_2}} \\
 &= \boxed{22.74\text{ k}\Omega}
 \end{aligned}$$

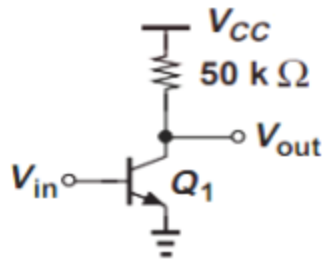
(b) First, consider a 5 % increase in R_E .

$$\begin{aligned}
 R_E &= 210\ \Omega \\
 \frac{V_{CC} - V_{BE} - I_E R_E}{R_1} - \frac{V_{BE} + I_E R_E}{R_2} &= I_B = \frac{I_C}{\beta} \\
 \frac{V_{CC} - V_T \ln(I_C/I_S) - \frac{1+\beta}{\beta} I_C R_E}{R_1} - \frac{V_T \ln(I_C/I_S) + \frac{1+\beta}{\beta} I_C R_E}{R_2} &= I_B = \frac{I_C}{\beta} \\
 I_C &= 243\ \mu\text{A} \\
 \frac{I_C - I_{C,nom}}{I_{C,nom}} \times 100 &= \boxed{-2.6\ \%}
 \end{aligned}$$

Now, consider a 5 % decrease in R_E .

$$\begin{aligned}
 R_E &= 190\ \Omega \\
 I_C &= 257\ \mu\text{A} \\
 \frac{I_C - I_{C,nom}}{I_{C,nom}} \times 100 &= \boxed{+2.8\ \%}
 \end{aligned}$$

5. So



$$A_v = g_m R_c = 20$$

$$\frac{I_c R_c}{V_T} = 20 \Rightarrow I_c = \frac{20 V_T}{R_c}$$

$$I_c = 0.0104 \text{ mA}$$

$$V_{cc} - (50 \text{ k}\Omega) \cdot (0.0104 \text{ mA}) = V_{BE}$$

$$\Rightarrow V_{cc} - 50 \times 0.0104 \text{ V} = 0.8 \text{ V}$$

$$\Rightarrow V_{cc} = 1.32 \text{ V}$$

6. Sol.

⑥

Given $I_c = I_S e^{\frac{V_{BE}}{2V_T}}$

$I_c = 1 \text{ mA}$

$A_v = ?$

Now we know that $A_v = g_m R_{out}$ (from small signal analysis)

$A_v = g_m R_c$

We also know that $g_m = \frac{2I_c}{V_{BE}}$

$g_m = \frac{I_S}{2V_T} e^{\frac{V_{BE}}{2V_T}}$

$g_m = \frac{I_c}{2V_T}$

$\therefore A_v = \frac{I_c}{2V_T} \times R_c$

$A_v = \frac{1 \times 10^{-3}}{2 \times 26 \times 10^{-3}} \times 1 \times 10^3$

$A_v = 19.23$

7. Sol.

⑦

Given $\beta = 100$, $I_S = 6 \times 10^{-16} \text{ A}$, $V_A = \infty$.

Let's first do the DC analysis of the circuit -

Then, Apply KVL,

$$2.5 = (50 \times 10^3) I_B + V_{BE} + (2 \times 10^3) I_E$$

Then,

$$2.5 = (50 \times 10^3) \frac{I_C}{\beta} + V_T \ln \left(\frac{I_C}{I_S} \right) + (2 \times 10^3) I_C \left(1 + \frac{1}{\beta} \right)$$

Solving this transcendental equation we will get

$$I_C = 708 \mu\text{A}$$

Now, $g_m = \frac{I_C}{V_T} = \frac{708 \times 10^{-6}}{26 \times 10^{-3}} = 27.2 \times 10^{-3} \text{ S}$

Now to get the voltage gain let's do the AC analysis

In AC analysis capacitor will provide less reactance path,

Let's work on output side loop, Apply KCL

$$g_m V_{\pi} = - \frac{V_{out}}{1 \times 10^3}$$

$$V_{out} = - g_m V_{\pi} \times 10^3 \quad \text{--- (2)}$$

Let's go to input side loop:-

Apply Nodal analysis,

$$\frac{V_{in} - V_{\pi}}{1 \times 10^3} = \frac{V_{\pi}}{50 \times 10^3} + \frac{V_{\pi}}{2 \times 10^3}$$

$$\Rightarrow V_{in} = 10^3 \left(\frac{1}{10^3} + \frac{1}{50 \times 10^3} + \frac{1}{2 \times 10^3} \right) V_{\pi}$$

$$r_{\pi} = \frac{\beta}{g_m} = \frac{100}{27 \cdot 2 \times 10^{-3}} = 3676.470.$$

$$v_{in} = 10^3 \left(\frac{1}{10^3} + \frac{1}{50 \times 10^3} + \frac{1}{3676.470} \right) v_{in}$$

$$v_{in} = 1.262 \cdot v_{\pi}$$

using (2), $v_{out} = -g_m v_{\pi} \times 10^3$

$$v_{out} = -27 \cdot 2 \times 10^{-3} \times 10^3 \times \frac{v_{in}}{1.262}$$

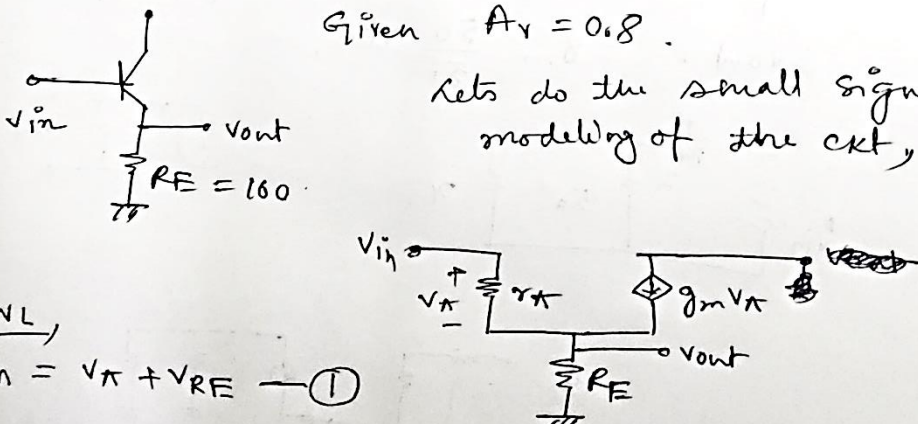
$$\frac{v_{out}}{v_{in}} = - \frac{27 \cdot 2 \times 10^{-3} \times 10^3}{1.262} = -21.55.$$

$$A_v = -21.55$$

8. Sol.

Given $A_v = 0.8$.

Let's do the small signal modeling of the ckt,



KVL,

$$v_{in} = v_{\pi} + v_{RE} \quad \text{--- (1)}$$

$v_{RE} = v_{out} \quad \text{--- (2)}$

KCL,

$$\frac{v_{\pi}}{r_{\pi}} + g_m v_{\pi} = I_E \Rightarrow \frac{v_{\pi}}{r_{\pi}} + g_m v_{\pi} = \frac{v_{out}}{R_E}$$

$\therefore v_{in} = v_{\pi} + \left(\frac{v_{\pi}}{r_{\pi}} + g_m v_{\pi} \right) R_E \Rightarrow v_{\pi} = \left(\frac{r_{\pi}}{\beta + 1} \right) \frac{v_{out}}{R_E}$

From ① & ③,

$$v_{in} = v_{\pi} + v_{out}$$

$$\Rightarrow v_{in} = \left(\frac{r_{\pi}}{\beta+1} \right) \frac{v_{out}}{R_E} + v_{out}$$

$$\Rightarrow A_v = \frac{v_{out}}{v_{in}} = \frac{1}{1 + \left(\frac{r_{\pi}}{\beta+1} \right) \frac{1}{R_E}}$$

upon simplification.
let $\beta \gg 1$

$$\therefore \beta+1 \rightarrow \beta.$$

$$A_v = \frac{1}{1 + \left(\frac{r_{\pi}}{\beta} \right) \frac{1}{R_E}}$$

we know that,

$$r_{\pi} = \frac{\beta}{g_m}$$

$$\frac{r_{\pi}}{\beta} = \frac{1}{g_m}$$

therefore,

$$A_v = \frac{1}{1 + \frac{(1/g_m)}{R_E}}$$

$$\therefore A_v = \frac{R_E}{R_E + 1/g_m}$$

$$A_v = \frac{R_E}{R_E + 1/g_m}$$

$$\Rightarrow 0.8 = \frac{100}{100 + \frac{V_T}{I_C}}$$

$$\frac{1}{g_m} = \frac{V_T}{I_C}$$

$$V_T = 26 \times 10^{-3}.$$

upon solving,

$$I_C = 1.04 \text{ mA.}$$