## **CS 538**

# Introduction to the Theory and Design of Programming Languages

Charles N. Fischer

Spring 2001

http://www.cs.wisc.edu/~fischer/cs538.html

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## Class Meets

Mondays, Wednesdays & Fridays, 11:00 — 11:50

376 Mechanical Engineering

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## **Key Dates**

February 21: Homework #1 (tentative)

March 19: Programming Assignment #1 -

Scheme (tentative)

March 28: Midterm Exam (tentative)

April 9: Programming Assignment #2 -

Standard ML (tentative)

April 30: Programming Assignment #3 -

Prolog (tentative)

May 9: Programming Assignment #4 -

Pizza and Python

May 13: Final Exam 12:25pm-2:25pm

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## **Class Text**

Required text:

Programming Languages: Concepts & Constructs, Second Edition, Ravi Sethi, Addison-Wesley, 1996.

Suggested supplemental Class Text:

Programming Language Pragmatics, Michael L. Scott, Morgan Kaufmann, 1999.

 Handouts and Web-based reading will also be used.

## Reading Assignment

- Sethi: Chapters 1-3 (as background)
- Scott: Chapters 1-2 (as background)

## **Class Notes**

 The transparencies used for each lecture will be made available prior to, and after, that lecture on the class Web page (under the "Lecture Nodes" link).

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## Instructional Computers

Departmental Unix Machines (nova1nova40) have been assigned to CS 538. All necessary compiler, interpreters and tools will be loaded onto these machines.

You may also use your own PC or workstation. It will be *your* responsibility to load needed software (instructions on where to find needed software are included on the class web page).

The Systems Lab teaches brief tutorials on Unix if you are unfamiliar with that OS.

## **Academic Misconduct Policy**

- You must do your assignments—no copying or sharing of solutions.
- You may discuss general concepts and Ideas.
- All cases of Misconduct *must* be reported to the Dean's office.
- Penalties may be severe.

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## Program & Homework Late Policy

- An assignment may be handed in one, two, or three class periods late, but not any later.
- One late period will be debited 10%, two late periods will be debited 20%, three late periods will be debited 30%.
- All students will be given 4 "free" late periods. That is, the first 40% in late debits will be automatically forgiven.
- Your 4 free late periods my be used at any time, and in any combination.

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## **Approximate Grade Weights**

Homework 1	10%
Program 1 - Scheme	15%
Program 2 - ML	15%
Program 3 - Prolog	15%
Program 4 - Pizza & Python	11%
Midterm Exam	17%
Final Exam (non-cumulative)	17%

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## Programming Languages to be Considered in Detail

#### 1. Scheme

A modern variant of Lisp.

A Functional Language: Functions are "first class" data values.

Dynamically Typed: A variable's type may change during execution; no type declarations are needed.

All memory allocation and deallocation is *automatic*.

Primary data structures, lists and numbers, are *unlimited* in size & may grow without bound.

Continuations provide a novel way to suspend and "re-execute" computations.

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## 2. ML ("Meta Language")

Strong, compile-time type checking.

Types are determined by *inference* rather than declaration.

Polymorphic (one function declaration can be used with many different types).

Pattern-directed programming (you define patterns that are automatically matched during a call).

Typed exceptions are provided.

Abstract data types, with constructors, are included.

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3. Prolog (*Pro*gramming in *Log*ic)

Programs are Facts and Rules.

Programmers are concerned with definition, not execution.

Execution order is automatically determined.

#### 4. Pizza

Extends a popular Object-oriented language, Java, to include

- Parametric polymorphism (similar to C++'s templates)
- First-class functional objects
- Algebraic data types, including patterns.

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### 5. Python

A simple, efficient scripting language that quickly build new programs out of existing applications and libraries.

Cleanly includes objects.

Scales nicely into larger applications.

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## **Evolution of Programming Languages**

In the beginning, ...

programs were written in absolute machine code—a sequence of bits that encode machine instructions.

#### Example:

34020005 0000000c 3c011001 ac220000

This form of programming is

- Very detailed
- Very tedious
- Very error-prone
- Very machine specific

## Symbolic Assemblers

Allow use of symbols for operation codes and labels.

#### Example:

```
li $v0,5
syscall
sw $v0,a
```

Far more readable, but still very detailed, tedious and machine-specific.

Types are machine types.

Control structures are conditional branches.

Subprograms are blocks of code called via a "subroutine branch" instruction.

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All labels are global.

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## Fortran (Formula Translator)

#### Example:

do 10 i=1,100 10 a(i)=0

Developed in the mid-50s.

A major step forward:

- Programming became more "problem oriented" and less "machine oriented."
- Notions of control structures (ifs and do loops) were introduced.
- Subprograms, calls, and parameters were made available.
- Notions of machine independence were introduced.
- Has evolved into more modern variants, including Fortran 77, Fortran 90 and HPF (High Performance Fortran)

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## Cobol (Common Business Oriented Language)

#### Example:

multiply i by 3 giving j.
move j to k.
write line1 after advancing
1 lines.

Developed in the early 60s.

The first widely-standardized programming language,

Once very widely used in the commercial world; still important.

Wordy in structure; designed for non-scientific users.

Raised the issue of who should program and how important readability and maintainability are.

## Algol 60 (Algorithmic Language)

#### Example:

```
real procedure cheb(x,n);
value x,n;
real x; integer n;
cheb := if n = 0 then 1
  else if n = 1 then x
  else 2 × x ×
  cheb(x,n-1)-cheb(x,n-2);
```

Developed about 1960.

Direct precursor of Pascal, C, C++ and Java.

Introduced many ideas now in wide use:

- Blocks with local declarations and scopes.
- Nested declarations and control structures.

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- Parameter passing
- Automatic recursion.

But,

- I/O wasn't standardized.
- IBM promoted Fortran and PL/I.

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## Lisp (List Processing Language)

#### Example:

```
((lambda (x) (* x x)) 10)
```

Developed in the early 60s.

A radical departure from earlier programming languages.

Programs and data are represented in a uniform list format.

Types are a property of data values, not variables or parameters.

A program can build and run new functions as it executes.

Data values were not fixed in size.

Memory management was automatic.

A formal semantics was developed to define precisely what a program means.

## Simula 67 (Simulation Algol)

#### Example:

```
Class Rectangle (Width, Height);
Real Width, Height;
Boolean Procedure IsSquare;
    IsSquare := Width=Height;
End of Rectangle;
```

Developed about 1967.

Introduced the notion of a class (for simulation purposes).

Included objects, a garbage collector, and notions of extending a class.

C++ was originally C with classes (as Simula was Algol with classes).

## C and C++

C was developed in the early 70's; C++ in the mid-80s.

These languages have a concise, expressive syntax; they generate high quality code sufficient for performance-critical applications.

C, along with Unix, provided the viability of platform-independent languages and applications.

C and C++ allow programmers a great deal of freedom in bending and breaking rules.

Raises the issue of whether one language can span both novice and expert programmers.

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Interesting issue—if most statements and expressions are meaningful, can errors be readily detected?

```
if (a=b)
   a=0;
else a = 1;
```

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## Java

Developed in the late 90s.

Cleaner object-oriented language than C++.

Introduced notions of dynamic loading of class definitions across the Web.

Much stronger emphasis on secure execution and detection of run-time errors.

Extended notions of platform independence to system independence.

## What Drives Research into New Programming Languages?

Why isn't C or C++ or C+++ enough?

## 1. Curiosity

What other forms can a programming language take?

What other notions of programming are possible?

## 2. Productivity

Procedural languages, including C, C++ and Java, are very detailed.

Many source lines imply significant development and maintenance expenses.

## 3. Reliability

Too much low-level detail in programs greatly enhances the

chance of minor errors. Even minor errors can raise significant problems in applications.

### 4. Security

Computers are entrusted with everincreasing responsibilities. How can we know that a program is safe and reliable enough to trust?

### 5. Execution speed

Procedural languages are closely tied to the standard sequential model of instruction execution. We may need radically different programming models to fully exploit parallel and distributed computers.

## Desirable Qualities in a Programming Language

Theoretically, all programming languages are equivalent (Why?)

If that is so, what properties are desirable in a programming language?

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It should be easy to use

It should be easy to read and understand.

It should be simple to write, without unexpected pitfalls.

It should be *orthogonal*—only one way to do each step or computation.

It should be natural for the application being programed.

The language should support abstraction

You can't anticipate all needed Data Structures and Operations, so adding new definitions easily and efficiently should be allowed.

- The language should support Testing, Debugging and Verification.
- The language should have a good development environment.

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Integrated Editors, Compilers, Debuggers, and Version Control are a big plus.

- The language should be portable, spanning many platforms and operating systems.
- It should be inexpensive to use:

Execution should be fast,

Memory needs should be modest,

Translation should be fast and modular,

Program creation and testing should be easy & cheap,

Maintenance should not be unduly cumbersome,

Components should be reusable.

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## **Programming Paradigms**

Programming languages naturally fall into a number of fundamental styles or *paradigms*.

### **Procedural Languages**

Most of the widely-known and widely-used programming languages (C, Fortran, Pascal, Ada, etc.) are procedural in nature.

Programs execute statement by statement, reading and modifying a shared memory.

This programming style closely models conventional sequential processors linked to a RAM.

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#### Question:

#### Given

Why can't 5 processors each execute one line to make the program run 5 times faster?

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## **Functional Languages**

Lisp, Scheme and ML are functional in nature.

Programs are expressions to be evaluated.

Language design aims to *minimize* side-effects, including assignment.

Alternative evaluation mechanisms are possible, including

Lazy (Demand Driven)

Eager (Data Driven or Speculative)

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## **Object-Oriented Languages**

C++, Java, Smalltalk, Pizza and Python are object-oriented.

Data and functions are encapsulated into Objects.

Objects are active, have persistent state, and uniform interfaces (messages or methods).

Notions of inheritance and common interfaces are central.

All objects that provide the same interface can be treated uniformly. In Java you can print any object that provides the tostring method. You can iterate through the elements of any Java object that implements the Enumeration interface.

Subclassing allows to you extend or redefine part of an object's behavior without reprogramming all of the object's definition. Thus in Java, you can take a Hashtable class (which is fairly elaborate) and create a subclass in which an existing method (like tostring) is redefined, or new operations are added.

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## Logic Programming Languages

Prolog notes that most programming languages address both the logic of a program (what is to be done) and the control flow of a program (how to do what you want).

A logic programming language, like Prolog, lets programmers focus on a program's logic without concern for control issue.

These languages have no real control structures, and little notion of "flow of control."

What results are programs that are unusually succinct and focused.

#### Example:

```
inOrder( [] ).
inOrder( [ _ ] ).
inOrder([a,b|c]) :- (a<b),
    inOrder([b|c]).</pre>
```

This is a *complete*, *executable* function that determines if a list is in order. It is naturally polymorphic, and is not cluttered with declarations, variables or explicit loops.

# Review of Concepts from Procedural Programming Languages

Declarations/Scope/Lifetime/Binding Static/Dynamic

- Identifiers are *declared*, either explicitly or implicitly (from context of first use).
- Declarations bind type and kind information to an identifier. Kind specifies the grouping of an identifier (variable, label, function, type name, etc.)
- Each identifier has a *scope* (or range) in a program—that part of the program in which the identifier is visible (i.e., may be used).

- Data objects have a *lifetime*—the span of time, during program execution, during which the object exists and may be used.
- Lifetimes of data objects are often tied to the scope of the identifier that denotes them. The objects are created when its identifier's scope is entered, and they may be deleted when the identifier's scope is exited. For example, memory for local variables within a function is usually allocated when the function is called (activated) and released when the call terminates.

In Java, a method may be loaded into memory when the object it is a member of is first accessed.

# Properties of an identifier (and the object it represents) may be set at

#### Compile-time

These are *static* properties as they do not change during execution. Examples include the type of a variable, the value of a constant, the initial value of a variable, or the body of a function.

#### Run-time

These are *dynamic* properties. Examples include the value of a variable, the lifetime of a heap object, the value of a function's parameter, the number of times a while loop iterates, etc.

# **Example: In Fortran**

- The scope of an identifier is the whole program or subprogram.
- Each identifier may be declared only once.
- Variable declarations may be implicit.
   (Using an identifier implicitly declares it as a variable.)
- The lifetime of data objects is the whole program.

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# **Block Structured Languages**

- Include Algol 60, Pascal, C and Java.
- Identifiers may have a non-global scope.
   Declarations may be *local* to a class, subprogram or block.
- Scopes may nest, with declarations propagating to inner (contained) scopes.
- The lexically nearest declaration of an identifier is bound to uses of that identifier.

Binding of an identifier to its corresponding declaration is usually static (also called lexical), though dynamic binding is also possible.

Static binding is done prior to execution—at compile-time.

Example (drawn from C):

```
int x,z;
void A() {
  float x,y;
  print(x,y,z);
}

void B() {
    print (x,y,z)
    int
    float
    print (x,y,z)
    int
    undeclared
    int
```

# **Block Structure Concepts**

Nested Visibility

No access to identifiers outside their scope.

- Nearest Declaration Applies
   Static name scoping.
- Automatic Allocation & Deallocation of Locals

Lifetime of data objects is bound to the scope of the Identifiers that denote them.

Variations in these rules of name scoping are possible.

For example, in Java, the lifetime of all class objects is from the time of their creation (via new) to the last visible reference to them.

#### Thus

```
... Object O;...
```

creates an *object reference* but does not allocate any memory space for o.

You need

... Object O = new Object(); ... to actually create memory space for o.

# **Dynamic Scoping**

An alternative to static scoping is dynamic scoping, which was used in early Lisp dialects (but not in Scheme, which is statically scoped).

Under dynamic scoping, identifiers are bound to the dynamically closest declaration of the identifier. Thus if an identifier is not locally declared, the call chain (sequence of callers) is examined to find a matching declaration.

### **Example:**

```
int x;
void print() {
   write(x); }
main () {
   bool x;
   print();
}
```

Under static scoping the x written in print is the lexically closest declaration of x, which is as an int.

Under dynamic scoping, since print has no local declaration of x, print's caller is examined. Since main calls print, and it has a declaration of x as a bool, that declaration is used.

Dynamic scoping makes type checking and variable access harder and more costly than static scoping. (Why?)

However, dynamic scoping does allow a notion of an "extended scope" in which declarations extend to subprograms called within that scope.

Though dynamic scoping may seen a bit bizarre, it is closely related to virtual functions used in C++ and Java.

#### Virtual Functions

A function declared within a class, C, may be redeclared within a class derived from C. Moreover, for uniformity of redeclaration, it is important that *all* calls, including those in methods within C, use the new declaration.

# Scope vs. Lifetime

It is usually required that the lifetime of a run-time object at least cover the scope of the identifier. That is, whenever you can access an identifier, the run-time object it denotes better exist.

But,

it is possible to have a run-time object's lifetime exceed the scope of its identifier. An example of this is static or own variables.

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```
In C:
    void p() {
        static int i = 0;
        print(i++);
    }
```

Each call to p prints a different value of i (0, 1, ...) Variable i retains its value across calls.

Some languages allow an explicit binding of an identifier for a fixed scope:

A declaration may appear wherever a statement or expression is allowed. Limited scopes enhance readability.

#### Structs vs. Blocks

Many programming languages, including C, C++, Pascal and Ada, have a notion of grouping data together into *structs* or *records*.

For example:

```
struct complex { float re, im; }
There is also the notion of grouping
statements and declarations into
blocks:
```

```
{ float re, im;
 re = 0.0; im = 1.0;
}
```

Blocks and structs look similar, but there are significant differences: Structs are *data*,

- As originally designed, structs contain only data (no functions or methods).
- Structs can be dynamically created, in any number, and included in other data structures (e.g., in an array of structs).
- All fields in a struct are visible outside the struct.

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Blocks are code,

- They can contain both code and data.
- Blocks can't be dynamically created during execution; they are "built into" a program.
- Locals in a block aren't visible outside the block.

By adding functions and initialization code to structs, we get *classes*—a nice blend of structs and blocks.

#### For example:

```
class complex{
  float re, im;
  complex (float v1, float v2){
    re = v1; im = v2; }
}
```

#### Classes

- Classes can be created as needed, in any number, and included in other data structure.
- They include both data (fields) and functions (methods).
- They include mechanisms to initialize themselves (constructors) and to finalize themselves (destructors).
- They allow controlled access to members (private and public declarations).

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# Type Equivalence in Classes

In C, C++ and Java, instances of the same struct or class are type-equivalent, and mutually assignable.

For example:

```
class MyClass { ... }
MyClass v1, v2;
v1 = v2; // Assignment is OK
```

We expect to be able to assign values of the same type, including class objects.

However, sometimes a class models a data object whose size or shape is set upon creation (in a constructor). Then we may *not* want assignment to be allowed.

```
class Point {
  int dimensions;
  float coordinates[];
  Point () {
    dimensions = 2;
    coordinates = new float[2];
  }
  Point (int d) {
    dimensions = d;
    coordinates = new float[d];
  }
}
Point plane = new Point();
Point solid = new Point(3);
plane = solid; //OK in Java
```

This assignment is allowed, even though the two objects represent points in different dimensions.

# **Subtypes**

In C++ and Java we can create subclasses—new classes derived from an existing class.

We can use subclasses to create new data objects that are similar (since they are based on a common parent), but still *type-inequivalent*.

#### Example:

```
class Point2 extends Point {
    Point2() {super(2); }
}
class Point3 extends Point {
    Point3() {super(3); }
}
Point2 plane = new Point2();
Point3 solid = new Point3();
plane = solid; //Illegal in Java
```

# Parametric Polymorphism

We can create distinct subclasses based on the values passed to constructors. But sometimes we want to create subclasses based on distinct *types*, and types can't be passed as parameters. (Types are not values, but rather a property of values.)

We see this problem in Java, which tries to create general purpose data structures by basing them on the class object. Since any object can be assigned to object (all classes must be a subclass of object), this works—at least partially.

- We can't guarantee that linked lists are type homogeneous (contain only a single type).
- We must cast object types back into their "real" types when we extract list values.

• We must use wrapper classes like Integer rather than int (because primitive types like int aren't objects, and aren't subclass of Object).

For example, to use LinkedList to build a linked list of ints we do the following:

```
LinkedList 1 =
   new LinkedList(new Integer(123));
   int i =
        ((Integer) l.head()).intValue();
This is pretty clumsy code. We'd
   prefer a mechanism that allows us to
   create a "custom version" of
   LinkedList, based on the type we
   want the list to contain.
```

We can't just call something like
LinkedList(int) Or
LinkedList(Integer) because
types can't be passed as parameters.

Parametric polymorphism is the solution. Using this mechanism, we can use type parameters to build a "custom version" of a class from a general purpose class.

C++ allows this using its template mechanism. Pizza, an extension of Java, also allows type parameters.

In both languages, type parameters are enclosed in "angle brackets" (e.g., LinkedList<T> passes T, a type, to the LinkedList class).

#### In Pizza we have

```
class LinkedList<T> {
   T value; LinkedList<T> next;
   T head() {return value;}
   LinkedList<T> tail() {
      return next;}
   LinkedList(T O) {
      value = 0; next = null;}
   LinkedList(T O,LinkedList<T> L)
      {value = 0; next = L;}
}
LinkedList<int> l =
      new LinkedList(123);
int i = l.head();
```

# Overloading and Ad-hoc Polymorphism

Classes usually allow overloading of method names, if only to support multiple constructors.

That is, more than one method definition with the same name is allowed within a class, as long as the method definitions differ in the number and/or types of the parameters they take.

For example,

```
class MyClass {
  int f(int i) { ... }
  int f(float g) { ... }
  int f(int i, int j) { ... }
}
```

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Overloading is sometimes called "ad hoc" polymorphism, because, to the programmer, it appears that one method can take a variety of different parameter types. This isn't true polymorphism because the methods have different bodies; there is no sharing of one definition among different parameter types. There is no guarantee that the different definitions do the same thing, even though they share a common name.

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# Issues in Overloading

Though many languages allow overloading, few allow overloaded methods to differ only on their result types. (Neither C++ nor Java allow this kind of overloading, though Ada does). For example,

```
class MyClass {
  int f() { ... }
  float f() { ... }
}
```

is illegal. This is unfortunate, since methods with the same name and parameters, but different result types, could be used to automatically convert result values to the type demanded by the context of call.

Why is this form of overloading usually disallowed?

It's because overload resolution (deciding which definition to use) becomes much harder. Consider

```
class MyClass {
  int f(int i, int j) { ... }
  float f(float i, float j) { ... }
  float f(int i, int j) { ... }
}
in
```

```
int a = f(f(1,2), f(3,4));
```

which definitions of £ do we use in each of the three calls? Getting the correctly answer can be tricky, though solution algorithms do exist.

# Reading Assignment

• Sethi: Chapters 4-5

• Scott: Chapters 3

# Operator Overloading

Some languages, like C++, allow operators to be overloaded. You may add new definitions to existing operators, and use them on your own types. For example,

```
class MyClass {
   int i;
  public:
   int operator+(int j) {
      return i+j; }
}
MyClass c;
int i = c+10;
int j = c.operator+(10);
int k = 10+c; // Illegal!
```

The expression 10+c is illegal because there is no definition of + for the types int and MyClass. We can create one by using C++'s friend mechanism to insert a definition into MyClass that will have access to MyClass's private data:

```
class MyClass {
   int i;
  public:
   int operator+(int j) {
      return i+j; }
  friend int operator+
      (int j, MyClass& v){
      return j+v.i; }
}
MyClass c;
int k = 10+c; // Now OK!
```

C++ limits operator overloading to existing predefined operators. A few languages, like Algol 68 (a successor to Algol 60, developed in 1968), allow programmers to define brand new operators.

In addition to defining the operator itself, it is also necessary to specify the operator's precedence (which operator is to be applied first) and its associativity (does the operator associate from left to right, or right to left, or not at all). Given this extra detail, it is possible to specify something like

```
op +++ prec = 8;
int op +++(int& i, int& j) {
  return (i++)+(j++); }
```

(Why is int& used as the parameter type rather than int?)

# Parameter Binding

Almost all programming languages have some notion of binding an actual parameter (provided at the point of call) to a formal parameter (used in the body of a subprogram).

There are many different, and inequivalent, methods of parameter binding. Exactly which is used depends upon the programming language in question.

Parameter Binding Modes include:

- Value: The formal parameter represents a local variable initialized to the value of the corresponding actual parameter.
- Result: The formal parameter represents a local variable. Its final

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- value, at the point of return, is copied into the corresponding actual parameter.
- Value/Result: A combination of the value and results modes. The formal parameter is a local variable initialized to the value of the corresponding actual parameter. The formal's final value, at the point of return, is copied into the corresponding actual parameter.
- Reference: The formal parameter is a pointer to the corresponding actual parameter. All references to the formal parameter indirectly access the corresponding actual parameter through the pointer.
- Name: The formal parameter represents a block of code

(sometimes called a *thunk*) that is evaluated to obtain the value or address of the corresponding actual parameter. Each reference to the formal parameter causes the thunk to be reevaluated.

Readonly (sometimes called Const):
 Only reads of the formal parameter are allowed. Either a copy of the actual parameter's value, or its address, may be used.

# What Parameter Modes do Programming Languages Use?

- C and C++: Value mode except for arrays where a pointer to the start of the array is passed.
- Java: Scalar types (int, float, char, etc.) are passed by value; objects are passed by reference.
- Fortran: Reference (even for constants!)
- Ada: Value/result, reference, and readonly are used.

## **Example**

What element of **k** is printed?

- The assignment to a does not affect
   i, since a is a value parameter.
- The assignment to **b** does affect **j**, since **b** is a reference parameter.
- c is a name parameter, so it is evaluated whenever it is used. In the print statement k[i][j] is printed.
  At that point i=3 and j=2, so k[3][2] is printed.

# Why are there so Many Different Parameter Modes?

Parameter modes reflect different views on how parameters are to be accessed, as well as different degrees of efficiency in accessing and using parameters.

- Call by value protects the actual parameter value. No matter what the subprogram does, the parameter can't be changed.
- Call by reference allows *immediate* updates to the actual parameter.
- Call by readonly protects the actual parameter and emphasizes the "constant" nature of the formal parameter.

- Call by value/result allows actual parameters to change, but treats a call as a single step (assign parameter values, execute the subprogram's body, update parameter values).
- Call by name delays evaluation of an actual parameter until it is actually needed (which may be never).

# Call by Name

Call by name is a special kind of parameter passing mode. It allows some calls to complete that otherwise would fail. Consider

f(i,j/0)

Normally, when <code>j/o</code> is evaluated, a divide fault would terminate execution. If <code>j/o</code> is passed by name, the division is delayed until the parameter is needed, which may be never.

Call by name also allows programmers to create some interesting solutions to hard programming problems.

Consider the conditional expression found in C, C++, and Java:

(cond?value1:value2)

What if we want to implement this as a function call:

```
condExpr(cond,value1,value2) {
  if cond
     return value1;
  else return value2;
}
```

With most parameter passing modes this implementation won't work! (Why?)

But if value1 and value2 are passed by name, the implementation is correct.

# Call by Name and Lazy Evaluation

Call by name has much of the flavor of *lazy evaluation*. With lazy evaluation, you don't compute a value but rather a *suspension*—a function that will provide a value when called.

This can be useful when we need to control how much of a computation is actually performed.

Consider an infinite list of integers. Mathematically it is represented as

1, 2, 3, ...

But how do we compute a data structure that represents an infinite list?

```
The obvious computation
```

A less obvious implementation, using suspensions, *does* work:

```
infList(int start) {
    return list(start,
        function() {
        return infList(start+1);
        });
}
```

Now, whenever we are given an infinite list, we get two things: the first integer in the list and a suspension function. When called, this function will give you the rest of the infinite list (again, one more

value and another suspension function).

The whole list is there, but only as much as you care to access is actually computed.

# **Eager Parameter Evaluation**

Sometimes we want parameters evaluated *eagerly*—as soon as they are known.

Consider a sorting routine that breaks an array in half, sorts each half, and then merges together the two sorted halves (this is a *merge sort*).

In outline form it is:

This definition lends itself nicely to parallel evaluation: The two halves of an input array can be sorted in parallel. Each of these two halves can again be split in two, allowing parallel sorting of four quarter-sized arrays,

then leading to 8 sorts of 1/8 sized arrays, etc.

But, to make this all work, the two parameters to merge must be evaluated eagerly, rather than in sequence.

# Type Equivalence

Programming languages use types to describe the values a data object may hold and the operations that may be performed.

By checking the types of values, potential errors in expressions, assignments and calls may be automatically detected. For example, type checking tells us that

123 + "123"

is illegal because addition is not defined for an integer, string combination.

Type checking is usually done at compile-time; this is *static typing*.

Type-checking may also be done at run-time; this is *dynamic typing*.

A program is *type-safe* if it is impossible to apply an operation to a value of the wrong type. In a type-safe language, plus is never told to add an integer to a string, because its definition does not allow that combination of operands. In type-safe programs an operator can still see an illegal value (e.g., a division by zero), but it can't see operands of the wrong type.

A *strongly-typed* programming language forbids the execution of type-unsafe programs.

Weakly-typed programming languages allow the execution of potentially type-unsafe programs.

The question reduces to whether the programming language allows

programmers to "break" the type rules, either knowingly or unknowingly.

Java is strongly typed; type errors preclude execution. C and C++ are weakly typed; you can break the rules if you wish. For example:

```
int i; int* p;
p = (int *) i * i;
```

Now p may be used as an integer pointer though multiplication need not produce valid integer pointers.

If we are going to do type checking in a program, we must decide whether two types, T1 and T2 are equivalent; that is, whether they be used interchangeably.

There are two major approaches to type equivalence:

Name Equivalence:

Two types are equivalent if and only if they refer to exactly the same type declaration.

For example,

```
type PackerSalaries = int[100];
type AssemblySizes = int[100];
PackerSalaries salary;
AssemblySizes size;
```

Is

sal = size;

allowed?

Using name equivalence, no. That is, salary  $\neq_N$  size since these two variables have different type declarations (that happen to be identical in structure).

Formally, we define  $\equiv_N$  (name type equivalence) as:

- (a)  $T \equiv_N T$
- (b) Given the declaration

Type T1 = T2; 
$$T1 \equiv_N T2$$

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We treat anonymous types (types not given a name) as an abbreviation for an implicit declaration of a new and unique type name.

```
Thus
  int A[10];
is an abbreviation for
  Type T<sub>new</sub> = int[10];
  T<sub>new</sub> A;
```

# Structural Equivalence

An alternative notion of type equivalence is structural equivalence (denoted  $\equiv_S$ ). Roughly, two types are structurally equivalent if the two types have the same definition, independent of where the definitions are located. That is, the two types have the same definitional structure.

#### Formally,

- (a)  $T \equiv_S T$
- (b) Given the declaration

Type 
$$T = Q$$
;  $T \equiv_S Q$ 

(c) If T and Q are defined using the same type constructor and corresponding parameters in the two definitions are equal or structurally equivalent

then 
$$T \equiv_S Q$$

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# Returning to our previous example, type PackerSalaries = int[100]; type AssemblySizes = int[100]; PackerSalaries salary;

AssemblySizes size;

salary  $\equiv_S$  size Since both are arrays and 100=100 and int  $\equiv_S$  int.

# Which notion of Equivalence do Programming Languages Use?

C and C++ use structural equivalence except for structs and classes (where name equivalence is used). For arrays, size is ignored.

Java uses structural equivalence for scalars. For arrays, it requires name equivalence for the component type, ignoring size. For classes it uses name equivalence except that a subtype may be used where a parent type is expected. Thus given

```
void subr(Object O) { ... };
the call
```

subr(new Integer(100)); is OK since Integer is a subclass of Object.

# **Automatic Type Conversions**

C, C++ and Java also allow various kinds of automatic type conversions.

In C, C++ and Java, a float will be automatically created from an int:

float f = 10; // No type error Also, an integer type (char, short, int, long) Will be *Widened*:

int i = 'x';

In C and C++ (but not Java), an integer value can also be *narrowed*, possibly with the loss of significant bits:

char c = 1000000;

# Reading Assignment

• Sethi: Chapter 10

 The Scheme Language Definition (linked from class web page)

Scott: Section 11.2

### Lisp & Scheme

Lisp (*List P*rocessing Language) is one of the oldest programming languages still in wide use.

It was developed in the late 50s and early 60s by John McCarthy.

Its innovations include:

- Support of symbolic computations.
- A Functional Programming style without emphasis on assignments and side-effects.
- A naturally recursive programming style.
- Dynamic (run-time) type checking.
- Dynamic data structures (lists, binary trees) that grow without limit.

- Automatic garbage collection to manage memory.
- Functions are treated as "first class" values; they may be passed as arguments, returned as result values, stored in data structures, and created during execution.
- A formal semantics (written in Lisp) defined the meaning of all valid programs.
- It provided an Integrated
   Programming Environment to create, edit and test Lisp programs.

#### **Scheme**

Scheme is a recent dialect of Lisp.

It uses lexical (static) scoping.

It supports true first-class functions.

It provides program-level access to control flow via *continuation* functions.

# **Atomic (Primitive) Data Types**

#### Symbols:

Essentially the same form as identifiers. Similar to enumeration values in C and C++.

Very flexible in structure; essentially any sequence of printable characters is allowed; anything that starts a valid number (except + or -) may not start a symbol.

Valid symbols include:

abc hello-world + <=!

#### Integers:

Any sequence of digits, optionally prefixed with a + or -. Usually unlimited in length.

#### Reals:

A floating point number in a decimal format (123.456) or in exponential format (1.23e45). A leading sign and a signed exponent are allowed (-12.3, 10.0e-20).

#### Rationals:

Rational numbers of the form integer/integer (e.g., 1/3 or 9/7) with an optional leading sign (-1/2, +7/8).

#### Complex:

Complex numbers of the form num+num i or num-num i, where num is an integer or real number. Example include 1+3i, -1.5-2.5i, 0+1i).

#### String:

A sequence of characters delimited by double quotes. Double quotes and backslashes must be escaped using a backslash. For example

"Hello World" "\"Wow!\""

#### Character:

A single character prefixed by #\. For example, #\a, #\0, #\\, #\#. Two special characters are #\space and #\newline.

#### Boolean:

True is represented as #t and false is represented as #f.

# **Binary Trees**

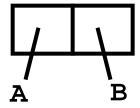
Binary trees are also called *S-Expressions* in Lisp and Scheme.

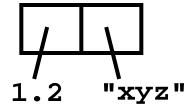
They are of the form (item . item )

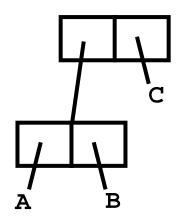
where item is any atomic value or any S-Expression. For example:

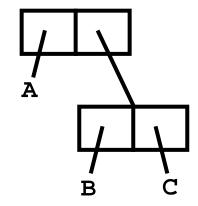
```
(A.B)
(1.2."xyz")
((A.B).C)
(A.(B.C))
```

S-Expressions are linearizations of binary trees:









S-Expressions are built and accessed using the predefined functions *cons*, *car* and *cdr*.

cons builds a new S-Expression from two S-Expressions that represent the left and right children.

cons(E1,E2) = (E1 . E2)

car returns are left subtree of an S-Expression.

car (E1 . E2) = E1

cdr returns are right subtree of an S-Expression.

cdr (E1 . E2) = E2

#### Lists

```
In Lisp and Scheme lists are a special,
widely-used form of S-Expressions.
() represents the empty or null list
(A) represents the list containing A.
By definition, (A) \equiv (A \cdot ())
(A B) represents the list containing A
and B. By definition,
(A B) \equiv (A . (B . ()))
In general, (A B C ... Z) \equiv
(A . (B . (C . . . . (Z . () ) . . . )))
(A B C) \equiv
               A
                   \mathbf{B}
```

#### **Function Calls**

In List and Scheme, function calls are represented as lists.

(A B C) means:

Evaluate **A** (to a function)

Evaluate **B** and **C** (as parameters)

Call a with B and c as its parameters

Use the value returned by the call as the "meaning" of (A B C).

cons, car and cdr are predefined symbols bound to built-in functions that build and access lists and S-Expressions.

Literals (of type integer, real, rational, complex, string, character and boolean) evaluate to themselves.

```
For example (\Rightarrow means "evaluates to")

(cons 1 2) \Rightarrow (1 . 2)

(cons 1 () ) \Rightarrow (1)

(car (cons 1 2)) \Rightarrow 1

(cdr (cons 1 ())) \Rightarrow ()

But,

(car (1 2)) fails during execution!

Why?
```

The expression (1 2) looks like a call, but 1 isn't a function. We need some way to "quote" symbols and lists we don't want evaluated.

```
(quote arg)
```

is a special function that returns its argument *unevaluated*.

Thus (quote (1 2)) doesn't try to evaluate the list (1 2); it just returns it.

Since quotation is often needed, it may be abbreviated using a single quote. That is

#### **User-defined Functions**

```
The list
 (lambda (args) (body))
evaluates to a function with (args)
as its argument list and (body) as
the function body.
No quotes are needed for (args) or
(body).
Thus
 (lambda (x) (+ x 1)) evaluates
to the increment function.
Similarly,
 ((lambda (x) (+ x 1)) 10) \Rightarrow
   11
```

We can bind values and functions to global symbols using the define function.

The general form is

```
(define id object)
```

id is not evaluated but object is. id is bound to the value object evaluates to.

For example,

```
(define pi 3.1415926535)
(define plus1
    (lambda (x) (+ x 1)) )
(define pi*2 (* pi 2))
```

Once a symbol is defined, it evaluates to the value it is bound to:

```
(plus1 12) \Rightarrow 13
```

```
Since functions are frequently
defined, we may abbreviate
(define id
   (lambda (args) (body)))
as
(define (id args) (body) )
Thus
  (define (plus1 x) (+ x 1))
```

# Conditional Expressions in Scheme

A predicate is a function that returns a boolean value. By convention, in Scheme, predicate names end with "?"

For example,

```
number? symbol? equal?
null? list?
```

In conditionals, #f is false, and everything else, including #f, is true.

The if expression is

```
(if pred E1 E2)
```

First pred is evaluated. Depending on its value (#f or not), either £1 or £2 is evaluated (but not both) and returned as the value of the if expression.

```
For example,
 (if (= 1 (+ 0 1))
      'Yes
      'No
(define
  (fact n)
  (if (= n 0)
       1
       (* n (fact (- n 1)))
```

#### **Generalized Conditional**

This is similar to a switch or case.

```
(cond
(p1 e1)
(p2 e2)
...
(else en)
```

Each of the predicates (p1, p2, ...) is evaluated until one is true (≠ #£). Then the corresponding expression (e1, e2, ...) is evaluated and returned as the value of the cond. else acts like a predicate that is always true.

#### Example:

```
(cond
    ((= a 1) 2)
    ((= a 2) 3)
    (else 4)
)
```

#### **Recursion in Scheme**

Recursion is widely used in Scheme and other functional programming languages.

Rather than using a loop to step through the elements of a list or array, recursion breaks a problem on a large data structure into a simpler problem on a smaller data structure.

A good example of this approach is the append function, which joins (or appends) two lists into one larger list containing all the elements of the two input lists (in the correct order).

Note that cons is not append. cons adds one element to the head of an existing list.

#### Thus

```
(cons '(a b) '(c d)) ⇒
    ((a b) c d)
(append '(a b) '(c d)) ⇒
    (a b c d)
```

The append function is predefined in Scheme, as are many other useful list-manipulating functions (consult the Scheme definition for what's available).

It is instructive to define append directly to see its recursive approach:

```
Let's trace (append '(a b) '(c d))
Our definition is
(define
  (append L1 L2)
  (if (null? L1)
        L2
        (cons (car L1)
              (append (cdr L1) L2))
Now L1 = (a b) and L2 = (c d).
(null? L1) is false, so we evaluate
(cons (car L1) (append (cdr L1) L2))
= (cons (car '(a b))
       (append (cdr '(a b)) '(c d)))
= (cons 'a (append '(b) '(c d))
We need to evaluate
 (append '(b) '(c d))
In this call, L1 = (b) and L2 = (c d).
L1 is not null, so we evaluate
(cons (car L1) (append (cdr L1) L2))
= (cons (car '(b))
        (append (cdr '(b)) '(c d)))
```

```
= (cons 'b (append '() '(c d))
We need to evaluate
 (append '() '(c d))
In this call, L1 = () and L2 = (c d).
L1 is null, so we return (c d).
Therefore
(cons 'b (append '() '(c d)) =
(cons 'b '(c d)) = (b c d) =
(append '(b) '(c d))
Finally,
(append '(a b) '(c d)) =
(cons 'a (append '(b) '(c d)) =
(cons 'a '(b c d)) = (a b c d)
Note:
Source files for append, and other
Scheme examples, may be found in
~cs538-1/public/scheme/example1.scm,
~cs538-1/public/scheme/example2.scm,
etc.
```

### Reversing a List

Another useful list-manipulation function is rev, which reverses the members of a list. That is, the last element becomes the first element, the next-to-last element becomes the second element, etc.

```
As an example, consider
(rev '(1 2))
Here \mathbf{L} = (1 \ 2). \mathbf{L} is not null so we
evaluate
(append (rev (cdr L))
                (list (car L))) =
(append (rev (cdr '(1 2)))
                (list (car '(1 2)))) =
(append (rev '(2)) (list 1)) =
(append (rev '(2)) '(1))
We must evaluate (rev '(2))
Here \mathbf{L} = (2). \mathbf{L} is not null so we
evaluate
(append (rev (cdr L))
                (list (car L))) =
(append (rev (cdr '(2)))
                (list (car '(2)))) =
(append (rev ())(list 2)) =
(append (rev ())'(2))
We must evaluate (rev '())
Here L = (). L is null so (rev \cdot ()) =
()
```

```
Thus (append (rev ())'(2)) =
(append () '(2)) = (2) = (rev '(2))

Finally, recall (rev '(1 2)) =
(append (rev '(2)) '(1)) =
(append '(2) '(1)) = (2 1)
```

As constructed, rev only reverses the "top level" elements of a list. That is, members of a list that themselves are lists *aren't* reversed.

```
For example,

(rev '( (1 2) (3 4))) =

((3 4) (1 2))
```

We can generalize **rev** to also reverse list members that happen to be lists.

To do this, it will be convenient to use Scheme's let construct.

#### The Let Construct

Scheme allows us to create local names, bound to values, for use in an expression.

```
The structure is

(let ((id1 val1)(id2 val2)...)

expr)
```

In this construct, vall is evaluated and bound to idl, which will exist only within this let expression. If idl is already defined (as a global or parameter name) the existing definition is hidden and the local definition, bound to vall, is used. Then vall is evaluated and bound to idl, .... Finally, expr is evaluated in a scope that includes idl, idl, ...

```
For example,
(let ((a 10) (b 20))
  (+ a b)) \Rightarrow 30
Using a let, the definition of
revall, a version of rev that
reverses all levels of a list, is easy:
(define (revall L)
  (if (null? L)
      L
      (let ((E (if (list? (car L))
                  (revall (car L))
                  (car L) )))
        (append (revall (cdr L))
                 (list E))
      )
(revall '( (1 2) (3 4))) \Rightarrow
 ((4 \ 3) \ (2 \ 1))
```

#### **Subsets**

Another good example of Scheme's recursive style of programming is subset computation.

Given a list of distinct atoms, we want to compute a list of all subsets of the list values.

For example,

```
(subsets '(1 2 3)) ⇒

(()(1)(2)(3)(1 2)(1 3)
(2 3)(1 2 3))
```

The order of atoms and sublists is unimportant, but all possible subsets of the list values must be included.

Given Scheme's recursive style of programming, we need a recursive definition of subsets.

That is, if we have a list of all subsets of n atoms, how do we extend this list to one containing all subsets of n+1 values?

First, we note that the number of subsets of n+1 values is exactly *twice* the number of subsets of n values.

For example,

```
(subsets '(1 2) ) ⇒
( () (1) (2) (1 2)), which
contains 4 subsets.
(subsets '(1 2 3)) Contains 8
subsets (as we saw earlier).
```

Moreover, the extended list (of subsets for n+1 values) is simply the list of subsets for n values *plus* the result of "distributing" the new value into each of the original subsets.

```
Thus (subsets '(1 2 3)) \Rightarrow
( () (1) (2) (3) (1 2) (1 3)
  (2\ 3)\ (1\ 2\ 3)) =
(() (1) (2) (12)) plus
((3)(13)(23)(123))
This insight leads to a concise
program for subsets.
We will let (distrib L E) be a
function that "distributes" E into
each list in L.
For example,
(distrib '(() (1) (2) (1 2)) 3) =
((3)(31)(32)(312))
(define (distrib L E)
  (if (null? L)
      ()
      (cons (cons E (car L))
            (distrib (cdr L) E))
```

We will let (extend L E) extend a list L by distributing element E through L and then appending this result to L.

```
For example,
(extend '( () (a) ) 'b) \Rightarrow
 ( () (a) (b) (b a))
(define (extend L E)
  (append L (distrib L E))
Now subsets is easy:
(define (subsets L)
  (if (null? L)
      (list ())
       (extend (subsets (cdr L))
               (car L))
```

#### Data Structures in Scheme

In Scheme, lists and S-expressions are basic. Arrays can be simulated using lists, but access to elements "deep" in the list can be slow (since a list is a linked structure).

To access an element deep within a list we can use:

- (list-tail L k)
  This returns list L after removing the first k elements. For example,
  (list-tail '(1 2 3 4 5) 2) ⇒
  (3 4 5)
- (list-ref L k)
  This returns the k-th element in L
  (counting from 0). For example,
  (list-ref '(1 2 3 4 5) 2) ⇒ 3

#### **Vectors in Scheme**

Scheme provides a vector type that directly implements one dimensional arrays.

```
Literals are of the form #( ... )

For example, #(1 2 3) or
#(1 2.0 "three")

The function (vector? val) tests
whether val is a vector or not.

(vector? 'abc) \Rightarrow #f

(vector? '(a b c)) \Rightarrow #f

(vector? #(a b c)) \Rightarrow #t
```

The function (vector v1 v2 ...) evaluates v1, v2, ... and puts them into a vector.

```
(vector 1 2 3) \Rightarrow #(1 2 3)
```

The function (make-vector k val) creates a vector composed of k copies of val. Thus

```
(make-vector 4 (/ 1 2)) \Rightarrow #(1/2 1/2 1/2 1/2)
```

The function (vector-ref vect k) returns the k-th element of vect, starting at position 0. It is essentially the same as vect[k] in C or Java. For example,

The function

(vector-set! vect k val) sets
the k-th element of vect, starting at
position 0, to be val. It is essentially
the same as vect[k]=val in C or
Java. The value returned by the
function is unspecified. The suffix "!"
in set! indicates that the function

```
has a side-effect. For example, (define v #(1 2 3 4 5)) (vector-set! v 2 0) v ⇒ #(1 2 0 4 5)
```

Vectors aren't lists (and lists aren't vectors).

Thus (car #(1 2 3)) doesn't work.
There are conversion routines:

 (vector->list v) converts vector v to a list containing the same values as v. For example,

```
(vector->list \#(1\ 2\ 3)) \Rightarrow (1 2 3)
```

(list->vector L) converts list L
to a vector containing the same
values as L. For example,

```
(list->vector '(1 2 3)) \Rightarrow #(1 2 3)
```

• In general Scheme names a conversion function from type T to type Q as T->Q. For example, string->list converts a string into a list containing the characters in the string.

#### **Records and Structs**

```
In Scheme we can represent a record, or struct, or class object as an association list of the form ((obj1 val1) (obj2 val2) ...)
In the association list, which is a list of (object value) sublists, object serves as a "key" to locate the desired sublist.
```

## The predefined Scheme function (assoc obj alist)

checks alist (an association list) to see if it contains a sublist with obj as its head. If it does, the list starting with obj is returned; otherwise #f (indicating failure) is returned.

For example,

```
(define L
  '( (a 10) (b 20) (c 30) ) )
(assoc 'a L) ⇒ (a 10)
(assoc 'b L) ⇒ (b 20)
(assoc 'x L) ⇒ #f
```

We can use non-atomic objects as keys too!

Using assoc, we can easily define a structure function:

```
(structure key alist) Will return
the value associated with key in
alist; in C or Java notation, it
returns alist.key.
```

```
(define
  (structure key alist)
  (if (assoc key alist)
      (car (cdr (assoc key alist)))
    #f
  )
)
```

We can improve this function in two ways:

- The same call to assoc is made twice; we can save the value computed by using a let expression.
- Often combinations of car and cdr are needed to extract a value. Scheme

has a number of predefined functions that combine several calls to car and cdr into one function. For example,

```
(caar x) \equiv (car (car x))

(cadr x) \equiv (car (cdr x))

(cdar x) \equiv (cdr (car x))

(cddr x) \equiv (cdr (cdr x))
```

Using these two insights we can now define a better version of structure

What does assoc do if more than one sublist with the same key exists?

It returns the first sublist with a matching key. In fact, this property can be used to make a simple and fast function that updates association lists:

```
(define
  (set-structure key alist val)
  (cons (list key val) alist)
)
```

If we want to be more spaceefficient, we can create a version that
updates the internal structure of an
association list, using set-cdr!
which changes the cdr value of a list:

# Functions are First-class Objects

Functions may be passed as parameters, returned as the value of a function call, stored in data objects, etc.

This is a consequence of the fact that (lambda (args) (body)) evaluates to a function just as (+ 1 1) evaluates to an integer.

## **Scoping**

In Scheme scoping is static (lexical). This means that non-local identifiers are bound to containing lambda parameters, or let values, or globally defined values. For example,

```
(define (f x) (lambda (y) (+ x y)))
```

Function  $\mathbf{f}$  takes one parameter,  $\mathbf{x}$ . It returns a function (of  $\mathbf{y}$ ), with  $\mathbf{x}$  in the returned function bound to the value of  $\mathbf{x}$  used when  $\mathbf{f}$  was called.

Thus

```
(f 10) \equiv (lambda (y) (+ 10 y))
((f 10) 12) \Rightarrow 22
```

Unbound symbols are assumed to be globals; there is a run-time error if an unbound global is referenced. For example,

```
(define (p y) (+ x y))
(p 20); error -- x is unbound
(define \times 10)
(p 20) \Rightarrow 30
We can use let bindings to create
private local variables for functions:
(define F
         (let ((X 1))
              (lambda () X)
F is a function (of no arguments).
(F) calls F.
(define X 22)
(F) \Rightarrow 1;X used in F is private
```

We can *encapsulate* internal state with a function by using private, let-bound variables:

# Let Bindings can be Subtle

You must check to see if the letbound value is created when the function is *created* or when it is *called*.

#### Compare

# Simulating Class Objects

Using association lists and private bound values, we can *encapsulate* data and functions. This gives us the effect of class objects.

```
(define (point x y)
  (list
   (list 'rect
         (lambda () (list x y)))
   (list 'polar
         (lambda ()
          (list
           (sqrt (+ (* x x) (* y y)))
           (atan (/ x y))
A call (point 1 1) creates an
association list of the form
( (rect funct) (polar funct) )
```

We can use **structure** to access components:

```
(define p (point 1 1))
( (structure 'rect p) ) \Rightarrow (1 1)
( (structure 'polar p) ) \Rightarrow
( \sqrt{2} \frac{\pi}{4})
```

We can add new functionality by just adding new (id function) pairs to the association list.

```
(define (point x y)
  (list
   (list 'rect
         (lambda () (list x y)))
   (list 'polar
         (lambda ()
          (list
           (sqrt (+ (* x x) (* y y)))
           (atan (/ x y))
   )))
   (list 'set-rect!
         (lambda (newx newy)
                  (set! x newx)
                  (set! y newy)
                  (list x y)
   ))
   (list 'set-polar!
         (lambda (r theta)
           (set! x (* r (sin theta)))
           (set! y (* r (cos theta)))
           (list r theta)
   ))
))
```

```
Now we have (define p (point 1 1)) ( (structure 'rect p) ) \Rightarrow (1 1) ( (structure 'polar p) ) \Rightarrow (\sqrt{2} \frac{\pi}{4}) ((structure 'set-polar! p) 1 \pi/4) \Rightarrow (1 \pi/4) ( (structure 'rect p) ) \Rightarrow (\frac{1}{\sqrt{2}} \frac{1}{\sqrt{2}})
```

# Limiting Access to Internal Structure

We can improve upon our association list approach by returning a single function (similar to a C++ or Java object) rather than an explicit list of (id function) pairs.

The function will take the name of the desired operation as one of its arguments.

# First, let's differentiate between (define def1 (let ( (I 0) ) (lambda () (set! I (+ I 1) I) ) ) and (define (def2) (let ( (I 0) ) (lambda () (set! I (+ I 1) I) )

**def1** is a function of zero arguments that increments a local variable and returns its updated value.

def2 is a function (of zero arguments) that *generates* a function of zero arguments (that increments a local variable and returns its updated value). Each call to def2 creates a different function.

# Stack Implemented as a Function

```
(define ( stack )
  (let ( (s () ) )
    (lambda (op . args) ; var # args
     (cond
      ((equal? op 'push!)
       (set! s (cons (car args) s))
        (car s))
      ((equal? op 'pop!)
        (if (null? s)
           #£
            (let ((top (car s)))
                (set! s (cdr s))
               top )))
      ((equal? op 'empty?)
       (null? s))
     (else #f)
```

```
(define stk (stack));new empty stack
(stk 'push! 1) ⇒ 1 ;s = (1)
(stk 'push! 3) ⇒ 3 ;s = (3 1)
(stk 'push! 'x) ⇒ x ;s = (x 3 1)
(stk 'pop!) ⇒ x ;s = (3 1)
(stk 'empty?) ⇒ #f ;s = (3 1)
(stk 'dump) ⇒ #f ;s = (3 1)
```

# **Higher-Order Functions**

A higher-order function is a function that takes a function as a parameter or one that returns a function as its result.

A very important (and useful) higherorder function is map, which applies a function to a list of values and produces a list or results:

Note: In Scheme's built-in implementation of map, the order of function application is unspecified.

Map may also be used with multiple argument functions by supplying more than one list of arguments:

```
(map + '(1 2 3) '(4 5 6)) \Rightarrow (5 7 9)
```

### The Reduce Function

Another useful higher-order function is reduce, which reduces a list of values to a single value by repeatedly applying a binary function to the list values.

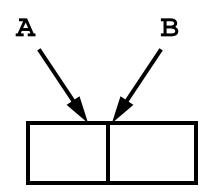
This function takes a binary function, a list of data values, and an identity value for the binary function:

```
(reduce append
'((1 2 3) (4 5 6) (7 8)) ())
\Rightarrow (1 2 3 4 5 6 7 8)
(reduce expt '(2 2 2 2) 1) \Rightarrow
2^{2^{2^2}} = 65536
(reduce expt '(2 2 2 2 2) 1)
\Rightarrow 2<sup>65536</sup>
(string-length
(number->string
(reduce expt '(2 2 2 2 2) 1)))
\Rightarrow 19729; digits in 2<sup>65536</sup>
```

# Sharing vs. Copying

In languages without side-effects an object can be copied by copying a pointer (reference) to the object; a complete new copy of the object isn't needed.

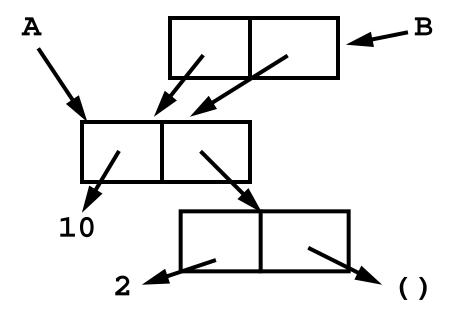
Hence in Scheme (define A B) normally means



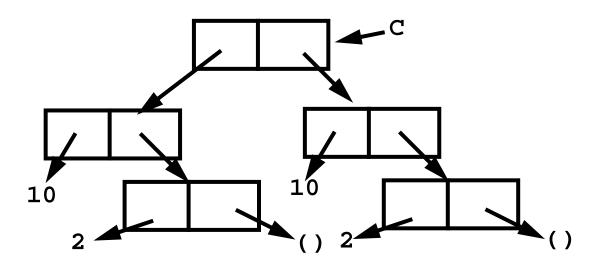
But, if side-effects are possible we may need to force a physical copy of an object or structure:

```
(define (copy obj)
  (if (pair? obj)
    (cons (copy (car obj))
          (copy (cdr obj)))
    obj
For example,
(define A '(1 2))
(define B (cons A A))
B = ((1 2) 1 2)
```

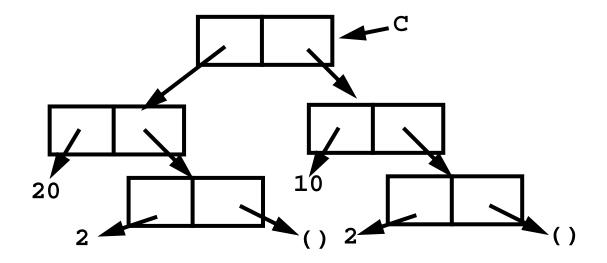
(set-car! (car B) 10) B = ((10 2) 10 2)



(define C (cons (copy A) (copy A)))



$$(set-car! (car C) 20)$$
  
C = ((20 2) 10 2)



Similar concerns apply to strings and vectors, because their internal structure can be changed.

# **Shallow & Deep Copying**

A copy operation that copies a pointer (or reference) rather than the object itself is a *shallow copy*.

For example, In Java,

```
Object O1 = new Object();
Object O2 = new Object();
O1 = O2; // shallow copy
```

If the structure within an object is physically copied, the operation is a deep copy.

In Java, for objects that support the clone operation,

```
O1 = O2.clone(); // deep copy
```

Even in Java's deep copy (via the clone() operation), objects referenced from within an object are shallow copied. Thus given

```
class List {
  int value;
  List next:
List L,M;
M = L.clone();
L. value and M. value are
independent, but L.next and M.next
refer to the same List object.
A complete deep copy, that copies all
objects linked directly or indirectly, is
expensive and tricky to implement.
(Consider a complete copy of a
circular linked list).
```

# **Equality Checking in Scheme**

In Scheme = is used to test for numeric equality (including comparison of different numeric types). Non-numeric arguments cause a run-time error. Thus

$$(= 1 1) \Rightarrow #t$$

$$(= 1 1.0) \Rightarrow #t$$

$$(= 1 2/2) \Rightarrow #t$$

$$(= 1 1+0.0i) \Rightarrow #t$$

To compare non-numeric values, we can use either:

pointer equivalence (do the two operands point to the same address in memory)

structural equivalence (do the two operands point to structures with the same size, shape and components, even if they are in different memory locations)

In general pointer equivalence is faster but less accurate.

Scheme implements both kinds of equivalence tests.

```
(eqv? obj1 obj2)
```

This tests if obj1 and obj2 are the exact same object. This works for atoms and pointers to the same structure.

```
(equal? obj1 obj2)
```

This tests if оьј1 and оьј2 are the same, component by component. This works for atoms, lists, vectors and strings.

```
(eqv? 1 1) ⇒ #t
(eqv? 1 (+ 0 1)) ⇒ #t
(eqv? 1/2 (- 1 1/2)) ⇒ #t
(eqv? (cons 1 2) (cons 1 2)) ⇒
    #f
(eqv? "abc" "abc") ⇒ #f
```

```
(equal? 1 1) ⇒ #t
(equal? 1 (+ 0 1)) ⇒ #t
(equal? 1/2 (- 1 1/2)) ⇒ #t
(equal? (cons 1 2) (cons 1 2)) ⇒
   #t
(equal? "abc" "abc") ⇒ #t
```

In general it is wise to use equal? unless speed is a critical factor.

### I/O in Scheme

Scheme provides simple read and write functions, directed to the "standard in" and "standard out" files.

#### (read)

Reads a single Scheme object (an atom, string, vector or list) from the standard in file. No quoting is needed.

#### (write obj)

Writes a single object, оьј, to the standard out file.

```
(display obj)
```

Writes obj to the standard out file in a more readable format. (Strings aren't quoted, and characters aren't escaped.)

#### (newline)

Forces a new line on standard out file.

## **Ports**

Ports are Scheme objects that interface with systems files. I/O to files is normally done through a port object bound to a system file.

(open-input-file "path to file")
This returns an input port associated with the "path to file" String (which is system dependent). A runtime error is signalled if "path to file" specifies an illegal or inaccessible file.

(read port)

Reads a single Scheme object (an atom, string, vector or list) from port, which must be an input port object.

#### (eof-object? obj)

When the end of an input file is reached, a special eof-object is returned. eof-object? tests whether an object is this special end-of-file marker.

(open-output-file "path to file")
This returns an output port associated with the "path to file" String (which is system dependent). A runtime error is signalled if "path to file" specifies an illegal or inaccessible file.

(write obj port)

Writes a single object, obj, to the output port specified by port.

(display obj port)

Writes obj to the output port specified by port. display uses a more readable format than write does. (Strings aren't quoted, and characters aren't escaped.)

(close-input-port port)

This closes the input port specified by port.

(close-output-port port)

This closes the output port specified by port.

# Example—Reading & Echoing a File

We will iterate through a file, reading and echoing its contents. We need a good way to do iteration; recursion is neither natural nor efficient here.

Scheme provides a nice generalization of the let expression that is similar to C's for loop.

A name for the let (x in the example) is provided. As usual, val1 is evaluated and bound to id1, val2 is evaluated and bound to id2, etc. In the body of the let, the let may be "called" (using its name) with a fresh

```
set of values for the let variables.
Thus (x v1 v2 ...) starts the next
iteration of the let with ial bound to
v1, id2, bound to v2, etc.
The calls look like recursion, but they
are implemented as loop iterations.
For example, in
(let loop ( (x 1) (sum 0) )
  (if (<= x 10)
       (loop (+ x 1) (+ sum x))
       sum
we sum the values of x from 1 to 10.
Compare it to
for (x=1,sum=0; x <= 10;
      sum+=x,x+=1)
 {}
```

Now a function to read and echo a file is straightforward:

```
(define (echo filename)
  (let (
  (p (open-input-file filename)))
    (let loop ((obj (read p)))
      (if (eof-object? obj)
          #t ;normal termination
          (begin
            (write obj)
            (newline)
            (loop (read p))
```

We can create an alternative to echo that uses

```
(call-with-input-file
  filename function)
```

This function opens filename, creates an input port from it, and then calls function with that port as an argument:

### **Control Flow in Scheme**

Normally, Scheme's control flow is simple and recursive:

- The first argument is evaluated to get a function.
- Remaining arguments are evaluated to get actual parameters.
- Actual parameters are bound to the function's formal parameters.
- The functions' body is evaluated to obtain the value of the function call.

This approach routinely leads to deeply nested expression evaluation.

As an example, consider a simple function that multiplies a list of integers:

what if we get clever and decide to improve this function by noting that if 0 appears *anywhere* in list L, the product *must be* 0.

This helps a bit—we never go past a zero in L, but we still unnecessarily do a sequence of pending multiplies, all of which must yield zero!

Can we escape from a sequence of nested calls once we know they're unnecessary?

# **Exceptions**

In languages like Java, a statement may throw an exception that's caught by an enclosing exception handler. Code between the statement that throws the exception and the handler that catches it is abandoned.

Let's solve the problem of avoiding multiplication of zero in Java, using its exception mechanism:

```
class Node {
  int val;
  Node next;
}
class Zero extends Throwable
  {};
```

```
int mult (Node L) {
  try {
    return multNode(L);
  } catch (Zero z) {
    return 0;
int multNode(Node L)
   throws Zero {
  if (L == null)
    return 1;
  else if (L.val == 0)
    throw new Zero();
  else return
   L.val * multNode(L.next);
In this implementation, no multiplies
by zero are ever done.
```

#### **Continuations**

In our Scheme implementation of \*list, we'd like a way to delay doing any multiplies until we know no zeros appear in the list. One approach is to build a *continuation*—a function that represents the context in which a function's return value will be used:

```
The top-level call is
```

```
(*listC L (lambda (x) x))
```

For ordinary lists \*listc expands to a series of multiplies, just like \*list did.

```
(define (id x) x)
(*listC '(1 2 3) id) ⇒
(*listC '(2 3)
   (lambda (n) (* n (id 1)))) ≡
(*listC '(2 3)
   (lambda (n) (* n 1))) ⇒
(*listC '(3)
   (lambda (n) (* n (* 2 1)))) ≡
(*listC '(3)
   (lambda (n) (* n 2))) ⇒
(*listC ()
   (lambda (n) (* n 2))) ⇒
(*listC ()
   (lambda (n) (* n (* 3 2)))) ≡
(*listC () (lambda (n) (* n 6)))
   ⇒ (* 1 6) ⇒ 6
```

But for a list with a zero in it, we get a different execution path:

```
(*listC '(1 0 3) id) ⇒
(*listC '(0 3)
  (lambda (n) (* n (id 1)))) ⇒ 0
```

No multiplies are done!

# Another Example of Continuations

Let's redo our list multiply example so that if a zero is seen in the list we return a function that computes the product of all the non-zero values and a parameter that is the "replacement value" for the unwanted zero value. The function gives the caller a chance to correct a probable error in the input data.

We create

```
(*list2 L) ≡
Product of all integers in L
if no zero appears
else
(lambda (n) (* n product-of-
all-nonzeros-in-L)
```

In the following, we check to see if \*1ist2 returns a number or a function. If a function is returned, we call it with 1, effectively removing 0 from the list

For ordinary lists \*list2 expands to a series of multiplies, just like \*list did.

```
(*listE '(1 2 3) id) ⇒
(*listE '(2 3)
    (lambda (m) (* m (id 1)))) ≡
(*listE '(2 3)
    (lambda (m) (* m 1))) ⇒
(*listE '(3)
    (lambda (m) (* m (* 2 1)))) ⇒
(*listE '(3)
    (lambda (m) (* m 2))) ⇒
(*listE ()
    (lambda (m) (* m 2))) ≡
(*listE ()
    (lambda (m) (* m (* 3 2)))) ≡
(*listE () (lambda (n) (* n 6)))
    ⇒ (* 1 6) ⇒ 6
```

But for a list with a zero in it, we get a different execution path:

```
(*listE '(1 0 3) id) ⇒
(*listC '(0 3)
    (lambda (m) (* m (id 1)))) ⇒
(lambda (n) (* (con n)
        (* listE '(3) id))) ≡
(lambda (n) (* (* n 1)
        (* listE '(3) id))) ≡
(lambda (n) (* (* n 1) 3))
This function multiplies n, the replacement value for 0, by 1 and 3, the non-zero values in the input list.
```

But note that only one zero value in the list is handled correctly!

#### **Continuations in Scheme**

```
Scheme provides a built-in
mechanism for creating
continuations. It has a long name:
call-with-current-continuation
This name is usually abbreviated as
call/cc
(perhaps using define).
call/cc takes a single function as its
argument. That function also takes a
single argument. That is, we use
call/cc as
(call/cc funct) Where
funct \equiv (lambda (con) (body))
call/cc calls the function that it is
given with the "current continuation"
as the function's argument.
```

#### **Current Continuation**

What is the current continuation?

It is itself a function of one argument. The current continuation function represents the execution context within which the call/cc appears. The argument to the continuation is a value to be substituted as the value of call/cc in that execution context.

```
For example, given

(+ (fct n) 3)

the current continuation for (fct n)
is (lambda (x) (+ x 3)

Given (* 2 (+ (fct z) 10))

the current continuation for (fct z)
is (lambda (m) (* 2 (+ m 10))
```

To use call/cc to grab a continuation in (say) (+ (fct n) 3) we make (fct n) the body of a function of one argument. Let's call that argument return. We therefore create

```
(lambda (return) (fct n))
Then
(call/cc
   (lambda (return) (fct n)))
```

binds the current continuation to return and executes (fct n).

We can ignore the current continuation bound to return and do a normal return

or

we can use return to force a return to the calling context of the call/cc.

The call (return value) forces value to be returned as the value of call/cc in its context of call.

#### Example:

(define (g con) (con 5))

Now during evaluation no divide by zero error occurs. Rather, when (g return) is called, 5 is passed to con, which is bound to return.
Therefore 5 is used as the value of the call to call/cc, and 50 is computed.

### Continuations are Just Functions

Continuations may be saved in variables or data structures and called in the future to "reactive" a completed or suspended computation.

```
(define CC ())
(define (F)
  (let (
    (v (call/cc
          (lambda(here)
             (set! CC here)
              1))))
     (display "The ans is:
     (display v)
     (newline)
This displays the ans is: 1
At any time in the future, (cc 10)
Will display The ans is: 10
```

#### List Multiplication Revisited

We can use call/cc to reimplement the original \*list to force an immediate return of 0 (much like a throw in Java):

A o in L forces a call of (return o) which makes o the value of call/cc.

### Interactive Replacement of Error Values

Using continuations, we can also redo \*listE so that zeroes can be replaced interactively! Multiple zeroes (in both original and replacement values) are correctly handled.

If a zero is seen, \*liste passes back to the caller (via return) a continuation that will set the next value of value. This value is checked, so if it is itself zero, a substitute is requested. Each occurrence of zero forces a return to the caller for a substitute value.

# Implementing Coroutines with call/cc

Coroutines are a very handy generalization of subroutines. A coroutine may *suspend* its execution and later *resume* from the point of suspension. Unlike subroutines, coroutines do no have to complete their execution before they return.

Coroutines are useful for computation of long or infinite streams of data, where we wish to compute some data, use it, compute additional data, use it, etc.

Subroutines aren't always able to handle this, as we may need to save a lot of internal state to resume with the correct next value.

# Producer/Consumer using Coroutines

The example we will use is one of a consumer of a potentially infinite stream of data. The next integer in the stream (represented as an unbounded list) is read. Call this value n. Then the next n integers are read and summed together. The answer is printed, and the user is asked whether another sum is required. Since we don't know in advance how many integers will be needed, we'll use a coroutine to produce the data list in segments, requesting another segment as necessary.

```
(define (consumer)
  (next 0); reset next
  (let loop ((data (moredata)))
    (let (
     (sum+restoflist
       (sum-n-elems (car data)
           (cons 0 (cdr data)))))
      (display (car sum+restoflist))
      (newline)
      (display "more? ")
      (if (equal? (read) 'y)
        (if (= 1)
            (length sum+restoflist))
         (loop (moredata))
         (loop (cdr sum+restoflist))
        #t ; Normal completion
```

Next, we'll consider sum-n-elems, which adds the first element of list (a running sum) to the next n elements on the list. We'll use moredata to extend the data list as needed.

The function moredata is called whenever we need more data. Initially a producer function is called to get the initial segment of data. producer actually returns the next data segment plus a continuation (stored in producer-cc) used to resume execution of producer when the next data segment is required.

```
(define moredata
 (let ( (producer-cc () ) )
   (lambda ()
     (let (
       (data+cont
         (if (null? producer-cc)
            (call/cc (lambda (here)
               (producer here)))
            (call/cc (lambda (here)
               (producer-cc here)))
        (set! producer-cc
              (cdr data+cont))
        (car data+cont)
```

Function (next z) returns the next z integers in an infinite sequence that starts at 1. A value z=0 is a special flag indicating that the sequence should be reset to start at 1.

```
(define next
  (let ( (i 1))
    (lambda (z)
      (if (= 0 z)
        (set! i 1)
        (let loop
           ((cnt z) (val i) (ints ()))
              (if (> cnt 0)
                  (loop (- cnt 1)
                         (+ val 1)
                         (append ints
                          (list val)))
                  (begin
                      (set! i val)
                      ints
) ) ) )
```

The function producer generates an infinite sequence of integers (1,2,3,...). It suspends every 5/10/15/25 elements and returns control to moredata.

```
(define (producer initial-return)
   (let
         loop
        (return initial-return) )
     (set! return
        (call/cc (lambda (here)
          (return (cons (next 5)
                          here)))))
     (set! return
        (call/cc (lambda (here)
          (return (cons (next 10)
                          here)))))
     (set!
           return
        (call/cc (lambda (here)
          (return (cons (next 15)
                          here)))))
     (loop
        (call/cc (lambda (here)
          (return (cons (next 25)
                          here)))))
```

### Reading Assignment

 MULTILISP: a language for concurrent symbolic computation, by Robert H. Halstead (linked from class web page)

### Lazy Evaluation

Lazy evaluation is sometimes called "call by need." We do an evaluation when a value is used; not when it is defined.

Scheme provides for lazy evaluation:

(delay expression)

Evaluation of expression is delayed. The call returns a "promise" that is essentially a lambda expression.

(force promise)

A promise, created by a call to delay, is evaluated. If the promise has already been evaluated, the value computed by the first call to force is reused.

#### Example:

Though and is predefined, writing a correct implementation for it is a bit tricky.

```
The obvious program
(define (and A B)
  (if A
      \mathbf{B}
      #£
is incorrect since в is always
evaluated whether it is needed or not.
In a call like
(and (not (= i 0)) (> (/ j i) 10))
unnecessary evaluation might be
fatal.
```

An argument to a function is *strict* if it is always used. Non-strict arguments may cause failure if evaluated unnecessarily.

With lazy evaluation, we can define a more robust and function:

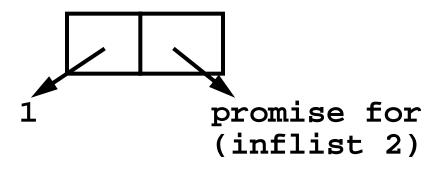
Delayed evaluation also allows us a neat implementation of suspensions.

The following definition of an infinite list of integers clearly fails

```
(define (inflist i)
  (cons i (inflist (+ i 1))))
```

But with use of delays we get the desired effect in finite time:

```
(define (inflist i)
      (cons i
          (delay (inflist (+ i 1)))))
Now a call like (inflist 1) creates
```



We need to slightly modify how we explore suspended infinite lists. We can't redefine car and cdr as these are far too fundamental to tamper with.

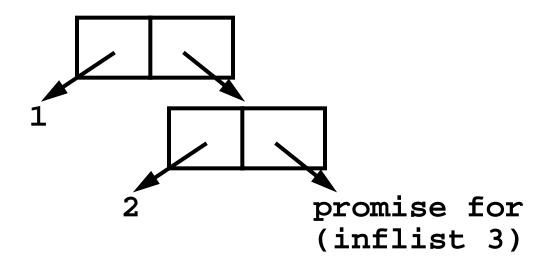
Instead we'll define head and tail to do much the same job:

```
(define head car)
(define (tail L)
  (force (cdr L)))
```

head looks at car values which are fully evaluated.

tail forces one level of evaluation of a delayed car and saves the evaluated value in place of the suspension (promise).

# Given (define IL (inflist 1)) (head (tail IL)) returns 2 and expands IL into



### **Exploiting Parallelism**

Conventional procedural programming languages are difficult to compile for multiprocessors.

Frequent assignments make it difficult to find independent computations.

Consider

```
do 10 I = 1,1000
    X(I) = 0
    A(I) = A(I+1)+1
    B(I) = B(I-1)-1
    C(I) = (C(I-2) + C(I+2))/2
10 continue
```

This loop defines 1000 values for arrays x, a, b and c.

Which computations can be done in parallel, partitioning parts of an array to several processors, each operating independently?

- x(I) = 0
   Assignments to x can be readily parallelized.
- A(I) = A(I+1)+1
   Note that each computation of A(I) uses an A(I+1) value that is yet to be changed. Thus a whole array of new A values can be computed from an array of "old" A values in parallel.
- B(I) = B(I-1)-1
  This is less obvious. Each B(I) uses
  B(I-1) which is defined in terms of
  B(I-2), etc. Ultimately all new B
  values depend only on B(0) and I.
  That is, B(I) = B(0) I. So this

computation can be parallelized, but it takes a fair amount of insight to realize it.

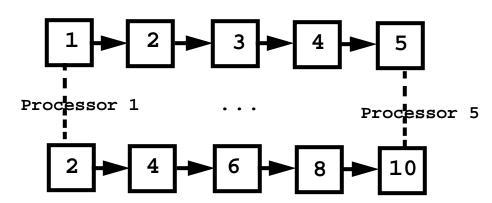
• C(I) = (C(I-2) + C(I+2))/2
It is clear that even and odd elements
of c don't interact. Hence two
processors could compute even and
odd elements of c in parallel. Beyond
this, since both earlier and later c
values are used in each computation
of an element, no further means of
parallel evaluation is evident. Serial
evaluation will probably be needed
for even or odd values.

# **Exploiting Parallelism in Scheme**

Assume we have a shared-memory multiprocessor. We might be able to assign different processors to evaluate various independent subexpressions.

For example, consider

We might assign a processor to each list element and compute the lambda function on each concurrently:



## How is Parallelism Found?

There are two approaches

- We can use a "smart" compiler that is able to find parallelism in existing programs written in standard serial programming languages.
- We can add features to an existing programming language that allows a programmer to show where parallel evaluation is desired.

## Concurrentization

Concurrentization (often called parallelization) is process of automatically finding potential concurrent execution in a serial program.

Automatically finding current execution is complicated by a number of factors:

#### Data Dependence

Not all expressions are independent. We may need to delay evaluation of an operator or subprogram until its operands are available.

Thus in (+ (\* x y) (\* y z))

we can't start the addition until both multiplications are done.

#### Control Dependence

Not all expressions need be (or should be) evaluated.

we don't want to do the division until we know  $\mathbf{a} \neq \mathbf{0}$ .

#### Side Effects

If one expression can write a value that another expression might read, we probably will need to *serialize* their execution.

Now in

(+ (f (rand!)) (g (rand!)))
we can't evaluate (f (rand!)) and
(g (rand!)) in parallel, because of
the side effect of set! in rand!. In
fact if we did, f and g might see exactly
the same "random" number! (Why?)

#### Granularity

Evaluating an expression concurrently has an overhead (to setup a concurrent computation). Evaluating some very simple expressions (like (car x) or (+ x 1)) in parallel isn't worth the overhead cost.

Estimating where the "break even" threshold is may be tricky.

# Utility of Concurrentization

Concurrentization has been most successful in engineering and scientific programs that are very regular in structure, evaluating large multidimensional arrays in simple nested loops. Many very complex simulations (weather, fluid dynamics, astrophysics) are run on multiprocessors after extensive concurrentization.

Concurrentization has been far less successful on non-scientific programs that don't use large arrays manipulated in nested for loops. A compiler, for example, is difficult to run (in parallel) on a multiprocessor.

# Concurrentization within Processors

Concurrentization is used extensively within many modern uniprocessors. Pentium and PowerPC processors routinely execute several instructions in parallel if they are independent (e.g., read and write distinct registers). This are *superscalar* processors.

These processors also routinely speculate on execution paths, "guessing" that a branch will (or won't) be taken even before the branch is executed! This allows for more concurrent execution than if strictly "in order" execution is done. These processors are called "out of order" processors.

# Adding Parallel Features to Programming Languages.

It is common to take an existing serial programming language and add features that support concurrent or parallel execution. For example versions for Fortran (like HPF—High Performance Fortran) add a parallel do loop that executes individual iterations in parallel.

Java supports threads, which may be executed in parallel. Synchronization and mutual exclusion are provided to avoid unintended interactions.

# Multilisp

Multilisp is a version of Scheme augmented with three parallel evaluation mechanisms:

- Pcall
   Arguments to a call are evaluated in parallel.
- Future
   Evaluation of an expression starts
   immediately. Rather than waiting for
   completion of the computation, a
   "future" is returned. This future will
   eventually transform itself into the
   result value (when the computation
   completes)
- Delay
   Evaluation is delayed until the result value is really needed.

## The Pcall Mechanism

Pcall is an extension to Scheme's function call mechanism that causes the function and its arguments to be all computed in parallel.

Thus

```
(pcall F X Y Z)
```

causes **F**, **x**, **y** and **z** to all be evaluated in parallel. When all evaluations are done, **F** is called with **x**, **y** and **z** as its parameters (just as in ordinary Scheme).

Compare

```
(+ (* X Y) (* Y Z))
With
(pcall + (* X Y) (* Y Z))
```

It may not look like pcall can give you that much parallel execution, but in the context of recursive definitions, the effect can be dramatic.

Consider treemap, a version of map that operates on binary trees (S-expressions).

```
(define (treemap fct tree)
  (if (pair? tree)
        (pcall cons
              (treemap fct (car tree))
              (treemap fct (cdr tree))
        )
        (fct tree)
))
Look at the execution of treemap on
the tree
        (((1 . 2) . (3 . 4)) .
              ((5 . 6) . (7 . 8)))
```

We start with one call that uses the whole tree. This splits into two parallel calls, one operating on

((1.2).(3.4))

and the other operating on

((5.6).(7.8))

Each of these calls splits into 2 calls, and finally we have 8 independent calls, each operating on the values 1 to 8.

#### **Futures**

Evaluation of an expression as a future is the most interesting feature of Multilisp.

The call

(future expr)

begins the evaluation of expr. But rather than waiting for expr's evaluation to complete, the call to future returns immediately with a new kind of data object—a future. This future is actually an "IOU." When you try to use the value of the future, the computation of expr may or may not be completed. If it is, you see the value computed instead of the future—it automatically transforms itself. Thus evaluation of expr appears instantaneous.

If the computation of expr is not yet completed, you are forced to wait until computation is completed. Then you may use the value and resume execution. But this is exactly what ordinary evaluation does anyway—you begin evaluation of expr and wait until evaluation completes and returns a value to you!

To see the usefulness of futures, consider the usual definition of Scheme's map function:

```
(define (map f L)
  (if (null? L)
     ()
     (cons (f (car L))
           (map f (cdr L)))
If we have a call
(map slow-function long-list)
Where slow-function executes
slowly and long-list is a large data
structure, we can expect to wait quite
a while for computation of the result
list to complete.
```

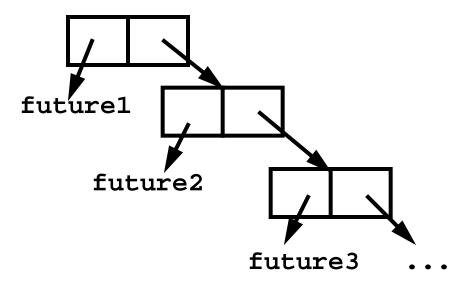
Now consider **fastmap**, a version of **map** that uses futures:

Now look at the call

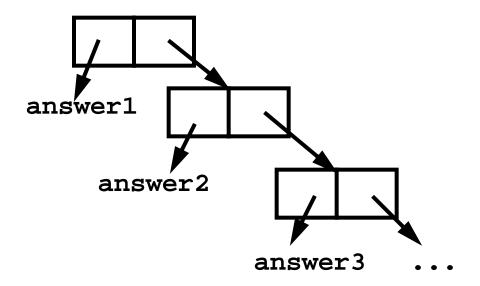
(fastmap slow-function long-list)
We will exploit a useful aspect of futures—they can be cons'ed together without delay, even if the computation isn't completed yet.

Why? Well a cons just stores a pair of pointers, and it really doesn't matter what the pointers reference (a future or an actual result value).

The call to fastmap can actually return before any of the call to slow-function have completed:



Eventually all the futures automatically transform themselves into data values:



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Note that pcall can be implemented using futures.

That is, instead of

(pcall F X Y Z)

we can use

(F (future X) (future Y) (future Z))
In fact the latter version is actually
more parallel—execution of F can
begin even if all the parameters aren't
completely evaluated.

(Why isn't **F** placed in a future?)

# Reading Assignment

- Sethi: Chapters 8 and 9
- Introduction to Standard ML (linked from class web page)

Scott: Section 7.1 and 7.2

## Another Example of Futures

The following function, partition, will take a list and a data value (called pivot). partition will partition the list into two sublists:

- (a) Those elements ≤ pivot

We want to add futures to partition, but where?

It makes sense to use a future when a computation may be lengthy and we may not need to use the value computed immediately.

What computation fits that pattern?

The computation of tail-part. We'll mark it in a blue box to show we plan to evaluate it using a future:

But this one change isn't enough! We soon access the car and cdr of tail-part, which forces us to wait for its computation to complete. To avoid this delay, we can place the four reference to car or cdr of tail-part into futures too:

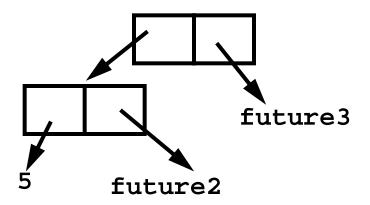
Now we can build the initial part of the partitioned list (that involving pivot and (car L) independently of the recursive call of partition, which completes the rest of the list.

For example,

(partition 17 '(5 3 8 ...)) creates a future (call it future1) to compute

(partition 17 '(3 8 ...))

It also creates futures to compute
(car tail-part) (future2) and
(cdr tail-part) (future3). The
call builds



## ML—Meta Language

SML is *Standard ML*, a popular ML variant.

ML is a functional language that is designed to be efficient and type-safe. It demonstrates that a functional language need not use Scheme's odd syntax and need not bear the overhead of dynamic typing.

SML's features and innovations include:

- 1. Strong, compile-time typing.
- 2. Automatic *type inference* rather than user-supplied type declarations.
- 3. Polymorphism, including "type variables."

4. Pattern-directed Programming

```
fun len([]) = 0
    len(a::b) = 1+len(b);
```

- 5. Exceptions
- 6. First-class functions
- 7. Abstract Data Types

```
coin of int |
bill of int |
check of string*real;
val dime = coin(10);
```

A good ML reference is "Elements of ML Programming," by Jeffrey Ullman (Prentice Hall, 1998)

## **SML** is Interactive

You enter a definition or expression, and SML returns a result *with* an inferred type.

The command

```
use "file name";
```

loads a set of ML definitions from a file.

For example (SML responses are in blue):

```
21;
val it = 21 : int
(2 div 3);
val it = 0 : int
true;
val it = true : bool
"xyz";
val it = "xyz" : string
```

# **Basic SML Predefined Types**

#### Unit

Its only value is (). Type unit is similar to void in C; it is used where a type is needed, but no "real" type is appropriate. For example, a call to a write function may return unit as its result.

#### Integer

Constants are sequences of digits.

Negative values are prefixed with a rather than a - (- is a binary subtraction operator). For example, ~123 is negative 123.

Standard operators include

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#### Real

Both fractional (123.456) and exponent forms (10e7) are allowed. Negative signs and exponents use ~ rather than - (~10.0e~12).

Standard operators include

Note that = and <> aren't allowed! (Why?)

Conversion routines include real(int) to convert an int to a real,

floor(real) to take the floor of a real,

ceil(real) to take the ceiling of a real.

round(real) to round a real,
trunc(real) to truncate a real.

For example, real(3) returns 3.0, floor(3.1) returns 3, ceiling(3.3) returns 4, round(~3.6) returns ~4, trunc(3.9) returns 3.

Mixed mode expressions, like 1 + 2.5 aren't allowed; you must do explicit conversion, like real(1) + 2.5

#### Strings

Strings are delimited by double quotes. Newlines are \n, tabs are \t, and \" and \\ escape double quotes and backslashes. E.g. "Bye now\n" The ^ operator is concatenation.

"abc" ^ "def" = "abcdef"

The usual relation operators are provided: < > <= >= = <>

#### Characters

Single characters are delimited by double quotes and prefixed by a #. For example, #"a" or #"\t". A character is not a string of length one. The str function may be used to convert a character into a string. Thus str(#"a") = "a"

#### Boolean

Constants are true and false.

Operators include andalso (short-circuit and), orelse (short-circuit or), not, = and <>.

A conditional expression,

(if boolval  $v_1$  else  $v_2$ ) is available.

## **Tuples**

A tuple type, composed of two or more values of any type is available.

Tuples are delimited by parentheses, and values are separated by commas.

Examples include:

```
(1,2);
val it = (1,2) : int * int
("xyz",1=2);
val it = ("xyz",false) :
    string * bool
(1,3.0,false);
val it = (1,3.0,false) :
    int * real * bool
(1,2,(3,4));
val it = (1,2,(3,4)) :
int * int * (int * int)
```

Equality is checked componentwise:

```
(1,2) = (0+1,1+1);
val it = true : bool
```

(1,2,3) = (1,2) causes a compiletime type error (tuples must be of the same length and have corresponding types to be compared).

#i selects the i-th component of a tuple (counting from 1). Hence

```
#2(1,2,3);
val it = 2 : int
```

## Lists

Lists are required to have a single element type for all their elements; their length is unbounded.

Lists are delimited by [ and ] and elements are separated by commas.

Thus [1,2,3] is an integer list. The empty (or null) list is [] or nil.

The cons operator is ::

Hence  $[1,2,3] \equiv 1::2::3::[]$ 

Lists are automatically typed by ML:

```
[1,2];
```

val it = [1,2] : int list

#### Cons

Cons is an infix operator represented as ::

The left operand of :: is any value of type T.

The right operand of :: is any list of type T list.

The result of :: is a list of type T list.

Hence :: is polymorphic.

[] is the empty list. It has a type

'a list. The symbol 'a, read as "alpha" or "tic a" is a *type variable*.

Thus [] is a polymorphic constant.

# List Equality

Two lists may be compared for equality if they are of the same type. Lists **L1** and **L2** are considered equal if:

- (1) They have the same number of elements
- (2) Corresponding members of the two lists are equal.

# **List Operators**

```
hd ≡ head of list operator ≈ car
t1 ≡ tail of list operator ≈ cdr
null ≡ null list predicate ≈ null?
@ ≡ infix list append operator ≈
append
```

#### Records

```
Their general form is
{name_1=val_1, name_2=val_2, ...}
Field selector names are local to a
record.
For example:
{a=1,b=2};
val it = \{a=1,b=2\}:
 {a:int, b:int}
{a=1,b="xyz"};
val it = {a=1,b="xyz"} :
 {a:int, b:string}
{a=1.0,b={c=[1,2]}};
val it = \{a=1.0,b=\{c=[1,2]\}\}:
{a:real, b:{c:int list}}
```

The order of fields is irrelevant; equality is tested using field names.

```
{a=1,b=2}={b=2,a=2-1};
val it = true : bool
```

**#id** extracts the field named id from a record.

```
#b {a=1,b=2};
val it = 2 : int
```

### **Identifiers**

There are two forms:

Alphanumeric (excluding reserved words)

Any sequence of letters, digits, single quotes and underscores; must begin with a letter or single quote.

Case *is* significant. Identifiers that begin with a single quote are *type* variables.

**Examples include:** 

abc a10 'polar sum\_of\_20

Symbolic

Any sequence (except predefined operators) of

! % & + - / : < = > ? @ \ ~ ^ | # \*

Usually used for user-defined operators.

Examples include: ++ <=> !=

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### **Comments**

```
Of form

(* text *)

May cross line boundaries.
```

### **Declaration of Values**

The basic form is

```
val id = expression;
```

This defines id to be bound to expression; ML answers with the name and value defined and the inferred type.

For example

```
val x = 10*10;
val x = 100 : int
```

Redefinition of an identifier is OK, but this is redefinition *not* assignment;

#### Thus

```
val x = 100;
val x = (x=100);
```

is fine; there is no type error even though the first **x** is an integer and then it is a boolean.

```
val x = 100 : int
val x = true : bool
```

## **Examples**

```
val x = 1;
val x = 1 : int
val z = (x,x,x);
val z = (1,1,1) : int * int * int
val L = [z,z];
val L = [(1,1,1),(1,1,1)] :
   (int * int * int) list
val r = {a=L};
val r = {a=[(1,1,1),(1,1,1)]} :
{a:(int * int * int) list}
```

After rebinding, the "nearest" (most recent) binding is used.

The and symbol (not boolean and) is used for simultaneous binding:

```
val x = 10;
val x = 10 : int
val x = true and y = x;
val x = true : bool
val y = 10 : int
```

Local definitions are temporary value definitions:

```
local
    val x = 10
in
    val u = x*x;
end;
val u = 100 : int
```

Let bindings are used in expressions:

```
let
    val x = 10
in
    5*x
end;
val it = 50 : int
```

### **Patterns**

In Scheme (and most other languages) we need *access* or *decomposition* functions to access the components of a structured object.

Thus we might have

```
(let ((h (car L) (t (cdr L)) )
   body )
```

Here car and cdr are used as access functions to locate the parts of L we want to access.

In ML, we can access components of lists (or tuples, or records) *directly* by using patterns. The context in which the identifier appears tells us the part of the structure it references.

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```
val x = (1,2);
val x = (1,2) : int * int
val(h,t) = x;
val h = 1 : int
val t = 2 : int
val L = [1,2,3];
val L = [1,2,3] : int list
val [v1, v2, v3] = L;
val v1 = 1 : int
val v2 = 2 : int
val v3 = 3 : int
val [1,x,3] = L;
val x = 2 : int
val [1,rest] = L;
(* This is illegal. Why? *)
val yy::rest = L;
val yy = 1 : int
val rest = [2,3] : int list
```

### Wildcards

An underscore (\_) may be used as a "wildcard" or "don't care" symbol. It matches part of a structure without defining an new binding.

```
val zz::_ = L;
val zz = 1 : int
```

Pattern matching works in records too.

```
val r = {a=1,b=2};
val r = {a=1,b=2} :
    {a:int, b:int}
val {a=va,b=vb} = r;
val va = 1 : int
val vb = 2 : int
val {a=wa,b=_}=r;
val wa = 1 : int
val {a=za, ...}=r;
val za = 1 : int
```

Patterns can be nested too.

```
val x = ((1,3.0),5);
val x = ((1,3.0),5):
  (int * real) * int
val ((1,y),_)=x;
val y = 3.0 : real
```

### **Functions**

Functions take a single argument (which can be a tuple). Function calls are of the form function\_name argument; For example size "xyz"; cos 3.14159; The more conventional form size("xyz"); Or cos(3.14159); is OK (the parentheses around the argument are allowed, but unnecessary). The form (size "xyz") Or  $(\cos 3.14159)$ is OK too.

```
Note that the call plus(1,2);
passes one argument, the tuple (1,2)
to plus.
The call dummy();
passes one argument, the unit value,
to dummy.
```

All parameters are passed by value.

## **Function Types**

The type of a function in ML is denoted as T1->T2. This says that a parameter of type T1 is mapped to a result of type T2.

The symbol **fn** denotes a value that is a function.

```
Thus
size;
val it = fn : string -> int
not;
val it = fn : bool -> bool
Math.cos;
val it = fn : real -> real
(Math is an ML structure—an external library member that contains separately compiled definitions).
```

### **User-Defined Functions**

The general form is fun name arg = expression; MI answers back with the name defined, the fact that it is a function (the fn symbol) and its inferred type. For example, fun twice x = 2\*x;val twice = fn : int -> int fun twotimes(x) = 2\*x; val twotimes = fn : int -> int fun fact n = if n=0then 1 else n\*fact(n-1); val fact = fn : int -> int

fun plus(x,y):int = x+y;
val plus = fn : int \* int -> int
The :int suffix is a type constraint.
It is needed to help ML decide that +
is integer plus rather than real plus.

# Patterns In Function Definitions

The following defines a predicate that tests whether a list, **L** is null (the predefined **null** function already does this).

```
fun isNull L =
   if L=[] then true else
false;
val isNull = fn : 'a list -> bool
```

However, we can decompose the definition using *patterns* to get a simpler and more elegant definition:

The "|" divides the function definition into different argument patterns; no explicit conditional logic is needed. The definition that matches a particular actual parameter is automatically selected.

If patterns that cover all possible arguments aren't specified, you may get a run-time Match exception.

If patterns overlap you may get a warning from the compiler.

```
fun append([],L)=L
    append(hd::tl,L)=
      hd::append(tl,L);
val append = fn :
 'a list * 'a list -> 'a list
If we add the pattern
append(L,[]) =L
we get a redundant pattern warning
(Why?)
fun append ([],L)=L
  append(hd::tl,L)=
      hd::append(tl,L)
    append(L,[]) = L;
stdIn:151.1-153.20 Error: match
redundant
          (nil,L) \Rightarrow \dots
          (hd :: tl,L) => ...
    --> (L,nil) => ...
```

But a more precise decomposition is fine:

# Function Types Can be Polytypes

Recall that 'a, 'b, ... represent type variables. That is, any valid type may be substituted for them when checking type correctness.

ML said the type of append is

```
val append = fn :
  'a list * 'a list -> 'a list
```

Why does 'a appear in three places?

We can define eitherNull, a predicate that determines whether either of two lists is null as

```
fun eitherNull(L1,L2) =
  null(L1) orelse null(L2);
val eitherNull =
```

fn : 'a list \* 'b list -> bool

Why are both 'a and 'b used in eitherNull's type?

## Currying

ML chooses the most general (least-restrictive) type possible for user-defined functions.

Functions are first-class objects, as in Scheme.

The function definition

fun f x y = expression; defines a function f (of x) that returns a function (of y).

Reducing multiple argument functions to a sequence of one argument functions is called *currying* (after Haskell Curry, a mathematician who popularized the approach).

#### Thus

```
fun f x y = x :: [y];
val f = fn : 'a -> 'a -> 'a list
says that f takes a parameter x, of
type 'a, and returns a function (of y,
whose type is 'a) that returns a list
of 'a.
```

Contrast this with the more conventional

```
fun g(x,y) = x :: [y];
val g = fn : 'a * 'a -> 'a list
```

Here g takes a pair of arguments (each of type 'a) and returns a value of type 'a list.

The advantage of currying is that we can bind one argument and leave the remaining argument(s) free.

```
For example
```

```
f(1);
```

is a legal call. It returns a function of type

```
fn : int -> int list
```

The function returned is equivalent to

```
fun h b = 1 :: [b];
```

val h = fn : int -> int list

## Map Revisited

ML supports the map function, which can be defined as

This type says that map takes a pair of arguments. One is a function from type 'a to type 'b. The second argument is a list of type 'a. The result is a list of type 'b.

In curried form map is defined as

This type says that map takes one argument that is a function from type 'a to type 'b. It returns a function that takes an argument that is a list of type 'a and returns a list of type 'b.

The advantage of the curried form of map is that we can now use map to create "specialized" functions in which the function that is mapped is fixed.

```
For example,
val neg = map not;
val neg =
  fn : bool list -> bool list
neg [true,false,true];
val it = [false,true,false] :
  bool list
```

### **Power Sets Revisited**

Let's compute power sets in ML.

We want a function **pow** that takes a list of values, viewed as a set, and which returns a list of lists. Each sublist will be one of the possible subsets of the original argument.

For example,

```
pow [1,2] = [[1,2],[1],[2],[]]
```

We first define a version of cons in curried form:

```
fun cons h t = h::t;
val cons = fn :
  'a -> 'a list -> 'a list
```

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Now we define **pow**. We define the powerset of the empty list, [], to be [[]]. That is, the power set of the empty set is set that contains only the empty set.

For a non-empty list, consisting of h::t, we compute the power set of t, which we call pset. Then the power set for h::t is just h distributed through pset appended to pset.

We distribute h through pset very elegantly: we just map the function (cons h) to pset. (cons h) adds h to the head of any list it is given. Thus mapping (cons h) to pset adds h to all lists in pset.

```
The complete definition is simply
fun pow [] = [[]]
    pow (h::t) =
    let
     val pset = pow t
    in
    (map (cons h) pset) @ pset
    end;
val pow =
  fn : 'a list -> 'a list list
Let's trace the computation of
pow [1,2].
Here h = 1 and t = [2]. We need to
compute pow [2].
Now h = 2 and t = [].
We know pow [] = [[]],
S0 pow [2] =
(map (cons 2) [[]])@[[]] =
([[2]])@[[]] = [[2],[]]
```

```
Therefore pow [1,2] =
  (map (cons 1) [[2],[]])
  @[[2],[]] =
  [[1,2],[1]]@[[2],[]] =
  [[1,2],[1],[2],[]]
```

## **Composing Functions**

We can define a composition function that composes two functions into one:

```
fun comp (f,g)(x) = f(g(x));
val comp = fn :
('a -> 'b) * ('c -> 'a) ->
 'c -> 'b
In curried form we have
fun comp f g x = f(g(x));
val comp = fn :
('a -> 'b) ->
('c -> 'a) -> 'c -> 'b
For example,
fun sqr x:int = x*x;
val sqr = fn : int -> int
comp sqr sqr;
val it = fn : int -> int
```

comp sqr sqr 3;

val it = 81 : int

In SMP o (lower-case O) is the infix composition operator.

Hence

 $sqr o sqr \equiv comp sqr sqr$ 

### Lambda Terms

ML needs a notation to write down unnamed (anonymous) functions, similar to the lambda expressions Scheme uses.

```
That notation is
fn arg => body;
For example,
val sqr = fn x:int => x*x;
val sqr = fn : int -> int
In fact the notation used to define
functions,
fun name arg = body;
is actually just an abbreviation for the
more verbose
val name = fn arg => body;
```

An anonymous function can be used wherever a function value is needed.

For example,

## Polymorphism vs. Overloading

ML supports polymorphism.

A function may accept a polytype (a set of types) rather than a single fixed type.

In all cases, the same function definition is used. Details of the supplied type are irrelevant and may be ignored.

```
For example,
fun id x = x;
val id = fn : 'a -> 'a
fun toList x = [x];
val toList = fn : 'a -> 'a list
```

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Overloading, as in C++ and Java, allows alternative definitions of the same method or operator, with selection based on type.

Thus in Java + may represent integer addition, floating point addition or string concatenation, even though these are really rather different operations.

In ML +, -, \* and = are overloaded.

When = is used (to test equality), ML deduces that an *equality type* is required. (Most, but not all, types can be compared for equality).

When ML decides an equality type is needed, it uses a type variable that begins with two tics rather than one.

```
fun eq(x,y) = (x=y);
val eq = fn : ''a * ''a -> bool
```

## Defining New Types in ML

We can create new names for existing types (type abbreviations) using type id = def; For example, type triple = int\*real\*string; type triple = int \* real \* string type rec1= {a:int,b:real,c:string}; type rec1 = {a:int, b:real, c:string} type 'a triple3 = 'a\*'a\*'a; type 'a triple3 = 'a \* 'a \* 'a type intTriple = int triple3; type intTriple = int triple3 These type definitions are essentiality macro-like name substitutions.

## The Datatype Mechanism

New types are defined using the datatype mechanism, which specifies new data value constructors.

For example,

```
datatype color =
  red|blue|green;
datatype color =
  blue | green | red
```

Pattern matching works on userdefined types using their constructors:

```
fun translate red = "rot"
    | translate blue = "blau"
    | translate green = "gruen";
val translate =
  fn : color -> string
```

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#### **SML Examples**

Source code for most of the SML examples presented here may be found in

~cs538-1/public/sml/class.sml

#### Parameterized Constructors

The constructors used to define data types may be parameterized:

```
datatype money =
   none
   | coin of int
   | bill of int
   | iou of real * string;
datatype money =
   bill of int | coin of int
   | iou of real * string | none
```

Now expressions like coin(25) or bill(5) Or iou(10.25, "Andy") represent valid values of type money.

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We can also define values and functions of type money:

```
val dime = coin(10);
val dime = coin 10 : money
val deadbeat =
iou(25.00, "Homer Simpson");
val deadbeat =
 iou (25.0, "Homer Simpson"):
 money
fun amount(none) = 0.0
    amount(coin(cents)) =
     real(cents)/100.0
    amount(bill(dollars)) =
     real(dollars)
    amount(iou(amt,_)) =
     0.5*amt;
 val amount = fn : money -> real
```

#### Polymorphic Datatypes

A user-defined data type may be polymorphic. An excellent example is datatype 'a option =

```
none | some of 'a;
datatype 'a option =
  none | some of 'a
val zilch = none;
val zilch = none : 'a option
val mucho =some(10e10);
val mucho =
some 1000000000000.0 : real option
type studentInfo =
 {name:string,
  ssNumber:int option};
type studentInfo = {name:string,
ssNumber: int option }
```

```
val newStudent =
{name="Mystery Man",
   ssNumber=none}:studentInfo;

val newStudent =
{name="Mystery Man",
   ssNumber=none} : studentInfo
```

#### Datatypes may be Recursive

Recursive datatypes allow linked structures *without* explicit pointers.

```
datatype binTree =
  null
| leaf
| node of binTree * binTree;
datatype binTree =
  leaf | node of binTree * binTree
  | null

fun size(null) = 0
  | size(leaf) = 1
  | size(node(t1,t2)) =
       size(t1)+size(t2) + 1

val size = fn : binTree -> int
```

# Recursive Datatypes may be Polymorphic

```
datatype 'a binTree =
   null
| leaf of 'a
| node of 'a binTree * 'a binTree
datatype 'a binTree =
  leaf of 'a |
  node of 'a binTree * 'a binTree
  | null
fun frontier(null) = []
  | frontier(leaf(v)) = [v]
  | frontier(node(t1,t2)) =
     frontier(t1) @ frontier(t2)
val frontier =
  fn : 'a binTree -> 'a list
```

We can model n-ary trees by using lists of subtrees:

```
datatype 'a Tree =
  null
  leaf of 'a
  node of 'a Tree list;
datatype 'a Tree = leaf of 'a
node of 'a Tree list | null
fun frontier(null) = []
    frontier(leaf(v)) = [v]
    frontier(node(h::t)) =
      frontier(h) @
      frontier(node(t))
   frontier(node([])) = []
val frontier = fn :
 'a Tree -> 'a list
```

## **Abstract Data Types**

ML also provides abstract data types in which the implementation of the type is *hidden* from users.

The general form is

abstype name = implementation with

val and fun definitions
end;

Users may access the name of the abstract type and the val and fun definitions that follow the with, but the implementation may be used only with the body of the abstype definition.

#### **Example**

```
abstype 'a stack =
 stk of 'a list
with
  val Null = stk([])
  fun empty(stk([])) = true
     empty(stk(_::_)) = false
  fun top(stk(h::_)) = h
  fun pop(stk(::t)) = stk(t)
  fun push(v,stk(L)) =
   stk(v::L)
end
type 'a stack
val Null = - : 'a stack
val empty = fn : 'a stack -> bool
val top = fn : 'a stack -> 'a
val pop =
  fn : 'a stack -> 'a stack
val push = fn :
  'a * 'a stack -> 'a stack
```

Local value and function definitions, not to be exported to users of the type can be created using the local definition mechanism described earlier:

```
local
    val and fun definitions
in
    exported definitions
end;
```

```
abstype 'a stack =
 stk of 'a list
with
 local
  fun size(stk(L))=length(L);
 in
  val Null = stk([])
  fun empty(s) =
    (size(s) = 0)
  fun top(stk(h::_)) = h
  fun pop(stk(_::t)) = stk(t)
  fun push(v,stk(L)) =
   stk(v::L)
 end
end
type 'a stack
val Null = - : 'a stack
val empty = fn : 'a stack -> bool
val top = fn : 'a stack -> 'a
val pop = fn :
 'a stack -> 'a stack
val push = fn :
 'a * 'a stack -> 'a stack
```

Why are abstract data types useful?

Because they hide an implementation of a type from a user, allowing implementation changes without any impact on user programs.

Consider a simple implementation of queues:

```
abstype 'a queue =
  q of 'a list
with
  val Null = q([])
  fun front(q(h::_)) = h
  fun rm(q(_::t)) = q(t)
  fun enter(v,q(L)) =
      q(rev(v::rev(L)))
end
type 'a queue
val Null = - : 'a queue
val front = fn : 'a queue -> 'a
```

```
val rm =
  fn : 'a queue -> 'a queue
val enter =
  fn : 'a * 'a queue -> 'a queue
```

This implementation of queues is valid, but somewhat inefficient. In particular to enter a new value onto the rear end of a queue, we do the following:

```
fun enter(v,q(L)) =
  q(rev(v::rev(L)))
```

We reverse the list that implements the queue, add the new value to the head of the reversed queue *then* reverse the list a second time.

A more efficient (but less obvious) implementation of a queue is to store it as two lists. One list represents the "front" of the queue. It is from this list that we extract the front value, and from which we remove elements.

The other list represents the "back" of the queue (in reversed order). We add elements to the rear of the queue by adding elements to the front of the list. From time to time, when the front list becomes null, we "promote" the rear list into the front list (by reversing it). Now access to both the front and the back of the queue is fast and direct. The new implementation is:

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```
abstype 'a queue =
  q of 'a list * 'a list
with
  val Null = q([],[])
  fun front(q(h::_{,})) = h
     front(q([],L)) =
        front(q(rev(L),[]))
  fun rm(q(::t,L)) = q(t,L)
      rm(q([],L)) =
        rm(q(rev(L),[]))
  fun enter(v,q(L1,L2)) =
     q(L1,v::L2)
end
type 'a queue
val Null = - : 'a queue
val front = fn :
  'a queue -> 'a
val rm = fn :
 'a queue -> 'a queue
val enter = fn :
 'a * 'a queue -> 'a queue
```

From the user's point of view, the two implementations are *identical* (they export exactly the same set of values and functions). Hence the new implementation can replace the old implementation without any impact at all to the user (except, of course, performance!).

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## **Exception Handling**

Our definitions of stacks and queues are incomplete. Reconsider our definition of stack:

```
abstype 'a stack =
 stk of 'a list
with
  val Null = stk([])
  fun empty(stk([])) = true
     empty(stk(_::_)) = false
  fun top(stk(h::_)) = h
  fun pop(stk(_::t)) = stk(t)
  fun push(v,stk(L)) =
   stk(v::L)
end
What happens if we evaluate
top(Null);
We get a "match failure" because our
definition of top is incomplete!
```

In ML we can *raise* an exception if an illegal or unexpected operation occurs. Asking for the top of an empty stack ought to raise an exception since the requested value does not exist.

ML contains a number of predefined exceptions, including

Match Empty Div Overflow (exception names by convention begin with a capital letter).

Predefined exception are raised by illegal values or operations. If they are not caught, the run-time system prints an error message.

```
fun f(1) = 2;
val f = fn : int -> int
f(2);
uncaught exception nonexhaustive
match failure
hd [];
uncaught exception Empty
1000000*1000000;
uncaught exception overflow
(1 div 0);
uncaught exception divide by zero
1.0/0.0;
val it = inf : real
(inf is the IEEE floating-point
standard "infinity" value)
```

#### **User Defined Exceptions**

```
New exceptions may be defined as exception name;
Or
exception name of type;
For example
exception IsZero;
exception IsZero
exception NegValue of real;
exception NegValue of real;
```

#### **Exceptions May be Raised**

The raise statement raises (throws) an exception: raise exceptionName; or raise exceptionName(expr); For example fun divide(a,0) = raise IsZero | divide(a,b) = a div b; val divide = fn : int \* int -> int divide(10,3); val it = 3 : int divide(10,0); uncaught exception IsZero

```
val sqrt = Real.Math.sqrt;
val sqrt = fn : real -> real
fun sqroot(x) =
  if x < 0.0
  then raise NegValue(x)
  else sqrt(x);
val sqroot = fn : real -> real
sqroot(2.0);
val it = 1.41421356237 : real
sqroot(~2.0);
uncaught exception NegValue
```

#### **Exception Handlers**

You may catch an exception by defining a *handler* for it:

#### Stacks Revisited

end

We can add an exception, Emptystk, to our earlier stack type to handle top or pop operations on an empty stack:

```
type 'a stack
val Null = - : 'a stack
exception EmptyStk
val empty = fn : 'a stack -> bool
val top = fn : 'a stack -> 'a
val pop = fn :
   'a stack -> 'a stack
val push = fn : 'a * 'a stack ->
'a stack

pop(Null);
uncaught exception EmptyStk
top(Null) handle EmptyStk => 0;
val it = 0 : int
```

## **User-Defined Operators**

SML allows users to define symbolic operators composed of non-alphanumeric characters. This means operator-like symbols can be created and used. Care must be taken to avoid predefined operators (like +, -, ^, @, etc.).

If we wish, we can redo our stack definition using symbols rather than identifiers.

We might choose the following symbols:

```
top |=
pop <==
push ==>
null <@>
empty <?>
```

Now we can have expressions like

```
<?> <@>;
val it = true : bool
|= (==> (1,<@>));
val it = 1 : int
```

Binary functions, like ==> (push) are much more readable if they are infix. That is, we'd like to be able to write

```
1 ==> 2+3 ==> <@>
```

which pushes 2+3, then 1 onto an empty stack.

To make a function (either identifier or symbolic) infix rather than prefix we use the definition

```
infix level name
Or
infixr level name
```

level is an integer representing the "precedence" level of the infix operator. o is the lowest precedence level; higher precedence operators are applied before lower precedence operators (in the absence of explicit parentheses).

infix defines a left-associative
operator (groups from left to right).
infixr defines a right-associative
operator (groups from right to left).

Thus

```
fun cat(L1,L2) = L1 @ L2;
infix 5 cat
```

makes cat a left associative infix operator at the same precedence level as @. We can now write

```
[1,2] cat [3,4,5] cat [6,7];
val it = [1,2,3,4,5,6,7] : int list
```

The standard predefined operators have the following precedence levels:

Level Operator

will work as expected, evaluating expressions like 2+3 before doing any pushes, with pushes done right to left.

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```
abstype 'a stack =
  stk of 'a list
with
   val <@> = stk([])
   exception emptyStk
   fun <?>(stk([])) = true
      <?>(stk(_::_)) = false
   fun |=(stk(h::_)) = h
    raise emptyStk
   fun <==(stk(::t)) = stk(t)</pre>
    <==(stk([])) =
          raise emptyStk
   fun ==>(v,stk(L)) =
           stk(v::L)
   infixr 2 ==>
end
```

```
type 'a stack
val <@> = - : 'a stack
exception emptyStk
val <?> = fn : 'a stack -> bool
val |= = fn : 'a stack -> 'a
val <== = fn :</pre>
  'a stack -> 'a stack
val ==> = fn : 'a * 'a stack ->
'a stack
infixr 2 ==>
Now we can write
val myStack =
 1 ==> 2+3 ==> <@>;
val myStack = - : int stack
= myStack;
val it = 1 : int
|= (<== myStack);
val it = 5 : int
```

## Using Infix Operators as Values

Sometimes we simply want to use an infix operator as a symbol whose value is a function.

For example, given

```
fun dupl f v = f(v,v);
val dupl =
  fn : ('a * 'a -> 'b) -> 'a -> 'b
we might try the call
dupl ^ "abc";
```

This fails because SML tries to parse dupl and "abc" as the operands of ^.

To pass an operator as an ordinary function value, we prefix it with op which tells the SML compiler that the following symbol is an infix operator.

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# Thus dupl op ^ "abc"; val it = "abcabc" : string works fine.

### The Case Expression

ML contains a case expression patterned on switch and case statements found in other languages.

As in function definitions, patterns are used to choose among a variety of values.

The general form of the case is

```
case expr of
  pattern<sub>1</sub> => expr<sub>1</sub>|
  pattern<sub>n</sub> => expr<sub>2</sub>|
   ...
  pattern<sub>n</sub> => expr<sub>n</sub>;
```

If no pattern matches, a Match exception is thrown.

It is common to use \_ (the wildcard) as the last pattern in a case.

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#### Examples include

```
case c of
 red => "rot" |
blue => "blau"
green => "gruen";
case pair of
 (1,_) => "win" |
 (2,_) => "place" |
 (3,_) => "show"
 ( , ) => "loser";
case intOption of
none => 0
 some(v) => v;
```

## Imperative Features of ML

ML provides references to heap locations that may be updated. This is essentially the same as access to heap objects via references (Java) or pointers (C and C++).

The expression

```
ref val
```

creates a reference to a heap location initialized to val. For example,

```
ref 0;
val it = ref 0 : int ref
```

The prefix operator! fetches the value contained in a heap location (just as \* dereferences a pointer in C or C++).

Thus

```
! (ref 0);
val it = 0 : int
```

### The expression

ref := val

```
updates the heap location referenced by ref to contain val. The unit value, (), is returned.
```

#### Hence

```
val x = ref 0;
val x = ref 0 : int ref
!x;
val it = 0 : int
x:=1;
val it = () : unit
!x;
val it = 1 : int
```

## Sequential Composition

Expressions or statements are sequenced using ";". Hence

```
val a = (1+2;3+4);
val a = 7 : int
(x:=1;!x);
val it = 1 : int
```

### **Iteration**

```
while expr1 do expr2
implements iteration (and returns
unit); Thus
(while false do 10);
val it = () : unit
while !x > 0 do x:= !x-1;
val it = () : unit
!x;
val it = 0 : int
```

# Simple I/O

```
The function
 print;
 val it = fn : string -> unit
prints a string onto standard output.
For example,
print("Hello World\n");
 Hello World
The conversion routines
 Real.toString;
 val it = fn : real -> string
 Int.toString;
 val it = fn : int -> string
 Bool.toString;
 val it = fn : bool -> string
convert a value (real, int or bool)
into a string. Unlike Java, the call
must be explicit.
```

```
For example,
print(Int.toString(123));
123
Also available are
Real.fromString;
val it = fn : string -> real
option
Int.fromString;
val it = fn : string -> int
option
Bool.fromString;
val it = fn : string -> bool
option
which convert from a string to a
real Or int Or bool if possible.
(That's why the option type is used).
```

```
For example,
case (Int.fromString("123"))
  of
   SOME(i) => i | NONE => 0;
val it = 123 : int
case (Int.fromString(
        "One two three")) of
   SOME(i) => i | NONE => 0;
val it = 0 : int
```

### Text I/O

The structure **TextIO** contains a wide variety of I/O types, values and functions. You load these by entering:

open TextIO;

Among the values loaded are

- type instream
  This is the type that represents input text files.
- type outstream
   This is the type that represents output text files.
- type vector = string
   Makes vector a synonym for string.
- type elem = char
   Makes elem a synonym for char.

val stdIn : instream
 val stdOut : outstream
 val stdErr : outstream
 Predefined input and output streams.

• val openIn :
 string -> instream
 val openOut :
 string -> outstream
 Open an input or output stream.
 For example,
 val out =
 openOut("/tmp/test1");
 val out = - : outstream

• val input :
 instream -> vector
Read a line of input into a string
 (vector is defined as equivalent to
 string). For example (user input is
 in red):

```
val s = input(stdIn);
 Hello!
  val s = "Hello!\n" : vector
val inputN :
  instream * int -> vector
 Read the next n input characters into
 a string. For example,
 val t = inputN(stdIn,3);
 abcde
 val t = "abc" : vector
val inputAll:
  instream -> vector
 Read the rest of the input file into a
 string (with newlines separating
 lines). For example,
 val u = inputAll(stdIn);
  Four score and
  seven years ago ...
  val u = "Four score and\nseven
  years ago ...\n" : vector
```

- val endOfStream :
   instream -> bool
  Are we at the end of this input
  stream?
- val output :
   outstream \* vector -> unit
  Output a string on the specified
   output stream. For example,
   output(stdOut,
   "That's all folks!\n");
  That's all folks!

# **String Operations**

ML provides a wide variety of string manipulation routines. Included are:

- The string concatenation operator, ^"abc" ^ "def" = "abcdef"
- The standard 6 relational operators:

```
< > <= >= = <>
```

• The string size operator:

```
val size : string -> int
size ("abcd");
val it = 4 : int
```

• The string subscripting operator (indexing from 0):

```
val sub =
  fn : string * int -> char
sub("abcde",2);
val it = #"c" : char
```

• The substring function
val substring:
string \* int \* int -> string
This function is called as
substring(string,start,len)
start is the starting position,
counting from 0.
len is the length of the desired
substring. For example,
substring("abcdefghij",3,4)
val it = "defg": string

 Concatenation of a list of strings into a single string:

```
concat :
  string list -> string
For example,
concat ["What's"," up","?"];
val it = "What's up?" : string
```

Convert a character into a string:

```
str : char -> string
For example,
  str(#"x");
val it = "x" : string
```

 "Explode" a string into a list of characters:

```
explode : string -> char list
For example,
explode("abcde");
val it =
[#"a",#"b",#"c",#"d",#"e"] :
char list
```

 "Implode" a list of characters into a string.

```
implode : char list -> string
For example,
implode
[#"a",#"b",#"c",#"d",#"e"];
val it = "abcde" : string
```

## Structures and Signatures

In C++ and Java you can group variable and function definitions into classes. In Java you can also group classes into packages.

In ML you can group value, exception and function definitions into structures.

You can then import selected definitions from the structure (using the notation structure.name) or you can open the structure, thereby importing all the definitions within the structure.

(Examples used in this section may be found at

~cs538-1/public/sml/struct.sml)

```
The general form of a structure
definition is
structure name =
struct
  val, exception and
  fun definitions
end
For example,
structure Mapping =
struct
  exception NotFound;
  val create = [];
  fun lookup(key,[]) =
      raise NotFound
      lookup(key,
            (key1,value1)::rest) =
      if key = key1
      then value1
      else lookup(key,rest);
```

```
fun insert(key,value,[]) =
                 [(key, value)]
      insert(key, value,
         (key1,value1)::rest) =
      if key = key1
      then (key, value)::rest
      else (key1,value1)::
            insert(key, value, rest);
end;
We can access members of this
structure as Mapping.name. Thus
Mapping.insert(538, "languages",[]);
val it = [(538,"languages")] :
(int * string) list
open Mapping;
exception NotFound
val create : 'a list
val insert : ''a * 'b * (''a * 'b)
 list -> (''a * 'b) list
val lookup : ''a * (''a * 'b)
 list -> 'b
```

## **Signatures**

Each structure has a *signature*, which is it type.

For example, Mapping's signature is

```
structure Mapping :
    sig
    exception NotFound
    val create : 'a list
    val insert : ''a * 'b *
        (''a * 'b) list ->
        (''a * 'b) list
    val lookup : ''a *
        (''a * 'b) list -> 'b
    end
```

```
You can define a signature as
signature name = sig
  type definitions for values,
    functions and exceptions
end
For example,
signature Str2IntMapping =
sig
  exception NotFound;
val lookup:
    string * (string*int) list
    -> int;
end;
```

### Signatures can be used to

- Restrict the type of a value or function in a structure.
- Hide selected definitions that appear in a structure

For example

```
structure Str2IntMap :
   Str2IntMapping = Mapping;
```

defines a new structure, str2IntMap, created by restricting Mapping to the str2IntMapping signature. When we do this we get

```
open Str2IntMap;
```

```
exception NotFound
val lookup : string *
  (string * int) list -> int
```

Only lookup and NotFound are created, and lookup is limited to keys that are strings.

# Extending ML's Polymorphism

In languages like C++ and Java we must use types like void\* or object to simulate the polymorphism that ML provides. In ML whenever possible a general type (a polytype) is used rather than a fixed type. Thus in

```
fun len([]) = 0
    | len(a::b) = 1 + len(b);
we get a type of
'a list -> int
```

because this is the most general type possible that is consistent with len's definition.

Is this form of polymorphism general enough to capture the general idea of making program definitions as type-independent as possible?

It isn't, and to see why consider the following ML definition of a merge sort. A merge sort operates by first splitting a list into two equal length sublists. The following function does this:

After the input list is split into two halves, each half is recursively sorted, then the sorted halves are merged together into a single list.

The following ML function merges two sorted lists into one:

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```
fun merge([],[]) = []
    merge([],hd::tl) = hd::tl
    merge(hd::tl,[]) = hd::tl
    merge(hd::tl,h::t) =
    if hd <= h
    then hd::merge(tl,h::t)
    else h::merge(hd::tl,t)
With these two subroutines, a
definition of a sort is easy:
fun sort [] = []
    sort([a]) = [a]
    sort(a::b::rest) =
    let val (left,right)
       split(a::b::rest) in
      merge(sort(left),
            sort(right))
    end;
```

This definition looks very general—it should work for a list of any type.

Unfortunately, when ML types the functions we get a surprise:

```
val split = fn : 'a list ->
  'a list * 'a list

val merge = fn : int list *
  int list -> int list

val sort = fn :
  int list -> int list
```

split is polymorphic, but merge and sort are limited to integer lists!

Where did this restriction come from?

The problem is that we did a comparison in merge using the <= operator, and ML typed this as an integer comparison.

We can make our definition of sort more general by adding a comparison function, le(a,b) as a parameter to merge and sort. If we curry this parameter we may be able to hide it from end users. Our updated definitions are:

```
fun merge(le,[],[]) = []
    | merge(le,[],hd::tl) = hd::tl
    | merge(le,hd::tl,[]) = hd::tl
    | merge(le,hd::tl,h::t) =
        if le(hd,h)
        then hd::merge(le,tl,h::t)
        else h::merge(le,hd::tl,t)
```

```
fun sort le [] = []
    sort le [a] = [a]
    sort le (a::b::rest) =
     let val (left,right) =
       split(a::b::rest) in
         merge(le, sort le left,
                    sort le right)
     end;
Now the types of merge and sort
are:
val merge = fn :
 ('a * 'a -> bool) *
  'a list * 'a list -> 'a list
val sort = fn : ('a * 'a -> bool)
      -> 'a list -> 'a list
We can now "customize" sort by
choosing a particular definition for
the le parameter:
fun le(a,b) = a <= b;
```

val le = fn : int \* int -> bool

```
fun intsort L = sort le L;
val intsort =
  fn : int list -> int list
intsort(
 [4,9,0,2,111,~22,8,~123]);
val it = [~123,~22,0,2,4,8,9,111]
: int list
fun strle(a:string,b) =
  a <= b;
val strle =
  fn : string * string -> bool
fun strsort L = sort strle L;
val strsort =
 fn : string list -> string list
strsort(
 ["aac", "aaa", "ABC", "123"]);
val it =
["123","ABC","aaa","aac"] :
string list
```

Making the comparison relation an explicit parameter works, but it is a bit ugly and inefficient. Moreover, if we have several functions that depend on the comparison relation, we need to ensure that they all use the same relation. Thus if we wish to define a predicate inorder that tests if a list is already sorted, we can use:

```
fun inOrder le [] = true
  | inOrder le [a] = true
  | inOrder le (a::b::rest) =
      le(a,b) andalso
      inOrder le (b::rest);
val inOrder = fn :
  ('a * 'a -> bool) -> 'a list ->
      bool
```

Now sort and inorder need to use the same definition of le. But how can we enforce this?

The structure mechanism we studied earlier can help. We can put a single definition of le in the structure, and share it:

```
structure Sorting =
struct
  fun le(a,b) = a <= b;
  fun split [] = ([],[])
      split [a] = ([a],[])
     split (a::b::rest) =
      let val (left,right) =
        split rest in
         (a::left,b::right)
      end:
  fun merge([],[]) = []
      merge([],hd::tl) = hd::tl
      merge(hd::tl,[]) = hd::tl
      merge(hd::tl,h::t) =
      if le(hd,h)
      then hd::merge(tl,h::t)
      else h::merge(hd::tl,t)
```

```
fun sort [] = []
      sort([a]) = [a]
     sort(a::b::rest) =
      let val (left,right) =
        split(a::b::rest) in
         merge(sort(left),
               sort(right))
      end;
  fun inOrder [] = true
      inOrder [a] = true
      inOrder (a::b::rest) =
       le(a,b) andalso
        inOrder (b::rest);
end;
structure Sorting :
 siq
  val inOrder : int list -> bool
   val le : int * int -> bool
   val merge : int list *
     int list -> int list
    val sort:
      int list -> int list
```

```
val split : 'a list ->
  'a list * 'a list
end
```

To sort a type other than integers, we replace the definition of le in the structure.

But rather than actually edit that definition, ML gives us a powerful mechanism to parameterize a structure. This is the *functor*, which allows us to use one or more structures as parameters in the definition of a structure.

#### **Functors**

The general form of a functor is

```
functor name
  (structName:signature) =
    structure definition;
```

This functor will create a specific version of the structure definition using the structure parameter passed to it.

For our purposes this is ideal—we pass in a structure defining an ordering relation (the le function). This then creates a custom version of all the functions defined in the structure body, using the specific le definition provided.

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```
We first define
signature Order =
sig
  type elem
  val le : elem*elem -> bool
end;
This defines the type of a structure
that defines a le predicate defined on
a pair of types called elem.
An example of such a structure is
structure IntOrder:Order =
struct
  type elem = int;
  fun le(a,b) = a <= b;
end;
Now we just define a functor that
creates a sorting structure based on
an order structure:
```

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```
functor MakeSorting(0:Order) =
struct
 open O; (* makes le available*)
  fun split [] = ([],[])
      split [a] = ([a],[])
     split (a::b::rest) =
      let val (left,right) =
        split rest in
         (a::left,b::right)
      end:
  fun merge([],[]) = []
      merge([],hd::tl) = hd::tl
      merge(hd::tl,[]) = hd::tl
      merge(hd::tl,h::t) =
      if le(hd,h)
      then hd::merge(tl,h::t)
      else h::merge(hd::tl,t)
```

```
Now
```

```
structure IntSorting =
 MakeSorting(IntOrder);
creates a custom structure for sorting
integers:
 IntSorting.sort [3,0,~22,8];
 val it = [~22,0,3,8] : elem list
To sort strings, we just define a
structure containing an le defined
for strings with order as its
signature (i.e., type) and pass it to
MakeSorting:
structure StrOrder:Order =
struct
  type elem = string
  fun le(a:string,b) = a <= b;</pre>
end;
```

```
structure StrSorting =
  MakeSorting(StrOrder);
StrSorting.sort(
 ["cc", "abc", "xyz"]);
val it = ["abc","cc","xyz"] :
 StrOrder.elem list
StrSorting.inOrder(
 ["cc", "abc", "xyz"]);
val it = false : bool
StrSorting.inOrder(
 [3,0,~22,8]);
stdIn:593.1-593.32 Error:
operator and operand don't agree
[literal]
 operator domain: strOrder.elem
list
                   int list
  operand:
  in expression:
   StrSorting.inOrder (3 :: 0 ::
~22 :: <exp> :: <exp>)
```

# The SML Basis Library

SML provides a wide variety of useful types and functions, grouped into structures, that are included in the *Basis Library*.

A web page fully documenting the Basis Library is linked from the ML page that is part of the Programming Languages Links page on the CS 538 home page.

Many useful types, operators and functions are "preloaded" when you start the SML compiler. These are listed in the "Top-level Environment" section of the Basis Library documentation.

Many other useful definitions must be explicitly fetched from the structures they are defined in.

For example, the Math structure contains a number of useful mathematical values and operations.

You may simply enter

```
open Math;
```

while will load all the definitions in Math. Doing this may load more definitions than you want. What's worse, a definition loaded may redefine a definition you currently want to stay active. (Recall that ML has virtually no overloading, so functions with the same name in different structures are common.)

A more selective way to access a definition is to qualify it with the structure's name. Hence

```
Math.pi;
val it = 3.14159265359 : real
```

gets the value of pi defined in Math. Should you tire of repeatedly qualifying a name, you can (of course) define a local value to hold its value. Thus

```
val pi = Math.pi;
val pi = 3.14159265359 : real
works fine.
```

# An Overview of Structures in the Basis Library

The Basis Library contains a wide variety of useful structures. Here is an overview of some of the most important ones.

## • Option

Operations for the option type.

## Bool

Operations for the **bool** type.

## Char

Operations for the **char** type.

## String

Operations for the string type.

## Byte

Operations for the **byte** type.

### Int

Operations for the **int** type.

## IntInf

Operations for an unbounded precision integer type.

## Real

Operations for the **real** type.

### Math

Various mathematical values and operations.

## • List

Operations for the list type.

## ListPair

Operations on pairs of lists.

#### Vector

A polymorphic type for immutable (unchangeable) sequences.

 IntVector, RealVector, BoolVector, CharVector

Monomorphic types for immutable sequences.

## • Array

A polymorphic type for mutable (changeable) sequences.

 IntArray, RealArray, BoolArray, CharArray

Monomorphic types for mutable sequences.

Array2

A polymorphic 2 dimensional mutable type.

• IntArray2, RealArray2, BoolArray2, CharArray2

Monomorphic 2 dimensional mutable types.

• TextIO

Character-oriented text IO.

• BinIO

Binary IO operations.

• OS, Unix, Date, Time, Timer
Operating systems types and operations.

# ML Type Inference

One of the most novel aspects of ML is the fact that it infers types for all user declarations.

How does this type inference mechanism work?

Essentially, the ML compiler creates an unknown type for each declaration the user makes. It then solves for these unknowns using known types and a set of type inference rules. That is, for a user-defined identifier i, ML wants to determine  $\tau(i)$ , the type of i.

## The type inference rules are:

1. The types of all predefined literals, constants and functions are known in advance. They may be looked-up and used. For example,

```
2 : int
true : bool
[] : 'a list
:: : 'a * 'a list -> 'a list
```

2. All occurrences of the same symbol (using scoping rules) have the same type.

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3. In the expression

```
I = J
we know T(I) = T(J).
```

4. In a conditional

```
(if E1 then E2 else E3)
We know that
T(E1) = bool,
T(E2) = T(E3) = T(conditional)
```

5. In a function call

(f 
$$x$$
)

We know that if  $T(f) = a - b$ 

then  $T(x) = a$  and  $T(f(x)) = b$ 

6. In a function definition

```
fun f x = expr;
if t(x) = 'a and T(expr) = 'b
then T(f) = 'a -> 'b
```

7. In a tuple  $(e_1, e_2, \ldots, e_n)$  if we know that  $T(e_i) = 'a_i \ 1 \le i \le n$  then  $T(e_1, e_2, \ldots, e_n) = 'a_1 * 'a_2 * \ldots * 'a_n$ 

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8. In a record

```
{ a=e_1,b=e_2, \dots }
if T(e_i) = 'a_i 1 \le i \le n then
the type of the record =
{a:'a<sub>1</sub>, b:'a<sub>2</sub>, ...}
```

9. In a list  $[v_1, v_2, \dots v_n]$  if we know that  $\mathbf{T}(v_i) = \mathbf{a}_i \quad 1 \le i \le n$  then we know that

$$a_1=a_2=\ldots=a_n$$
 and 
$$T([v_1,v_2,\ldots,v_n])=a_1$$
 list

# To Solve for Types:

- 1. Assign each untyped symbol its own distinct type variable.
- 2. Use rules (1) to (9) to solve for and simplify unknown types.
- 3. Verify that each solution "works" (causes no type errors) throughout the program.

## **Examples**

```
Consider
fun fact(n)=
   if n=1 then 1 else n*fact(n-1);
To begin, we'll assign type variables:
T(fact) = 'a -> 'b
(fact is a function)
T(n) = 'c
```

Now we begin to solve for the types 'a, 'b and 'c must represent.

We know (rule 5) that 'c = 'a since n is the argument of fact.

We know (rule 3) that c = T(1) = int since n=1 is part of the definition.

We know (rule 4) that  $\tau(1) = \tau(ifexpression) = be since the ifexpression is the body of fact.$ 

Thus, we have

These types are correct for all occurrences of fact and n in the definition.

# A Polymorphic Function:

```
fun leng(L) =
 if L = []
 then 0
 else 1+len(tl L);
To begin, we know that
T([]) = 'a list and
T(tl) = 'b list -> 'b list
We assign types to leng and L:
T(leng) = 'c -> 'd
T(L) = 'e
Since L is the argument of leng,
'e = 'c
From the expression L=[] we know
'e = 'a list
```

From the fact that o is the result of the then, we know the if returns an int, SO 'd = int.

Thus T(leng) = 'a list -> int and
T(L) = 'a list

These solutions are type correct throughout the definition.

# Type Inference for Patterns

Type inference works for patterns too.

Consider fun leng [] = 0leng (a::b) = 1 + leng b; We first create type variables: T(leng) = 'a -> 'bT(a) = 'cT(b) = 'dFrom leng [] we conclude that 'a = 'e list From leng [] = 0 we conclude that b = intFrom leng (a::b) we conclude that 'c ='e and 'd = 'e list Thus we have T(leng) = 'e list -> int

T(a) = 'e

T(b) = 'e list

This solution is type correct throughout the definition.

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# Not Everything can be Automatically Typed in ML

Let's try to type

fun f x = (x x);

We assume

T(f) = 'a -> 'b

t(x) = 'c

Now (as usual)  $\cdot a = \cdot c$  since x is the argument of f.

From the call (x x) we conclude that 'c must be of the form 'd -> 'e (since x is being used as a function).

Moreover, 'c = 'd since x is an argument in (x x).

Thus 'c = 'd ->'e = 'c ->'e.

But 'c = 'c->'e has no solution, so in ML this definition is invalid. We

can't pass a function to itself as an argument—the type system doesn't allow it.

In Scheme this is allowed:

(define (f x) (x x))

but a call like

(f f)

certainly doesn't do anything good!

# **Type Unions**

Let's try to type

fun f g = ((g 3), (g true));

Now the type of g is 'a -> 'b since g is used as a function.

The call (g 3) says 'a = int and the call (g true) says 'a = boolean.

Does this mean g is polymorphic?

That is, is the type of £

NO!

All functions have the type 'a -> 'b but not all functions can be passed to £.

Consider not: bool->bool.

The call (not 3) is certainly illegal.

What we'd like in this case is a *union* type. That is, we'd like to be able to type g as (int|bool)-> b which ML doesn't allow.

Fortunately, ML does allow type constructors, which are just what we need.

Given

```
datatype T =
   I of int|B of bool;
we can redefine f as
fun f g =
   (g (I(3)), g (B(true)));
val f = fn : (T -> 'a) -> 'a * 'a
```

```
Finally, note that in a definition like
let
  val f =
    fn x => x (* id function*)
in (f 3,f true)
end;
type inference works fine:
val it = (3,true) : int * bool
Here we define f in advance, so its type is known when calls to it are seen.
```

# Reading Assignment

• Sethi: Chapter 11

• Scott: Section 11.3

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# **Prolog**

Prolog presents a view of programming that is very different from most other programming languages.

A famous text book is entitled

"Algorithms + Data Structures = Programs"

This formula represents well the conventional approach to programming that most programming languages support.

In Prolog there is an alternative rule of programming:

"Algorithms = Logic + Control"

This rule encompasses a nonprocedural view of programming.

Logic (what the program is to compute) comes first.

Then control (how to implement the logic) is considered.

In Prolog we program the logic of a program, but the Prolog system *automatically* implements the control.

Logic is essential—control is just efficiency.

# Logic Programming

Prolog implements logic programming.

In fact Prolog means Programming in Logic.

In Prolog programs are statements of rules and facts.

Program execution is deduction—can an answer be inferred from known rules and facts.

Prolog was developed in 1972 by Kowalski and Colmerauer at the University of Marseilles.

# **Elementary Data Objects**

- In Prolog *integers* and *atoms* are the elementary data objects.
- Integers are ordinary integer literals and values.
- Atoms are identifiers that begin with a lower-case letter (much like symbolic values in Scheme).
- In Prolog data objects are called terms.
- In Prolog we define relations among terms (integers, atoms or other terms).
- A predicate names a relation.
   Predicates begin with lower-case letters.
- To define a predicate, we write clauses that define the relation.

- There are two kinds of program clauses, facts and rules.
- A fact is a predicate that prefixes a sequence of terms, and which ends with a period (".").

As an example, consider the following facts which define "fatherof" and "motherof" relations.

```
fatherOf(tom,dick).
fatherOf(dick,harry).
fatherOf(jane,harry).
motherOf(tom,judy).
motherOf(dick,mary).
motherOf(jane,mary).
```

The symbols fatherof and motherof are predicates. The symbols tom, dick, harry, judy, mary and jane are atoms.

Once we have entered rules and facts that define relations, we can make queries (ask the Prolog system questions).

Prolog has two interactive modes that you can switch between.

To enter definition mode (to define rules and facts) you enter

[user].

You then enter facts and rules, terminating this phase with ^D (end of file).

Alternatively, you can enter

['filename'].

to read in rules and facts stored in the file named **filename**.

When you start Prolog, or after you leave definitions mode, you are in query mode.

In query mode you see a prompt of the form

| ?- or ?- (depending on the system you are running).

In query mode, Prolog allows you to ask whether a relation among terms is *true* or *false*.

Thus given our definition of motherof and fatherof relations, we can ask:

| ?- fatherOf(tom,dick).
yes

A "yes" response means that Prolog is able to conclude from the facts and rules it has been given that the relation queried does hold.

# | ?- fatherOf(georgeW,george). no

A "no" response to a query means that Prolog is unable to conclude that the relation holds from what it has been told. The relation may actually be true, but Prolog may lack necessary facts or rules to deduce this.

## Variables in Queries

One of the attractive features of Prolog is the fact that *variables* may be included in queries. A variable always begins with a capital letter.

When a variable is seen, Prolog tries to find a value (binding) for the variable that will make the queried relation true.

For example,

fatherOf(X,harry).

asks Prolog to find an value for x such that x's father is harry.

When we enter the query, Prolog gives us a solution (if one can be found):

?- fatherOf(X,harry).

X = dick

If no solution can be found, it tells us so:

```
| ?- fatherOf(Y, jane).
```

Since solutions to queries need not be unique, Prolog will give us alternate solutions if we ask for them. We do so by entering a ";" after a solution is printed. We get a "no" when no more solutions can be found:

```
| ?- fatherOf(X,harry).
X = dick;
X = jane;
no
```

Variables may be placed anywhere in a query. Thus we may ask

```
| ?- fatherOf(jane,X).
X = harry;
no
```

We may use more than one variable if we wish:

```
| ?- fatherOf(X,Y).
X = tom,
Y = dick;
X = dick,
Y = harry;
X = jane,
Y = harry;
no
```

(This query displays all the fatherOf relations).

# Conjunction of Goals

More than one relation can be included as the "goal" of a query. A comma (",") is used as an AND operator to indicate a conjunction of goals—all must be satisfied by a solution to the query.

```
| ?-
fatherOf(jane,X),motherOf(jane,Y).
X = harry,
Y = mary;
no
```

A given variable may appear more than once in a query. The same value of the variable must be used in all places in which the variable appears (this is called *unification*).

```
For example,
| ?-
fatherOf(tom,X),fatherOf(X,harry).
X = dick ;
no
```

### Rules in Prolog

Rules allow us to state that a relation will hold depending on the truth (correctness) of other relations.

In effect a rules says,

"If I know that certain relations hold, then I also know that this relation holds."

A rule in Prolog is of the form  $rel_1 := rel_2$ ,  $rel_3$ , ...  $rel_n$ .

This says  $rel_1$  can be assumed true if we can establish that  $rel_2$  and  $rel_3$  and all relations to  $rel_n$  are true.

rel<sub>1</sub> is called the *head* of the rule. rel<sub>2</sub> to rel<sub>n</sub> form the *body* of the

rule.

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#### **Example**

```
The following two rules define a
grandMotherof relation using the
mother of and father of relations:
grandMotherOf(X,GM) :-
  motherOf(X,M),
     motherOf(M,GM).
grandMotherOf(X,GM) :-
  fatherOf(X,F),
    motherOf(F,GM).
 ?- grandMotherOf(tom,GM).
GM = mary :
no
 ?- grandMotherOf(dick,GM).
no
?- grandMotherOf(X,mary).
X = tom :
no
```

As is the case for all programming, in all languages, you must be careful when you define a rule that it correctly captures the idea you have in mind.

Consider the following rule that defines a sibling relation between two people:

```
sibling(X,Y) :-
motherOf(X,M), motherOf(Y,M),
fatherOf(X,F), fatherOf(Y,F).
```

This rule says that x and y are siblings if each has the same mother and the same father.

But the rule is wrong! Why?

Let's give it a try:

```
| ?- sibling(X,Y).
X = Y = tom
```

Darn! That's right, you can't be your own sibling. So we refine the rule to force **x** and **y** to be distinct:

```
sibling(X,Y) :-
motherOf(X,M), motherOf(Y,M),
fatherOf(X,F), fatherOf(Y,F),
\+(X=Y).
```

In Quintus prolog "\+" represents not; most other Prologs include a not relation.

```
| ?- sibling(X,Y).
X = dick,
Y = jane;
X = jane,
Y = dick;
no
```

Note that distinct but equivalent solutions

(like x = dick, Y = jane VS.

x = jane, y = dick) often appear in Prolog solutions. You may sometimes need to "filter out" solutions that are effectively redundant (perhaps by formulating stricter or more precise rules).

### **How Prolog Solves Queries**

The unique feature of Prolog is that it automatically chooses the facts and rules needed to solve a query.

But how does it make its choice?

It starts by trying to solve each goal in a query, left to right (recall goals are connected using "," which is the and operator).

For each goal it tries to *match* a corresponding fact or the head of a corresponding rule.

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A fact or head of rule matches a goal if:

- Both use the same predicate.
- Both have the same number of terms following the predicate.
- Each term in the goal and fact or rule head match (are equal), possibly binding a free variable to force a match.

For example, assume we wish to match the following goal:

This can match the fact

$$x(a,b)$$
.

or the head of the rule

$$x(Y,Z) :- Y = Z.$$

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But x(a,B) can't match

y(a,b) (wrong predicate name) or x(b,d) (first terms don't match) or x(a,b,c) (wrong number of terms).

If we succeed in matching a rule, we have solved the goal in question; we can go on to match any remaining goals.

If we match the head of a rule, we aren't done—we add the body of the rule to the list of goals that must be solved.

Thus if we match the goal x(a,B) with the rule

$$x(Y,Z) :- Y = Z.$$

then we must solve a=в which is done by making в equal to a.

# Backtracking

If we reach a point where a goal can't be matched, or the body of a rule can't be matched, we backtrack to the last (most recent) spot where a choice of matching a particular fact or rule was made. We then try to match a different fact or rule. If this can't be done, we go back to the next previous place where a choice was made and try a different match there. We try alternatives until we are able to solve all the goals in our query or until all possible choices have been tried and found to fail. If this happens, we answer "no" the query can't be solved.

As we try to match facts and rules we try them in their order of definition.

#### **Example**

```
Let's trace how
  ?- grandMotherOf(tom,GM).
is solved.
Recall that
grandMotherOf(X,GM) :-
  motherOf(X,M),
     motherOf(M,GM).
grandMotherOf(X,GM) :-
  fatherOf(X,F),
    motherOf(F,GM).
fatherOf(tom,dick).
fatherOf(dick, harry).
fatherOf(jane, harry).
motherOf(tom, judy).
motherOf(dick, mary).
motherOf(jane,mary).
```

We try the first grandMotherOf rule first.

This forces x = tom. We have to solve motherOf(tom, M), motherOf(M, GM).

We now try to solve

motherOf(tom,M)

This forces  $\mathbf{M} = \mathbf{judy}$ .

We then try to solve

motherOf(judy,GM)

None of the motherof rules match this goal, so we backtrack. No other motherof rule can solve

motherOf(tom, M)

so we backtrack again and try the second grandMotherOf rule:

```
grandMotherOf(X,GM) :-
  fatherOf(X,F),
    motherOf(F,GM).
This matches, forcing x = tom.
We have to solve
fatherOf(tom,F), motherOf(F,GM).
We can match the first goal with
fatherOf(tom,dick).
This forces \mathbf{F} = \mathbf{dick}.
We then must solve
motherOf(dick,GM)
which can be matched by
motherOf(dick, mary).
We have matched all our goals, so we
know the query is true, with
GM = mary.
```

# List Processing in Prolog

Prolog has a notation similar to "cons cells" of Lisp and Scheme.

The "." functor (predicate name) acts like cons.

Hence .(a,b) in Prolog is essentially the same as (a . b) in Scheme.

Lists in Prolog are formed much the same way as in Scheme and ML:

```
[] is the empty list
[1,2,3] is an abbreviation for
.(1, .(2, .(3,[])))
just as
(1,2,3) in Scheme is an abbreviation
for
(cons 1 (cons 2 (cons 3 () )))
```

The notation [H|T] represents a list with H matching the head of the list and T matching the rest of the list.

```
Thus [1,2,3] \equiv [1|[2,3]] \equiv [1,2|[3]] \equiv [1,2,3|[]]
```

As in ML, "\_" (underscore) can be used as a wildcard or "don't care" symbol in matches.

Given the fact

The query

$$| ?- p([X|Y]).$$

answers

$$X = 1,$$
  
 $Y = [2,3,4]$ 

### The query

$$p([_,_,X|Y]).$$

#### answers

$$X = 3$$
,

$$Y = [4]$$

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### List Operations in Prolog

List operations are defined using rules and facts. The definitions are similar to those used in Scheme or ML, but they are *non-procedural*.

That is you don't given an execution order. Instead, you give recursive rules and non-recursive "base cases" that characterize the operation you are defining.

Consider append:

```
append([],L,L).
append([H|T1],L2,[H,T3]) :-
append(T1,L2,T3).
```

The first fact says that an empty list (argument 1) appended to any list L (argument 2) gives L (argument 3) as its answer.

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The rule in line 2 says that if you take a list that begins with H and has T1 as the rest of the list and append it to a list L then the resulting appended list will begin with H.

Moreover, the rest of the resulting list, **T3**, is the result of appending **T1** (the rest of the first list) with **L2** (the second input list).

The query

| ?- append([1],[2,3],[1,2,3]).
answers

#### Yes

because with H=1, T1=[], L2 =[2,3] and T3=[2,3] it must be the case that append([],[2,3],[2,3]) is true and fact (1) says that this is so.

### **Inverting Inputs and Outputs**

In Prolog the division between "inputs" and "outputs" is intentionally vague. We can exploit this. It is often possible to "invert" a query and ask what *inputs* would compute a given output. Few other languages allow this level of flexibility.

Consider the query

```
append([1],X,[1,2,3]).
```

This asks Prolog to find a list x such that if we append [1] to x we will get [1,2,3].

Prolog answers

$$X = [2,3]$$

How does it choose this answer?

First Prolog tries to match the query against fact (1) or rule (2).

Fact (1) doesn't match (the first arguments differ) so we match rule (2).

This gives us H=1, T1=[], L2=x and T3 = [2,3].

We next have to solve the body of rule (2) which is

append([],L2,[2,3]).

Fact (1) matches this, and tells us that **L2=[2,3]=x**, and that's our answer!

#### The Member Relation

A common predicate when manipulating lists is a membership test—is a given value a member of a list?

An "obvious" definition is a recursive one similar to what we might program in Scheme or ML:

```
member(x,[x|_]).
member(x,[_|Y]):- member(x,Y).
This definition states that the first argument, x, is a member of the second argument (a list) if x matches the head of the list or if x is (recursively) a member of the rest of
```

the list.

Note that we don't have to "tell" Prolog that **x** can't be a member of an empty list—if we don't tell Prolog that something is true, it automatically assumes that it must be false.

Thus saying nothing about membership in an empty list is the same as saying that membership in an empty list is impossible.

Since inputs and outputs in a relation are blurred, we can use member in an unexpected way—to iterate through a list of values.

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If we want to know if any member of a list **L** satisfies a predicate **p**, we can simply write:

member(X,L),p(X).

There is no explicit iteration or searching. We simply ask Prolog to find an x such that member(x,L) is true (x is in L) and p(x) is true. Backtracking will find the "right" value for x (if any such x exists).

This is sometimes called the "guess and verify" technique.

Thus we can query

member(
$$X,[3,-3,0,10,-10]$$
), ( $X > 0$ ).

This asks for an x in the list [3,-3,0,10,-10] which is greater than o.

Prolog answers

```
x = 3;
x = 10;
```

Note too that our "obvious" definition of member is not the only one possible.

An alternative definition (which is far less obvious) is

```
member(X,L) :-
   append(_,[X|_],L).
```

This definition says **x** is a member of **L** if I can take some list (whose value I don't care about) and append it to a list that begins with **x** (and which ends with values I don't care about) and get a list equal to **L**.

Said more clearly, x is a member of L if x is anywhere in the "middle" of L.

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Prolog solves a query involving member by partitioning the list L in all possible ways, and checking to see if x ever is the head of the second list. Thus for member(x,[1,2,3]), it tries the partition [] and [1,2,3] (exposing 1 as a possible x), then [1] and [2,3] (exposing 2) and finally [1,2] and [3] (exposing 3).

# **Sorting Algorithms**

Sorting algorithms are good examples of Prolog's definitional capabilities. In a Prolog definition the "logic" of a sorting algorithm is apparent, stripped of the cumbersome details of data structures and control structures that dominate algorithms in other programming languages.

Consider the simplest possible sort imaginable, which we'll call the "naive sort."

At the simplest level a sorting of a list requires just two things:

- The sorting is a permutation (a reordering) of the values in **L**.
- The values are "in order" (ascending or descending).

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We can implement this concept of a sort directly in Prolog. We

- (a) permute an input list
- (b) check if it is in sorted order
- (c) repeat (a) & (b) until a sorting is found.

#### **Permutations**

Let's first look at how permutations are defined in Prolog. In most languages generating permutations is non-trivial—you need data structures to store the permutations you are generating and control structures to visit all permutations in some order.

In Prolog, permutations are defined quite concisely, though with a bit of subtlety:

perm(x, y) will be true if list y is a permutation of list x.

Only two definitions are needed:

```
perm([],[]).
perm(L,[H|T]):-
  append(V,[H|U],L),
  append(V,U,W), perm(W,T).
```

The first definition,

```
perm([],[]).
```

is trivial. An empty list may only be permuted into another empty list.

The second definition is rather more complex:

```
perm(L,[H|T]) :-
append(V,[H|U],L),
append(V,U,W), perm(W,T).
```

This rule says a list L may be permuted in to a list that begins with H and ends with list T if:

- (1) L may be partitioned into two lists, v and [н|u]. (That is, н is somewhere in the "middle" of L).
- (2) Lists v and v (all of L except н) may be appended into list w.
- (3) List w may be permuted into T.

Let's see **perm** in action:

```
| ?- perm([1,2,3],X).
X = [1,2,3];
X = [1,3,2];
X = [2,1,3];
X = [2,3,1];
X = [3,1,2];
x = [3,2,1];
```

We'll trace how the first few answers are computed. Note though that *all* permutations are generated, and with no apparent data structures or control structures.

```
We start with L=[1,2,3] and X=[H|T].
```

We first solve append(V,[H|U],L), which simplifies to append(V,[H|U],[1,2,3]).

One solution to this goal is

V = [], H = 1, U = [2,3]

We next solve append(v,v,w) which simplifies to append([],[2,3],w).

The only solution for this is w=[2,3].

Finally, we solve perm(W,T), which simplifies to perm([2,3],T).

One solution to this is T=[2,3].

This gives us our first solution: [H|T]=[1,2,3].

To get our next solution we backtrack. Where is the most recent place we made a choice of how to solve a goal?

It was at perm([2,3],T). We chose T=[2,3], but T=[3,2] is another solution. Using this solution, we get out next answer [H|T]=[1,3,2].

Let's try one more. We backtrack again. No more solutions are possible for perm([2,3],T), so we backtrack to an earlier choice point.

At append(V,[H|U],[1,2,3]) another solution is

V=[1], H = 2, U = [3]

Using this binding, we solve append(V,U,W) which simplifies to append([1],[3],W). The solution to this must be w=[1,3].

We then solve perm(W,T) which simplifies to perm([1,3],T). One solution to this is T=[1,3]. This makes our third solution for [H|T] = [2,1,3].

You can check out the other bindings that lead to the last three solutions.

#### A Permutation Sort

Now that we know how to generate permutations, the definition of a permutation sort is almost trivial.

We define an inorder relation that characterizes our notion of when a list is properly sorted:

```
inOrder([]).
inOrder([_]).
inOrder([A,B|T]) :-
    A =< B, inOrder([B|T]).</pre>
```

These definitions state that a null list, and a list with only one element are always in sorted order. Longer lists are in order if the first two elements are in proper order. (A=<B) checks this and then the rest of the list, excluding the first element, is checked.

Now our naive permutation sort is only one line long:

```
naiveSort(L1,L2) :-
   perm(L1,L2), inOrder(L2).
And the definition works too!
| ?-
naiveSort([1,2,3],[3,2,1]).
no
?- naiveSort([3,2,1],L).
L = [1,2,3];
no
| ?-
naiveSort([7,3,88,2,1,6,77,-23,5],L).
L = [-23,1,2,3,5,6,7,77,88]
```

Though this sort works, it is hopelessly inefficient—it repeatedly "shuffles" the input until it happens to find an ordering that is sorted. The process is largely undirected. We don't "aim" toward a correct ordering, but just search until we get lucky.

#### A Bubble Sort

Perhaps the best known sorting technique is the interchange or "bubble" sort. The idea is simple. We examine a list of values, looking for a pair of adjacent values that are "out of order." If we find such a pair, we swap the two values (placing them in correct order). Otherwise, the whole list must be in sorted order and we are done.

In conventional languages we need a lot of code to search for out-of-order pairs, and to systematically reorder them. In Prolog, the whole sort may be defined in a few lines:

```
bubbleSort(L,L) :- inOrder(L).
bubbleSort(L1,L2) :-
append(X,[A,B|Y],L1), A > B,
append(X,[B,A|Y],T),
bubbleSort(T,L2).
```

The first line says that if **L** is already in sorted order, we are done.

The second line is a bit more complex. It defines what it means for a list L2 to be a sorting for list L1, using our insight that we should swap out-of-order neighbors. We first partition list L1 into two lists, x and [A,B|Y]. This "exposes" two adjacent values in L, A and B. Next we verify that A and B are out-of-order (A>B). Next, in append(X,[B,A|Y],T), We determine that list T is just our input L, with A and B swapped into B followed by A.

Finally, we verify that bubblesort(T,L2) holds. That is, T may be bubble-sorted into L2.

This approach is rather more directed than our permutation sort—we look for an out-of-order pair of values, swap them, and then sort the "improved" list. Eventually there will be no more out-of-order pairs, the list will be in sorted order, and we will be done.

## Merge Sort

Another popular sort in the "merge sort" which we have already seen in Scheme and ML. The idea here is to first split a list of length **L** into two sublists of length **L/2**. Each of these two lists is recursively sorted. Finally, the two sorted sublists are merged together to form a complete sorted list.

The bubble sort can take time proportional to  $n^2$  to sort n elements (as many as  $n^2/2$  swaps may be needed). The merge sort does better—it takes time proportional to  $n \log_2 n$  to sort n elements (a list of size n can only be split in half  $\log_2 n$  times).

We first need Prolog rules on how to split a list into two equal halves:

```
split([],[],[]).
split([A],[A],[]).
split([A,B|T],[A|P1],[B|P2]) :-
    split(T,P1,P2).
```

The first two lines characterize trivial splits. The third rule distributes one of the first two elements to each of the two sublists, and then recursively splits the rest of the list.

We also need rules that characterize how to merge two sorted sublists into a complete sorted list:

```
merge([],L,L).
merge(L,[],L).
merge([A|T1],[B|T2],[A|L2]) :-
    A =< B, merge(T1,[B|T2],L2).
merge([A|T1],[B|T2],[B|L2]) :-
    A > B, merge([A|T1],T2,L2).
```

The first 2 lines handle merging null lists. The third line handles the case where the head of the first sublist is ≤ the head of the second sublist; the final rule handles the case where the head of the second sublist is smaller.

With the above definitions, a merge sort requires only three lines:

```
mergeSort([],[]).
mergeSort([A],[A]).
mergeSort(L1,L2) :-
    split(L1,P1,P2),
    mergeSort(P1,S1),
    mergeSort(P2,S2),
    merge(S1,S2,L2).
```

The first two lines handle the trivial cases of lists of length 0 or 1. The last line contains the full "logic" of a merge sort: split the input list, L into two half-sized lists P1 and P2. Then merge sort P1 into S1 and P2 into S2. Finally, merge S1 and S2 into a sorted list L2. That's it!

#### **Quick Sort**

The median sort partitions its input list rather blindly, alternating values between the two lists. What if we partitioned the input list based on values rather than positions?

The quick sort does this. It selects a "pivot" value (the head of the input list) and divides the input into two sublists based on whether the values in the list are less than the pivot or greater than or equal to the pivot. Next the two sublists are recursively sorted. But now, after sorting, no merge phase is needed. Rather, the two sorted sublists can simply be appended, since we know all values in the first list are less than all values in the second list.

We need a Prolog relation that characterizes how we will do our partitioning. We we define partition(E,L1,L2,L3) to be true if L1 can be partitioned into L2 and L3 using E as the pivot element. The necessary rules are:

```
partition(E,[],[],[]).
partition(E,[A|T1],[A|T2],L3) :-
    A<E, partition(E,T1,T2,L3).
partition(E,[A|T1],L2,[A|T3]) :-
    A>=E, partition(E,T1,L2,T3)
```

The first line defines a trivial partition of a null list. The second line handles the case in which the first element of the list to be partitioned is less than the pivot, while the final line handles the case in which the list head is greater than or equal to the pivot.

With our notion of partitioning defined, the quicksort itself requires only 2 lines:

```
qsort([],[]).
qsort([A|T],L) :-
   partition(A,T,L1,L2),
   qsort(L1,S1),qsort(L2,S2),
   append(S1,[A|S2],L).
```

The first line defines a trivial sort of an empty list.

The second line says to sort a list that begins with  $\mathbf{A}$  and ends with list  $\mathbf{T}$ , we partition  $\mathbf{T}$  into sublists  $\mathbf{L}\mathbf{1}$  and  $\mathbf{L}\mathbf{2}$ , based on  $\mathbf{A}$ . Then we recursively quick sort  $\mathbf{L}\mathbf{1}$  into  $\mathbf{s}\mathbf{1}$  and  $\mathbf{L}\mathbf{2}$  into  $\mathbf{s}\mathbf{2}$ . Finally we append  $\mathbf{s}\mathbf{1}$  to  $[\mathbf{A}|\mathbf{s}\mathbf{2}]$  ( $\mathbf{A}$  must be > all values in  $\mathbf{s}\mathbf{1}$  and  $\mathbf{A}$  must be  $\leq$  all values in  $\mathbf{s}\mathbf{2}$ ). The result is  $\mathbf{L}$ , a sorting of  $[\mathbf{A}|\mathbf{T}]$ .

## **Arithmetic in Prolog**

The = predicate can be used to test bound variables for equality (actually, identity).

If one or both of ='s arguments are free variables, = forces a binding or an equality constraint.

#### Thus

```
| ?- 1=2.
no
| ?- X=2.
X = 2
| ?- Y=X.
Y = X = _10751
| ?- X=Y, X=joe.
X = Y = joe
```

## Arithmetic Terms are Symbolic

Evaluation of an arithmetic term into a numeric value must be *forced*.

That is, 1+2 is an infix representation of the relation +(1,2). This term is not an integer!

**Therefore** 

no

To force arithmetic evaluation, we use the infix predicate is.

The right-hand side of is must be all ground terms (literals or variables that are already bound). No free (unbound) variables are allowed.

Hence

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```
|?- 2 is 1+1.
yes
| ?- X is 3*4.
X = 12
| ?- Y is Z+1.
! Instantiation error in argument
2 of is/2
! goal: _10712 is _10715+1
```

The requirement that the right-hand side of an is relation be ground is essentially procedural. It exists to avoid having to invert complex equations. Consider,

```
(0 is (I**N)+(J**N)-K**N)), N>2.
```

## Counting in Prolog

Rules that involve counting often use the is predicate to evaluate a numeric value.

Consider the relation len(L,N) that is true if the length of list L is N.

```
len([],0).
len([_|T],N):-
    len(T,M), N is M+1.
| ?- len([1,2,3],X).

X = 3
| ?- len(Y,2).
Y = [_10903,_10905]
```

The symbols \_10903 and \_10905 are "internal variables" created as needed when a particular value is not forced in a solution.

## **Debugging Prolog**

Care is required in developing and testing Prolog programs because the language is untyped; undeclared predicates or relations are simply treated as false.

Thus in a definition like

```
adj([A,B|_]) :- A=B.
adj([_,B|T]) :- adk([B|T]).
| ?- adj([1,2,2]).
```

no

(Quintus does warn when an undefined relation is referenced, but many other Prologs don't).

```
Similarly, given
 member(A,[A|_]).
 member(A,[_|T]) :-
  member(A,[T]).
?- member(2,[1,2]).
Infinite recursion! (Why?)
If you're not sure what is going on,
Prolog's trace feature is very handy.
The command
trace.
turns on tracing. (notrace turns
tracing off).
Hence
?- trace.
yes
[trace]
?- member(2,[1,2]).
```

```
(1) 0 Call: member(2,[1,2]) ?
   (1) 1 Head [1->2]:
member(2,[1,2]) ?
   (1) 1 Head [2]:
member(2,[1,2]) ?
   (2) 1 Call: member(2,[[2]]) ?
   (2) 2 Head [1->2]:
member(2,[[2]]) ?
   (2) 2 Head [2]:
member(2,[[2]]) ?
   (3) 2 Call: member(2,[[]]) ?
   (3) 3 Head [1->2]:
member(2,[[]]) ?
  (3) 3 Head [2]: member(2,[[]])
   (4) 3 Call: member(2,[[]]) ?
   (4) 4 Head [1->2]:
member(2,[[]]) ?
   (4) 4 Head [2]: member(2,[[]])
?
   (5) 4 Call: member(2,[[]]) ?
```

### **Termination Issues in Prolog**

Searching infinite domains (like integers) can lead to non-termination, with Prolog trying *every* value.

Consider

```
odd(1).
odd(N) :- odd(M), N is M+2.
| ?- odd(X).
X = 1;
X = 3;
X = 5;
X = 7
```

#### A query

?- odd(X), X=2.

going into an *infinite* search, generating each and every odd integer and finding none is equal to 2!

The obvious alternative,

odd(2) (which is equivalent to

x=2, odd(x)) also does an infinite, but fruitless search.

We'll soon learn that Prolog does have a mechanism to "cut off" fruitless searches.

#### **Definition Order can Matter**

Ideally, the order of definition of facts and rules should not matter.

But,

in practice definition order can matter. A good general guideline is to define facts before rules. To see why, consider a very complete database of motherof relations that goes back as far as

```
motherOf(cain,eve).
Now we define
isMortal(X):-
  isMortal(Y), motherOf(X,Y).
isMortal(eve).
```

These definitions state that the first woman was mortal, and all individuals descended from her are also mortal.

But when we try as trivial a query as | ?- isMortal(eve).

we go into an infinite search! Why?

Let's trace what Prolog does when it sees

?- isMortal(eve).

It matches with the first definition
involving isMortal, which is
isMortal(X):-

isMortal(Y), motherOf(X,Y).

It sets x=eve and tries to solve
isMortal(Y), motherOf(eve,Y).
It will then expand isMortal(Y) into

```
isMortal(Z), motherOf(Y,Z).
An infinite expansion ensues.
The solution is simple—place the
"base case" fact that terminates
recursion first.
If we use
isMortal(eve).
isMortal(X) :-
  isMortal(Y), motherOf(X,Y).
yes
?- isMortal(eve).
yes
But now another problem appears!
If we ask
?- isMortal(clarkKent).
we go into another infinite search!
Why?
```

The problem is that Clark Kent is from the planet Krypton, and hence won't appear in our motherof database.

Let's trace the query.

It doesn't match isMortal(eve).

We next try

```
isMortal(clarkKent) :-
   isMortal(Y),
   motherOf(clarkKent,Y).
```

We try **Y=eve**, but **eve** isn't Clark's mother. So we recurse, getting:

```
isMortal(Z), motherOf(Y,Z),
motherOf(clarkKent,Y).
```

But eve isn't Clark's grandmother either! So we keep going further back, trying to find a chain of descendents that leads from eve to clarkkent. No such chain exists, and there is no

limit to how long a chain Prolog will try.

There is a solution though!
We simply rewrite our recursive definition to be

```
isMortal(X) :-
  motherOf(X,Y),isMortal(Y).
```

This is logically the same, but now we work from the individual x back toward eve, rather than from eve toward x. Since we have no motherof relation involving clarkKent, we immediately stop our search and answer no!

# Extra-logical Aspects of Prolog

To make a Prolog program more efficient, or to represent negative information, Prolog needs features that have a procedural flavor. These constructs are called "extra-logical" because they go beyond Prolog's core of logic-based inference.

#### The Cut

The most commonly used extralogical feature of Prolog is the "cut symbol," "!"

A ! in a goal, fact or rule "cuts off" backtracking.

In particular, once a ! is reached (and automatically matched), we may not backtrack across it. The rule we've selected and the bindings we've already selected are "locked in" or "frozen."

For example, given

x(A):-y(A,B), z(B), !, v(B,C).
once the ! is hit we can't backtrack
to resatisfy y(A,B) or z(B) in some
other way. We are locked into this

rule, with the bindings of **A** and **B** already in place.

We can backtrack to try various solutions to  $\mathbf{v}(\mathbf{B},\mathbf{C})$ .

It is sometimes useful to have several 's in a rule. This allows us to find a partial solution, lock it in, find a further solution, then lock it in, etc.

For example, in a rule

a(x) - b(x), !, c(x,y), !, d(y). we first try to satisfy b(x), perhaps trying several facts or rules that define the b relation. Once we have a solution to b(x), we lock it in, along with the binding for x.

Then we try to satisfy c(x, y), using the fixed binding for x, but perhaps trying several bindings for y until c(x, y) is satisfied.

We then lock in this match using another !.

Finally we check if a(Y) can be satisfied with the binding of Y already selected and locked in.

#### When are Cuts Needed?

A cut can be useful in improving efficiency, by forcing Prolog to avoid useless or redundant searches.

Consider a query like

```
member(X,list1),
  member(X,list2), isPrime(X).
```

This asks Prolog to find an x that is in list1 and also in list2 and also is prime.

x will be bound, in sequence, to each value in list1. We then check if x is also in list2, and then check if x is prime.

Assume we find x=8 is in list1 and list2. isPrime(8) fails (of course). We backtrack to member(x,list2) and try to resatisfy it with the same value of x.

But clearly there is never any point in trying to resatisfy member(X,list2). Once we know a value of x is in list2, we test it using isPrime(X). If it fails, we want to go right back to member(X,list1) and get a different x.

To create a version of member that never backtracks once it has been satisfied we can use !.

```
We define
```

```
member1(X,[X|_]) :- !.
member1(X,[_|Y]) :-
   member1(X,Y).

Our query is now
member(X,list1),
   member1(X,list2), isPrime(X).

(Why isn't member1 used in both terms?)
```

## **Expressing Negative Information**

Sometimes it is useful to state rules about what *can't* be true. This allows us to avoid long and fruitless searches.

fail is a goal that always fails. It can be used to represent goals or results that can never be true.

Assume we want to optimize our grandMotherOf rules by stating that a male can never be anyone's grandmother (and hence a complete search of all motherOf and fatherOf relations is useless).

A rule to do this is

```
grandMotherOf(X,GM) :-
male(GM), fail.
```

This rule doesn't do quite what we hope it will!

Why?

The standard approach in Prolog is to try other rules if the current rule fails.

Hence we need some way to "cut off" any further backtracking once this negative rule is found to be applicable.

This can be done using

```
grandMotherOf(X,GM) :-
male(GM),!, fail.
```

# Other Extra-Logical Operators

• Assert and Retract

These operators allow a Prolog program to add new rules during execution and (perhaps) later remove them. This allows programs to learn as they execute.

var and nonvar

var(x) tests whether x is unbound (free).

nonvar(Y) tests whether Y is bound (no longer free).

These two operators are useful in tailoring rules to particular combinations of bound and unbound variables.

For example, the rule

```
grandMotherOf(X,GM) :-
male(GM),!, fail.
```

might backfire if **GM** is not yet bound. We could set **GM** to a person for whom **male(GM)** is true, then fail because we don't want grandmothers who are male!

To remedy this problem. we use the rule only when **GM** is bound. Our rule becomes

```
grandMotherOf(X,GM) :-
nonvar(GM), male(GM),!, fail.
```

# An Example of Extra-Logical Programming

Factorial is a very common example program. It's well known, and easy to code in most languages.

In Prolog the "obvious" solution is:

```
fact(N,1) :- N =< 1.
fact(N,F) :- N > 1, M is N-1,
  fact(M,G), F is N*G.
```

This definition is clearly correct. It mimics the usual recursive solution.

But,

in Prolog "inputs" and "outputs" are less distinct than in most languages.

In fact, we can envision 4 different combinations of inputs and outputs, based on what is fixed (and thus an

- input) and what is free (and hence is to be computed):
- 1. N and F are both ground (fixed). We simple must decide if F=N!
- 2. N is ground and F is free. This is how fact is usually used. We must compute an F such that F=N!
- 3. **F** is fixed and **n** is free. This is an uncommon usage. We must find an **n** such that **F=N!**, or determine that no such **n** is possible.
- 4. Both **n** and **f** are free. We generate, in sequence, pairs of **n** and **f** values such that **F**=**N**!.

Our solution works for combinations 1 and 2 (where  $\mathbf{n}$  is fixed), but not combinations 3 and 4. (The problem is that  $\mathbf{n} = < 1$  and  $\mathbf{n} > 1$  can't be satisfied when  $\mathbf{n}$  is free).

We'll need to use **nonvar** and **!** to form a solution that works for all 4 combinations of inputs.

We first handle the case where **n** is ground:

```
fact(1,1).
fact(N,1):- nonvar(N), N =< 1,!.
fact(N,F):- nonvar(N), N > 1,!,
  M is N-1, fact(M,G), F is N*G,!.
The first rule handles the base case of
N=1.
```

The second rule handles the case of **N<1**.

The third rule handles the case of N >1. The value of F is computed recursively. The first I in each of these rules forces that rule to be the only one used for the values of N that match. Moreover, the second I in the third rule states that after F is computed, further backtracking is useless; there is only one F value for any given N value.

To handle the case where **F** is bound and **N** is free, we use

```
fact(N,F) :- nonvar(F), !,
fact(M,G), N is M+1, F2 is N*G,
F =< F2, !, F=F2.</pre>
```

In this rule we generate N, F2 pairs until F2 >= F. Then we check if F=F2. If this is so, we have the N we want. Otherwise, no such N can exist and we fail (and answer no).

For the case where both n and f are free we use:

fact(N,F) :- fact(M,G), N is M+1,
 F is N\*G.

This systematically generates N, F pairs, starting with N=2, F=2 and then recursively building successor values (N=3, F=6, then N=4, F=24, etc.)

## Parallelism in Prolog

One reason that Prolog is of interest to computer scientists is that its search mechanism lends itself to parallel evaluation.

In fact, it supports two different kinds of parallelism:

- AND Parallelism
- OR Parallelism

#### And Parallelism

When we have a goal that contains subgoals connected by the "," (And) operator, we may be able to utilize "and parallelism."

Rather than solve subgoals in sequence, we may be able to solve them in parallel *if* bindings can be properly propagated.

Thus in

a(X), b(X,Y), c(X,Z), d(Y,Z).

we may be able to first solve a(x), binding x, then solve b(x, y) and c(x,z) in parallel, binding y and z, then finally solve d(y,z).

An example of this sort of and parallelism is

member(X,list1),
 member1(X,list2), isPrime(X).
Here We can let member(X,list1)

select an x value, then test

member1(X,list2) and isPrime(X)
in parallel. If one or the other fails,
we just select another x from list1
and retest member1(X,list2) and
isPrime(X) in parallel.

#### **OR Parallelism**

When we match a goal we almost always have a choice of several rules or facts that may be applicable. Rather than try them in sequence, we can try several matches of different facts or rules in parallel. This is "or parallelism."

Thus given

```
a(X) := b(X).
a(Y) := c(Y).
```

when we try to solve

we can simultaneously check both **b(10)** and **c(10)**.

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```
Recall our definition of
member(X,L) :-
 append(P,[X|S],L).
where append is defined as
append([],L,L).
append([X|L1],L2,[X|L3]) :-
 append(L1,L2,L3).
Assume we have the query
  ? member(2,[1,2,3]).
This immediately simplifies to
append(P,[2|S],[1,2,3]).
Now there are two append
definitions we can try in parallel:
(1) match append(P,[2|S],[1,2,3])
With append([],L,L). This requires
that [2|s] = [1,2,3], which must
fail.
(2) match append(P,[2|S],[1,2,3])
```

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With append([X|L1],L2,[X,L3]).

This requires that P=[x|L1], [2|S]=L2, [1,2,3]=[x,L3]. Simplifying, we require that x=1, P=[1|L1], L3=[2,3].

Moreover we must solve append(L1,L2,L3) which simplifies to append(L1,[2|S],[2,3]).

We can match this call to append in two different ways, so or parallelism can be used again.

When we try matching append(L1,[2|S],[2,3]) against append([],L,L) We get [2|S]=[2,3], which is satisfiable if s is bound to [3]. We therefore signal back that the query is true.

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## Speculative Parallelism

Prolog also lends itself nicely to speculative parallelism. In this form of parallelism, we "guess" or speculate that some computation may be needed in the future and start it early. This speculative computation can often be done in parallel with the main (non-speculative) computation.

Recall our example of

```
member(X,list1),
  member1(X,list2), isPrime(X).
```

After member(X,list1) has generated a preliminary solution for x, it is tested (perhaps in parallel) by member1(X,list2) and isPrime(X).

But this value of x may be rejected by one or both of these tests. If it is,

we'll ask member(x,list1) to find a new binding for x. If we wish, this next binding can be generated speculatively, while the current value of x is being tested. In this way if the current value of x is rejected, we'll have a new value ready to try (or know that no other binding of x is possible).

If the current value of **x** is accepted, the extra speculative work we did is ignored. It wasn't needed, but was useful insurance in case further **x** bindings were needed.

## Reading Assignment

 Java for C++ Programmers (linked from class web page)

• Scott: Chapter 10

# Java & Object-Oriented Programming

Java is a fairly new and very popular programming language designed to support secure, platform-independent programming.

It is a good alternative to C or C++, trading a bit of efficiency for easier programming, debugging and maintenance.

Java is routinely interpreted (at the byte-code level), making it significantly slower than compiled C or C++. However true Java compilers exist, and are becoming more wide-spread. (IBM's Jalapeno project is a good example). When compiled, Java's execution speed is close to that of C or C++.

#### **Basic Notions**

In Java data is either primitive or an object (an instance of some class).

All code is written inside classes, so Java programming consists of writing classes.

Primitive data types are quite close to those of C or C++:

boolean (not a numeric type)

**char** (Unicode, 16 bits)

byte

short

int

long (64 bits)

float

double

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## **Objects**

- All Java objects are instances of classes.
- All objects are heap-allocated, with automatic garbage collection.
- A reference to an object, in a variable, parameter or another object, is actually a pointer to some object allocated within the heap.
- No explicit pointer manipulation operations (like \* or -> or ++) are needed or allowed.
- Example:

```
class Point {int x,y;}
Point data = new Point();
```

- Declaring an object reference (like class **Point**) does not automatically allocate space for an object. The reference is initialized to **null** unless an explicit initializer is included.
- Fields are accessed just as they are in C:
   data.x references field x in object
   data.
- Object references are automatically checked for validity (null or non-null).
   Hence

data.x = 0;

forces a run-time exception if data contains **null** rather than a valid object reference.

Java makes it *impossible* for an object reference to access an illegal address. A references is either null or a pointer to a valid, type-correct object in the heap. (This makes Java programs far more secure and reliable than C or C++ programs).

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#### Class Members

Classes contain members. Class members are either fields (data) or methods (functions).

```
Example:
```

```
class Point {
  int x,y;
  void clear() {x=0; y=0;}
}
Point d = new Point():
d.clear();
```

A special method is a constructor.

A constructor has no result type. It is used only to define the initialization of an object after the object has been created.

Constructors may be overloaded.

```
class Point {
   int x,y;
   Point() {x=0; y=0;}
   Point(int xin, int yin) {
      x = xin; y = yin;
   }
}
```

#### **Static Members**

Class members may be static.

A static member is allocated only once—for all instances of the class.

Ordinary members (called *instance* members) apply only to a particular class instance (i.e., only one object created from the class definition).

```
class Point {
   int x,y;
   static int howMany = 0;
   Point() {x=0; y=0;
        howMany++;}
   static void reset() {
        howMany = 0;
   }
}
```

Static member functions (methods) may not access non-static data. (Why?)

Static members are accessed using a class name rather than the name of an object reference.

For example,

Point.reset();

## Visibility of Class Members

Class members may be declared as public, private or protected.

Public members may be accessed from outside a class.

Private members of a class may be accessed only from with the class itself.

Protected members may be accessed only from with the class itself or from within one of its subclasses.

Members nor marked public, private or protected are shared at the package level—similar to C++'s friend mechanism.

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```
Example:
 class Customer {
   int id:
   private int pinCode;
Customer me = new Customer();
me.id = 1234; //OK
me.pinCode = 7777;
 //Compile-time error
In a class, a special method, main,
declared as
 static public void
    main(String[] args)
is automatically executed when a
class is run.
main is very useful as a "test driver"
for auxiliary and library classes.
```

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#### Final Members

A field may be declared *final* making it effectively a constant.

```
class Point {
    int x,y;
    static final Point origin
          = new Point(0,0);
    Point(int xin, int yin) {
       x = xin; y = yin;
Final fields may be used to create
constants within a class:
class Card {
  final static int Clubs = 1;
  final static int Diamonds = 2;
  final static int Hearts = 3;
  final static int Spades = 4;
  int suit = Spades;
```

Inside a class suit names are available for use without qualification. E.g.,

```
int suit = Spades;
```

Outside a class, the field names must be qualified using the class name:

```
Card c = new Card();
c.suit = Card.Clubs;
```

Methods may also be marked as final. This forbids redeclaration in a subclass, allowing a more efficient implementation. Security may also be improved if a key method is known to be unchangeable.

## Java Arrays

In Java, arrays are implemented as a special kind of class. Arrays of primitive types are implemented as an object that contains a block of values within it. Arrays of objects are implemented as an object that contains a block of object references within it. Allocating an array of objects does not allocate the objects themselves. Hence within an array of objects, some positions may reference actual objects while other may contain null (this can be advantageous) if objects are large.

Multi-dimensional arrays are arrays of arrays. Arrays within an array *need not* all have the same size.

Hence we may see

```
int[][] TwoDim = new int[3][];
TwoDim[0] = new int[1];
TwoDim[1] = new int[2];
TwoDim[2] = new int[3];
The size of an array is part of its
value; not its type.
Thus
int [] A = new int[10];
int [] B = new int[5];
A = B;
is valid.
Pascal showed that making an array's
```

Pascal showed that making an array's size part of its type is undesirable. (Why?)

Still, forcing an array to have a fixed size can be necessary (e.g., an array indexed by months). (How do we simulate a fixed-size array?).

## Subclassing in Java

When a new class is defined in terms of an existing class, the new class *extends* the existing class. The new class *inherits* all public and protected members of its *parent* (or *base*) class.

The new class may add new methods or fields. It may also redefine inherited methods or fields.

```
class Point {
   int x,y;
   Point(int xin, int yin) {
      x = xin; y = yin;
   }
   static float dist(
      Point P1, Point P2) {
      return (float) Math.sqrt(
          (P1.x-P2.x)*(P1.x-P2.x)+
          (P1.y-P2.y)*(P1.y-P2.y));
   }
}
```

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Note that although Point3 redefines dist, the old definition of dist is still available by using the parent class as a qualifier (Point.dist).

The same is true for fields that are hidden when a field in a parent is redeclared.

Non-static methods are automatically virtual: a redefined method is automatically used in all inherited methods including those defined in parent classes that think they are using an earlier definition of the class.

Static methods in Java are *not* virtual (this can make them easier to implement efficiently).

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#### **Abstract Classes and Methods**

Sometimes a Java class is not meant to be used by itself because it is intentionally incomplete.

Rather, the class is meant to be starting point for the creation (via subclassing) of more complete classes.

Such classes are abstract.

```
Example:
abstract class Shape {
   Point location;
}
class Circle extends Shape {
   float radius;
}
```

Methods can also be made abstract to indicate that their actual definition will appear in subclasses:

```
abstract class Shape {
   Point location;
   abstract float area();
}
class Circle extends Shape {
   float radius;
   float area(){
    return Math.pi*radius*radius;
   }
}
```

## Subtyping and Inheritance

We can use a subtyping mechanism, as found in C++ or Java, for two different purposes:

 We may wish to inherit the actual implementations of classes and members to use as the basis of a more complete or extended class.
 To inherit an implementation, we say a given class "extends" an existing class:

class Derived extends Base
{ ... };

Class Derived contains all of the members of Base plus any others it cares to add.

We may wish to inherit an interface—
 a set of method names and values
 that will be available for use.
 To inherit (or claim) an interface, we
 use a Java interface definition.
 An interface doesn't implement
 anything; rather, it gives a name to a
 set of operations or values that may
 be available within one or more
 classes.

## Why are Interfaces Important?

Many classes, although very different, share a common subset of values or operations. We may be willing to use any such class as long as only interface values or operations are used.

For example, many objects can be ordered (or at least partially-ordered) using a "less than" operation.

If we always implement less than the same way, for example,

then we can create an interface that admits all classes that know about the lessThan function:

```
interface Compare {
 boolean lessThan(Object o1,
                      Object o2);
Now different classes can each
implement the compare interface,
proclaiming to the world that they
know how to compare objects of the
class they define:
class IntCompare implements Compare {
public boolean lessThan(Object i1,
                         Object i2){
 return ((Integer)il).intValue() <</pre>
        ((Integer)i2).intValue(); }
class StringCompare implements
  Compare {
public boolean lessThan(Object i1,
                         Object i2){
 return
((String)i1).compareTo((String)i2)<0;
```

The advantage of using interfaces is that we can now define a method or class that only depends on the given interface, and which will accept *any* type that implements that interface.

```
class PrintCompare {
  public static void printAns(
   Object v1, Object v2, Compare c){
    System.out.println(
     v1.toString() + " < " +
     v2.toString() + " is " +
     new Boolean(c.lessThan(v1,v2))
       .toString());
} }
class Test {
 public static void
    main(String args[]){
     Integer i1 = new Integer(2);
     Integer i2 = new Integer(1);
     PrintCompare.printAns(
       i1,i2,new IntCompare());
     String s2 = "abcdef";
     String s1 = "xyzaa";
     PrintCompare.printAns(
      s1,s2,new StringCompare());}}
```

Since classes may have many methods and modes of use or operation, a given class may implement many different interfaces. For example, many classes support the clonable interface, which states that objects of the class may be duplicated (cloned).

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# Multiple Inheritance

We have seen that a class may be derived from a given parent class. It is sometimes useful to allow a class to be derived from more than one parent, inheriting members of all parents. This is *multiple inheritance*; it is allowed by C++ and Python, but not by Java.

The basic idea is that sometimes we want a "composite" object formed from more than one source. Hence a computer Object can be viewed as both a PhysicalObject (With height, weight, color, cost, etc.) and also a CPUImplementation (With memory size, processor design, processor speed, I/O ports, etc.)

Using multiple inheritance we merge aspects of a PhysicalObject and a CPUImplementation, and perhaps add additional data:

```
class PhysicalObject {
  float height, width, weight;
  Color outsideColor;
class CPUImplementation {
  CPUClass CPUKind;
  int memorySize, CPUSpeed;
class Computer: PhysicalObject,
  CPUImplementation {
  String myURL; ...
The advantages of multiple
inheritance are obvious—you can
build a class from many sources
rather than just one.
```

### There are problems though:

- If the same name appears in more than one parent, which is used? For example, if both parents contain a "copyright" field, which do you get? C++ forbids access to fields common to several parents, though accidental clashes of member names are certainly possible. Python relies on order of specification of the parents (which can be somewhat arbitrary).
- Access to fields and methods can be less efficient. A method in a parent class can't know how fields in derived class will be allocated when multiple parents may exist. Hence some form of indirection may be needed.
   For example, in class
   PhysicalObject, we may believe

that height is the first field allocated, while in CPUImplementation We May believe that CPUKind is allocated first. But in class Computer, which contains both height and CPUKind, both fields can't come first.

### **Exceptions in Java**

Java provides a fairly elaborate exception handling mechanism based on the throw-catch model.

All exceptions are objects, required to be a subclass of **Throwable**.

Class Throwable has two subclasses, Exception and Error. Class Exception has a subclass RuntimeException.

Exceptions may be explicitly thrown (using a throw statement) or they may be implicitly thrown as the result of a run-time error.

For example, an

ArithmeticException is thrown for certain run-time arithmetic errors, like division by zero.

Unlike other languages, Java divides exceptions into two general classes: checked and unchecked.

A checked exception *must* either be caught (using a try-catch block) or propagated (by marking a method as throwing the exception).

This means that checked exceptions cannot be ignored—you must be prepared to catch them or you must "advertise" to your callers that you may throw an exception back to them.

Unchecked exceptions need not be caught or marked as potentially thrown. This makes exception handling for such exceptions optional. Unchecked exceptions are typically those that might occur so

Often (like NullPointerException Or ArithmeticException) that forced checks could unnecessarily clutter a program without significant benefit.

How are checked and unchecked exceptions distinguished?

- Any exception that is a member (or subclass) of Error or RuntimeException is unchecked.
- All other exceptions must be checked.
   Exceptions are propagated dynamically:
- When an exception is thrown (explicitly or implicitly) the innermost try-catch block that can "catch" the exception is selected, and

- the catch block that matches the exception is executed.
- A catch block "catches" a given exception if the class of the exception is the same as the class used in the catch. An exception that is a subclass of the catch's exception class will also be caught. Thus an catch that handles class Throwable Catches all exceptions.
- If no catch can handle the exception in the current method, a return to the method's caller is forced, and the exception is rethrown from the point of call.
- This process is repeated until a catch that can handle the exception is found or until we force a return from the main method.

- If a return from the main method is forced, no handler exists. A run-time error message is printed ("Uncaught exception") and execution is terminated.
- One of the limitations of Java's exception mechanism (and similar mechanisms found in other languages) is that there is no "retry" mechanism. Once an exception is thrown, we never go back to the point where the exception occurred. This is why Scheme's call/cc mechanism is considered so special and unique.

### Example: class badValue extends Exception{ float value: badValue(float f) {value=f;} } float sqrt(float val) throws badValue { if (val < 0.0)throw new badValue(val); else return (float) Math.sqrt(val); } try { System.out.println( "Ans = " + sqrt(-123.0)); } catch (badValue b) { System.out.println( "Can't take sqrt of "+b)

# Reading Assignment

 Pizza Tutorial (linked from class web page)

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### Threads and Parallelism in Java

Java is one of the few "main stream" programming languages to explicitly provide for user-programmed parallelism in the form of threads.

A Java programmer may organize a program as several threads that may execute concurrently.

Even if the program is run on a uniprocessor, use of threads may improve performance. This is because the threads can be multi-programmed, with threads switched automatically on I/O delays, page faults or even cache misses.

A program that is designed to support multiple threads is also "prepared" for future upgrades to multiprocessors or multi-threaded processors.

### Java Threads

In Java any class that implements the **Runnable** interface can be started as a concurrent thread:

```
interface Runnable {
    public void run();
}
```

When the thread is started, the method run begins to execute (perhaps concurrently with other threads of the main program).

You create a thread using the **Thread** constructor:

```
new Thread(RunnableObject)
```

Creating a thread does not start it; you must execute the start method within the Thread object.

When this is done, the run method immediately starts, and continues until that method terminates normally, or it throws an uncaught exception, or it is explicitly stopped, or the main program stops.

On uniprocessors, thread execution is interleaved; on multiprocessors or multithreaded architectures execution can be concurrent.

```
class DoSort implements Runnable {
  int [] data;
  DoSort(int[] in) {data=in;}
  public void run(){
    // sort the data array;
  }
}
```

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```
class Test {
  public static void
     main(String args[]){
    DoSort d =
        new DoSort(new int[1000]);
    Thread t1 = new Thread(d);
    t1.start();
    // We can continue while t1
    // does its sort
  }
}
```

We can start multiple threads, and the threads can use sleep to delay or synchronize their execution:

```
class PingPong
   implements Runnable {
  int delay; String word;
  PingPong(String s,int i) {
     delay=i;word=s;};
  public void run() {
     try {
      while(true) {
         System.out.print(word+" ");
         Thread.sleep(delay);
     }}
  catch (InterruptedException e)
     {}
}
```

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```
public static void
    main(String args[]){
    Thread t1 = new Thread(
        new PingPong("ping",33));
    Thread t2 = new Thread(
        new PingPong("PONG",100));
    t1.start();
    t2.start();
}

ping PONG ping ping PONG ping
ping ping PONG ping ping ping PONG
ping ...
```

# Synchronization in Java

We often want threads to co-operate, typically in how they access shared data structures.

Since thread execution is asynchronous, the details of how threads interact can be unpredictable.

Consider a method

```
update() {
    n = n+1;
    val = f(n);
}
```

that updates fields of an object.

If two or more threads execute update concurrently, we might get unexpected or even illegal behavior.

(Why?)

A Java method may be *synchronized*, which guarantees that at most one thread can execute the method at a time. Other threads wishing access, are forced to wait until the currently executing thread completes.

#### Thus

void synchronized update() { ... } can safely be used to update an object, even if multiple threads are active.

There is also a synchronized statement in Java that forces threads to execute a block of code sequentially.

```
synchronized(obj) {
   obj.n = obj.n+1;
   obj.val = f(obj.n);
}
```

# Synchronization Primitives

The following operations are provided to allow threads to safely interact:

wait() Sleep until awakened

wait(n) Sleep until awakened

or until n milliseconds

pass

notify() Wake up one sleeping

thread

notifyAll() Wake up all sleeping

threads

Using these primitives, correct concurrent access to a shared data structure can be programed.

Consider a **Buffer** class in which independent threads may try to store or fetch data objects:

```
class Buffer {
  private Queue q;
  Buffer() { q = new Queue(); }
  public synchronized void
  put(Object obj) {
    q.enqueue(obj);
    notify();//Why is this needed?
  public synchronized Object
  get() {
    while (q.isEmpty()) {
     //Why a while loop?
     wait();
    }
    return q.dequeue();
```

# Locks, Semaphores and Monitors

Java's synchronization mechanisms are based upon the notion of a *lock*. A lock is a special value that can be held by at most one thread.

If a thread holds a lock, it has permission to do some "critical" operation like writing a shared variable or restructuring a shared data object.

If a thread wants to do an operation but doesn't hold the necessary lock, it must wait until it gets the lock.

In Java there is a lock associated with each run-time object.

# Lock Granularity and Access

Though each Java object has a lock, you often don't want to lock and unlock each object you access.

If you are manipulating a large data structure (like a tree or hash table), acquiring the lock for each object in the tree or table can be costly and error-prone.

Instead, it is common to create a lock corresponding to a group of objects. Hence holding the lock to the root of a tree may give you permission to access the whole tree.

There is a danger though—if all or most of a large structure is held by one thread, then other threads won't be able to access that structure concurrently.

For example, a large shared data base (like one used to record current bookings for an airline) shouldn't be held exclusively by one thread—hundreds of concurrent threads may want to access it at any time. An intermediate lock, like all reservations for a single fight, is more reasonable.

There is also an issue of how long you hold a lock. The ideal is to have exclusive access for as short a period as is necessary. Work that is not subject to interference by other threads (like computations using local variables) should be done before a lock is obtained. Hence Java's synchronized statement allows a method to get exclusive access to an object for a limited region, enhancing shared access.

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### **Deadlock**

A variety of programming problems appear in concurrent programs that don't exist in ordinary sequential programs.

The most serious of these is *deadlock*:

Two or more threads hold locks that other threads require. Each waits for the other thread to release a needed lock, and no thread is able to execute.

As an example of how deadlock may occur, consider two threads, £1 and £2. Each requires two files, a master file and a log file. Since these files are shared, each has a lock.

Assume £1 gets the lock for the master file while £2 (at the same instant) gets the lock for the log file.

Now each is stuck. Each has one file, and will wait forever for the other file to be released.

In Java deadlock avoidance is wholly up to the programmer. There are no language-level guarantees that deadlock can't happen.

Some languages have experimented with ways to help programmers avoid deadlock:

- If all locks must be claimed at once, deadlock can be avoided. You either get all of them or none, but you can't block other threads while making no progress yourself.
- Locks (and the resources they control) can be ordered, with the rule that you must acquire locks in the

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- proper order. Now two threads can't each hold locks the other needs.
- The language can require that the largest set of locks ever needed be declared in advance. When locks are requested, the operating system can track what's claimed and what may be needed, and refuse to honor unsafe requests.

### **Fairness & Starvation**

When one thread has a lock, other threads who want the lock will be suspended until the lock is released.

It can happen that a waiting thread may be forced to wait indefinitely to acquire a lock, due to an unfair waiting policy. A waiting thread that never gets a lock it needs due to unfair lock allocation faces *starvation*.

As an example, if we place waiting threads on a stack, newly arrived threads will get access to a lock before earlier arrivals. This can lead to starvation. Most thread managers try to be fair and guarantee that all waiting threads have a fair chance to acquire a lock.

# How are Locks Implemented?

Internally, Java needs operations to acquire a lock and release a lock. These operations can be implemented using the notion of a *semaphore*.

A semaphore is an integer value (often just a single bit) with two atomic operations: *up* and *down*.

up(s) increments s atomically.

down(s) decrements s atomically. But if s is already zero, the process doing the down operation is put in a wait state until s becomes positive (eventually some other process should do an up operation).

Now locks are easy to implement.

You do a down(lock) to claim a lock. If someone else has it, you are forced

to wait until the lock is released. If the lock value is > 0 you get it and all others are "locked out."

When you want to release a lock, you do up(lock), which makes lock non-zero and eligible for another thread to claim.

In fact, since only one thread will ever have a lock, the lock value needs to be only one bit, with 1 meaning currently free and unlocked and 0 meaning currently claimed and locked.

### **Monitors**

Direct manipulation of semaphores is tedious and error-prone. If you acquire a lock but forget to release it, threads may be blocked forever.

Depending on where down and up operations are placed, it may be difficult to understand how synchronization is being performed.

Few modern languages allow direct use of semaphores. Instead, semaphores are used in the implementation of higher-level constructs like *monitors*.

A monitor is a language construct that guarantees that a block of code will be executed synchronously (one thread at a time).

The Java synchronized statement is a form of monitor.

When

```
synchronized(obj) { ... }
is executed, "invisible" getLock and
freeLock Operations are added:
synchronized(obj) {
  getLock(obj)
  ...
  freeLock(obj);
}
```

This allows the body of the synchronized statement to execute only when it has the lock for obj. Thus two different threads can never simultaneously execute the body of a synchronized statement because two threads can't simultaneously hold obj's lock.

```
In fact, synchronized methods are
really just methods whose bodies are
enclosed in an invisible
synchronized Statement.
If we execute
 obj.method()
where method is synchronized,
method's body is executed as if it
were of the form
synchronized(obj) {
  body of method
Operations like sleep, wait, notify
and notifyall also implicitly cause
threads to release locks, allowing
other threads to proceed.
```

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### Pizza

Pizza is an extension to Java developed in the late 90s by Odersky and Wadler.

Pizza shows that many of the best ideas of functional languages can be incorporated into a "mainstream" language, giving it added power and expressability.

Pizza adds to Java:

### 1. Parametric Polymorphism

Classes can be parameterized with types, allowing the creation of "custom" data types with full compile-time type checking.

### 2. First-class Functions

Functions can be passed, returned and stored just like other types.

3. Patterns and Value Constructors

Classes can be subdivided into a number of value constructors, and patterns can be used to structure the definition of methods.

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## Parametric Polymorphism

Java allows a form of polymorphism by defining *container classes* (lists, stacks, queues, etc.) in terms of values of type object.

For example, to implement a linked list we might use:

We use class object because any object can be assigned to object (all classes must be a subclass of Object).

Using this class, we can create a linked list of any subtype of object. But,

- We can't guarantee that linked lists are type homogeneous (contain only a single type).
- We must cast object types back into their "real" types when we extract list values.
- We must use wrapper classes like Integer rather than int (because primitive types like int aren't objects, and aren't subclass of Object).

For example, to use LinkedList to build a linked list of ints we do the following:

```
LinkedList L =
   new LinkedList(new Integer(123));
  int i =
   ((Integer) L.head()).intValue();
This is pretty clumsy code. We'd
prefer a mechanism that allows us to
create a "custom version" of
LinkedList, based on the type we
want the list to contain.
We can't just call something like
 LinkedList(int) Of
 LinkedList(Integer) because
types can't be passed as parameters.
Parametric polymorphism is the
solution. Using this mechanism, we
can use type parameters to build a
```

"custom version" of a class from a general purpose class.

C++ allows this using its *template* mechanism. Pizza also allows type parameters.

In both languages, type parameters are enclosed in "angle brackets" (e.g., LinkedList<T> passes T, a type, to the LinkedList class).

In Pizza we have

```
class LinkedList<T> {
   T value; LinkedList<T> next;
   T head() {return value;}
   LinkedList<T> tail() {
      return next;}
   LinkedList(T O) {
      value = O; next = null;}
   LinkedList(T O,LinkedList<T> L)
      {value = O; next = L;}
}
```

When linked list objects are created (using new) no type qualifiers are needed—the type of the constructor's parameters are used. We can create

```
LinkedList<int> L1 =
    new LinkedList(123);
int i = L1.head();
LinkedList<String> L2 =
    new LinkedList("abc");
String s = L2.head();
LinkedList<LinkedList<int> > L3 =
    new LinkedList(L1);
int j = L3.head().head();
```

## **Bounded Polymorphism**

In Pizza we can use interfaces to bound the type parameters a class will accept.

```
Recall our compare interface:

interface Compare {

boolean lessThan(Object o1,

Object o2);

}

We can specify that a parameterized class will only takes types that implement Compare:

class LinkedList<T implements

Compare> { ... }
```

In fact, we can improve upon how interfaces are defined and used.

Recall that in method lessThan we had to use parameters declared as type object to be general enough to match (and accept) any object type. This leads to clumsy casting (with run-time correctness checks) when lessThan is implemented for a particular type:

```
Pizza allows us to parameterize class
definitions with type parameters, so
why not do the same for interfaces?
In fact, this is just what Pizza does.
We can now define compare as
interface Compare<T> {
  boolean lessThan(T o1, T o2);
Now we define class LinkedList as
class LinkedList<T implements</pre>
            Compare<T> > { ... }
Given this form of interface
definition, no casting (from type
Object) is needed in classes that
implement compare:
class IntCompare implements
  Compare<Integer> {
public boolean lessThan(Integer i1,
                         Integer i2){
 return i1.intValue() <</pre>
        i2.intValue();}
}
```

## First-class Functions in Pizza

In Java, functions are treated as constants that may appear only in classes.

To pass a function as a parameter, you must pass a class that contains that function as a member. For example,

```
class Fct {
  int f(int i) { return i+1; }
}
class Test {
  static int call(Fct g, int arg)
      { return g.f(arg); }
}
```

Changing the value of a function is even nastier. Since you can't assign to a member function, you have to use subclassing to override an existing definition:

```
class Fct2 extends Fct {
  int f(int i) { return i+111; }
}
```

Computing new functions during executions is nastier still, as Java doesn't have any notion of a lambdaterm (that builds a new function).

Pizza makes functions first-class, as in ML. You can have function parameters, variables and return values. You can also define new functions within a method.

The notation used to define the type of a function value is

$$(T_1, T_2, ...) -> T_0$$

This says the function will take the list  $(\mathbf{T}_1, \mathbf{T}_2, \ldots)$  as it arguments and will return  $\mathbf{T}_0$  as its result.

Thus

(int)->int

represents the type of a method like

int plus1(int i) {return i+1;}

The notation used by Java for fixed functions still works. Thus

static int f(int i){return 2\*i;};
denotes a function constant, f.

The definition

static (int)->int g = f; defines a field of type (int)->int named g that is initialized to the value of f.

The definition

defines a constant function that takes as parameters a function value of type (int)->int and an int value. It calls the function parameter with the int parameter and returns the value the function computes.

```
Pizza also has a notation for
anonymous functions (function
literals), similar to fn in ML and
lambda in Scheme. The notation
fun (T_1 a_1, T_2 a_2, ...) -> T_0
  {Body}
defines a nameless function with
arguments declared as (T_1 \ a_1, \ T_2 \ a_2,
...) and a result type of \mathbf{T}_0. The
function's body is computed by
executing the block {Body}.
For example,
static (int)->int compose(
  (int)->int f, (int)->int g){
   return fun (int i) -> int
    {return f(g(i));};
defines a method named compose. It
takes as parameters two functions, £
and g, each of type (int)->int.
```

The function returns a function as its result. The type of the result is (int)->int and its value is the composition of functions f and g: return f(g(i));
Thus we can now have a call like compose(f1,f2)(100)
Which computes f1(f2(100)).

With function parameters, some familiar functions can be readily programmed:

And we can make such operations polymorphic by using parametric polymorphism:

# Algebraic Data Types

Pizza also provides "algebraic data types" which allow a type to be defined as a number of cases. This is essentially the pattern-oriented approach we saw in ML.

A list is a good example of the utility of algebraic data types. Lists come in two forms, null and non-null, and we must constantly ask which form of list we currently have. With patterns, the need to consider both forms is enforced, leading to a more reliable programming style.

In Pizza, patterns are modeled as "cases" and grafted onto the existing switch statement (this formulation is a bit clumsy):

And guess what! We can use parametric polymorphism along with algebraic data types:

# Enumerations as Algebraic Data Types

We can use algebraic data types to obtain a construct missing from Java and Pizza—enumerations.

We simply define an algebraic data type whose constructors are not parameterized:

```
class Color {
  case Red;
  case Blue;
  case Green;
  String toString() {
    switch(this) {
    case Red: return "red";
    case Blue: return "blue";
    case Green: return "green";
  }
}
```

This approach is better than simply defining enumeration values as constant (final) integers:

```
final int Red = 1;
final int Blue = 2;
final int Green = 3;
```

With the algebraic data type approach, **Red**, **Blue** and **Green**, are not integers. They are constructors for the type **color**. This leads to more thorough type checking.

#### GJ—Generic Java

The Pizza project has lead to the development of GJ (Generic Java) an extension to Java that explicitly supports generics (type parameters) using parametric polymorphism.

The goals of GJ are

 Direct support for generics. Many Java data types are generic over some data type; this is especially common for reusable libraries such as collection classes.

GJ supports the use of such types, for instance allowing one to write the GJ type **vector**<string> as opposed to the Java type **vector**. With GJ, fewer casts are required, and the compiler catches more errors.

- GJ is a superset of the Java programming language. Every Java source program is still legal in GJ and retains the same meaning in GJ.
- The GJ compiler can be used as a Java compiler.
- GJ compiles into JVM (Java Virtual Machine) code, so GJ programs run on any Java platform, including Java compliant browsers.
- Class files produced by the GJ compiler can be freely mixed with those produced by other Java compilers.
- GJ is compatible with existing libraries. One can call *any* Java library function from GJ, and *any* GJ library function from Java. Further, where it

is sensible, one can assign GJ types (with type parameters) to existing Java libraries. For instance, the GJ type vector<string> is implemented by the existing Java library type vector.

- GJ supports efficient translation. GJ is translated by *erasure*: no information about type parameters is maintained at run-time. This means GJ code is pretty much identical to Java code for the same purpose, and equally efficient.
- The GJ system is freely available and fully documented. The GJ compiler is itself written in GJ, so it runs on any platform that supports Java. The GJ compiler is available for download,

and there is extensive documentation.

 GJ has been proposed (by Sun Microsystems) as the basis for the implementation of generics (type parameters) in the next major revision of Java.

# Reading Assignment

 Python Tutorial (linked from class web page)

#### Rosser Memorial Lecture

"Seas Of Cameras And Projectors For Tele-immersion And The Office Of The Future,"

presented by Professor Henry Fuchs, University of North Carolina, Thursday, May 3, 4 p.m., AB20 Weeks Hall (Geology)

## **Scripting Languages**

The languages we've seen so far are "complete" programming languages. They are designed to encode a complete program, perhaps with the assistance of library routines.

However, throughout the history of programming another sort of programming language has evolved (and flourished)—the scripting language.

Scripting languages evolved as simple tools to "glue" together existing programs and utilities.

When batch programming (rather than interactive programming) was dominant, command languages evolved to program the steps necessary to run a program.

## **JCL**

One of the most widely used command languages was IBM's *JCL* (Job Control Language). It was designed to "program" a batch operating system. It directed the steps required to put together a program and run it. A JCL program

- 1. Identified your job to the system.
- 2. Directed the execution of the program(s).
- 3. Described the devices (readers, printers, etc.) and data needed by the program(s).

The following example demonstrates the JCL necessary to run an assembler language program. The job's name is

MYPROG, and it belongs to Clem Kaddiddlehopper who wants to have the output returned to room 222.

## **Shell Scripts**

By today's standards JCL is crude indeed, but it did establish the notion of a specialized programming language used to "program" the steps of an operating system. These ideas evolved into the far more powerful shell scripts used by systems like Unix.

Many utility programs provided by Unix (and other operating systems) are not conventional programs compiled from C or C++. Instead, they are small shell scripts that tie together existing programs into new and useful forms.

#### Here is a typical Unix shell script:

```
# wl - run word count,
# then print (lpr) a set of files
#
# Usage: wl file1 [file2] ...
set T=/tmp/wl.$$ # temporary file
wc -l $* > $T # get line counts
lpr $T $* # print line counts,
# then files
rm $T # remove temporary file
```

Shell scripts are useful because they are more direct and concise than ordinary C or C++ programs.

Experienced Unix programmers prefer to build a new utility from existing ones rather than from scratch. It's much easier, faster, and far less error prone. Other scripting languages, like Python, can be used in shell scripts.

## JavaScript and VBScript

In the HTML that implements web pages it is often necessary to perform simple computations. You could, of course, write a Java applet, and call it, but this may be overkill.

Instead, you can use a simple scripting language that is directly executable by a web browser. Two major web-oriented scripting languages are JavaScript (by Sun Microsystems) and VBScript (by Microsoft).

JavaScript is not full Java; it is a distinct scripting language based (loosely) on Java. Similarly, VBScript isn't full Visual Basic, its a language based on it.

Let's look at a simple JavaScript script that counts the Wednesdays in a month (if that's of interest to you!)

```
<SCRIPT LANGUAGE="JavaScript">
<!-- Begin
var now = new Date();
var month = now.getMonth();
var date = now.getDate();
var day = now.getDay();
var year = now.getYear();
m = new Array("January", "February",
"March", "April", "May", "June", "July",
"August", "September", "October",
"November", "Decemeber");
d = new Array("Sunday", "Monday",
"Tuesday", "Wednesday", "Thursday",
"Friday", "Saturday");
if (year < 2000) year = year + 1900;
//End of Month Calculations
var monarr = new Array(31, 28, 31,
30, 31, 30, 31, 31, 30, 31, 30, 31);
// check for leap year
if (((year % 4 == 0) && (year % 100
!= 0)) || (year % 400 == 0))
monarr[1] = "29";
```

```
//Finds the First Day for this Month
while (date != 1){
date = date - 1;
day = day - 1;
if (day < 0) day = day + 7;
//Count # of Wed in this month
weekday = 0;
while (date != monarr[month]){
date = date + 1;
day = day + 1;
if (day > 6)
day = 7 - day;
if (d[day] == "Wednesday")
weekday = weekday + 1;
//Fix For Months beginning on a Wed
if (d[day] == "Wednesday") weekday =
weekday + 1;
document.write (m[month] +
" contains " + weekday + " " + d[3] +
"s");// End -->
</script>
```

Like most scripting languages, in JavaScript there are no variable type declarations; types are dynamic. Control structures and expressions look like those found in Java. Though not shown, functions are included.

The idea is to make it easy to add a bit of computation, while retaining most of the concepts and notation of conventional programming languages.

## **Python**

One of the newest and most innovative scripting languages is *Python*, developed by Guido van Rossum in the mid-90s. Python is named after the BBC "Monty Python" television series.

Python blends the expressive power and flexibility of earlier scripting languages with the power of object-oriented programming languages.

It offers a lot to programmers:

- An interactive development mode as well as an executable "batch" mode for completed programs.
- Very reasonable execution speed. Like Java, Python programs are compiled.
   Also like Java, the compiled code is in

an intermediate language for which an interpreter is written. Like Java this insulates Python from many of the vagaries of the actual machines on which it runs, giving it portability of an equivalent level to that of Java. Unlike Java, Python retains the interactivity for which interpreters are highly prized.

- Python programs require no compilation or linking. Nevertheless, the semi-compiled Python program still runs much faster than its traditionally interpreted rivals such as the shells, awk and perl.
- Python is freely available on almost all platforms and operating systems (Unix, Linux, Windows, MacOs, etc.)

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- Python is completely object oriented.
   It comes with a full set of objected oriented features.
- Python presents a first class object model with first class functions and multiple inheritance. Also included are classes, modules, exceptions and late (run-time) binding.
- Python allows a clean and open program layout. Python code is less cluttered with the syntactic "noise" of declarations and scope definitions. Scope in a Python program is defined by the *indentation* of the code in question. Python thus breaks with current language designs in that white space has now once again acquired significance.

- Like Java, Python offers automated memory management through runtime reference counting and garbage collection of unreferenced objects.
- Python can be embedded in other products and programs as a control language.
- Python's interface is well exposed and is reasonably small and simple.
- Python's license is truly public.
   Python programs can be used or sold without copyright restrictions.
- Python is extendable. You can dynamically load compiled Python, Python source, or even dynamically load new machine (object) code to provide new features and new facilities.

- Python allows low-level access to its interpreter. It exposes its internal plumbing to a significant degree to allow programs to make use of the way the plumbing works.
- Python has a rich set of external library services available. This includes, network services, a GUI API (based on tcl/Tk), Web support for the generation of HTML and the CGI interfaces, direct access to databases, etc.

# **Using Python**

Python may be used in either interactive or batch mode.

In interactive mode you start up the Python interpreter and enter executable statements. Just naming a variable (a trivial expression) evaluates it and echoes its value.

For example (>>> is the Python interactive prompt):

```
>>> 1
1
>>> a=1
>>> a
1
>>> b=2.5
>>> b
```

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```
>>> a+b
3.5
>>> print a+b
3.5
```

You can also incorporate Python statements into a file and execute them in batch mode. One way to do this is to enter the command

```
python file.py
```

where file.py contains the Python code you want executed. Be careful though; in batch mode you must use a print (or some other output statement) to force output to be printed. Thus

1 a=1

a

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b=2.5

b

a+b

print a+b

when run in batch mode prints only 3.5 (the output of the print statement).

You can also run Python programs as Unix shell scripts by adding the line #! /usr/bin/env python to the head of your Python file.

(Since # begins Python comments, you can also feed the same augmented file directly to the Python interpreter)

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# **Python Command Format**

In Python, individual primitive commands and expressions must appear on a single line.

This means that

does not assign 1+ь to a! Rather, it assigns 1 to a, then evaluates +ь.

If you wish to span more than one line, you must use \ to escape the line:

is equivalent to

$$a = 1 + b$$

Compound statements, like if statements and while loops, can span multiple lines, but individual statements within an if or while (if they are primitive) must appear one a single line.

Why this restriction?

With it, ; 's are mostly unnecessary!

A ; at the end of a statement is legal but usually unnecessary, as the end-of-line forces the statement to end.

You can use a ; to squeeze more than one statement onto a line, if you wish:

a=1; b=2; c=3

#### **Identifiers and Reserved Words**

Identifiers look much the same as in most programming languages. They are composed of letters, digits and underscores. Identifiers must begin with a letter or underscore. Case is significant. As in C and C++, identifiers that begin with an underscore often have special meaning.

Python contains a fairly typical set of reserved words:

```
del
                               raise
and
                 for
                        is
                        lambda
assert elif
                 from
                               return
break else
                 global not
                               try
class except
                 if
                               while
                        or
continue exec
                 import pass
def
        finally
                        print
                 in
```

#### **Numeric Types**

There are four numeric types:

- Integers, represented as a 32 bit (or longer) quantity. Digits sequences (possibly) signed are integer literals:
   1 -123 +456
- 2. Long integers, of unlimited precision. An integer literal followed by an 1 or L is a long integer literal:

  1234567890000000000000
- 3. Floating point values, represented as a 64 bit floating point number. Literals are of fixed decimal or exponential form:

123.456 1e10 6.0231023

4. Complex numbers, represented as a pair of floating point numbers. In complex literals j or j is used to

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denote the imaginary part of the complex value:

1.0+2.0j -22.1j 10e10J+20.0

There is no character type. A literal like 'a' or "a" denotes a string of length one.

There is no boolean type. A zero numeric value (any form), or **None** (the equivalent of void) or an empty string, list, tuple or dictionary is treated as false; other values are treated as true.

Hence

"abc" and "def"

is treated as true in an if, since both strings are non-empty.

## **Arithmetic Operators**

**Description** Exponentiation Unary plus **Unary minus** Bit-wise complement (int or long only) Multiplication Division Remainder Binary plus Binary minus Bit-wise left shift (int or long only) << Bit-wise right shift (int or long only) >> Bit-wise and (int or long only) & Bit-wise or (int or long only) Bit-wise Xor (int or long only)

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Less than

Greater than

>= Greater than or equal

Less than or equal

== Equal

! = Not equal

and Boolean and

or Boolean or

not Boolean not

#### **Operator Precedence Levels**

Listed from lowest to highest:

or Boolean OR

and Boolean AND

not Boolean NOT

<, <=, >, >=, <>, !=, == Comparisons

Bitwise OR

A Bitwise XOR

& Bitwise AND

<<, >> Shifts

+, - Addition and subtraction

\*, /, % Multiplication, division,

remainder

\*\* Exponentiation

+, - Positive, negative (unary)

Bitwise not

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## **Arithmetic Operator Use**

Arithmetic operators may be used with any arithmetic type, with conversions automatically applied. Bit-wise operations are restricted to integers and long integers. The result type is determined by the "generality" of the operands. (Long is more general than int, float is more general than both int and long, complex is the most general numeric type). Thus

```
>>> 1+2
3
>>> 1+111L
112L
>>> 1+1.1
2.1
>>> 1+2.0j
(1+2j)
```

Unlike almost all other programming languages, relational operators may be "chained" (as in standard mathematics).

**Therefore** 

$$a > b > c$$
  
Means (a > b) and (b > c)

## **Assignment Statements**

In Python assignment is a statement *not* an expression.

**Thus** 

$$a+(b=2)$$

is illegal.

Chained assignments are allowed:

$$a = b = 3$$

Since Python is dynamically typed, the type (and value) associated with an identifier can change because of an assignment:

```
>>> a = 0
>>> print a
0
>>> a = a + 0L
>>> print a
```

0L
>>> a = a + 0.0
>>> print a
0.0
>>> a = a + 0.0J
>>> print a
0j

#### If and While Statements

Python contains if and while statements that are fairly similar to those found in C and Java.

There are some significant differences though.

A line that contains an if, else or while ends in a ":". Thus we might write:

Moreover the indentation of the then part is *significant*! You don't need { and } in Python because all statements indented at the same level are assumed to be part of the same block.

In the following Python statements

if a>0: b=1 c=2

d=3

the assignments to b and c constitute then part; the assignment to a follows the if statement, and is independent of it. In interactive mode a blank line is needed to allow the interpreter to determine where the if statement ends; this blank line is not needed in batch mode.

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#### The if Statement

The full form of the if statement is
if expression:
 statement(s)
elif expression:
 statement(s)
...
else:
 statement(s)

Note those pesky: 's at the end of the if, elif and else lines. The expressions following the if and optional elif lines are evaluated until one evaluates to true. Then the following statement(s), delimited by indentation, are executed. If no expression evaluates to true, the statements following the else are executed.

Use of else and elif are optional; a "bare" if may be used.

If any of the lists of statements is to be null, use pass to indicate that nothing is to be done.

For example

```
if a>0:
    b=1
elif a < 0:
    pass
else
    b=0</pre>
```

This if sets b to 1 if a is > 0; it sets b to 0 if a == 0, and does nothing if a < 0.

#### While Loops

Python contains a fairly conventional while loop:

```
while expression: body
```

Note the ":" that ends the header line. Also, indentation delimits the body of the loop; no braces are needed. For example,

```
>>> a=0; b=0
>>> while a < 5:
... b = b+a**2
... a= a+1
...
>>> print a,b
5 30
```

# Break, Continue and Else in Loops

Like C, C++ and Java, Python allows use of **break** within a loop to force loop termination. For example,

```
>>> a=1
>>> while a < 10:
... if a+a == a**2:
... break
... else:
... a=a+1
...
>>> print a
```

A continue may be used to force the next loop iteration:

```
>>> a=1
>>> while a < 100:
... a=a+1
... if a%2==0:
... continue
... a=3*a
...
>>> print a
105
```

Python also allows you to add an else clause to a while (or for) loop. The syntax is while expression:

body
else:

statement(s)

The else statements are executed when the termination condition becomes false, but not when the loop is terminated with a break. As a result, you can readily program "search loops" that need to handle the special case of search failure:

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## **Sequence Types**

Python includes three *sequence types:* strings, tuples and lists. All sequence types may be indexed, using a very general indexing system.

Strings are sequences of characters; tuples and lists may contain any type or combination of types (like Scheme lists).

Strings and tuples are *immutable* (their components may not be changed). Lists *are* mutable, and be updated, much like arrays.

Strings may be delimited by either a single quote (') or a double quote (") or even a triple quote (''' or """). A given string must start and stop with the same delimiter. Triply quoted strings may span multiple lines. There

is no character type or value; characters are simply strings of length 1. Legal strings include

```
'abc' "xyz" '''It's OK!'''
```

Lists are delimited by "[" and "]".
Empty (or null lists) are allowed. Valid list literals include

```
[1,2,3] ["one",1]
[['a'],['b'],['c']] []
```

Tuples are a sequence of values separated by commas. A tuple may be enclosed within parentheses, but this isn't required. A empty tuple is (). A singleton tuple ends with a comma (to distinguish it from a simple scalar value).

Thus (1,) or just 1, is a valid tuple of length one.

## **Indexing Sequence Types**

Python provides a very general and powerful indexing mechanism. An index is enclosed in brackets, just like a subscript in C or Java. Indexing starts at 0.

Thus we may have

```
>>> 'abcde'[2]
'c'
>>> [1,2,3,4,5][1]
2
>>> (1.1,2.2,3.3)[0]
1.1
```

Using an index that's too big raises an IndexError exception:

```
>>> 'abc'[3]
IndexError: string index out of
range
```

Unlike most languages, you can use negative index values; these simply index from the right:

```
>>> 'abc'[-1]
'c'
>>> [5,4,3,2,1][-2]
2
>>> (1,2,3,4)[-4]
1
```

You may also access a *slice* of a sequence value by supplying a *range* of index values. The notation is

```
data[i:j]
```

which selects the values in data that are >=i and < j. Thus

```
>>> 'abcde'[1:2]
'b'
>>> 'abcde'[0:3]
'abc'
```

```
>>> 'abcde'[2:2]
```

You may *omit* a lower or upper bound on a range. A missing lower bound defaults to 0 and a missing upper bound defaults to the maximum legal index. For example,

```
>>> [1,2,3,4,5][2:]
[3, 4, 5]
>>> [1,2,3,4,5][:3]
[1, 2, 3]
```

An upper bound that's too large in a range is interpreted as the maximum legal index:

```
>>> 'abcdef'[3:100]
'def'
```

You may use negative values in ranges too—they're interpreted as being relative to the right end of the sequence:

```
>>> 'abcde'[0:-2]
'abc'
>>> 'abcdefg'[-5:-2]
'cde'
>>> 'abcde'[-3:]
'cde'
>>> 'abcde'[:-1]
'abcd'
```

Since arrays may be assigned to, you may assign a slice to change several values at once:

```
>>> a=[1,2,3,4]
>>> a[0:2]=[-1,-2]
>>> a
[-1, -2, 3, 4]
>>> a[2:]=[33,44]
>>> a
[-1, -2, 33, 44]
```

The length of the value assigned to a slice *need not* be the same size as the slice itself, so you can shrink or expand a list by assigning slices:

```
>>> a=[1,2,3,4,5]
>>> a[2:3]=[3.1,3.2]
>>> a
[1, 2, 3.1, 3.2, 4, 5]
>>> a[4:]=[]
>>> a
[1, 2, 3.1, 3.2]
>>> a
[1, 2, 3.1, 3.2]
>>> a[:0]=[-3,-2,-1]
>>> a
[-3, -2, -1, 1, 2, 3.1, 3.2]
```

# Other Operations on Sequences

Besides indexing and slicing, a number of other useful operations are provided for sequence types (strings, lists and tuples).

#### These include:

```
+ (catenation):
>>> [1,2,3]+[4,5,6]
[1, 2, 3, 4, 5, 6]
>>> (1,2,3)+(4,5)
(1, 2, 3, 4, 5)
>>> (1,2,3)+[4,5]
TypeError: illegal argument
type for built-in operation
>>> "abc"+"def"
'abcdef'
```

```
• * (Repetition):
  >>> 'abc'*2
  'abcabc'
  >>> [3,4,5]*3
  [3, 4, 5, 3, 4, 5, 3, 4, 5]
• Membership (in, not in)
  >>> 3 in [1,2,3,4]
  1
  >>> 'c' in 'abcde'
  1
• max and min:
  >>> max([3,8,-9,22,4])
  22
  >>> min('aa','bb','abc')
   'aa'
```

## **Operations on Lists**

As well as the operations available for all sequence types (including lists), there are many other useful operations available for lists. These include:

• count (Count occurrences of an item in a list):

```
>>> [1,2,3,3,21].count(3)
2
```

• index (Find first occurrence of an item in a list):

```
>>> [1,2,3,3,21].index(3)
2
>>> [1,2,3,3,21].index(17)
ValueError: list.index(x): x
not in list
```

• remove (Find and remove an item from a list):

```
>>> a=[1,2,3,4,5]
>>> a.remove(4)
>>> a
[1, 2, 3, 5]
>>> a.remove(17)
ValueError: list.remove(x): x
not in list
```

• pop (Fetch and remove i-th element of a list):

```
>>> a=[1,2,3,4,5]
>>> a.pop(3)
4
>>> a
[1, 2, 3, 5]
>>> a.pop()
5
>>> a
[1, 2, 3]
```

• reverse a list:

```
>>> a=[1,2,3,4,5]
>>> a.reverse()
>>> a
[5, 4, 3, 2, 1]
```

• sort a list:

• Create a range of values:

```
>>> range(1,5)
[1, 2, 3, 4]
>>> range(1,10,2)
[1, 3, 5, 7, 9]
```

#### **Dictionaries**

Python also provides a dictionary type (sometimes called an associative array). In a dictionary you can use a number (including a float or complex), string or tuple as an index. In fact any immutable type can be an index (this excludes lists and dictionaries).

```
An empty dictionary is denoted { }.

A non-empty dictionary may be written as { key1:value1, key2:value2, ... }

For example, c={ 'bmw':540, 'lexus':'sc 430', 'porsche':'boxster'}
```

You can use a dictionary much like an array, indexing it using keys, and updating it by assigning a new value to a key:

```
>>> c['bmw']
540
>>> c['bmw']='m5'
>>> c['honda']='accord'
You can delete a value using del:
>>> del c['honda']
>>> c['honda']
KeyError: honda
```

You can also check to see if a given key is valid, and also list all keys, values, or key-value pairs in use:

```
>>> c.has_key('edsel')
0
>>> c.keys()
['bmw', 'porsche', 'lexus']
>>> c.values()
['m5', 'boxster', 'sc 430']
>>> c.items()
[('bmw', 'm5'), ('porsche', 'boxster'), ('lexus', 'sc 430')]
```

### For Loops

In Python's **for** loops, you don't explicitly control the steps of an iteration. Instead, you provide a sequence type (a string, list or sequence), and Python *automatically* steps through the values.

Like a while loop, you must end the for loop header with a ":" and the body is delimited using indentation. For example,

```
>>> for c in 'abc':
... print c
...
a
b
c
```

The range function, which creates a list of values in a fixed range is useful in for loops:

```
>>> a=[5,2,1,4]
>>> for i in range(0,len(a)):
... a[i]=2*a[i]
...
>>> print a
[10, 4, 2, 8]
```

You can use an else with for loops too. Once the values in the specified sequence are exhausted, the else is executed unless the for is exited using a break. For example,

```
for i in a:
    if i < 0:
        print 'Neg val:',i
        break
else:
        print 'No neg vals'</pre>
```

#### **Function Definitions**

Function definitions are of the form

```
def name(args):
    body
```

The symbol def tells Python that a function is to be defined. The function is called name and args is a tuple defining the names of the function's arguments. The body of the function is delimited using indentation. For example,

```
def fact(n):
    if n<=1:
        return 1
    else:
        return n*fact(n-1)
>>> fact(5)
120
>>> fact(20L)
```

# 2432902008176640000L >>> fact(2.5) 3.75 >>> fact(2+1J) (1+3j)

Scalar parameters are passed by value; mutable objects are allocated in the heap and hence are passed (in effect) by reference:

```
>>> def asg(ar):
... a[1]=0
... print ar
...
>>> a=[1,2,3,4.5]
>>> asg(a)
[1, 0, 3, 4.5]
```

Arguments may be given a *default* value, making them *optional* in a call. Optional parameters must follow required parameters in definitions. For example,

```
>>> def expo(val,exp=2):
... return val**exp
...
>>> expo(3,3)
27
>>> expo(3)
9
>>> expo()
TypeError: not enough arguments;
expected 1, got 0
```

A variable number of arguments is allowed; you prefix the last formal parameter with a \*; this parameter is bound to a tuple containing all the actual parameters provided by the caller:

```
>>> def sum(*args):
... sum=0
... for i in args:
... sum=sum+i
... return sum
...
>>> sum(1,2,3)
6
>>> sum(2)
2
>>> sum()
0
```

You may also use the name of formal parameters in a call, making the order of parameters less important:

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# **Scoping Rules in Functions**

Each function body has its own local namespace during execution. An identifier is resolved (if possible) in the local namespace, then (if necessary) in the global namespace.

#### Thus

```
>>> def f():
... a=11
... return a+b
...
>>> b=2;f()
13
>>> a=22;f()
13
>>> b=33;f()
44
```

Assignments are to local variables, even if a global exists. To *force* an assignment to refer to a global identifier, you use the declaration

```
global id
```

which tells Python that in this function is should be considered global rather than local. For example,

```
>>> a=1;b=2
>>> def f():
... global a
... a=111;b=222
...
>>> f();print a,b
111 2
```

# Other Operations on Functions

Since Python is interpreted, you can dynamically create and execute Python code.

The function eval(string) interprets string as a Python expression (in the current execution environment) and returns what is computed. For example,

```
>>> a=1;b=2
>>> eval('a+b')
3
```

exec(string) executes string as
arbitrary Python code (in the current
environment):

```
>>> a=1;b=2
>>> exec('for op in "+-*/":
print(eval("a"+op+"b"))')
3
-1
2
0
```

execfile(string) executes the contents of the file whose pathname is specified by string. This can be useful in loading an existing set of Python definitions.

#### The expression

lambda args: expression
creates an anonymous function with
args as its argument list and
expression as it body. For example,
>>> (lambda a:a+1)(2)

And there are definitions of map, reduce and filter to map a function to a list of values, to reduce a list (using a binary function) and to select values from a list (using a predicate):

```
>>> def double(a):
... return 2*a;
...
>>> map(double,[1,2,3,4])
[2, 4, 6, 8]
```

```
>>> def sum(a,b):
... return a+b
...
>>> reduce(sum,[1,2,3,4,5])
15
>>> def even(a):
... return not(a%2)
...
>>> filter(even,[1,2,3,4,5])
[2, 4]
```

# I/O in Python

The easiest way to print information in Python is the print statement. You supply a list of values separated by commas. Values are converted to strings (using the str() function) and printed to standard out, with a terminating new line automatically included. For example,

```
>>> print "1+1=",1+1
1+1= 2
```

If you don't want the automatic end of line, add a comma to the end of the print list:

```
>>> for i in range(1,11):
... print i,
...
1 2 3 4 5 6 7 8 9 10
```

For those who love C's printf, Python provides a nice formatting capability using a printf-like notation. The expression

format % tuple

formats a tuple of values using a format string. The detailed formatting rules are those of C's printf. Thus

#### File-oriented I/O

```
You open a file using
open(name, mode)
which returns a "file object."
name is a string representing the file's
path name; mode is a string
representing the desired access
mode('r' for read, 'w' for write,
etc.).
Thus
>>> f=open("/tmp/f1","w");
>>> f
<open file '/tmp/f1', mode 'w' at</pre>
decd8>
opens a temp file for writing.
The command
 f.read(n)
reads n bytes (as a string).
```

f.read() reads the whole file into a string. At end-of-file, f.read returns the null string:

```
>>> f = open("/tmp/ttt","r")
>>> f.read(3)
'aaa'
>>> f.read(5)
' bbb '
>>> f.read()
'ccc\012ddd eee fff\012g h i\012'
>>> f.read()
'!
f.readline() reads a whole line of input, and f.readlines() reads the
```

f.readline() reads a whole line of input, and f.readlines() reads the whole input file into a list of strings:

```
>>> f = open("/tmp/ttt","r")
>>> f.readline()
'aaa bbb ccc\012'
>>> f.readline()
```

```
'ddd eee fff\012'
>>> f.readline()
'g h i\012'
>>> f.readline()
>>> f = open("/tmp/ttt","r")
>>> f.readlines()
['aaa bbb ccc\012', 'ddd eee
fff\012', 'g h i\012']
f.write(string) Writes a string
to file object f; f.close() closes a
file object:
>>> f = open("/tmp/ttt","w")
>>> f.write("abcd")
>>> f.write("%d %d"%(1,-1))
>>> f.close()
>>> f = open("/tmp/ttt","r")
>>> f.readlines()
['abcd1 -1']
```

# Classes in Python

Python contains a class creation mechanism that's fairly similar to what's found in C++ or Java.

There are significant differences though:

- All class member are public.
- Instance fields aren't declared. Rather, you just create data fields as needed by assignment (often in constructors).
- There are class fields (shared by all class instances), but there are no class methods. That is, all methods are instance methods.

• All instance methods (including constructors) must explicitly provide an initial parameter that represents the object instance. This parameter is typically called self. It's roughly the equivalent of this in C++ or Java.

# **Defining Classes**

You define a class by executing a class definition of the form

class name:

statement(s)

A class definition creates a class object from which class instances may be created (just like in Java). The statements within a class definition may be data members (to be shared among all class instances) as well as function definitions (prefixed by a def command). Each function must take (at least) an initial parameter that represents the class instance within which the function (instance method) will operate. For example,

```
class Example:
    cnt=1
    def msg(self):
        print "Bo"+"o"*Example.cnt+
        "!"*self.n
>>> Example.cnt
1
>>> Example.msg
<unbound method Example.msg>
```

**Example.msg** is unbound because we haven't created any instances of the **Example** class yet.

We create class instances by using the class name as a function:

```
>>> e=Example()
>>> e.msg()
AttributeError: n
```

We get the AttributeError message regarding n because we haven't defined n yet! One way to do

this is to just assign to it, using the usual field notation:

```
>>> e.n=1
>>> e.msg()
Boo!
>>> e.n=2;Example.cnt=2
>>> e.msg()
Booo!!
```

We can also call an instance method by making the class object an explicit parameter:

```
>>> Example.msg(e)
Booo!!
```

It's nice to have data members initialized when an object is created. This is usually done with a constructor, and Python allows this too.

A special method named \_\_init\_\_ is called whenever an object is created. This method takes self as its first parameter; other parameters (possibly made optional) are allowed.

We can therefore extend our **Example** class with a constructor:

You can also define the equivalent of Java's tostring method by defining a member function named

```
\_\_str\_\_(self).
```

For example, if we add

```
def __str__(self):
    return "<%d>"%self.n
```

to Example,

then we can include **Example** Objects in **print** Statements:

```
>>> e=Example(2)
```

>>> print e

<2>

#### **Inheritance**

Like any language that supports classes, Python allows inheritance from a parent (or base) class. In fact, Python allows *multiple inheritance* in which a class inherits definitions from more than one parent.

When defining a class you specify parents classes as follows:

class name(parent classes):
 statement(s)

The subclass has access to its own definitions as well as those available to its parents. All methods are virtual, so the most recent definition of a method is always used.

```
class C:
    def DoIt(self):
        self.PrintIt()
    def PrintIt(self):
        print "C rules!"

class D(C):
    def PrintIt(self):
        print "D rules!"
    def TestIt(self):
        self.DoIt()

dvar = D()
    dvar.TestIt()
```

If you specify more than one parent for a class, lookup is depth-first, left to right, in the list of parents provided. For example, given

class A(B,C): ...

we first look for a non-local definition in **B** (and its parents), then in **c** (and its parents).

# Operator Overloading

You can overload definitions of all of Python's operators to apply to newly defined classes. Each operator has a corresponding method name assigned to it. For example, + uses \_\_add\_\_, - uses \_\_sub\_\_, etc.

```
Given
class Triple:
 def init (self,A=0,B=0,C=0):
   self.a=A
   self.b=B
   self.c=C
 def __str__(self):
   return "(%d,%d,%d)"%
    (self.a,self.b,self.c)
 def __add__(self,other):
   return Triple(self.a+other.a,
    self.b+other.b,
    self.c+other.c)
the following code
t1=Triple(1,2,3)
t2=Triple(4,5,6)
print t1+t2
produces
(5,7,9)
```

# **Exceptions**

Python provides an exception mechanism that's quite similar to the one used by Java.

You "throw" an exception by using a raise statement:

raise exceptionValue

There are numerous predefined exceptions, including OverflowError (arithmetic overflow), EOFError (when end-of-file is hit), NameError (when an undeclared identifier is referenced), etc.

You may define your own exceptions as subclasses of the predefined class **Exception**:

```
class badValue(Exception):
   def __init__(self,val):
     self.value=val
```

You catch exceptions in Python's version of a **try** statement:

```
try:
    statement(s)
except exceptionName1, id1:
    statement(s)
...
```

except exceptionName<sub>n</sub>, id<sub>n</sub>:
 statement(s)

As was the case in Java, an exception raised within the try body is handled by an except clause if the raised exception matches the class named in

the except clause. If the raised exception is not matched by any except clause, the next enclosing try is considered, or the exception is reraised at the point of call.

For example, using our badvalue exception class,

```
def sqrt(val):
    if val < 0.0:
        raise badValue(val)
    else:
        return cmath.sqrt(val)

try:
    print "Ans =",sqrt(-123.0)
except badValue,b:
    print "Can't take sqrt of",
        b.value

When executed, we get
Ans = Can't take sqrt of -123.0</pre>
```

#### **Modules**

Python contains a module feature that allows you to access Python code stored in files or libraries. If you have a source file mydefs.py the command

import mydefs

will read in all the definitions stored in the file. What's read in can be seen by executing

dir(mydefs)

To access an imported definition, you qualify it with the name of the module. For example,

mydefs.fct

accesses for which is defined in module mydefs.

To avoid explicit qualification you can use the command

from modulename import id<sub>1</sub>, id<sub>2</sub>, ...

This makes id, id, ... available without qualification. For example,

```
>>> from test import sqrt
>>> sqrt(123)
(11.0905365064+0j)
```

You can use the command

trom modulename import \*
to import (without qualification) all
the definitions in modulename.

# The Python Library

One of the great strengths of Python is that it contains a vast number of modules (at least several hundred) known collectively as the *Python Library*. What makes Python really useful is the range of prewritten modules you can access. Included are network access modules, multimedia utilities, data base access, and much more.

See

www.python.org/doc/lib
for an up-to-date listing of what's
available.