

Notes 1

Thursday, February 8, 2024 1:11 PM

Division

compute all x values in A which are disqualified then remove them from A
 An x value is disqualified if we attaching a y value from B, we obtain a tuple <x,y> that is not in A
 compute disqualified tuples

$\pi_x((\pi_x(A) \times B) - A)$
 compute non disqualified x values

$\pi_x(A) - \pi_x((\pi_x(A) \times B) - A)$
 x col projected get x values / column projected

example

$\pi_x(A) \times B$
 $\begin{array}{cc} s_1 & p_2 \\ s_2 & p_2 \\ s_3 & p_2 \\ s_4 & p_4 \end{array} \rightarrow \begin{array}{cc} s_1 & p_2 \\ s_2 & p_2 \\ s_3 & p_2 \\ s_4 & p_4 \end{array} \rightarrow \text{call C}$
 $C - A = \{ \emptyset \}$ empty relation

$\pi_x(A) - (\text{no x values}) = \pi_x(A)$
 all x values in A

example 2

$\pi_x((\pi_x(A) \times B) - A)$
 $\pi_x(A) \times B$
 $\begin{array}{cc} s_1 & p_2 \\ s_2 & p_4 \\ s_3 & p_4 \\ s_4 & p_4 \end{array} \Rightarrow \begin{array}{cc} s_1 & p_2 \\ s_1 & p_4 \\ s_2 & p_2 \\ s_2 & p_4 \\ s_3 & p_2 \\ s_3 & p_4 \\ s_4 & p_2 \\ s_4 & p_4 \end{array} \xrightarrow{\text{Subtract A}} \begin{array}{cc} s_2 & p_4 \\ s_3 & p_4 \end{array} \text{ call D}$
 now do $\pi_x(A) - \pi_x(D) \Rightarrow \begin{array}{cc} s_1 & s_2 \\ s_2 & s_3 \\ s_3 & s_4 \\ s_4 & \end{array} \Rightarrow \boxed{\begin{array}{c} s_1 \\ s_4 \end{array}}$

example 3

$\pi_x(A) - \pi_x((\pi_x(A) \times B) - A)$
 $\pi_x(A) \times B$
 $\begin{array}{cc} s_1 & p_1 \\ s_2 & p_2 \\ s_3 & p_4 \\ s_4 & p_4 \end{array} \rightarrow \begin{array}{cc} s_1 & p_1 \\ s_2 & p_2 \\ s_1 & p_4 \\ s_2 & p_1 \\ s_2 & p_2 \\ s_2 & p_4 \\ s_3 & p_1 \\ s_3 & p_2 \end{array} \xrightarrow{-A} \begin{array}{cc} s_2 & p_1 \\ s_3 & p_1 \\ s_4 & p_1 \end{array} \text{ call E}$
 do $\pi_x(A) - \pi_x(E)$
 $\begin{array}{cc} s_1 & s_2 \\ s_2 & s_3 \\ s_3 & s_4 \end{array} \rightarrow \boxed{\begin{array}{c} s_1 \end{array}}$
 Answer: $\boxed{\begin{array}{cc} s_1 & p_1 \\ s_2 & p_2 \\ s_3 & p_4 \\ s_4 & p_4 \end{array}}$

Q1 get list of all sid where bid is 103 from Reserves

$\pi_{sid}(\sigma_{bid=103}(\text{Reserves})) \bowtie \text{Sailors}$
 or
 $\pi_{sid}(\sigma_{bid=103}(\pi_{sid}(\text{Reserves}) \bowtie \text{Sailors}))$

Q2 don't try to do a join on full tables that is an expensive action
 try to do selection on tables to make them smaller

$\pi_{sid}(\sigma_{color='Red'}(\text{Boats}) \bowtie \text{Reserves} \bowtie \text{Sailors})$

Method 2

$\pi_{sid}(\pi_{sid}(\sigma_{color='Red'}(\text{Boats}) \bowtie \text{Reserves}) \bowtie \text{Sailors})$
 project sid to check with sailers

Q3 Select ~~boat~~ tuples from Sailors \rightarrow project sid A
 \downarrow
 natural join with Reserves \rightarrow project bid B

natural join with Boats \rightarrow project name C
output (C)

$$\pi_{name} \left(\pi_{bid} \left(\left(\pi_{sid \mid sname = 'Lubber'} (Sailors) \right) \bowtie Reserves \right) \bowtie Boats \right)$$

(A)
(B)
(C)

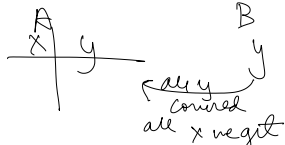
Q4 natural join of Sailors & Reserves has only those tuples which are there in the fields for both the relations & relations match
So ~~no~~ do $\pi_{name} (Sailors \bowtie Reserves)$

Q5 names of red or green
 $\pi_{Temp} (\sigma_{color = 'red'} (Boats) \cup (\sigma_{color = 'green'} (Boats)))$
Temp contains those tuples (with no projections) which have red or green boats
Now project out of result of Temp
 $\pi_{name} (Temp \bowtie Reserves \bowtie Sailors)$

Method 2
 $\pi_{name} (\pi_{Temp} (\sigma_{color = 'red' \vee color = 'green'} (Boats)))$
 $\pi_{name} (Temp \bowtie Reserves \bowtie Sailors)$

Q6 AND
 $\pi_{Temp} (\sigma_{color = 'red' \wedge color = 'green'} (Boats))$
 $\pi_{name} (Temp \bowtie Reserves \bowtie Sailors)$
Correct
 $\pi_{Temp1} (\pi_{sid} (\sigma_{color = 'red'} (Boats) \bowtie Reserves))$
 $\pi_{Temp2} (\pi_{sid} (\sigma_{color = 'green'} (Boats) \bowtie Reserves))$
 $\pi_{name} ((Temp1 \bowtie Temp2) \bowtie Sailors)$

Q8 division \rightarrow get $\left[\begin{array}{l} \text{all from A} \\ \text{where every } y \text{ in B is covered in those } x \end{array} \right]$



2 columns from Reserves \rightarrow one col from boat

get only one column from Reserves where we have an sid which is collection of all bid
return all sid \rightarrow only one first col
then we get sid \rightarrow then we get name after doing a natural join

Q9 first select all attributes in relation B
 $\begin{array}{c} A \\ x, y \end{array} \leftarrow \begin{array}{c} B \\ y \end{array}$ Compute not all y in B but only specific y
(n)

Relational Calculus

Relational algebra: ~~non~~ procedural
Relational calculus: nonprocedural / declarative
Allows us to describe the set of answers without being explicit about how they should be computed
Tuple Relational Calculus used in SQL
Domain Relational Calculus used in DQE
Query by language \rightarrow a database query language

Tuple Relational Calculus
A tuple variable takes on tuples of a relation as its values

$\{T \mid \phi(T)\}$ query form

① $\{S \mid S \in Sailors \wedge S.rating > 7\}$

② $\{P \mid \exists S \in Sailors (S.rating > 7 \wedge P.name = S.name)$

- \wedge Page = > age)

$$\textcircled{3} \{ p \mid \exists R \in \text{Reserves} \exists S \in \text{Sailors} (R.sid = S.sid \wedge p.name = S.name \wedge p.day = R.day \wedge p.bid = R.bid) \}$$

Domain Relational Calculus

A domain variable takes on / ranges over the values in the domain of some attribute

DRC query form

$$\{ \langle x_1, x_2, \dots, x_n \rangle \mid \phi(\langle x_1, x_2, \dots, x_n \rangle) \}$$

$$\textcircled{1} \{ \langle INTA \rangle \mid \langle INTA \rangle \in \text{Sailors} \wedge T \geq 7 \}$$

$$\textcircled{2} \{ \langle N \rangle \mid \exists I, T, A (\langle INTA \rangle \in \text{Sailors} \wedge \exists I_r, Br, D (\langle I_r, Br, D \rangle \in \text{Reserves} \wedge I_r = I \wedge Br = 103)) \}$$

$$\{ \langle N \rangle \mid \exists I, T, A (\langle I, T, A \rangle \in \text{Sailors} \wedge \exists (I_r, Br, D) \in \text{Reserves} (I_r = I \wedge Br = 103)) \}$$

$$\{ \langle T \rangle \mid \exists I, T, A (\langle INTA \rangle \in \text{Sailors} \wedge \exists D (\langle I, 103, D \rangle \in \text{Reserves})) \}$$

$$\textcircled{3} \{ p \mid \exists S \in \text{Sailors} \exists R \in \text{Reserves} (R.sid = S.sid \wedge R.bid = 103 \wedge p.sname = S.sname) \}$$

$$\textcircled{4} \{ p \mid \exists S \in \text{Sailors} \exists R \in \text{Reserves} (R.sid = S.sid \wedge p.sname = S.sname) \wedge \exists B \in \text{Boats} (B.bid = R.bid \wedge B.color = 'red') \}$$

$$\textcircled{4} \{ \langle N \rangle \mid \exists I, T, A (\langle INTA \rangle \in \text{Sailors} \wedge \exists \langle I_r, Br \rangle \in \text{Reserves} \wedge \exists \langle Br, BN, 'red' \rangle \in \text{Boats}) \}$$

$$\textcircled{5} \{ p \mid \exists S \in \text{Sailors} \exists R_1 \in \text{Reserves} \exists R_2 \in \text{Reserves} (S.sid = R_1.sid \wedge R_1.sid = R_2.sid \wedge R_1.bid \neq R_2.bid \wedge p.sname = S.sname) \}$$

$$\textcircled{5} \{ \langle N \rangle \mid \exists I, T, A (\langle INTA \rangle \in \text{Sailors} \wedge \exists Br_1, Br_2, D_1, D_2 (\langle I, Br_1, D_1 \rangle \in \text{Reserves} \wedge \langle I, Br_2, D_2 \rangle \in \text{Reserves} \wedge Br_1 \neq Br_2)) \}$$

$$\textcircled{6} \{ p \mid \exists S \in \text{Sailors} \forall B \in \text{Boats} (\exists R \in \text{Reserves} (S.sid = R.sid \wedge R.bid = B.bid \wedge p.sname = S.sname)) \}$$

$$\textcircled{6} \{ \langle N \rangle \mid \exists I, T, A (\langle INTA \rangle \in \text{Sailors} \wedge \forall B, BN, C (\neg (\langle B, BN, C \rangle \in \text{Boats}) \vee (\exists \langle I_r, Br, D \rangle \in \text{Reserves} (I = I_r \wedge Br = B)))) \}$$