



An operational semantics of interactions for verifying partially observed executions of distributed systems

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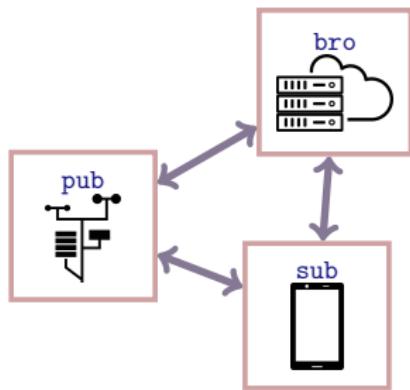


DisTA





Distributed Systems

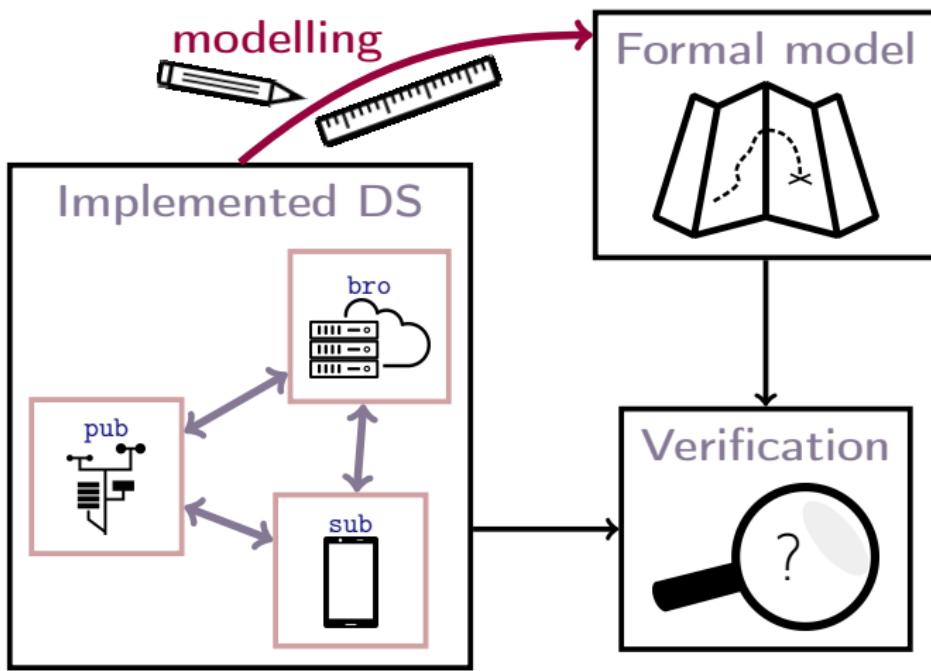


- ▶ distant machines (no global clock)
- ▶ asynchronous message passing

← MQTT example (publish/subscribe)

Formal analysis for increasing the quality of DSs

- ▶ allows verifying intractably (for humans) complex properties
- ▶ automatizable





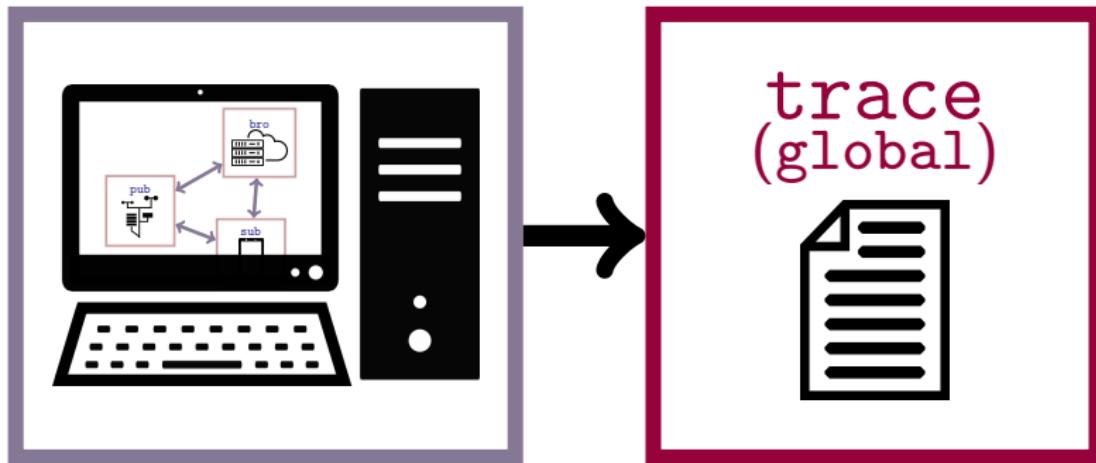
What can be verified ? Executions

- ▶ observing & logging events during execution
- ▶ different architectures
(Francalanza, Perez & Sanchez 2018)



Different architectures for observation

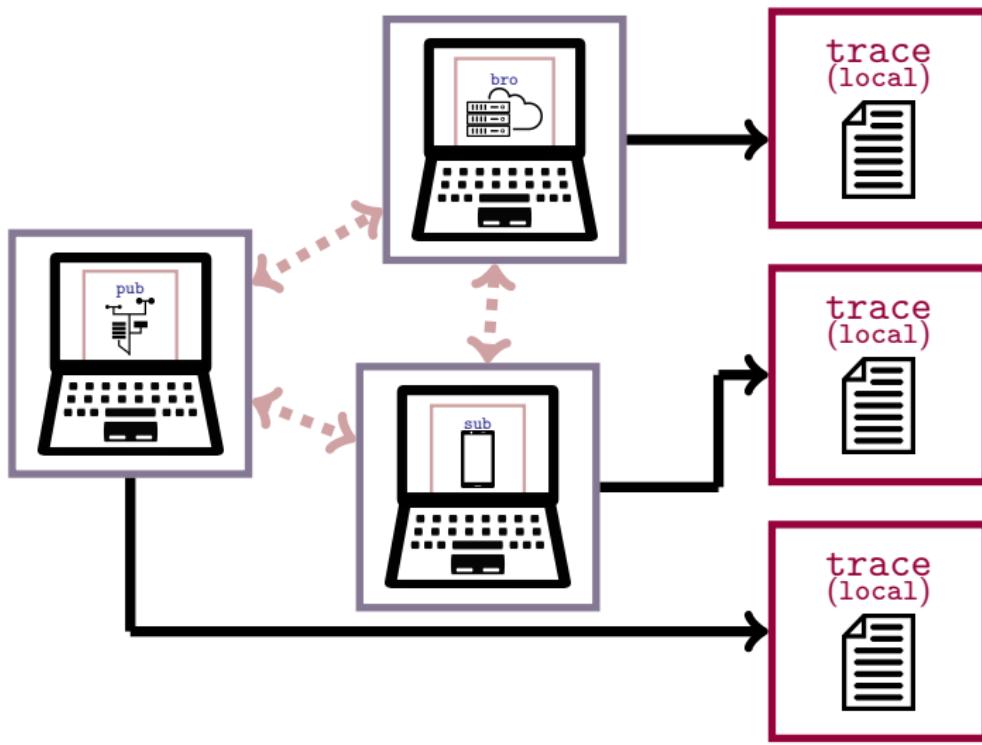
- ▶ centralized case (single machine):





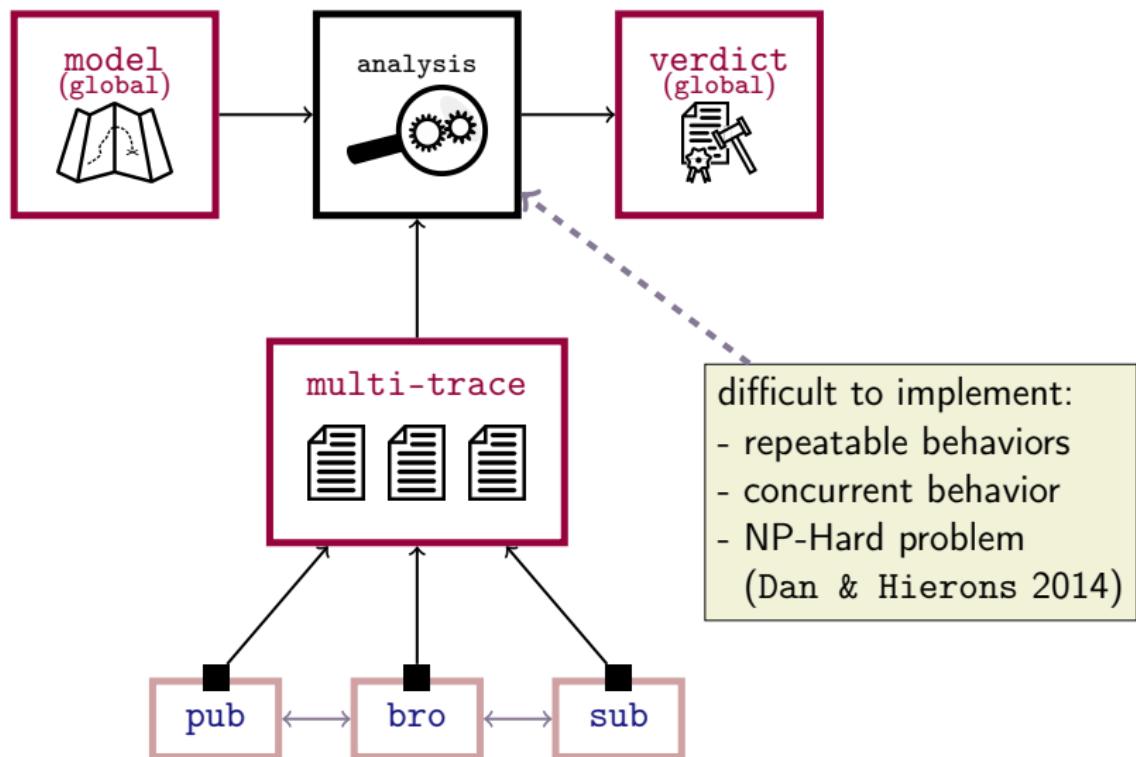
Different architectures for observation

- ▶ distributed case (distant machines):





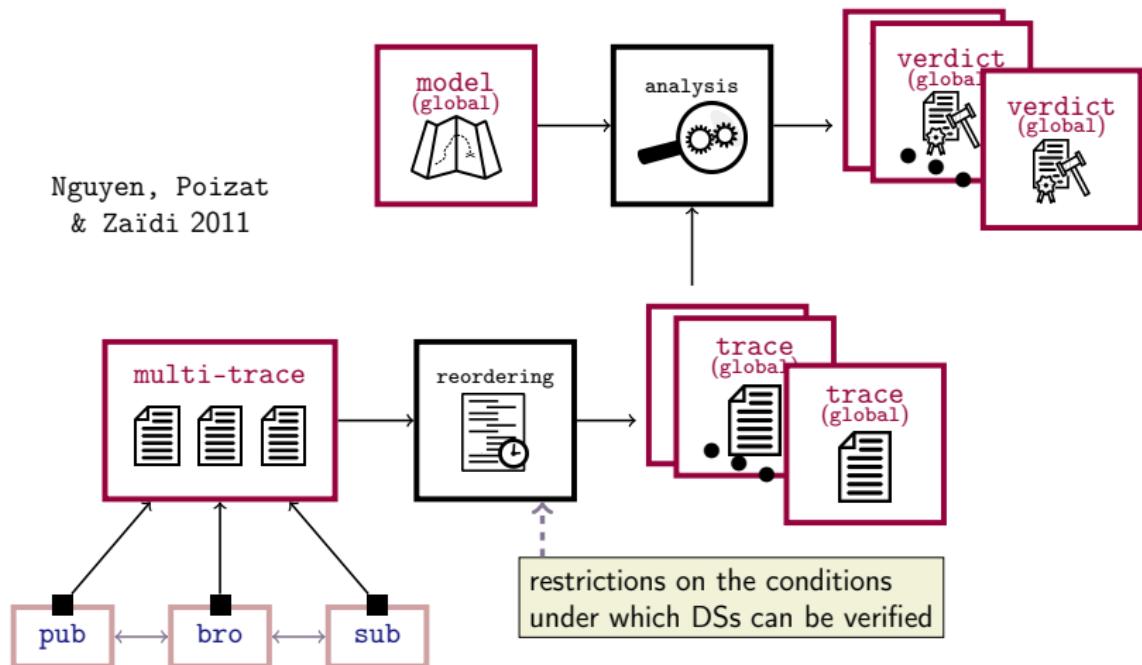
Offline analysis (Runtime Verification) from multi-traces





In practice: RV with reordered execution traces

Nguyen, Poizat
& Zaïdi 2011



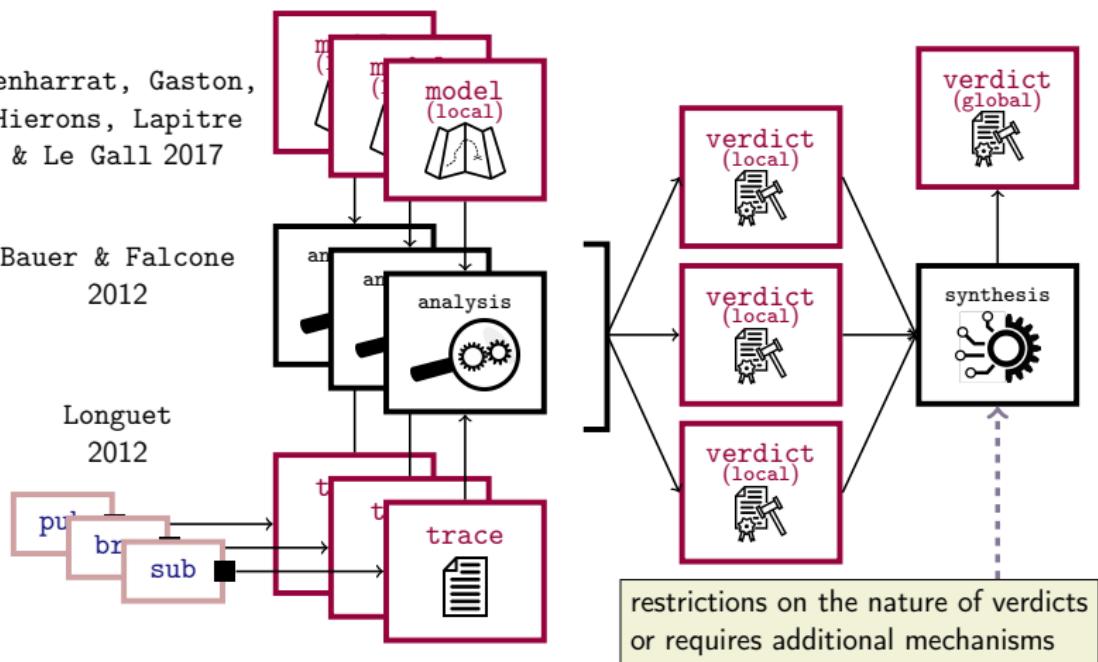


In practice: RV using local analyses

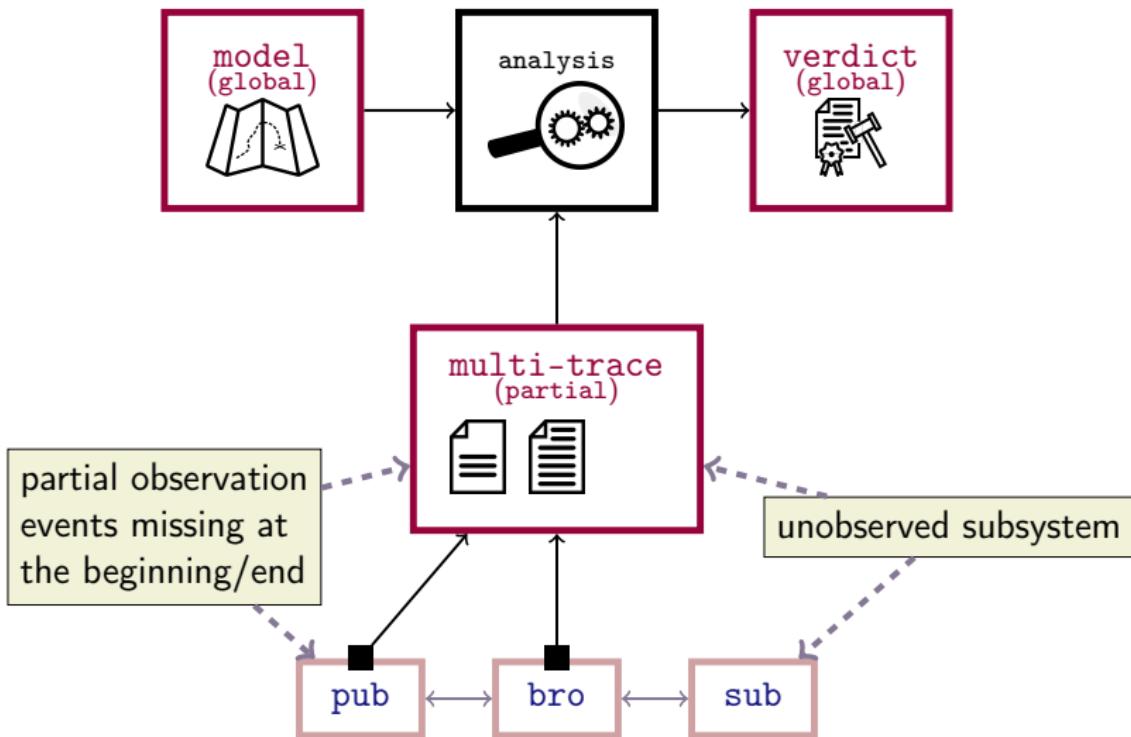
Benharrat, Gaston,
Hierons, Lapitre
& Le Gall 2017

Bauer & Falcone
2012

Longuet
2012

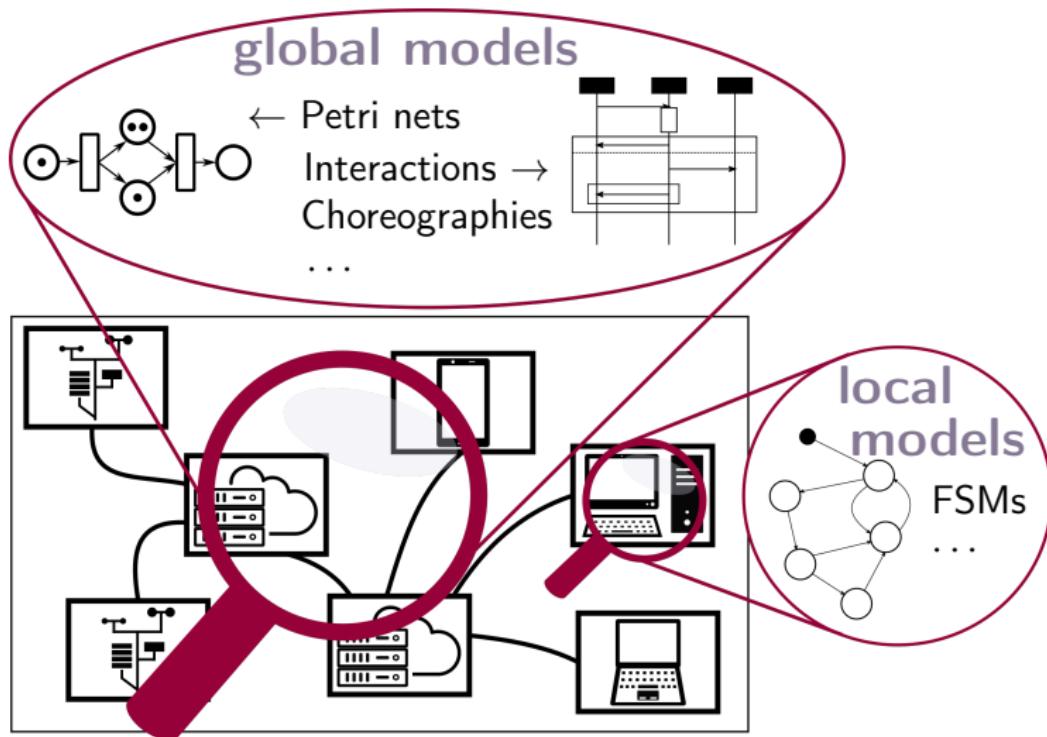


Our goal: RV from partial multi-traces without restrictions

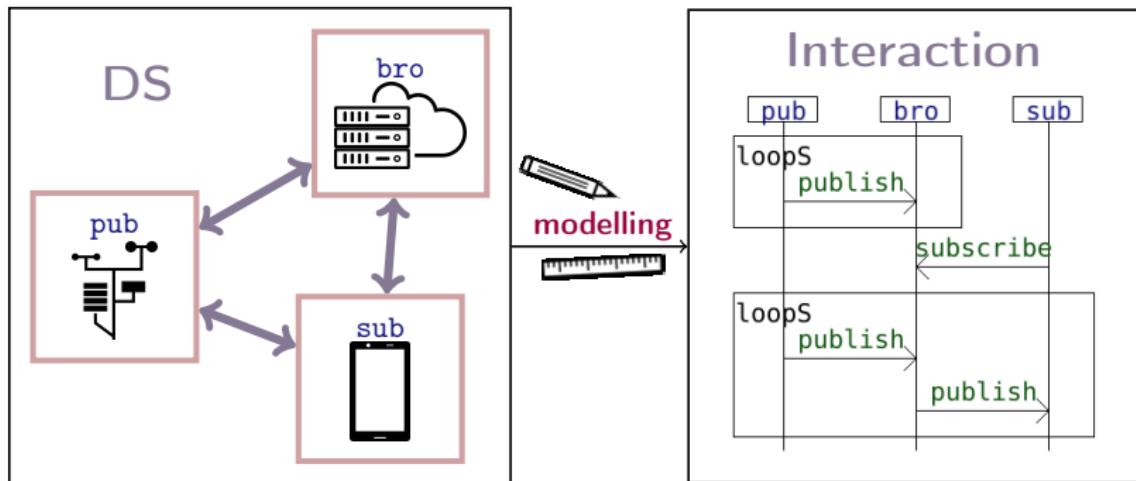




How can RV be performed ? Various formalisms



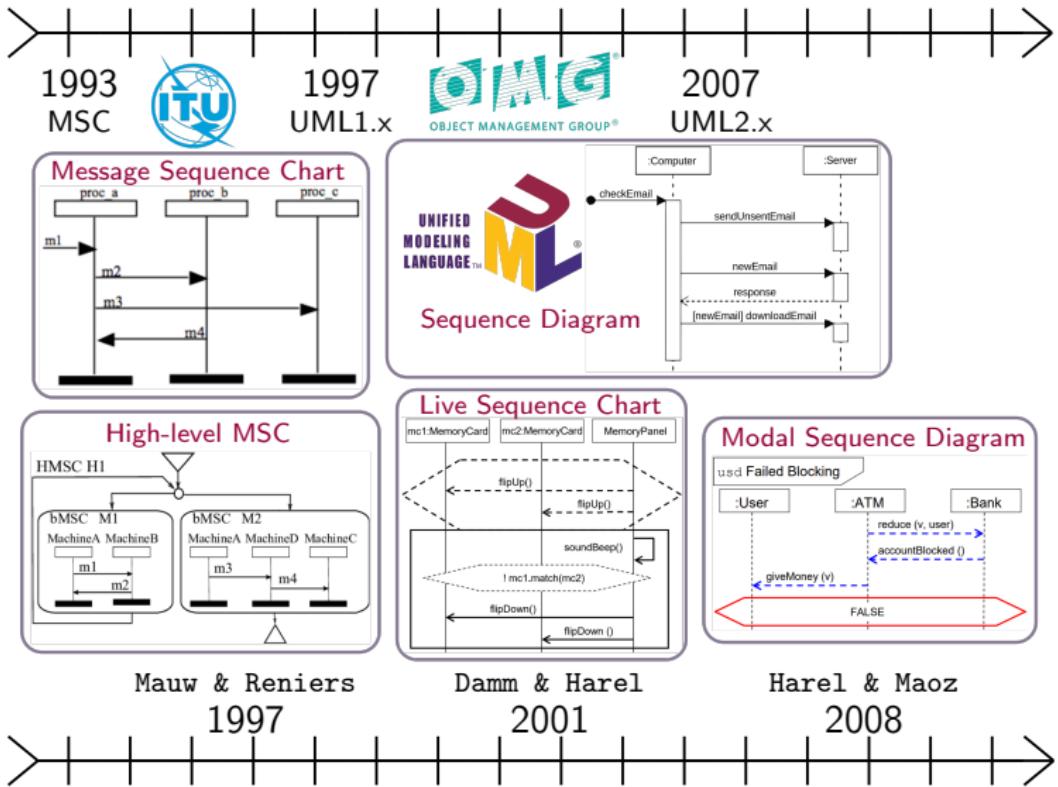
Interaction models



- ▶ focuses on the flow of communications (global model)
- ▶ intuitive graphical representation
- ▶ nuanced specifications via dedicated operators

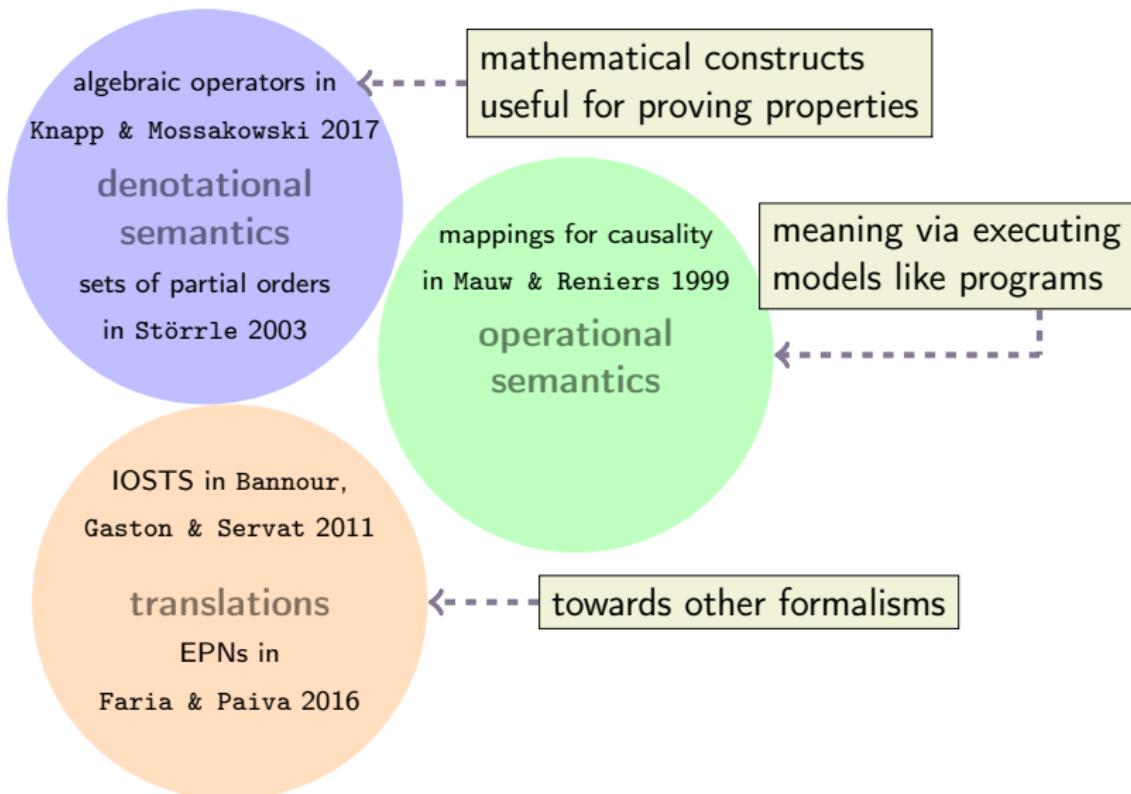


A short history of interaction languages





On the semantics of interactions





1. Interaction Language & denotational semantics

2. Operational semantics

3. Execution semantics

4. Multi-trace analysis algorithms

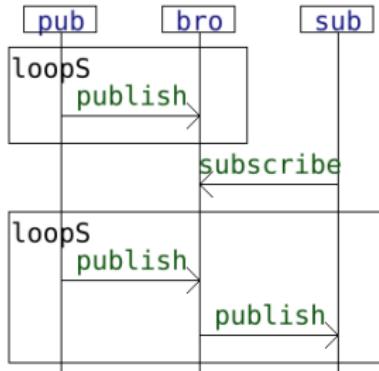
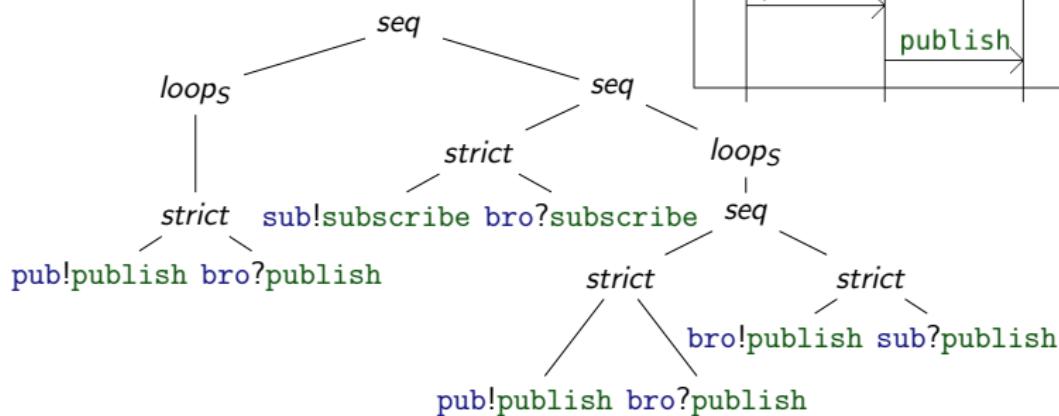
5. Implementation



Interactions as terms of a term algebra

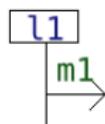
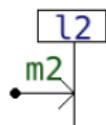
$$\mathbb{A} = L \times \{!, ?\} \times M$$

$$\left(\mathbb{I}, \left\{ \begin{array}{l} \emptyset, \ a \in \mathbb{A}, \\ alt, \ strict, \ seq, \ par \\ loop_X, \ loop_S, \ loop_P \end{array} \right\} \right)$$





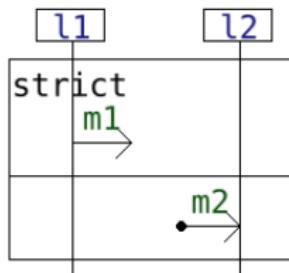
Empty interaction & Atomic emissions & receptions

 \emptyset $\{\epsilon\}$ $l_1!m_1$  $\{l_1!m_1\}$ $l_2?m_2$  $\{l_2?m_2\}$



Strict Sequencing

strict
 $l_1!m_1 \quad l_2?m_2$

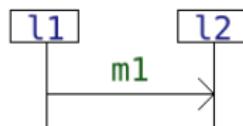


$$\{l_1!m_1\}; \{l_2?m_2\} = \{l_1!m_1.l_2?m_2\}$$



Strict Sequencing

strict
/ \
 $l_1!m_1 \quad l_2?m_1$

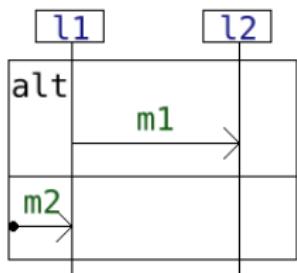


$$\{l_1!m_1\}; \{l_2?m_1\} = \{l_1!m_1.l_2?m_1\}$$



Alternative

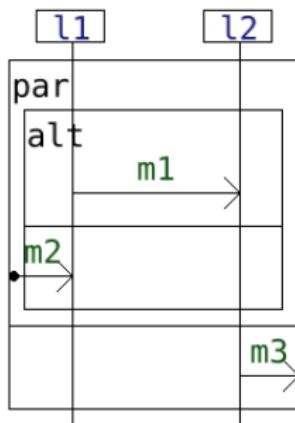
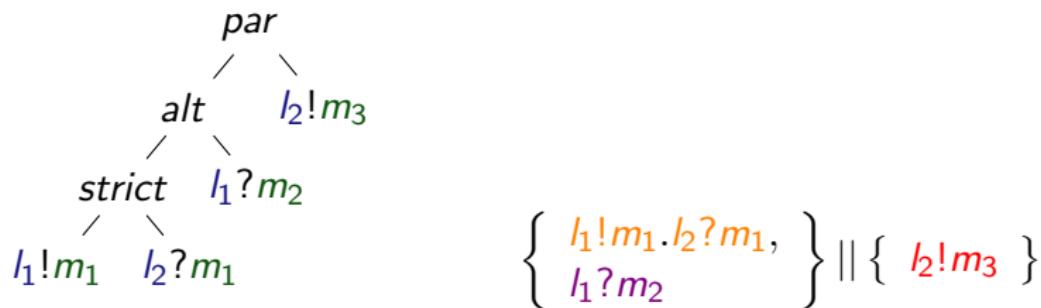
$$\begin{array}{c}
 alt \\
 / \quad \backslash \\
 strict \quad l_1?m_2 \\
 / \quad \backslash \\
 l_1!m_1 \quad l_2?m_1
 \end{array}
 \qquad
 \{l_1!m_1, l_2?m_1\} \cup \{l_1?m_2\}$$



$$= \left\{ \begin{array}{l} l_1!m_1, l_2?m_1, \\ l_1?m_2 \end{array} \right\}$$



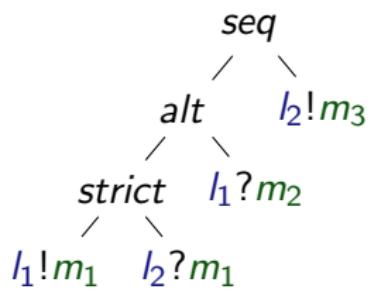
Interleaving



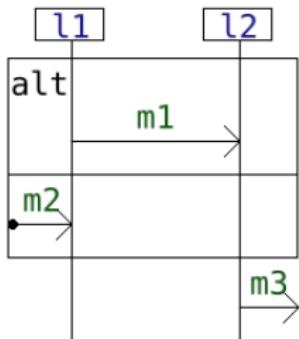
$$= \left\{ \begin{array}{l} l_2!m_3, l_1!m_1, l_2?m_1, \\ l_1!m_1, l_2!m_3, l_2?m_1, \\ l_1!m_1, l_2?m_1, l_2!m_3, \\ l_2!m_3, l_1?m_2, \\ l_1?m_2, l_2!m_3 \end{array} \right\}$$



Weak Sequencing



$$\left\{ \begin{array}{l} l_1!m_1.l_2?m_1, \\ l_1?m_2 \end{array} \right\}; \times \left\{ l_2!m_3 \right\}$$



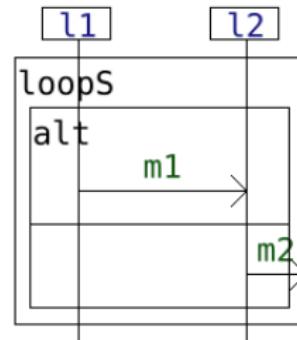
$$= \left\{ \begin{array}{l} l_1!m_1.l_2?m_1.l_2!m_3, \\ l_2!m_3.l_1?m_2, \\ l_1?m_2.l_2!m_3 \end{array} \right\}$$



Repetitions

loop operators (Kleene closures)

name	repetition with	operator
$loop_x$	<i>strict</i>	$;^*$
$loops$	<i>seq</i>	$;*\ast$
$loop_P$	<i>par</i>	$ ^*$



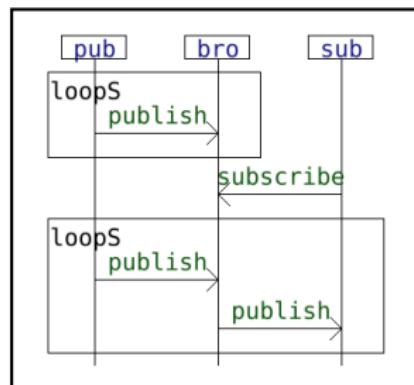


Syntax & denotational trace semantics

$$\left(\mathbb{I}, \left\{ \begin{array}{l} \emptyset, \quad a \in \mathbb{A}, \\ alt, \ strict, \ seq, \ par \\ loop_x, \ loop_S, \ loop_P \end{array} \right\} \right)$$

↓
homomorphism σ

$$\left(\mathcal{P}(\mathbb{T}), \left\{ \begin{array}{l} \{\epsilon\}, \ \{a\}, \\ \cup, \ ;, \ ;*, \ ||, \\ ;*, \ ;***, \ ||* \end{array} \right\} \right)$$



$$\left\{ \begin{array}{l} sub!subscribe.bro?subscribe, \\ \dots, \\ pub!publish\dots, \\ \dots \end{array} \right\}$$



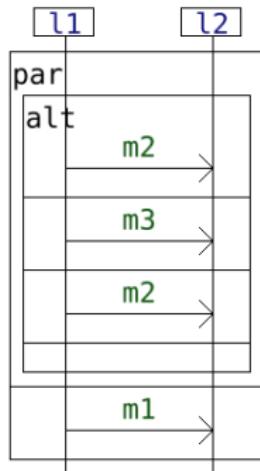
Equivalent terms & normal forms

**algebraic property
of operator**

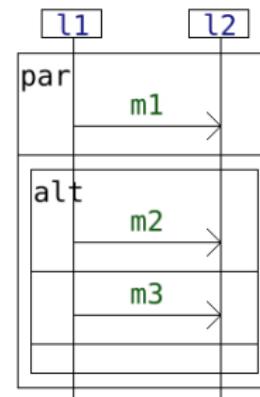
$$\begin{aligned} T_1 \parallel T_2 &= T_2 \parallel T_1 \\ T ;_{\approx} \{\epsilon\} &= T \end{aligned}$$

**equation on
interaction terms**

$$\begin{aligned} par(i_1, i_2) &\approx par(i_2, i_1) \\ seq(i, \emptyset) &\approx i \end{aligned}$$



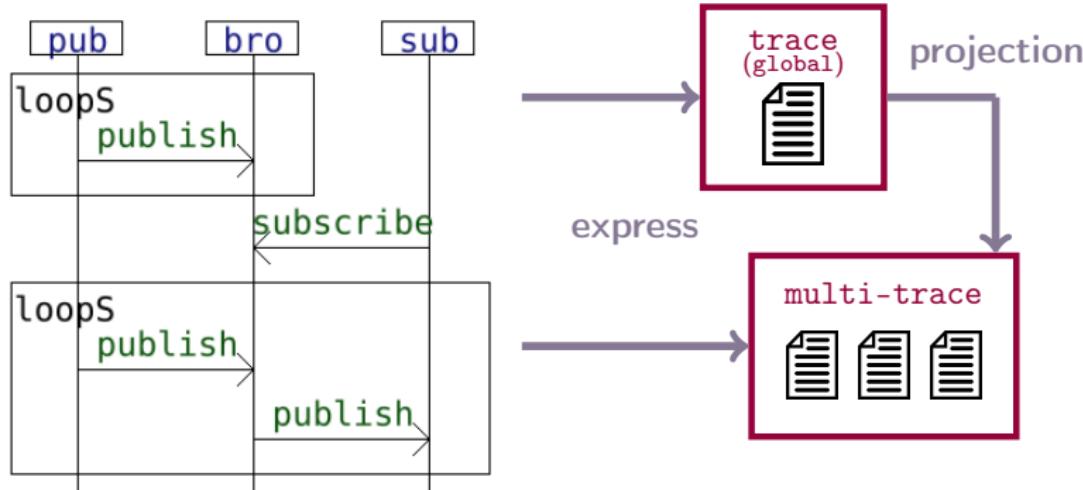
\approx



Computing **normal forms** via **term rewriting**



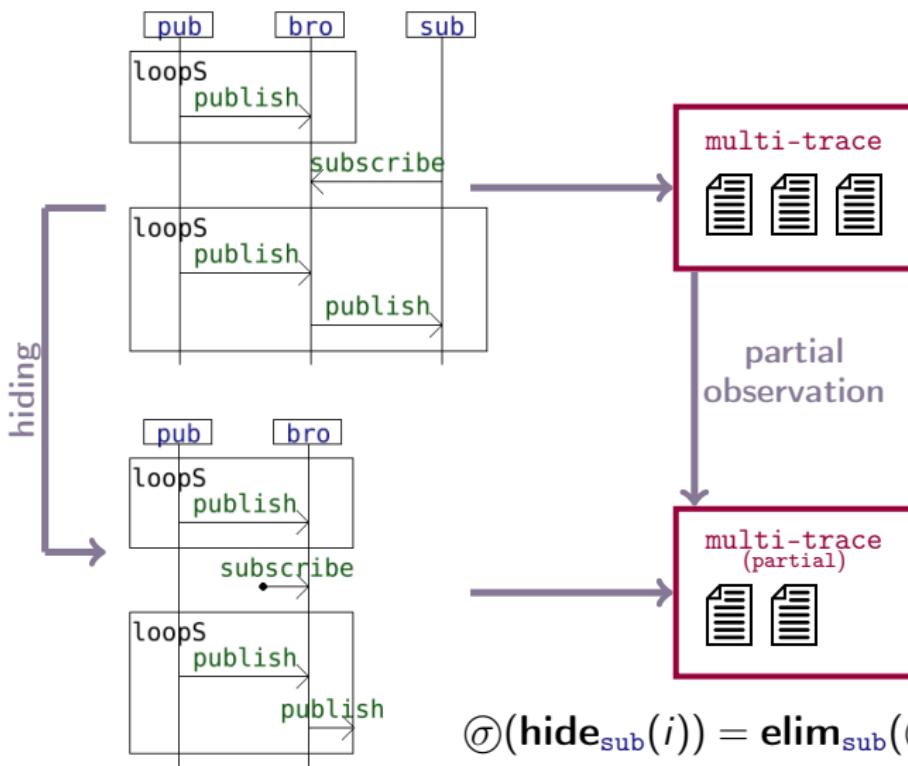
Multi-trace semantics



$$\textcircled{\sigma}(i) = \mathbf{proj}(\sigma(i))$$



Hiding

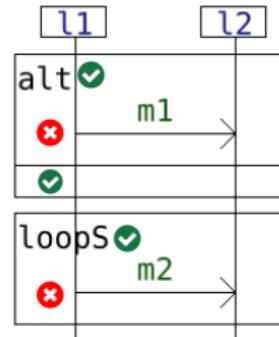
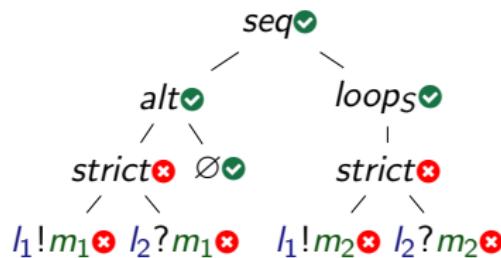




Operational semantics



Termination predicate



Termination

$$\begin{array}{c} \frac{}{\emptyset \downarrow} \quad \frac{i_1 \downarrow}{alt(i_1, i_2) \downarrow} \quad \frac{i_2 \downarrow}{alt(i_1, i_2) \downarrow} \\ \forall f \in \{strict, seq, par\} \quad \frac{i_1 \downarrow \quad i_2 \downarrow}{f(i_1, i_2) \downarrow} \\ \forall k \in \{X, S, P\} \quad \frac{}{loop_k(i_1) \downarrow} \end{array}$$

Characterisation

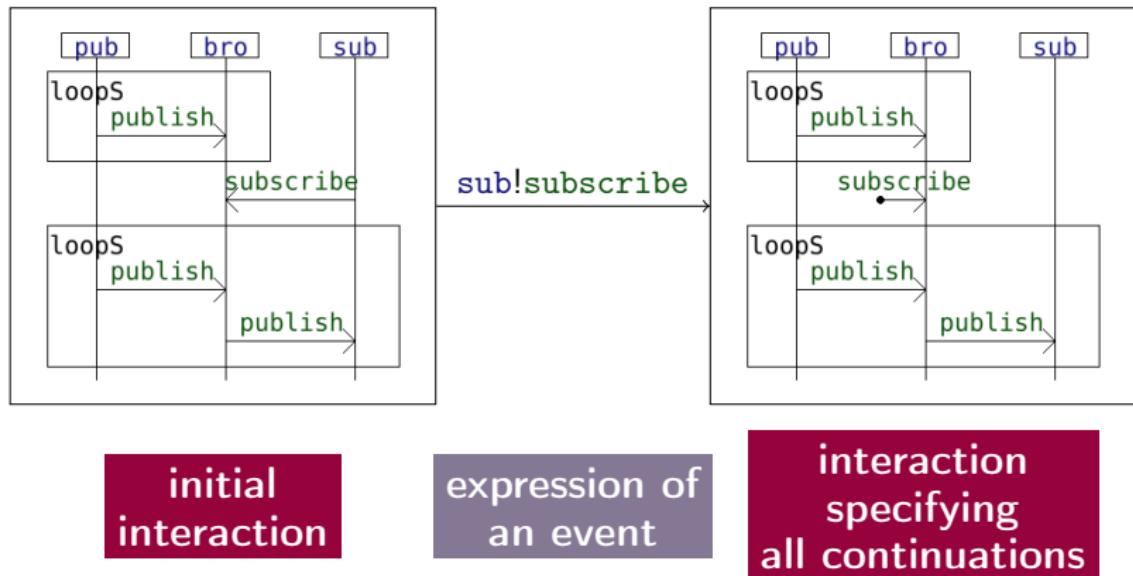
For any $i \in \mathbb{I}$:



$$(i \downarrow) \Leftrightarrow (\epsilon \in \sigma(i))$$



Principle of the operational semantics



rules & induction: process calculus, π -calculus, etc.

Rooda, van Beek
& Baeten 2007

Despeyroux
2001



Rules of the operational semantics

$$\begin{array}{c}
 \frac{}{a \xrightarrow{a} \emptyset} \quad \frac{i_1 \xrightarrow{a} i'_1}{alt(i_1, i_2) \xrightarrow{a} i'_1} \quad \frac{i_2 \xrightarrow{a} i'_2}{alt(i_1, i_2) \xrightarrow{a} i'_2} \\
 \frac{i_1 \xrightarrow{a} i'_1}{par(i_1, i_2) \xrightarrow{a} par(i'_1, i_2)} \quad \frac{i_2 \xrightarrow{a} i'_2}{par(i_1, i_2) \xrightarrow{a} par(i_1, i'_2)} \\
 \frac{i_1 \xrightarrow{a} i'_1}{strict(i_1, i_2) \xrightarrow{a} strict(i'_1, i_2)} \quad \frac{i_2 \xrightarrow{a} i'_2}{strict(i_1, i_2) \xrightarrow{a} i'_2} \quad i_1 \downarrow \\
 \frac{i_1 \xrightarrow{a} i'_1}{seq(i_1, i_2) \xrightarrow{a} seq(i'_1, i_2)} \quad \frac{i_1 \xrightarrow{\theta(a)} i'_1 \quad i_2 \xrightarrow{a} i'_2}{seq(i_1, i_2) \xrightarrow{a} seq(i'_1, i'_2)} \\
 \frac{i_1 \xrightarrow{a} i'_1}{loop_X(i_1) \xrightarrow{a} strict(i'_1, loop_X(i_1))} \quad \frac{i_1 \xrightarrow{a} i'_1}{loop_P(i_1) \xrightarrow{a} par(i'_1, loop_P(i_1))} \\
 \frac{i_1 \xrightarrow{a} i'_1 \quad loop_S(i_1) \xrightarrow{\theta(a)} i''}{loop_S(i_1) \xrightarrow{a} seq(i'', seq(i'_1, loop_S(i_1)))}
 \end{array}$$



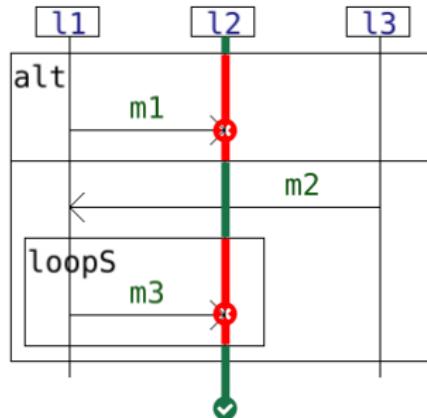
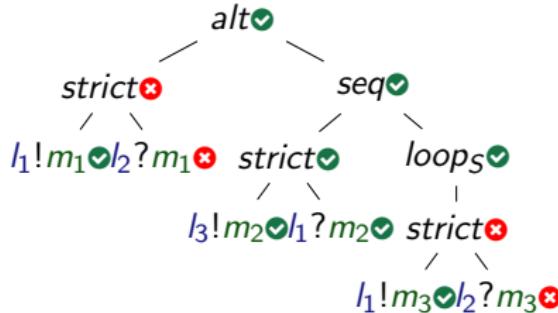
Rules of the operational semantics

Mauw & Reniers 1999, process algebra

$$\begin{array}{c}
 \frac{}{a \xrightarrow{a} \emptyset} \quad \frac{i_1 \xrightarrow{a} i'_1}{alt(i_1, i_2) \xrightarrow{a} i'_1} \quad \frac{i_2 \xrightarrow{a} i'_2}{alt(i_1, i_2) \xrightarrow{a} i'_2} \\
 \frac{i_1 \xrightarrow{a} i'_1}{par(i_1, i_2) \xrightarrow{a} par(i'_1, i_2)} \quad \frac{i_2 \xrightarrow{a} i'_2}{par(i_1, i_2) \xrightarrow{a} par(i_1, i'_2)} \\
 \frac{i_1 \xrightarrow{a} i'_1}{strict(i_1, i_2) \xrightarrow{a} strict(i'_1, i_2)} \quad \frac{i_2 \xrightarrow{a} i'_2}{strict(i_1, i_2) \xrightarrow{a} i'_2} \quad i_1 \downarrow \\
 \frac{i_1 \xrightarrow{a} i'_1}{seq(i_1, i_2) \xrightarrow{a} seq(i'_1, i_2)} \quad \frac{\begin{array}{c} i_1 \xrightarrow{\theta(a)} i'_1 \\ i_2 \xrightarrow{a} i'_2 \end{array}}{seq(i_1, i_2) \xrightarrow{a} seq(i'_1, i'_2)} \\
 \frac{i_1 \xrightarrow{a} i'_1}{loop_X(i_1) \xrightarrow{a} strict(i'_1, loop_X(i_1))} \quad \frac{i_1 \xrightarrow{a} i'_1}{loop_P(i_1) \xrightarrow{a} par(i'_1, loop_P(i_1))} \\
 \frac{\begin{array}{c} i_1 \xrightarrow{a} i'_1 \\ loop_S(i_1) \xrightarrow{\theta(a)} i' \end{array}}{loop_S(i_1) \xrightarrow{a} seq(i', seq(i'_1, loop_S(i_1)))}
 \end{array}$$



Evasion predicate



Evasion

$$\frac{}{\emptyset \downarrow^* I} \quad \frac{\theta(a) \neq I}{a \downarrow^* I}$$

...

Characterisation

For any $i \in \mathbb{I}$ and $I \in L$:

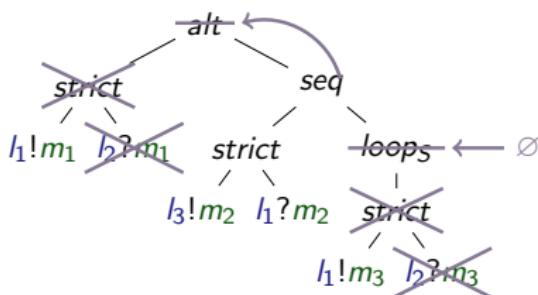


$$(i \downarrow^* I) \Leftrightarrow (\exists t \in \sigma(i), \neg(t \ast I))$$



Pruning relation

$$\begin{array}{c}
 \frac{}{\emptyset \xrightarrow{I} \emptyset} \quad \frac{\theta(a) \neq I}{a \xrightarrow{I} a} \quad \frac{i_1 \xrightarrow{I} i'_1 \quad i_2 \xrightarrow{I} i'_2}{f(i_1, i_2) \xrightarrow{I} f(i'_1, i'_2)} \\
 \\
 \frac{i_1 \xrightarrow{I} i'_1 \quad i_2 \xrightarrow{I} i'_2}{alt(i_1, i_2) \xrightarrow{I} alt(i'_1, i'_2)} \quad \frac{i_1 \xrightarrow{I} i'_1}{alt(i_1, i_2) \xrightarrow{I} i'_1} \quad \frac{i_2 \xrightarrow{I} i'_2}{alt(i_1, i_2) \xrightarrow{I} i'_2} \quad i_1 \not\sim^* I \\
 \\
 \frac{i_1 \xrightarrow{I} i'_1}{loop_k(i_1) \xrightarrow{I} loop_k(i'_1)} \quad \frac{}{loop_k(i_1) \xrightarrow{I} \emptyset} \quad i_1 \not\sim^* I
 \end{array}$$



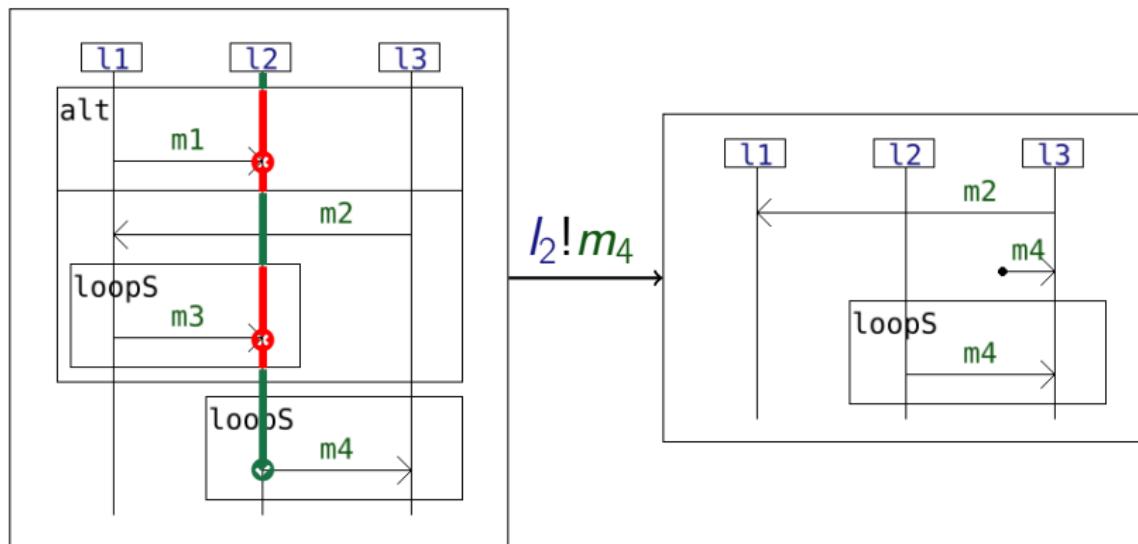
Characterisation

For any $i \in \mathbb{I}$ and $I \in L$:

$$(i \xrightarrow{I} i') \Rightarrow \left(\begin{array}{l} \sigma(i') = \\ \{t \in \sigma(i) \mid \neg(t \otimes I)\} \end{array} \right)$$

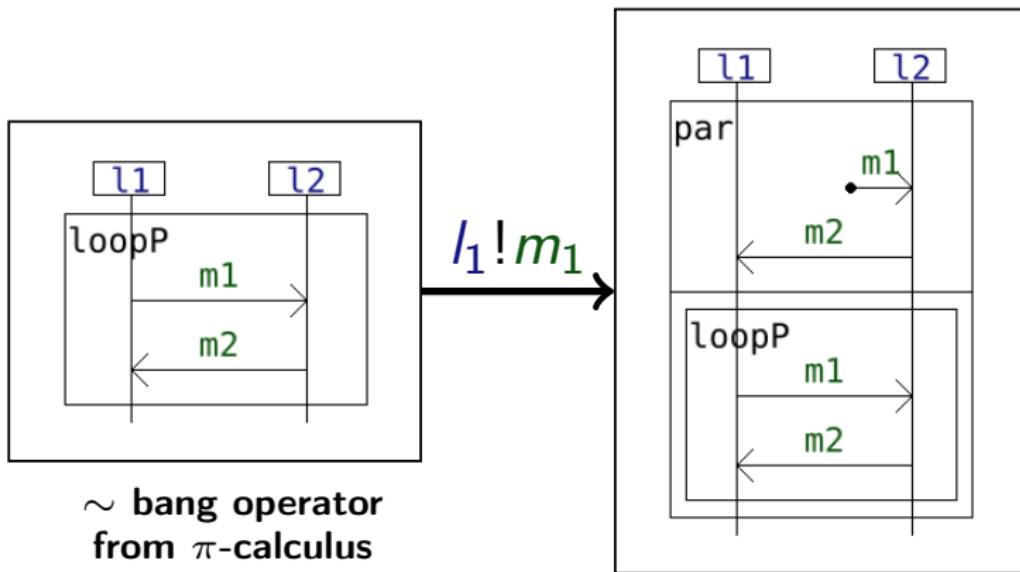


Executing actions on the right of seq





Executing actions underneath a $loopP$





Operational semantics & equivalence

Operational semantics σ_o

We define $\sigma_o : \mathbb{I}_\Omega \rightarrow \mathcal{P}(\mathbb{T}_\Omega)$ by:

$$\frac{i \downarrow}{\epsilon \in \sigma_o(i)} \qquad \frac{t \in \sigma_o(i') \quad i \xrightarrow{a} i'}{a.t \in \sigma_o(i)}$$

Equivalence of the σ_o and σ semantics

For any interaction $i \in \mathbb{I}_\Omega$:

$$\sigma_o(i) = \sigma(i)$$





Need for an algorithmization

- ▶ problems:
 - prove that $i \xrightarrow{a} i'$
 - determine if i can express a and compute i'
- ▶ naive implementation of operational semantics:
 - computes all (a, i') s.t. $i \xrightarrow{a} i'$
 - no term simplification → degradation of term at each step
- ▶ non-trivial implementation: "execution semantics"

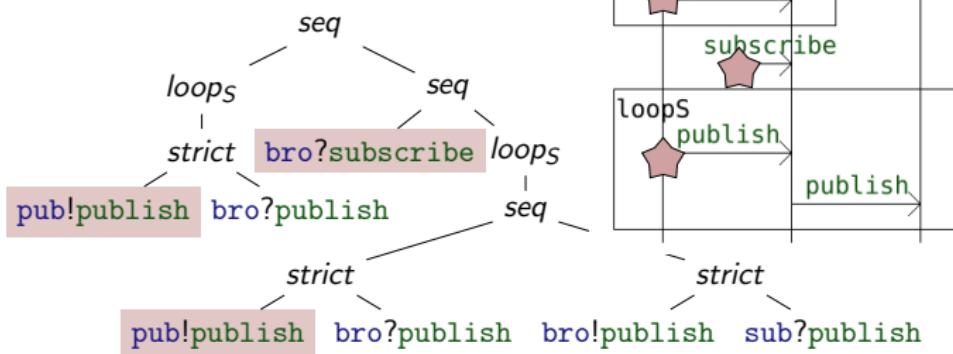


Execution semantics



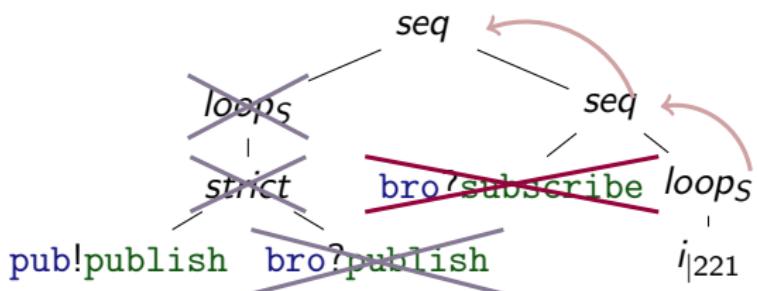
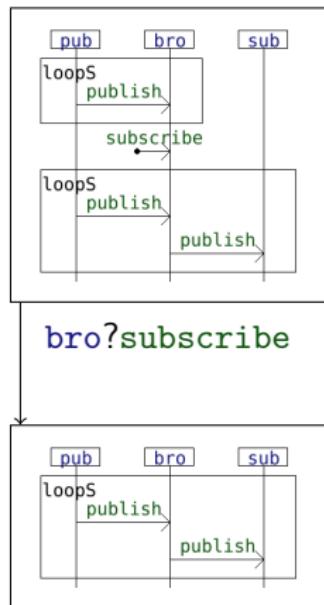
Frontier of execution

- $\text{frt}(i) = \text{match } i \text{ with}$
- $\emptyset \rightarrow \emptyset$
- $a \in A_\Omega \rightarrow \{\epsilon\}$
- $\text{strict}(i_1, i_2) \rightarrow \begin{cases} 1.\text{frt}(i_1) \cup 2.\text{frt}(i_2) & \text{if } i_1 \downarrow \\ 1.\text{frt}(i_1) & \text{else} \end{cases}$
- $\text{seq}(i_1, i_2) \rightarrow 1.\text{frt}(i_1) \cup \{p \mid p \in 2.\text{frt}(i_2), i_1 \downarrow^\times \theta(i_{|p})\}$
- $f(i_1, i_2) \rightarrow 1.\text{frt}(i_1) \cup 2.\text{frt}(i_2) \text{ for } f \in \{\text{alt}, \text{par}\}$
- $\text{loop}_k(i_1) \rightarrow 1.\text{frt}(i_1) \text{ for } k \in \{X, S, P\}$

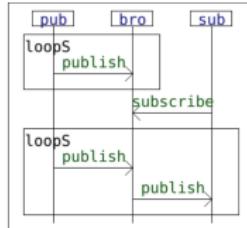


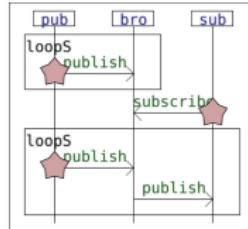


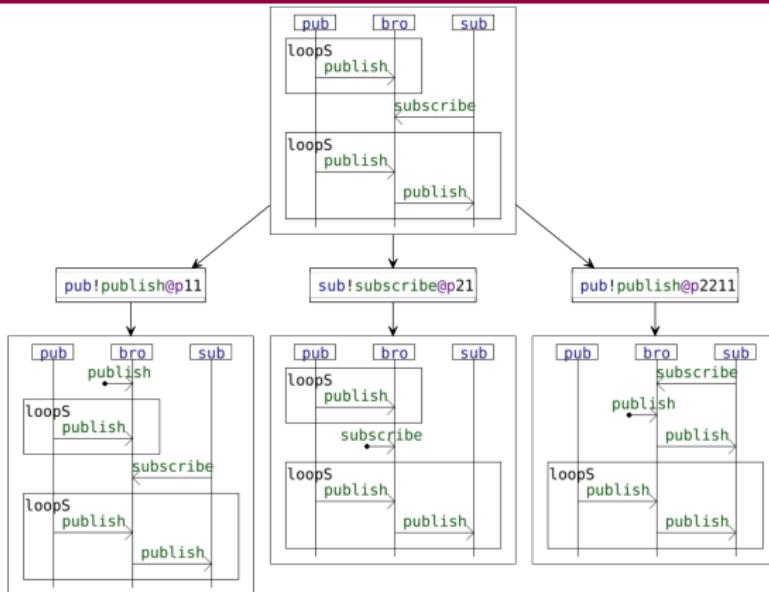
Execution

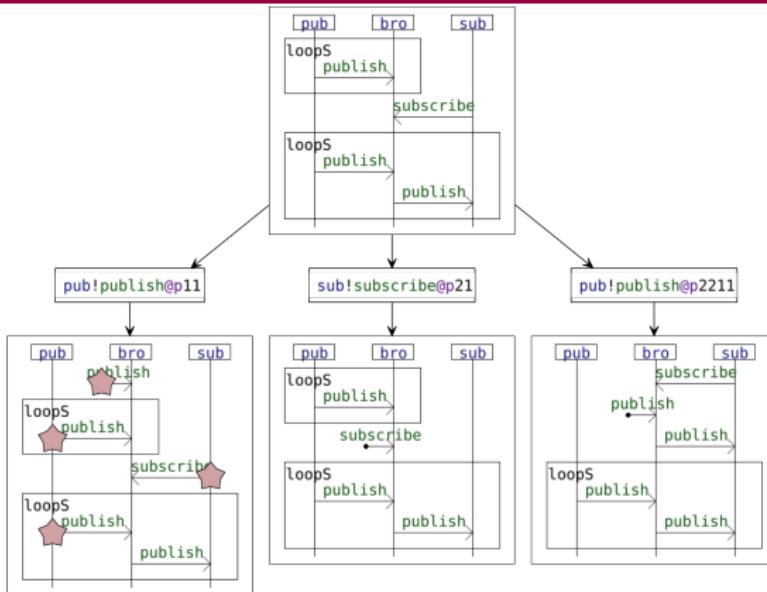


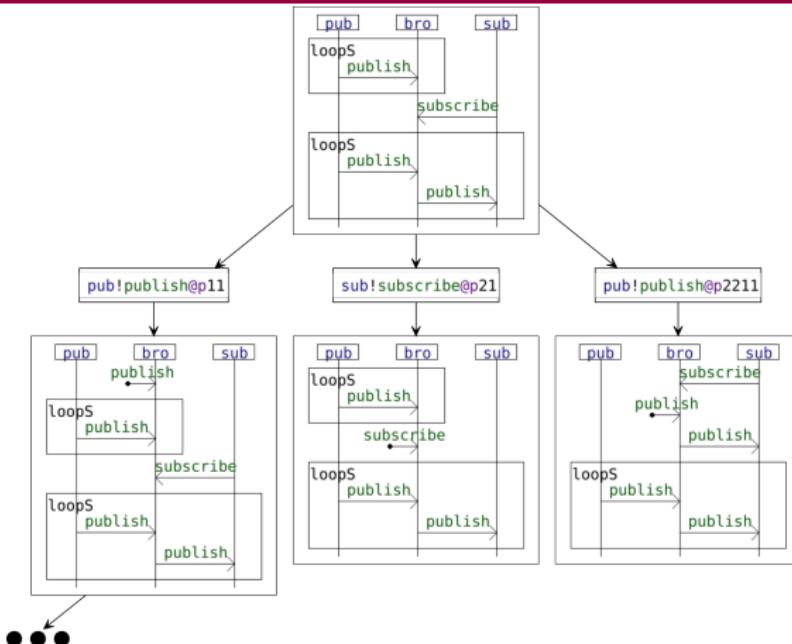
Muroor Nadumane 2020

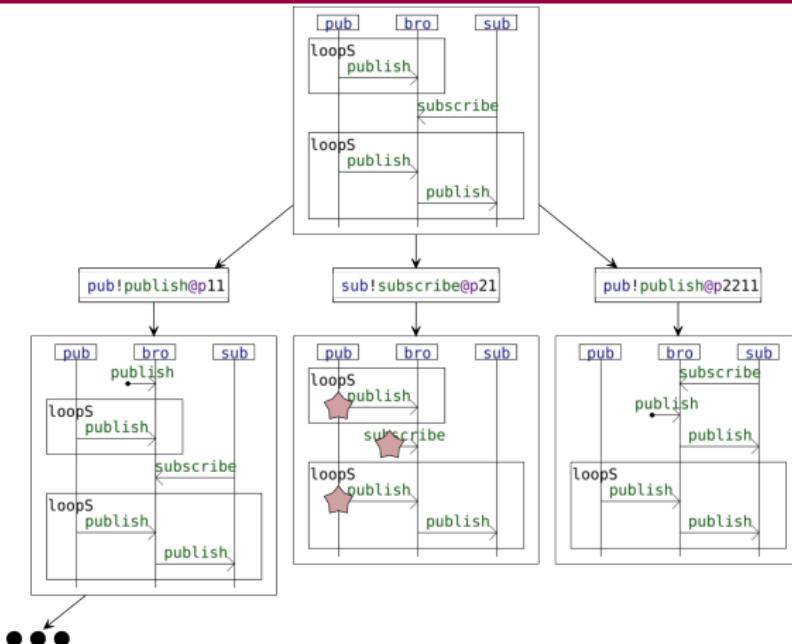


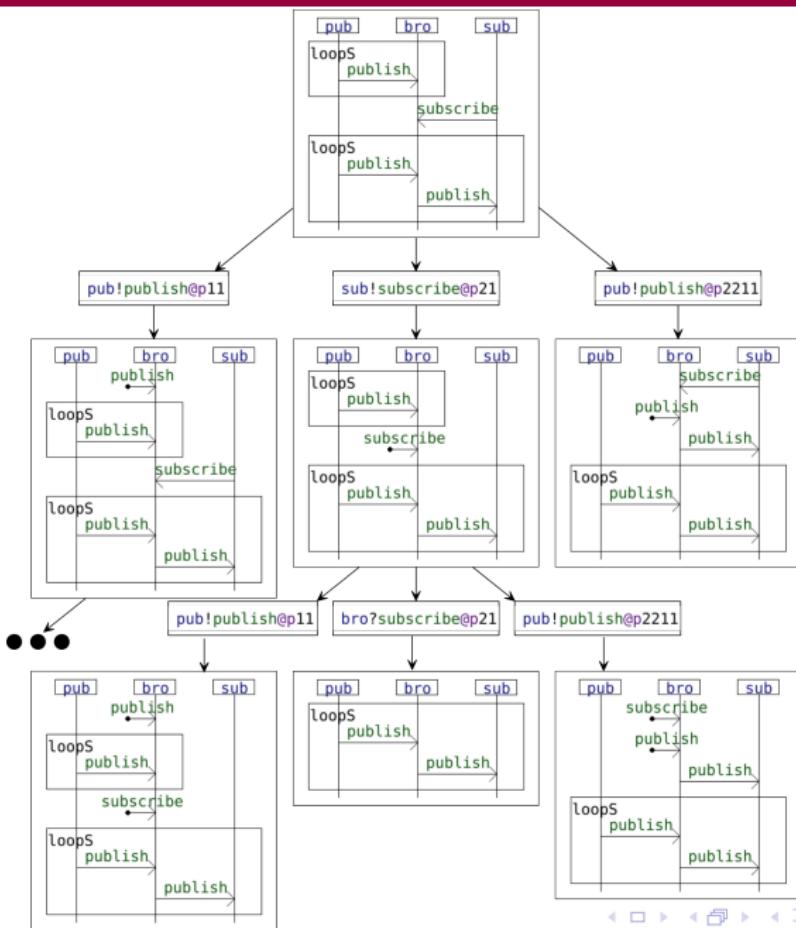


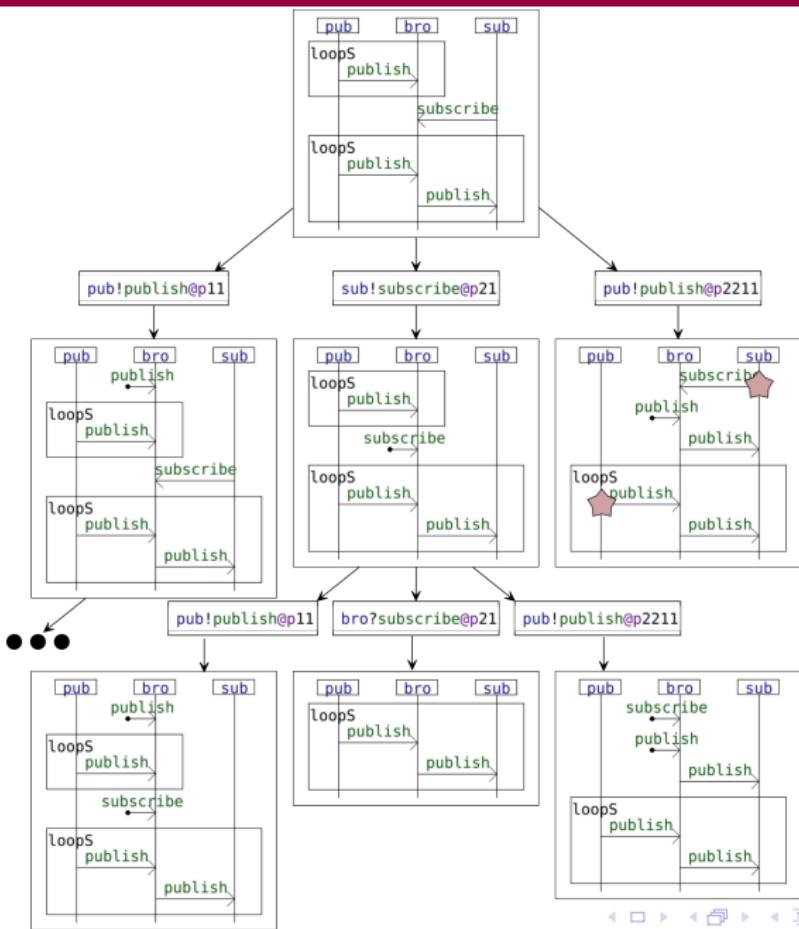


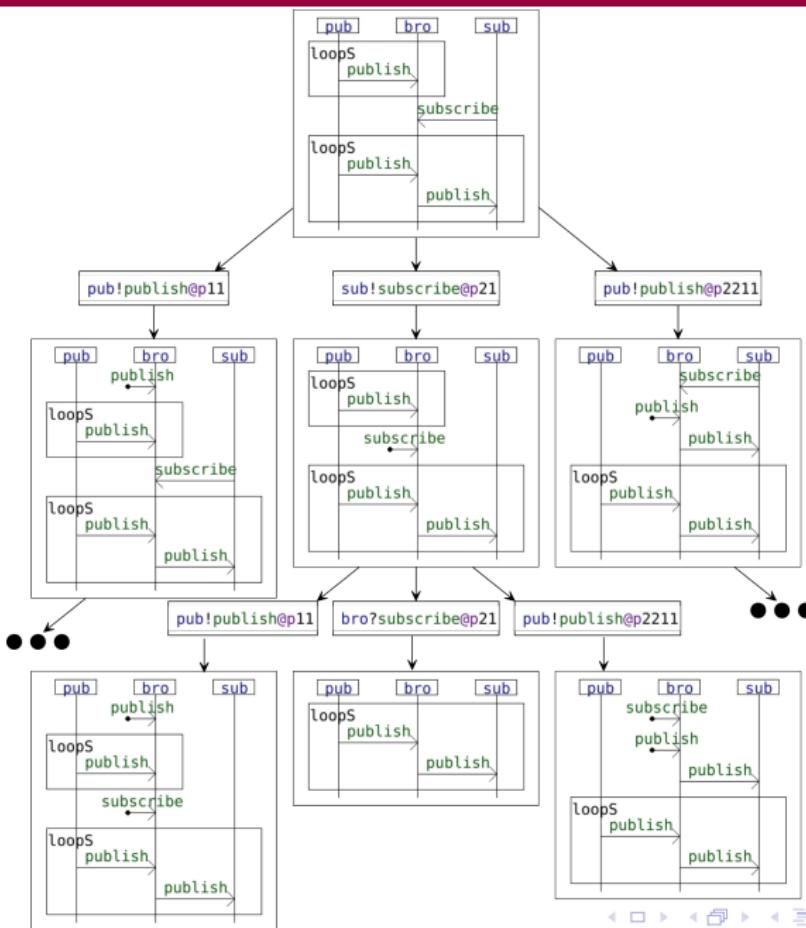














Execution semantics & equivalence

Execution semantics σ_e

We define $\sigma_e : \mathbb{I}_\Omega \rightarrow \mathcal{P}(\mathbb{T}_\Omega)$ as:

$$\sigma_e(i) = \text{empty}(i) \cup \bigcup_{p \in \text{front}(i)} i|_p \cdot \sigma_e(\chi(i, p))$$

with

$$\text{empty}(i) = \begin{cases} \{\epsilon\} & \text{if } i \downarrow \\ \emptyset & \text{if } i \not\downarrow \end{cases}$$

Equivalence of the semantics

For any interaction $i \in \mathbb{I}_\Omega$:

$$\sigma_e(i) = \sigma_o(i)$$





Comparison of semantics

	denotational	operational	execution
intuition of meaning	✓✓	✓	✗
related to	Knapp & Mossakowski 2017	Mauw & Reniers 1999	Muroor Nadumane 2020
use for proofs	✓✓ (hiding)		✗
easy implem. & use for RV	✗		✓✓
also	✓ (normal forms)	✓ (execution tree)	



Multi-trace analysis algorithms



Full observation (accepted behavior)

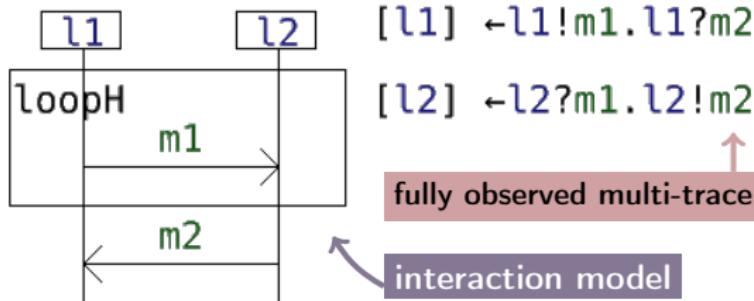
executed behavior
as a global trace

$l_1!m_1$

$l_2?m_1$

$l_2!m_2$

$l_1?m_2$



$[l_1] \leftarrow l_1!m_1.l_1?m_2$

$[l_2] \leftarrow l_2?m_1.l_2!m_2$

fully observed multi-trace

interaction model

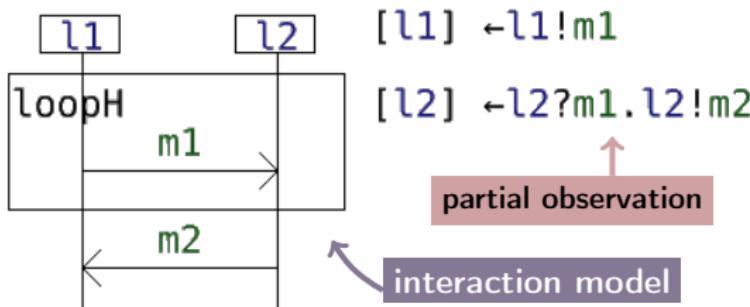


Projection of a global prefix (accepted behavior)

executed behavior
as a global trace

$l_1!m_1$
$l_2?m_1$
$l_2!m_2$
$l_1?m_2$

unobserved



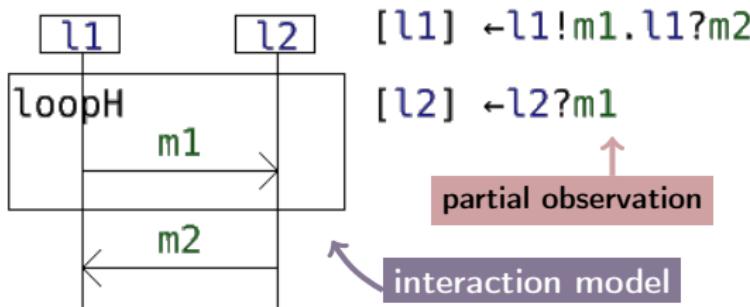


Prefix in the sense of multi-traces (accepted behavior)

executed behavior
as a global trace

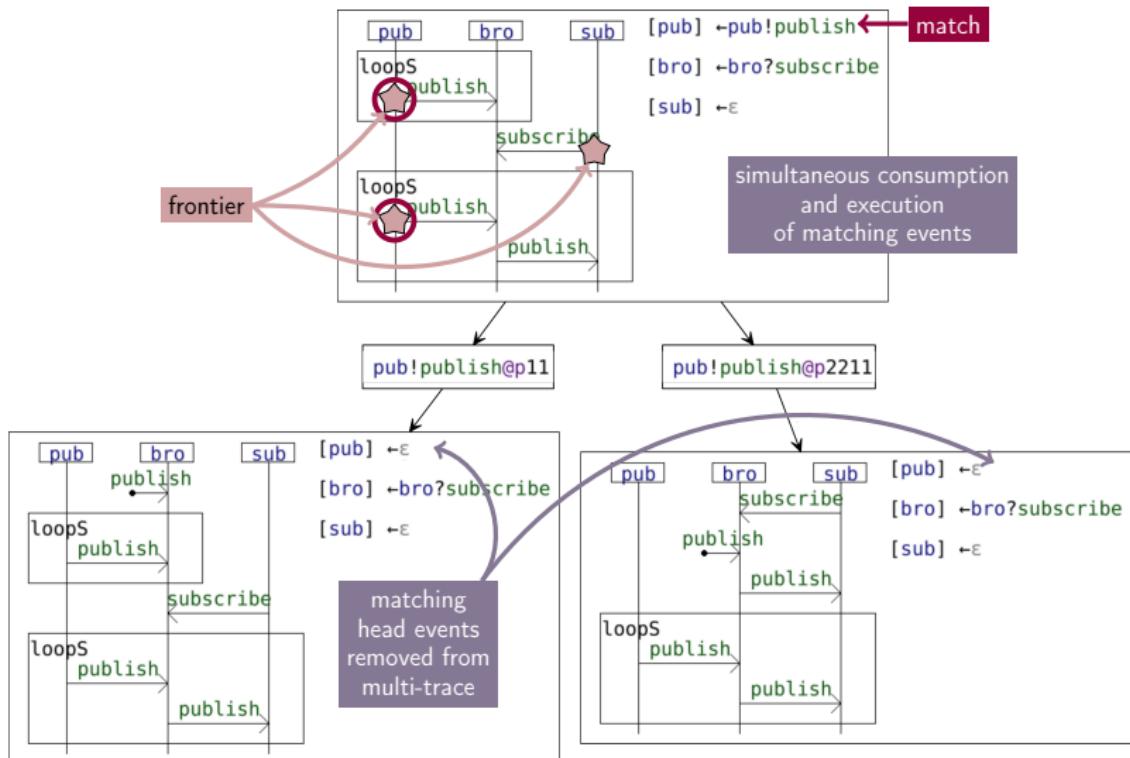
$l_1!m_1$
$l_2?m_1$
$l_1!m_2$
$l_1?m_2$

unobserved



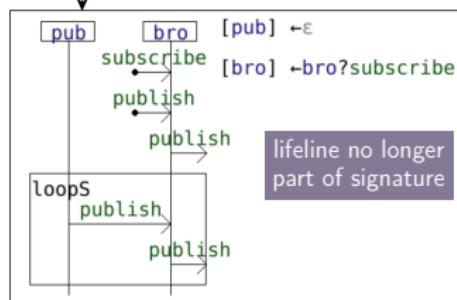
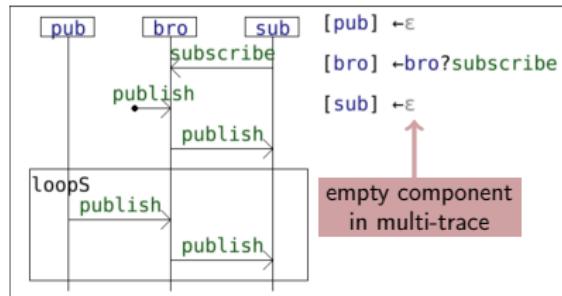


Consuming events



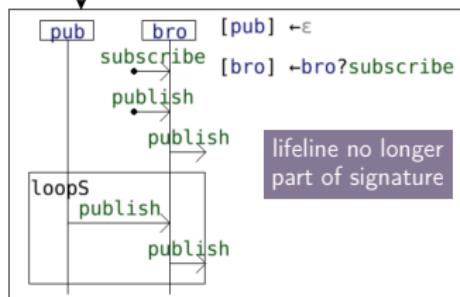
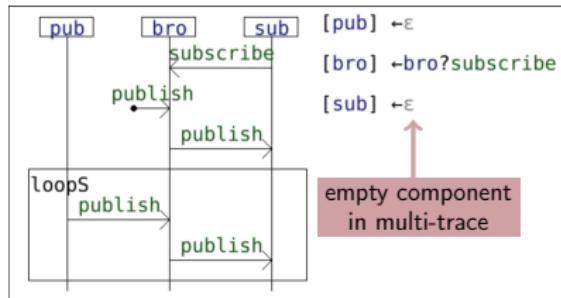


Hiding

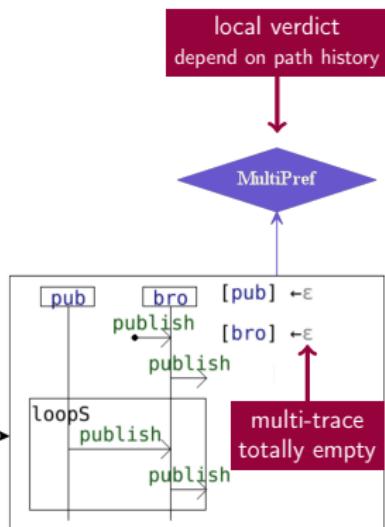




Hiding & verdicts



$\xrightarrow{\text{bro?subscribe@p1}}$





An analysis algorithm with hiding steps

Analysis relation \sim on nodes of $(\mathbb{I} \times \mathbb{M}) \cup \{Obs, Out\}$

The analysis relation \sim is s.t.:

$$(R_h) \frac{i \quad \mu}{\text{hide}_{\textcolor{blue}{I}}(i) \quad \text{elim}_{\textcolor{blue}{I}}(\mu)} \mu_{\mid I} = \epsilon \quad (R_e) \frac{i \quad a \xrightarrow{\vec{\odot}} \mu}{i' \quad \mu} i \xrightarrow{a} i'$$

$$(R_p) \frac{i \quad \epsilon_L}{Obs} \quad (R_f) \frac{i \quad \mu}{Out} \left\{ \begin{array}{l} (\exists I \in L \text{ s.t. } \mu_{\mid I} = \epsilon) \\ \wedge (\exists i \xrightarrow{a} i' \text{ s.t. } \mu = a \xrightarrow{\vec{\odot}} \mu') \end{array} \right.$$

Algorithm

$\omega : \mathbb{I} \times \mathbb{M} \rightarrow \{Pass, Fail\}$ is s.t.:

- ▶ $\omega(i, \mu) = Pass$ iff \exists a path $(i, \mu) \xrightarrow{*} Obs$
- ▶ $\omega(i, \mu) = Fail$ otherwise

Correctness

For any $i \in \mathbb{I}$ and $\mu \in \mathbb{M}$:

$$(\omega(i, \mu) = Pass) \Leftrightarrow (\mu \in \overline{\textcircled{O}}(i))$$



Implementation



Coq proofs

- ▶ proof of equivalence between 3 semantics:

github.com/erwanM974/coq_hibou_label_semantics_equivalence

~ 3100 loc

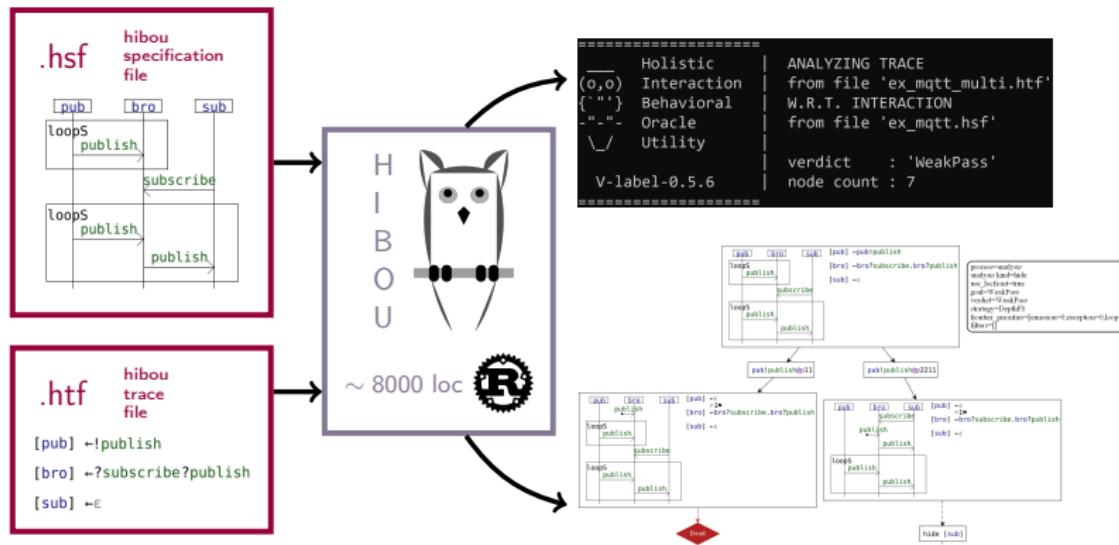
- ▶ proof of correctness for analysis algorithm:

github.com/erwanM974/coq_hibou_label_multi_trace_analysis

~ 1300 loc



HIBOU tool



github.com/erwanM974/hibou_label

- ▶ multi-trace analysis (hide, simulation, local frontiers, goals, heuristics, filters, etc.)
- ▶ exploration of execution trees
- ▶ computation of normal forms
- ▶ ease of use features (input languages, configuration, graphical outputs, etc.)



The need to handle data



concrete
message
arguments

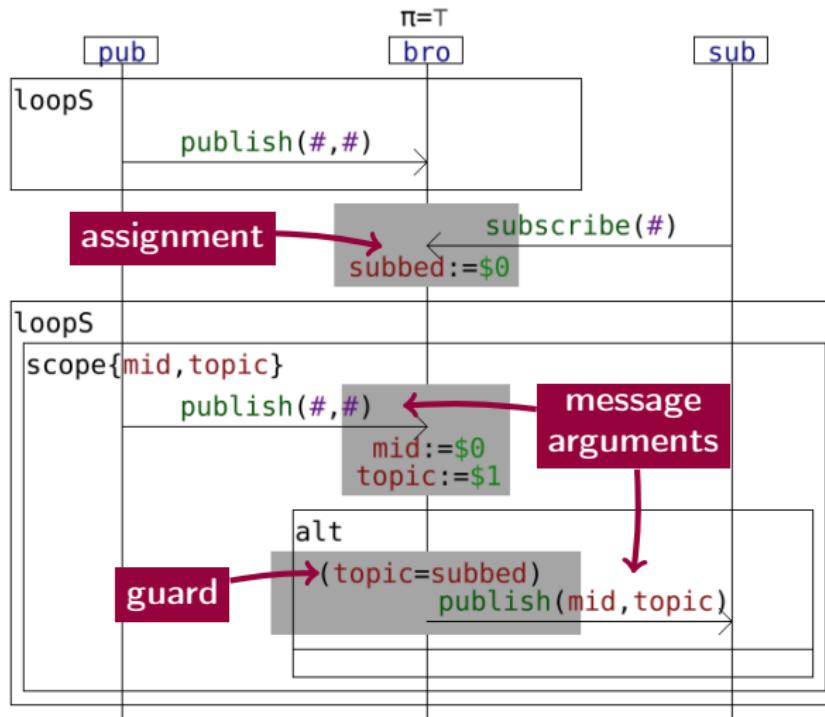
```
[pub] ← !publish(429, "a")
```

```
[bro] ← ?subscribe("b")...+1
```

```
[sub] ← ε
```

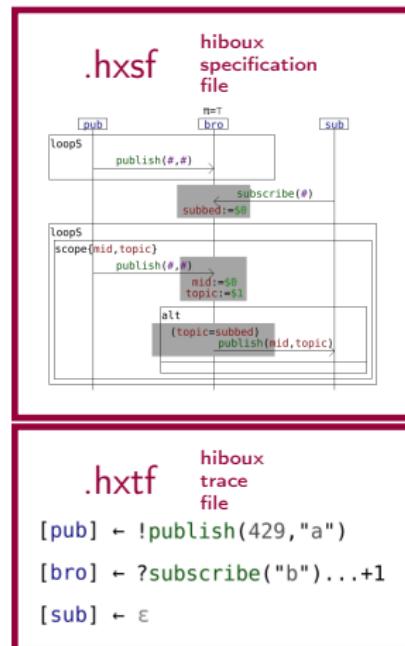


Enriching interactions with data

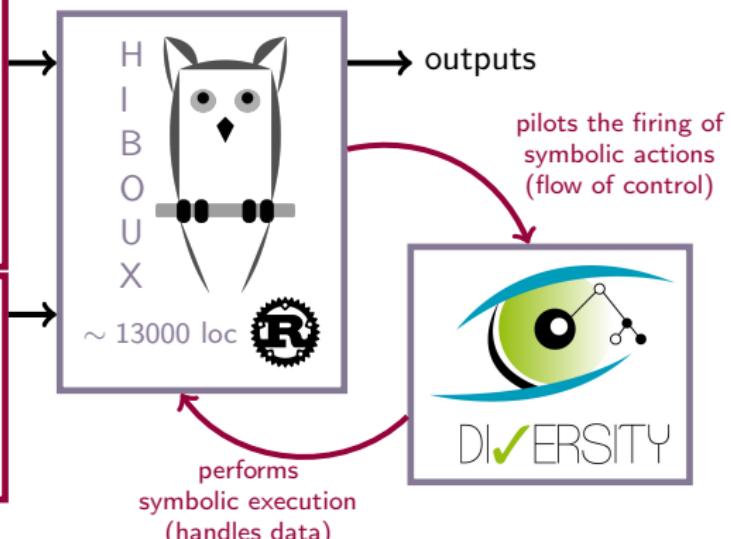




HIBOUX tool

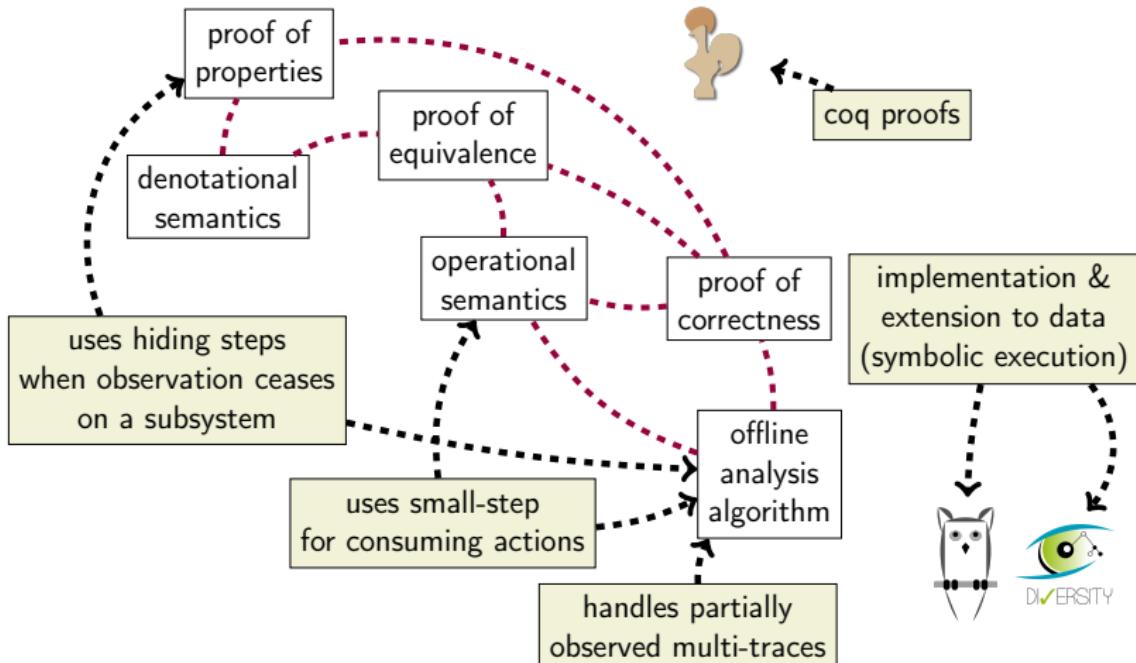


github.com/erwanM974/hibou_efm





Conclusion





Perspectives

- ▶ further validation & use of the tools on case studies
- ▶ formalizing data & time in interaction models
- ▶ horizontal composition of interactions
(reverse of hiding → from local to global)
- ▶ online analysis



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Appendix

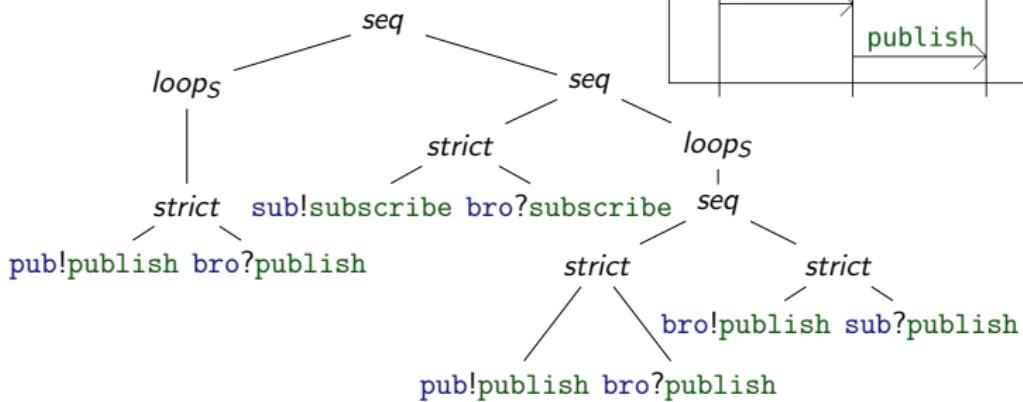


Details on the syntax

$$\Omega = (L, M)$$

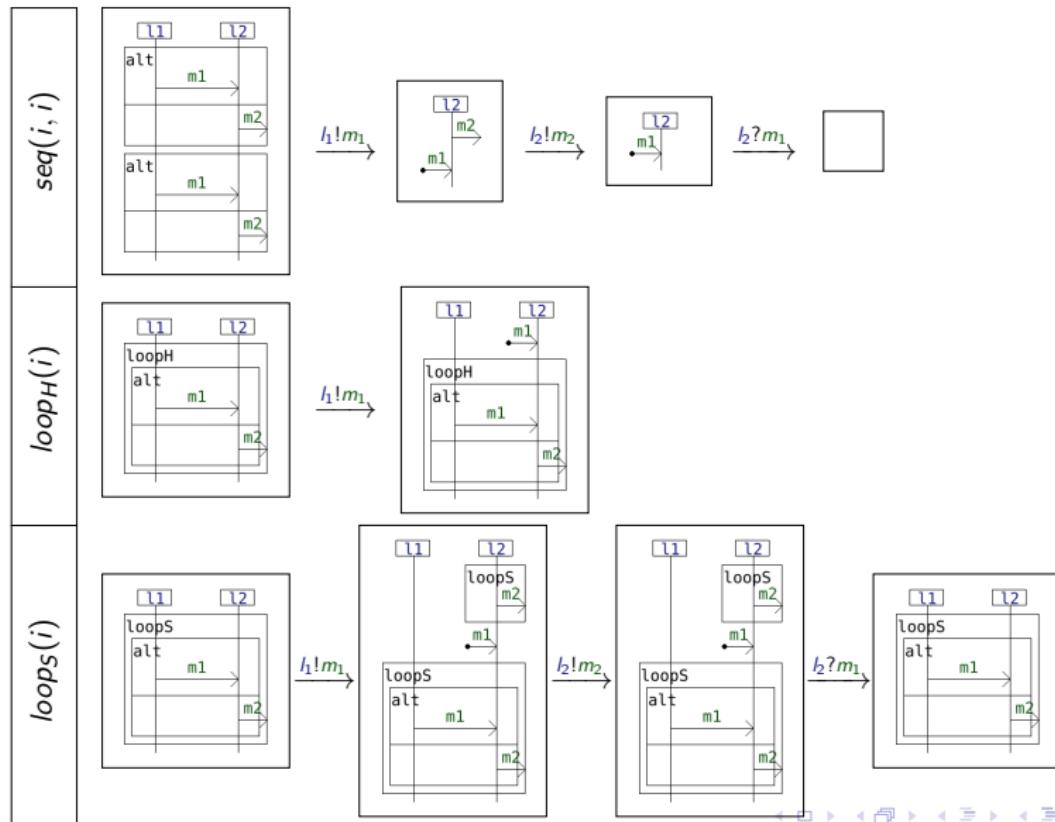
$$\mathbb{A}_\Omega = L \times \{!, ?\} \times M$$

$$\left(\mathbb{I}_\Omega, \left\{ \begin{array}{l} \emptyset, \quad a \in \mathbb{A}_\Omega, \\ alt, \ strict, \ seq, \ par \\ loop_S, \ loop_H, \ loop_S, \ loop_P \end{array} \right\} \right)$$





$loop_H$ & $loops$



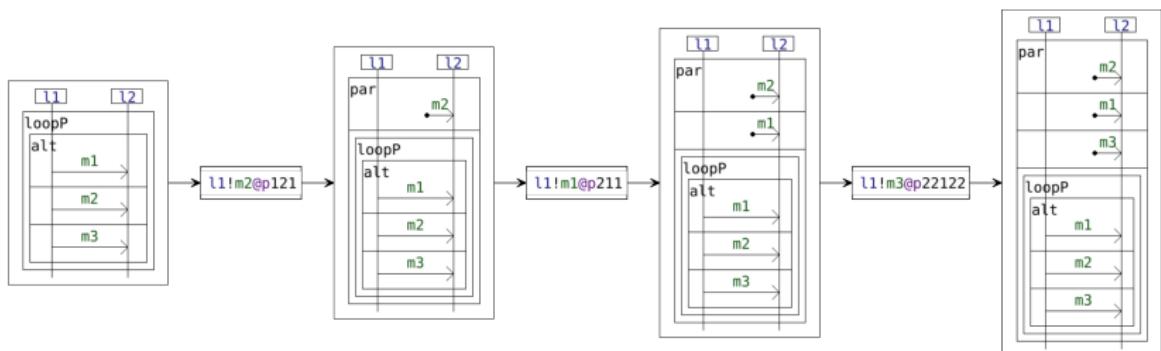
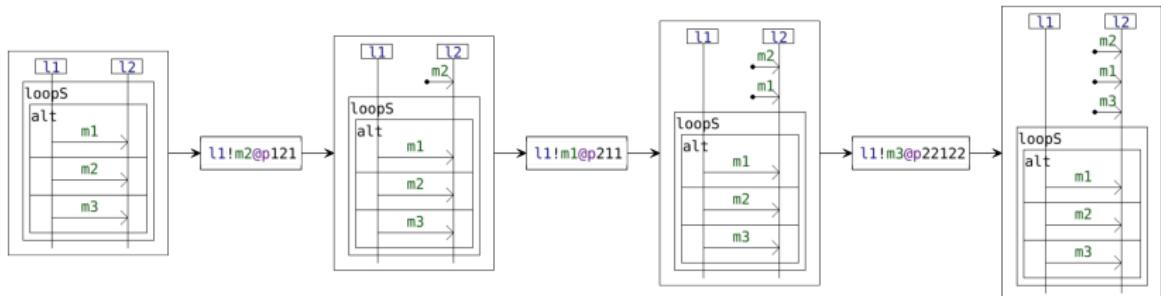


Co-regions

diagram	syntax	equivalent
	$ \begin{array}{c} coreg(\{l_2\}) \\ / \quad \backslash \\ strict \quad strict \\ l_1!m_1 \, l_2?m_1 \, l_1!m_2 \, l_2?m_2 \end{array} $	



Communication medium within the language itself (buffers, bags, etc.)





Equations on interactions

$$\forall f \in \{\text{strict}, \text{seq}, \text{par}\},$$

$$f(\emptyset, y) \approx y$$

$$\forall f \in \{\text{strict}, \text{seq}, \text{par}\},$$

$$f(x, \emptyset) \approx x$$

$$\forall f \in \{\text{strict}, \text{seq}, \text{par}, \text{alt}\},$$

$$f(f(x, y), z) \approx f(x, f(y, z))$$

$$\forall f \in \{\text{par}, \text{alt}\},$$

$$f(x, y) \approx f(y, x)$$

$$\text{alt}(x, x) \approx x$$

$$\forall f \in \{\text{strict}, \text{seq}, \text{par}\},$$

$$f(x, \text{alt}(y, z)) \approx \text{alt}(f(x, y), f(x, z))$$

$$\forall f \in \{\text{strict}, \text{seq}, \text{par}\},$$

$$f(\text{alt}(x, y), z) \approx \text{alt}(f(x, z), f(y, z))$$

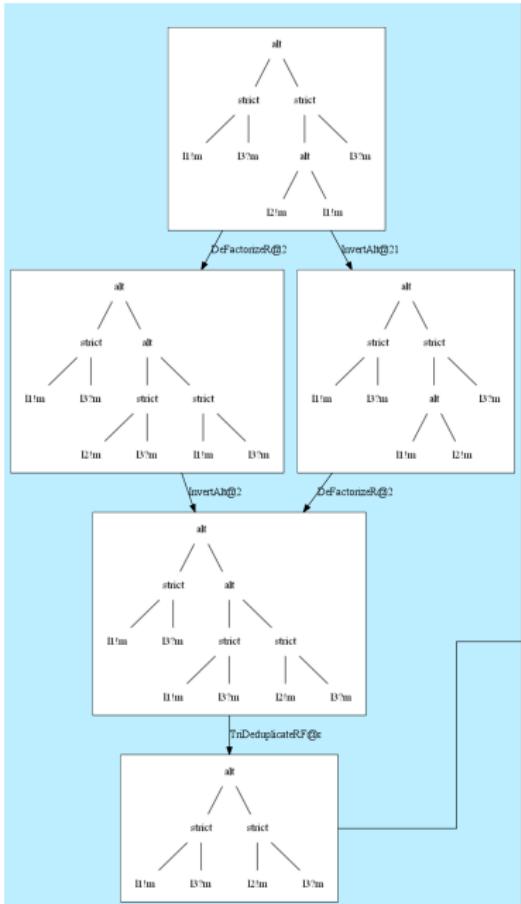
$$\forall k \in \{X, H, S, P\},$$

$$\text{loop}_k(\emptyset) \approx \emptyset$$

$$\forall (k_1, k_2) \in \{X, H, S, P\}^2,$$

$$\text{loop}_{k_1}(\text{loop}_{k_2}(x)) \approx \text{loop}_{\min(k_1, k_2)}(x)$$

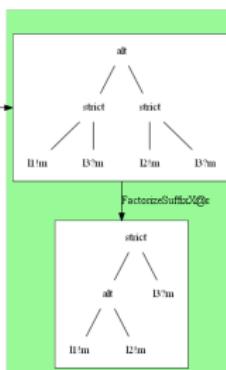
Match algebraic properties of underlying operators
(neutral element, associativity, commutativity, etc.)



Computing normal forms

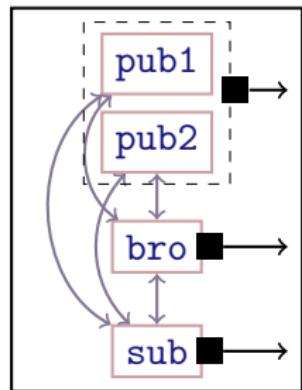
2 convergent rewrite systems

- orienting equations (termination)
- class rewriting (AC)
- ordered rewriting
(unique representants of AC-classes)
- two phases (distributivity)

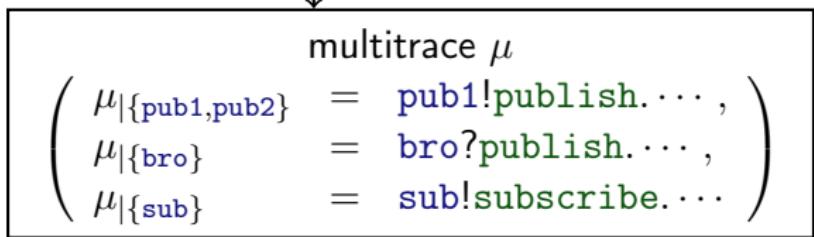




Having co-localized lifelines



given the partition of L

$$C = \left(\begin{array}{c} \{\text{pub1}, \text{pub2}\}, \\ \{\text{bro}\}, \\ \{\text{sub}\} \end{array} \right)$$




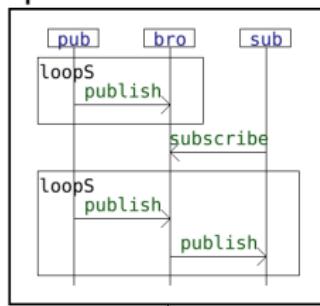
Denotational multi-trace semantics (general case)

Given a partition C of L defining the components of multi-traces:

$$\left(\mathbb{I}_\Omega, \left\{ \begin{array}{l} \emptyset, a \in \mathbb{A}_\Omega, \\ alt, strict, seq, par \\ loop_x, loop_h, loop_s, loop_p \end{array} \right\} \right)$$

↓
homomorphism \circledcirc_C

$$\left(\mathcal{P}(\mathbb{T}_{\Omega|C}), \left\{ \begin{array}{l} \{\epsilon_C\}, \{a \xrightarrow{\cdot} \epsilon_C\}, \\ \cup, \odot, \otimes, \mathbb{I}\mathbb{I}, \\ \odot^*, \otimes^*, \mathbb{I}\mathbb{I}^*, \end{array} \right\} \right)$$



$$\left\{ \begin{array}{l} (!\text{subscribe}, ?\text{subscribe}, \epsilon), \\ \dots, \\ (!\text{publish}\dots, ?\text{publish}, \epsilon), \\ \dots \end{array} \right\}$$



Multi-trace semantics up to the discrete partition

In the case where $C = (\{I\})_{I \in L} = \check{L}$, we have $\otimes = \odot$ and hence:

$$\begin{array}{c}
 \left(\mathbb{I}_\Omega, \left\{ \begin{array}{l} \emptyset, a \in \mathbb{A}_\Omega, \\ alt, strict, seq, par \\ loop_X, loop_H, loops, loop_P \end{array} \right\} \right) \\
 \sigma \swarrow \quad \quad \quad \searrow \odot_{\check{L}} \\
 \left(\mathcal{P}(\mathbb{T}_\Omega), \left\{ \begin{array}{l} \{\epsilon\}, \{a\}, \\ \cup, ;, ;*, ||, \\ ;^*, ;_*^*, ;**^*, ||* \end{array} \right\} \right) \xrightarrow{\text{proj}_{\check{L}}} \left(\mathcal{P}(\mathbb{T}_{\Omega|\check{L}}), \left\{ \begin{array}{l} \{\epsilon_{\check{L}}\}, \{a \vec{\odot} \epsilon_{\check{L}}\}, \\ \cup, \odot, \otimes, \mathbb{I}, \\ \odot^*, \otimes^*, \otimes^*, \mathbb{I}^* \end{array} \right\} \right)
 \end{array}$$

$\sigma|_{\check{L}} = \text{proj}_{\check{L}} \circ \sigma$



Projection preserves some algebraic structures

For any sets of traces T , T_1 and T_2 :

$$\mathbf{proj}_C(T_1 \cup T_2) = \mathbf{proj}_C(T_1) \cup \mathbf{proj}_C(T_2)$$

$$\mathbf{proj}_C(T_1; T_2) = \mathbf{proj}_C(T_1) \odot \mathbf{proj}_C(T_2)$$

$$\mathbf{proj}_C(T_1 || T_2) = \mathbf{proj}_C(T_1) \oslash \mathbf{proj}_C(T_2)$$

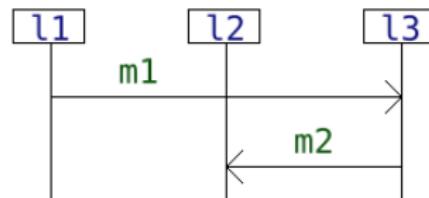
$$\mathbf{proj}_C(T^{;*}) = \mathbf{proj}_C(T)^{\odot *}$$

$$\mathbf{proj}_C(T^{\parallel *}) = \mathbf{proj}_C(T)^{\oslash *}$$



Counter example

Given $L = \{l_1, l_2, l_3\}$ and the partition $C = (\{l_1, l_2\}, \{l_3\})$



$$\begin{aligned} \text{proj}_C \left(\begin{array}{c} \{l_1!m_1.l_3?m_1\} \\ ;* \{l_3!m_2.l_2?m_2\} \end{array} \right) &= \text{proj}_C(\{l_1!m_1.l_3?m_1.l_3!m_2.l_2?m_2\}) \\ &= \left\{ \left(\begin{array}{c} l_1!m_1.l_2?m_2, \\ l_3?m_1.l_3!m_2 \end{array} \right) \right\} \end{aligned}$$

$$\begin{aligned} \left(\begin{array}{c} \text{proj}_C(\{l_1!m_1.l_3?m_1\}) \\ \otimes_c \text{proj}_C(\{l_3!m_2.l_2?m_2\}) \end{array} \right) &= \left\{ \left(\begin{array}{c} l_1!m_1, \\ l_3?m_1 \end{array} \right) \right\} \otimes_c \left\{ \left(\begin{array}{c} l_2?m_2, \\ l_3!m_2 \end{array} \right) \right\} \\ &= \left\{ \left(\begin{array}{c} l_1!m_1.l_2?m_2, \\ l_3?m_1.l_3!m_2 \end{array} \right), \left(\begin{array}{c} l_2?m_2.l_1!m_1, \\ l_3?m_1.l_3!m_2 \end{array} \right) \right\} \end{aligned}$$



Semantics of prefixes and slices

full observation

```
[l1]   ← l1!m1 . l1!m1 . l1?m4
[l2,l3] ← l2?m1 . l3!m4 . l2!m3
```

early cessation of observation

```
[l1]   ← l1!m1 . l1!m1 . l1?m4
[l2,l3] ← l2?m1
```

late start of observation

```
[l1]   ← l1!m1 . l1?m4
[l2,l3] ← l2?m1 . l3!m4 . l2!m3
```

both

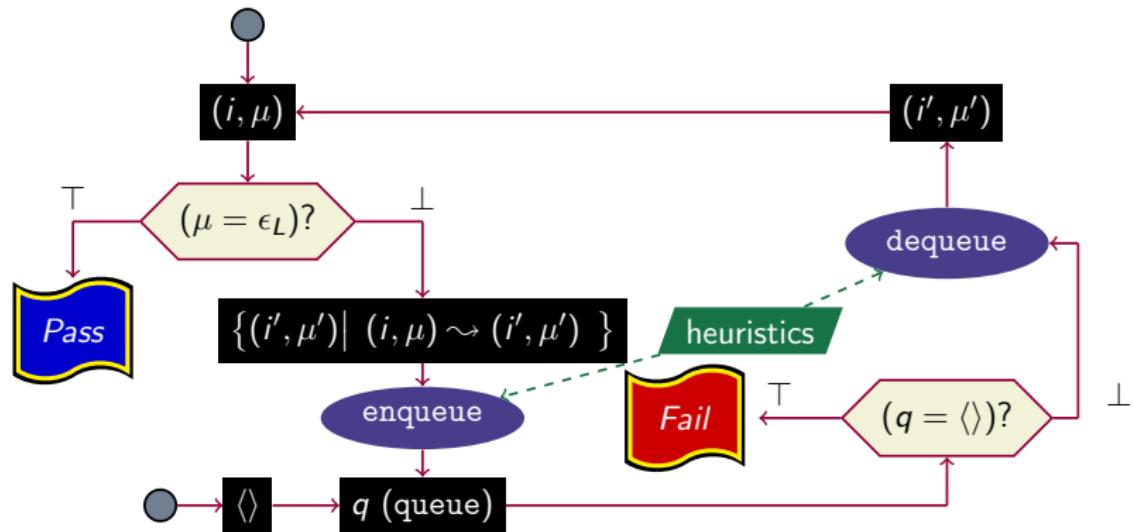
```
[l1]   ← l1!m1 . l1?m4
[l2,l3] ← l2?m1
```

For any interaction $i \in \mathbb{I}_\Omega$:

- ▶ $\sigma_{|C}^\dagger(i) = \text{proj}_C(\overline{\sigma(i)})$
- ▶ $\overline{\sigma_{|C}}(i) = \overline{\sigma_{|C}(i)}$
- ▶ $\overline{\text{@}_C}(i) = \overline{\text{@}_C(i)}$
- ▶ $\overline{\sigma_{|C}}(i) = \underline{\overline{\sigma_{|C}(i)}}$

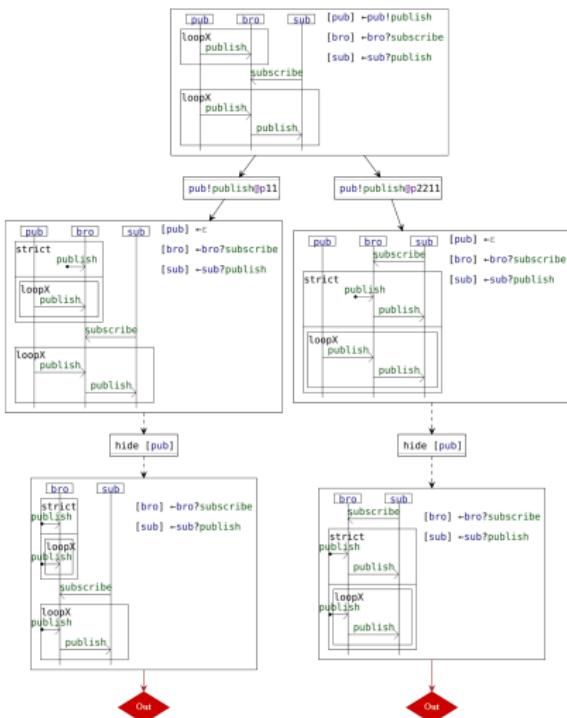


Using heuristics, etc.

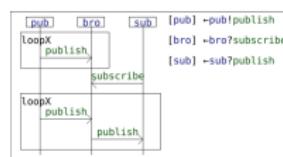




Reducing the search space with local frontiers



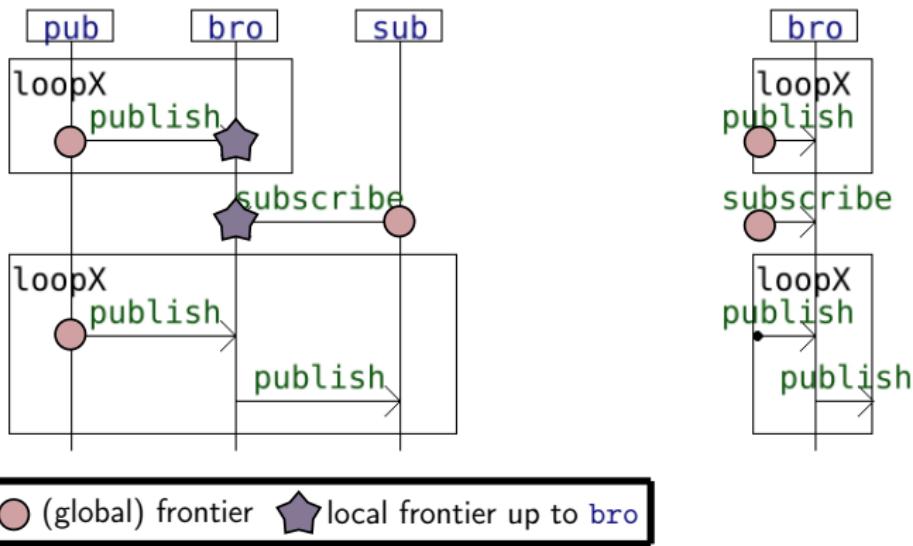
pointlessly explored paths



direct verdict

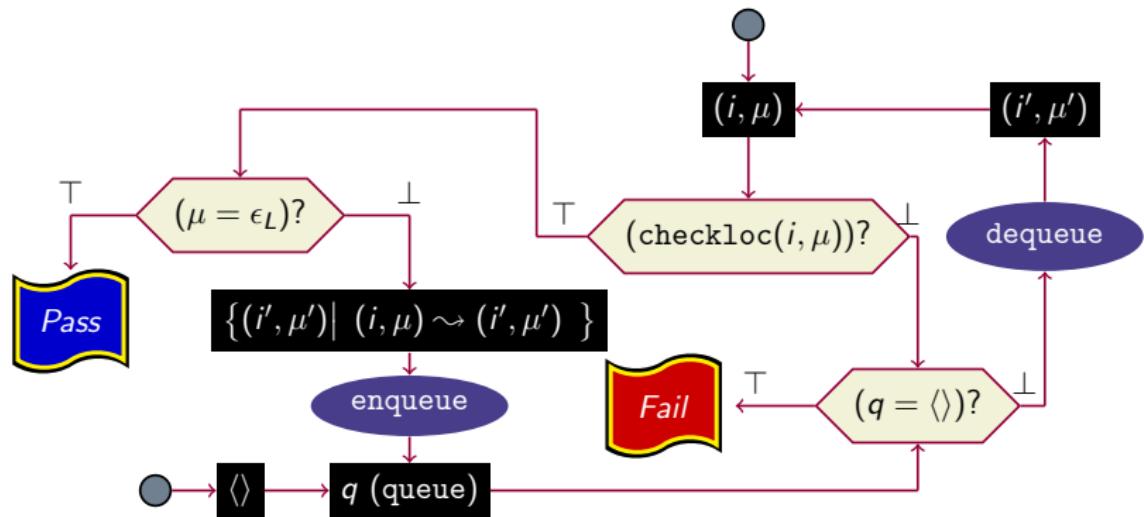


Local frontiers



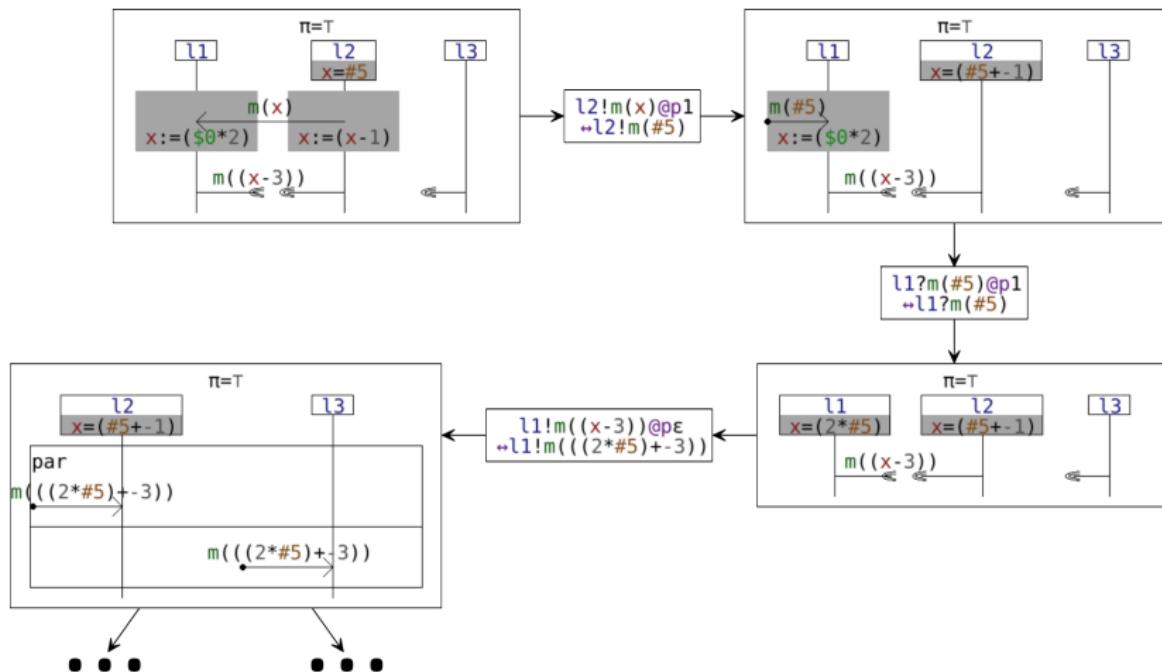


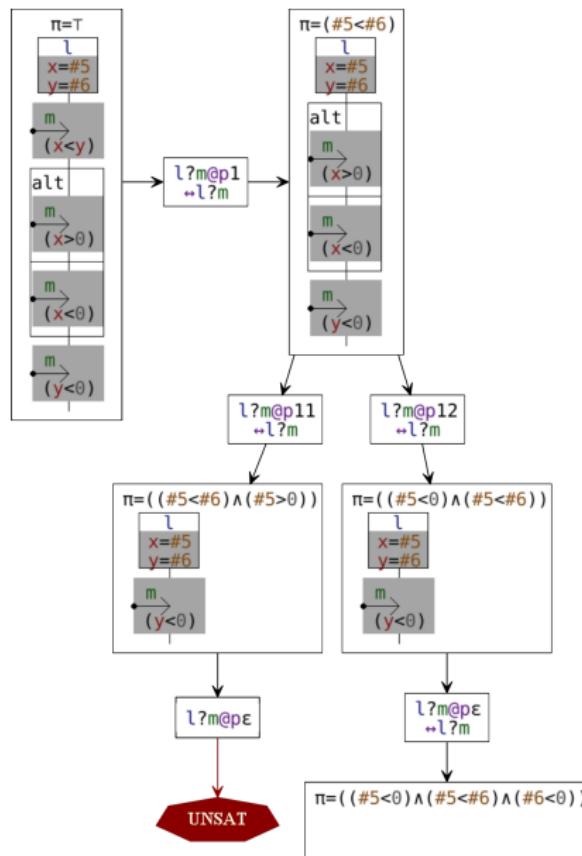
Algorithm with the checking of local frontiers





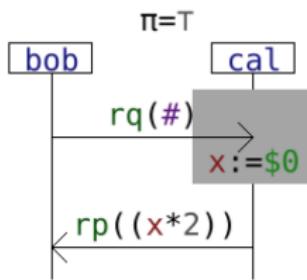
Value passing & symbolic execution







Analyses with data



Accepted behavior

```
[bob] bob!rq(4);
[cal] cal?rq(4).cal!rp(8)
```

Wrong computation

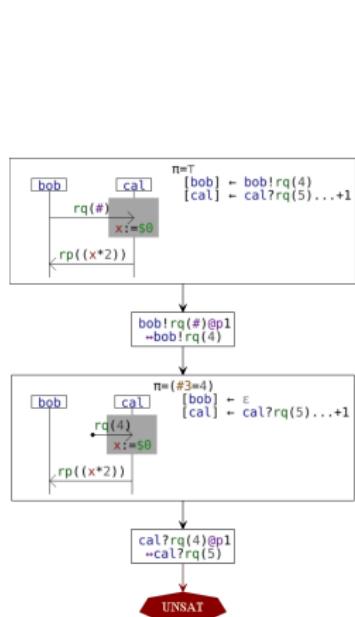
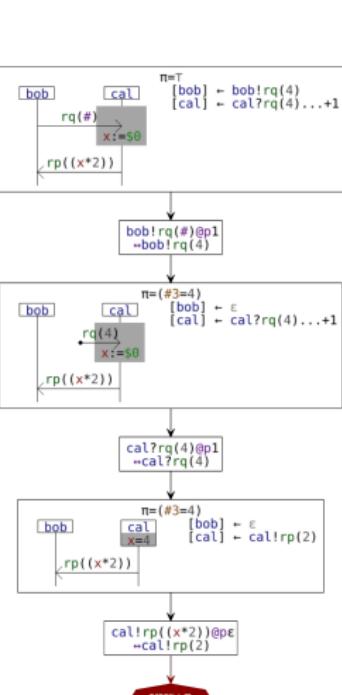
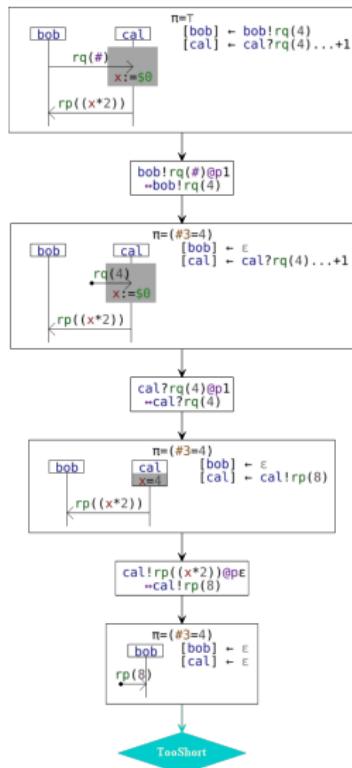
```
[bob] bob!rq(4);
[cal] cal?rq(4).cal!rp(2)
```

Man-in-the-middle

```
[bob] bob!rq(4);
[cal] cal?rq(5).cal!rp(10)
```

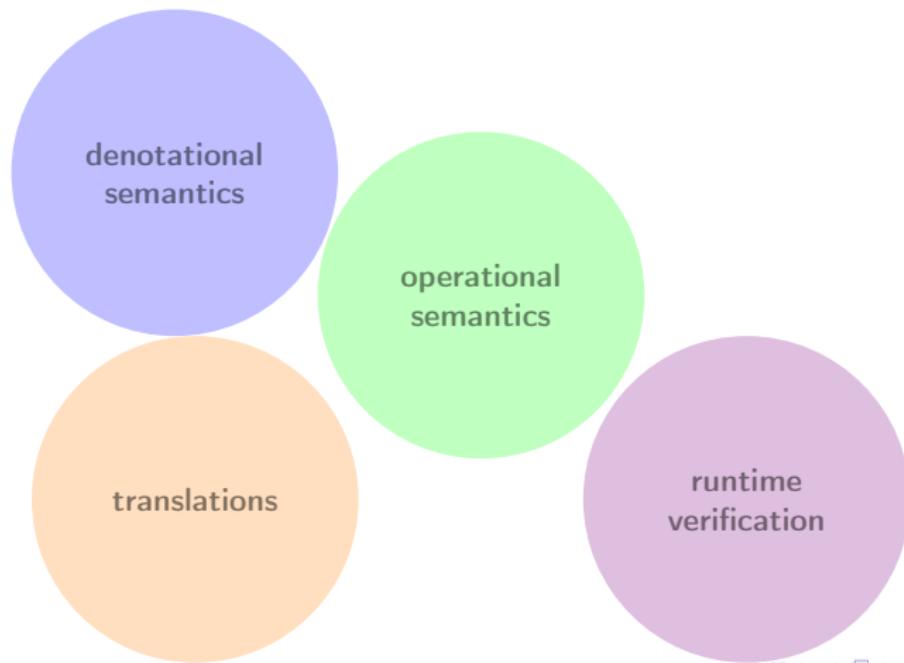


Analyses with data



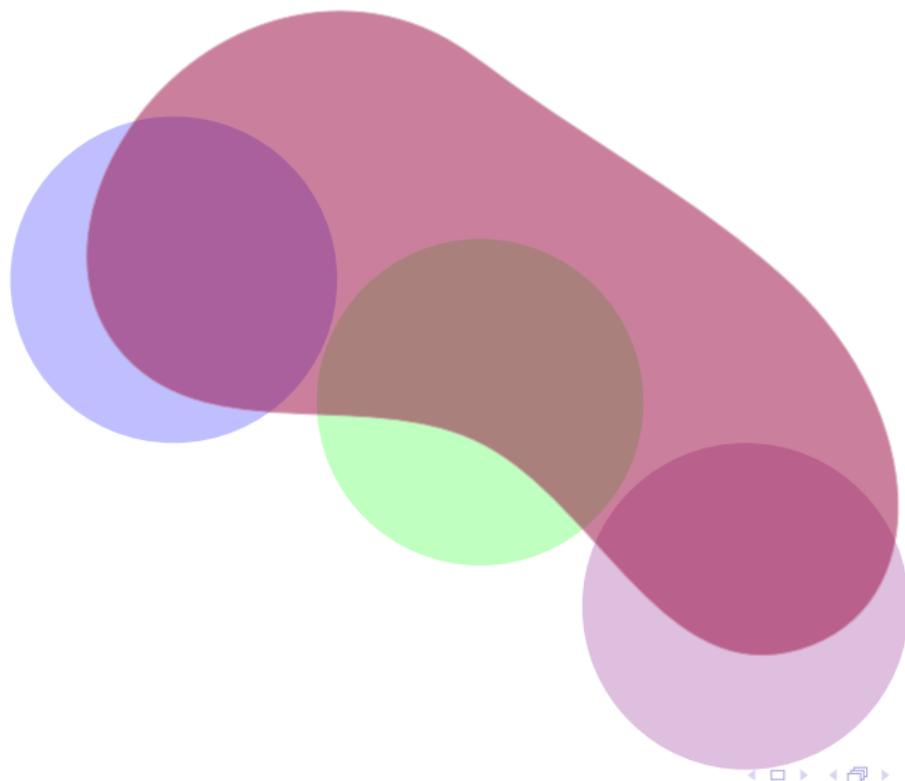


Position and main results of the thesis





Position and main results of the thesis





Position and main results of the thesis

