4190.310 Programming Language The K-- Language

1 Syntax

```
Expression \ e \ \rightarrow \ {\tt unit}
                                                                                  unit
                           x := e
                                                                                  {\it assignment}
                                                                                 sequence
                           \quad \text{if } e \text{ then } e \text{ else } e \\
                                                                                 branch
                           \quad \text{while } e \text{ do } e
                                                                                  while loop
                           \quad \text{for } x \ := \ e \ \text{to} \ e \ \text{do} \ e
                                                                                 for loop
                           {\tt read}\ x
                                                                                 input
                           \quad \text{write } e
                                                                                 output
                           \mathtt{let}\ x\ :=\ e\ \mathtt{in}\ e
                                                                                  variable binding
                           let proc f(x) = e in e
                                                                                 procedure binding
                           f(e)
                                                                                  call by value
                           f<x>
                                                                                  call by reference
                                                                                 integer
                                                                                 boolean
                           true | false
                                                                                  identifier
                                                                                 arithmetic operation
                           e + e | e - e | e * e | e / e
                           e < e \mid e = e \mid \text{not } e
                                                                                 conditional operation
```

1.1 Program

A program is an expression.

1.2 Identifiers

Alpha-numeric identifiers are [a-zA-Z][a-zA-Z0-9_]*. Identifiers are case sensitive: z and Z are different. The reserved words cannot be used as identifiers: unit true false not if then else let in end proc while do for to read write

1.3 Numbers/Comments

Numbers are integers, optionally prefixed with -(for negative integer): -?[0-9] $^+$. A comment is any character sequence within the comment block (* *). The comment block can be nested.

1.4 Precedence/Associativity

In parsing K-- program text, the precedence of the K-- constructs in decreasing order is as follows. Symbols in the same set have identical precedence. Symbols with subscript L (respectively R) are left (respectively right) associative. Symbols without subscript are nonassociative.

```
 \{ \text{not} \}_R, \\ \{ *, / \}_L, \\ \{ +, - \}_L, \\ \{ =, < \}_L, \\ \{ \text{write} \}_R, \\ \{ := \}_R, \\ \{ \text{then} \}, \\ \{ \text{do} \}, \\ \{ ; \}_L, \\ \{ \text{in} \}
```

For example, K-- program

```
x := e1; e2 \Rightarrow (x := e1); e2 while e do e1; e2 \Rightarrow (while e do e1); e2 if e1 then e2 else e3; e4 \Rightarrow (if e1 then e2 else e3); e4
```

Rule of thumb: for your test programs, if your programs are hard to read (hence can be parsed not as you expected) then put parentheses around.

2 Domains

3 Semantics

$$\begin{aligned} & \text{EQUALT} \ \frac{\sigma, M \vdash e_1 \Rightarrow v_1, M'}{\sigma, M \vdash e_1 = e_2 \Rightarrow \text{true}, M''} & v_1 = v_2 = n \\ & \sigma, M \vdash e_1 = e_2 \Rightarrow \text{true}, M'' & \forall v_1 = v_2 = b \\ & \forall v_1 = v_2 = \cdot \end{aligned}$$

EQUALF
$$\frac{\sigma, M \vdash e_1 \Rightarrow v_1, M' \qquad \sigma, M' \vdash e_2 \Rightarrow v_2, M''}{\sigma, M \vdash e_1 = e_2 \Rightarrow \text{false}, M''}$$
 otherwise

LESS
$$\frac{\sigma, M \vdash e_1 \Rightarrow n_1, M' \qquad \sigma, M' \vdash e_2 \Rightarrow n_2, M''}{\sigma, M \vdash e_1 < e_2 \Rightarrow n_1 < n_2, M''}$$

NOT
$$\frac{\sigma, M \vdash e \Rightarrow b, M'}{\sigma, M \vdash \text{not } e \Rightarrow not \ b, M'}$$

ASSIGN
$$\frac{\sigma, M \vdash e \Rightarrow v, M'}{\sigma, M \vdash x := e \Rightarrow v, M' \{ \sigma(x) \mapsto v \}}$$

SEQ
$$\frac{\sigma, M \vdash e_1 \Rightarrow v_1, M' \qquad \sigma, M' \vdash e_2 \Rightarrow v_2, M''}{\sigma, M \vdash e_1 \; ; \; e_2 \Rightarrow v_2, M''}$$

IFT
$$\frac{\sigma, M \vdash e \Rightarrow true, M' \qquad \sigma, M' \vdash e_1 \Rightarrow v, M''}{\sigma, M \vdash \text{if } e \text{ then } e_1 \text{ else } e_2 \Rightarrow v, M''}$$

$$\text{IFF } \frac{\sigma, M \vdash e \Rightarrow false, M' \qquad \sigma, M' \vdash e_2 \Rightarrow v, M''}{\sigma, M \vdash \text{if } e \text{ then } e_1 \text{ else } e_2 \Rightarrow v, M''}$$

WHILEF
$$\frac{\sigma, M \vdash e_1 \Rightarrow false, M'}{\sigma, M \vdash \texttt{while} \ e_1 \ \texttt{do} \ e_2 \Rightarrow \cdot, M'}$$

$$\sigma, M \vdash e_1 \Rightarrow true, M'$$
 WHILET
$$\frac{\sigma, M' \vdash e_2 \Rightarrow v_1, M_1 \qquad \sigma, M_1 \vdash \texttt{while} \ e_1 \ \texttt{do} \ e_2 \Rightarrow v_2, M_2}{\sigma, M \vdash \texttt{while} \ e_1 \ \texttt{do} \ e_2 \Rightarrow v_2, M_2}$$

$$\sigma, M \vdash e_{I} \Rightarrow n_{1}, M' \qquad \sigma, M' \vdash e_{2} \Rightarrow n_{2}, M''$$

$$\sigma, M'' \{\sigma(x) \mapsto n_{1} + 0\} \vdash e_{3} \Rightarrow v_{0}, M_{0}$$

$$\vdots$$
FORT
$$\frac{\sigma, M_{n_{2} - n_{1} - 1} \{\sigma(x) \mapsto n_{1} + (n_{2} - n_{1})\} \vdash e_{3} \Rightarrow v_{n_{2} - n_{1}}, M_{n_{2} - n_{1}}}{\sigma, M \vdash \text{for } x := e_{I} \text{ to } e_{2} \text{ do } e_{3} \Rightarrow \cdot, M_{n_{2} - n_{1}}} n_{2} \geq n_{1}}$$

$$\text{FORF} \frac{\sigma, M \vdash e_{I} \Rightarrow n_{1}, M' \qquad \sigma, M' \vdash e_{2} \Rightarrow n_{2}, M''}{\sigma, M \vdash \text{for } x := e_{I} \text{ to } e_{2} \text{ do } e_{3} \Rightarrow \cdot, M''} n_{2} < n_{1}}$$

$$\text{TORF} \frac{\sigma, M \vdash e_{I} \Rightarrow v, M'}{\sigma, M \vdash \text{let } x := e_{I} \text{ in } e_{2} \Rightarrow v', M''} l \notin Dom M'$$

$$\text{LETV} \frac{\sigma, M \vdash \text{let } x := e_{I} \text{ in } e_{2} \Rightarrow v', M''}{\sigma, M \vdash \text{let } proc \ f(x) = e_{I} \text{ in } e_{2} \Rightarrow v, M'}$$

$$\text{CALLV} \frac{\sigma, M \vdash e \Rightarrow v, M'}{\sigma, M \vdash f(e) \Rightarrow v', M''} \sigma, M \vdash f(e) \Rightarrow v', M''}{\sigma, M \vdash f(e) \Rightarrow v', M''} \sigma (f) = \langle x, e', \sigma' \rangle$$

$$\text{CALLR} \frac{\sigma'\{x \mapsto \sigma(y)\}\{f \mapsto \langle x, e, \sigma' \rangle\}, M \vdash e \Rightarrow v, M'}{\sigma, M \vdash f < y > \Rightarrow v, M'}$$

$$\text{READ} \frac{\sigma, M \vdash e \Rightarrow n, M'}{\sigma, M \vdash \text{read} \ x \Rightarrow n, M\{\sigma(x) \mapsto n\}}$$

$$\text{WRITE} \frac{\sigma, M \vdash e \Rightarrow n, M'}{\sigma, M \vdash \text{write} \ e \Rightarrow n, M'}$$