

Problem 3

```
In[ ]:= exact =  $\frac{\pi^2}{8 \alpha} * \left(1 - \frac{2}{\pi \sqrt{\alpha}} \operatorname{Tanh}\left[\pi \frac{\sqrt{\alpha}}{2}\right]\right);$ 
summ = Sum[ $\frac{1}{m^2 (m^2 + \alpha)}$ , {m, 1, M, 2}];
Abs[N[exact /.  $\alpha \rightarrow 0.5$ ] - N[summ /. { $\alpha \rightarrow 0.5$ , M  $\rightarrow 31$ }]]
ClearAll["Global`*"]
```

Out[]:= 5.07488×10^{-6}

Problem 4

```
In[ ]:= ClearAll["Global`*"]
a = Sin[(2 m + k) x1 / 3] * Sin[k * y1] * Sin[(2 m + k) x2 / 3] * Sin[k * y2];
b = (k^2 + k * m + m^2)^2;
d = Sum[Sum[ $\frac{a}{b}$ , {m, 2, 12, 2}], {k, 1, 11, 2}];
N[d /. {x1  $\rightarrow 0.4$ , y1  $\rightarrow 0.65$ , x2  $\rightarrow 0.3$ , y2  $\rightarrow 0.45$ }]
```

Out[]:= 0.00428477

Problem 5

```
In[ ]:= k = {{1, 0, -1, 0}, {0, 0, 0, 0}, {-1, 0, 1, 0}, {0, 0, 0, 0}};
t = {{Cos[ $\theta$ ], Sin[ $\theta$ ], 0, 0}, {-Sin[ $\theta$ ], Cos[ $\theta$ ], 0, 0},
      {0, 0, Cos[ $\theta$ ], Sin[ $\theta$ ]}, {0, 0, -Sin[ $\theta$ ], Cos[ $\theta$ ]}};
result = Transpose[t].k.t;
MatrixForm[result]
```

Out[]//MatrixForm=

$$\begin{pmatrix} \cos^2[\theta] & \cos[\theta] \sin[\theta] & -\cos^2[\theta] & -\cos[\theta] \sin[\theta] \\ \cos[\theta] \sin[\theta] & \sin^2[\theta] & -\cos[\theta] \sin[\theta] & -\sin^2[\theta] \\ -\cos^2[\theta] & -\cos[\theta] \sin[\theta] & \cos^2[\theta] & \cos[\theta] \sin[\theta] \\ -\cos[\theta] \sin[\theta] & -\sin^2[\theta] & \cos[\theta] \sin[\theta] & \sin^2[\theta] \end{pmatrix}$$

Problem 6

```
In[ ]:= ClearAll["Global`*"]
```

$$\text{matrix} = \begin{pmatrix} x^2 + y^2 & x & y & 1 \\ x1^2 + y1^2 & x1 & y1 & 1 \\ x2^2 + y2^2 & x2 & y2 & 1 \\ x3^2 + y3^2 & x3 & y3 & 1 \end{pmatrix};$$

```
a = Det[matrix] /. {x1 -> -2, y1 -> 2, x2 -> 0, y2 -> 0, x3 -> 1, y3 -> 1}
Solve[a == 0, y] /. {x1 -> -2, y1 -> 2, x2 -> 0, y2 -> 0, x3 -> 1, y3 -> 1}
```

```
Out[ ]:= 4 x + 4 x^2 - 12 y + 4 y^2
```

```
Out[ ]:= {{y -> 1/2 (3 - Sqrt[9 - 4 x - 4 x^2])}, {y -> 1/2 (3 + Sqrt[9 - 4 x - 4 x^2])}}
```

Problem 7

```
In[ ]:= ClearAll["Global`*"]
```

$$A = \begin{pmatrix} \frac{10}{3} & \frac{5}{3} & \frac{10}{7} \\ \frac{10}{3} & \frac{30}{7} & \frac{50}{9} \\ \frac{20}{9} & 5 & \frac{50}{7} \end{pmatrix};$$

```
B = {5/3, 9/7, 2/3};
```

```
c = LinearSolve[A, B]
```

```
A.c == B (*if the answer is true. then what we obtained is verified*)
```

```
Out[ ]:= {33/26, -16/5, 126/65}
```

```
Out[ ]:= True
```

Problem 8

```
In[ ]:= ClearAll["Global`*"]
```

```
d = Det[{ {30 - λ, -√6, -√6}, {-√6, 41 - λ, -15}, {-√6, -15, 41 - λ} }];
```

```
Solve[d == 0, λ]
```

```
Out[ ]:= {{λ -> 24}, {λ -> 32}, {λ -> 56}}
```

Problem 9

```
In[ ]:= ClearAll["Global`*"];
```

$$d = \begin{pmatrix} 0 & 0 & 0 & 0.83 & 0.83 & 0.5 & 0.5 & 0.11 & 0.11 & 0 \\ 0.94 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0.98 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0.98 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0.98 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0.98 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0.98 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0.98 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0.97 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0.97 & 0 \end{pmatrix};$$

```
w = Eigensystem[d];
eigen = w[[1]]
real = Select[eigen, FreeQ[#, Complex] &]
Max[real]
```

```
Out[ ]:= {1.19025, 0.242897 + 0.862085 i, 0.242897 - 0.862085 i,
-0.804648 + 0.286163 i, -0.804648 - 0.286163 i, 0.159505 + 0.589166 i,
0.159505 - 0.589166 i, -0.19288 + 0.552497 i, -0.19288 - 0.552497 i, 0.}
```

```
Out[ ]:= {1.19025, 0.}
```

```
Out[ ]:= 1.19025
```

Problem 10

```
In[ ]:= ClearAll["Global`*"]
B = {{3, 6, 6}, {6, 3, 6}, {6, 6, 3}};
B.B - 12 B - 45 * IdentityMatrix[3] // MatrixForm
```

```
Out[ ]:= MatrixForm=
```

$$\begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$