

Efficient Polyhedral Gravity Modeling in Modern C++ and Python

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DOI: 10.xxxx/draft

Software

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Submitted: 01 January 1970 Published: unpublished

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Summary

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Polyhedral gravity models are ubiquitous for modeling the gravitational field of irregular bodies, 8 such as asteroids and comets. We present an open-source C++ library for the efficient, parallelized computation of a polyhedral gravity model. We also provide a Python interface to 10 the library using pybind11. The library is particularly focused on delivering high performance 11 and scalability which we achieve through vectorization and parallelization with xsimd and 12 thrust, respectively. The library supports many common formats, such as .stl, .off, .ply, .mesh 13 and tetgen's .node and .face.

Statement of Need

The complex gravitational fields of irregular bodies, such as asteroids and comets, are often modeled using polyhedral gravity models as they provide an analytic solution for the computation of the gravitational potential, acceleration (and second derivative) given a mesh of the body (Tsoulis, 2012; Tsoulis & Gavrillidou, 2021). The computation of the gravitational potential and acceleration is a computationally expensive task, especially for large meshes, which can however benefit from parallelization either over computed targets points for which we seek potential and acceleration or over the mesh. Thus, a high-performance implementation of a polyhedral gravity model is desirable.

While some research code for these models exists, they are not focused on usability and limited 24

- to FORTRAN TODO LINK and proprietary software like MATLAB TODO LINK. There is 25
- a lack of well-documented, maintained open-source implementations, particularly in modern 26
- programming languages and with a focus on scalability and performance. 27

The presented software has already seen application in several research works. It has been 28 used to optimize trajectories around the highly irregular comet 67P/Churyumov-Gerasimenko 29 (Maråk et al., 2023). Further, it has been used to study the effectiveness of so-called neural 30 density fields (Izzo & Gómez, 2022), where it can serve as a ground truth and to pretrain 31

neural networks (Schuhmacher et al., 2023). TODO_add_more_examples 32

Thus, overall this model is highly versatile and can be used in a wide range of applications. We 33 hope it will enable further research in the field, especially related to recent machine learning 34 techniques, which typically rely on Python implementations. 35

Polyhedral Model 36

On a mathematical level, the implemented model follows the approach by Petrović (Petrović, 37 1996) as refined by Tsoulis and Petrović (Tsoulis & Petrović, 2001). A comprehensive 38



- description of the mathematical foundations of the model is given in the associated student
- ⁴⁰ report (Schuhmacher, 2022).
- ⁴¹ Implementation-wise it makes use of the inherent parallelization opportunity of the approach
- 42 as it iterates over the mesh. This parallelization is achieved via *thrust* which allows utilizing
- 43 OpenMP and Intel TBB. On a finer scale, individual costly operations were investigated and,
- $_{\rm 44}$ $\,$ e.g., the arctan operations were vectorized using xsimd. On an application side, the user may
- $_{\tt 45}$ $\,$ use the implemented caching mechanism to avoid recomputation of mesh properties, such as
- 46 the face normals.
- Extensive tests using GoogleTest are used via GitHub Actions to ensure the (continued)
 correctness of the implementation.

⁴⁹ Installation & Contribution

- ⁵⁰ The library is available on GitHub¹ and can be installed with *pip* or from *conda*². Build
- ⁵¹ instructions using *CMake* are provided in the repository. The library is licensed under a GPL ⁵² license.
- 53 The project is open to contributions via pull requests with instructions on how to contribute
- 54 provided in the repository.

55 Usage Instructions

- ⁵⁶ We provide detailed usage instructions in the technical documentation on ReadTheDocs ³.
- 57 Additionally, a minimal working example is given in the repository readme and more extensive
- ⁵⁸ examples as a *Jupyter* notebook ⁴.

Acknowledgements

⁶⁰ The authors would like to thank Dario Izzo and Emmanuel Blazquez for their feedback on the ⁶¹ original model implementation.

References

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- Izzo, D., & Gómez, P. (2022). Geodesy of irregular small bodies via neural density fields.
 Communications Engineering, 1(1), 48.
- Maråk, R., Blazquez, E., & Gómez, P. (2023). Trajectory optimization of a spacecraft swarm
 orbiting around 67P/Churyumov-Gerasimenko. Proceedings of the 12th International
 Conference on Guidance, Navigation & Control Systems (GNC).
- Petrović, S. (1996). Determination of the potential of homogeneous polyhedral bodies using
 line integrals. *Journal of Geodesy*, *71*, 44–52.
- Schuhmacher, J. (2022). Efficient polyhedral gravity modeling in modern c++ [Master's thesis]. Technical University of Munich.
- 72 Schuhmacher, J., Gratl, F., Izzo, D., & Gómez, P. (2023). Investigation of the robustness of
- neural density fields. Proceedings of the 9th International Conference on Astrodynamics
- 74 Tools and Techniques, ICATT.

³https://polyhedral-gravity-model-cpp.readthedocs.io/en/latest/

 $^{{}^{1}} https://github.com/esa/polyhedral-gravity-model$

 $^{^{2}} https://anaconda.org/conda-forge/polyhedral-gravity-model$

 $^{{}^{4} {\}rm https://github.com/esa/polyhedral-gravity-model/blob/main/script/polyhedral-gravity.ipynb}$



- Tsoulis, D. (2012). Analytical computation of the full gravity tensor of a homogeneous
 arbitrarily shaped polyhedral source using line integrals. *Geophysics*, 77(2), F1–F11.
- Tsoulis, D., & Gavriilidou, G. (2021). A computational review of the line integral analytical formulation of the polyhedral gravity signal. *Geophysical Prospecting*, *69*(8-9), 1745–1760.
- ⁷⁹ Tsoulis, D., & Petrović, S. (2001). On the singularities of the gravity field of a homogeneous
- ⁸⁰ polyhedral body. *Geophysics*, 66(2), 535–539.

Schuhmacher et al. (2023). Efficient Polyhedral Gravity Modeling in Modern C++ and Python. Journal of Open Source Software, 0(0), ¿PAGE? 3 https://doi.org/10.xxxxx/draft.