

# CENG 391 Introduction to Image Understanding

December 22, 2016

## Fundamental Matrix Estimation

Write a C++/Python program that operates the following tasks.

1. Read the image("horse\_0.JPG")
2. Read the image("horse\_20.JPG")
3. Read the correspondences from the file "corrs.txt"
4. Normalized 8-point algorithm:
  - Normalize point coordinates for each image.
  - Compute  $\tilde{F}$  using DLT.
    - Construct a matrix A with normalized points as in the following:

$$x'^T F x = 0 \quad (1)$$

where  $\mathbf{x} = (x, y, 1)$  and  $\mathbf{x}' = (x', y', 1)$ .

—  $Af = 0$  where

$$A = \begin{bmatrix} x'_1 x_1 & x'_1 y_1 & x'_1 & y'_1 x_1 & y'_1 y_1 & y'_1 & x_1 & y_1 & 1 \\ \cdot & \cdot & \cdot & \cdot & \cdot & \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & \cdot & \cdot & \cdot & \cdot & \cdot \\ x'_n x_n & x'_n y_n & x'_n & y'_n x_n & y'_n y_n & y'_n & x_n & y_n & 1 \end{bmatrix} \quad (2)$$

— Select  $n$  as more than 8. Because 8 point correspondences are enough to find a unique solution for F.

- Find Fundamental matrix(F) by taking Singular Value Decomposition(SVD) of A.
- The last column of "SVD.vt" gives fundamental matrix( $\tilde{F}$ ).
- Unnormalize:  $F = T'^{-1}\tilde{F}T$
- Forcing Rank-2 Constraint
  - Matrix F is replaced by F' that minimizes the Frobenius norm  $\|F - F'\|$  subject to the condition  $\det(F')=0$ .
  - This can be done again using SVD. Let  $F = UDV^T$ , where D is a diagonal matrix  $D=\text{diag}(r,s,t)$ . Then,  $F'=U\text{diag}(r,s,0)V^T$ .

5. Apply RANSAC:

- (a) Choose the number of iterations  $N$  as 10000 initially.
- (b) Select 8 random correspondences.
- (c) Compute Fundamental Matrix (F) with these correspondences by applying Normalized 8-point algorithm.
- (d) Project points to epipolar lines by  $l' = F * x$
- (e) Count number of inliers as follows:
  - Compute the distance between the epipolar line and corresponding point.
  - Check whether the distance is smaller than **3 pixels**. If it is, then this correspondence is inlier.
- (f) Compute the inlier ratio as follows:

$$\text{inlierRatio} = \% \frac{\text{numberOfInliers}}{\text{numberOfCorrespondences}} \quad (3)$$

- (g) Update  $N$  as follows:
  - i. Calculate the probability( $w$ ) of each of the randomly selected correspondence is inlier.
  - ii.  $1 - (1 - w^s)^N \geq 0.99$ . From there, calculate  $N$ .
- (h) Repeat step[b-g]  $N$  times and save the fundamental matrix that gives the maximum inlier ratio.

6. Compute inliers with the best F that is calculated in previous step.

7. Compute final  $F$  with all of these inliers by using Normalized 8-point algorithm.
8. Optionally, you can calculate better fundamental matrix as you did in homework for the homography calculation.