For each α, choose random $\mathbf{x_v} \in \mathbf{Q}[\mathbb{Z}_2^{\mathbf{k}}]$