

Erstgutachterin: PD Dr. Jeanette Lorenz
Zweitgutachter: Prof. Dr. Wolfgang Dünneweber

Search for electroweakinos with the ATLAS detector

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Part I

Fundamental concepts

Chapter 3

Statistical data analysis

In high energy physics (HEP), statistical models are used to quantify the correspondence between theoretical predictions and the experimental observations. This chapter introduces the statistical concepts, methods and formulae used for statistical inference in this thesis. A frequentist approach is employed, interpreting probabilities as the frequencies of the outcomes of repeatable experiments that may either be real, based on computer simulations, or originate from mathematical abstraction [9]. The following description largely adheres to Refs. [160, 161].

3.1 The likelihood function

In measurements in HEP, a *statistical model* $f(\mathbf{x}|\boldsymbol{\phi})$ is a parametric family of probability density functions (pdfs) describing the probability of observing data \mathbf{x} given a set[†] of model parameters $\boldsymbol{\phi}$. The latter typically describe parameters of the physical theory or unknown detector effects. The *likelihood function* $L(\boldsymbol{\phi})$ is then numerically equivalent to $f(\mathbf{x}|\boldsymbol{\phi})$ with \mathbf{x} fixed. As opposed to the pdf $f(\mathbf{x})$, describing the value of f as a function of \mathbf{x} given a set of fixed parameters $\boldsymbol{\phi}$, the likelihood refers to the value of f as a function of $\boldsymbol{\phi}$ given a fixed[§] value of \mathbf{x} .

Searches for beyond the Standard Model (BSM) physics are often[‡] centred around the measurement of several disjoint binned distributions, called *channels* c , each associated with different event selection criteria yielding observed event counts \mathbf{n} . In such counting experiments, where each event is independently drawn from the same underlying distribution, each bin is described by a Poisson term. The Poisson probability to observe n events with an expectation of ν events, $\text{Pois}(n|\nu)$, is given by

$$\text{Pois}(n|\nu) = \frac{\nu^n}{n!} e^{-\nu}. \quad (3.1)$$

The expectation ν_{cb} in each channel c and bin b is a sum over the set of physics processes considered, called *samples* in the following,

$$\nu_{cb} = \sum_{s \in \text{samples}} \nu_{csb}(\boldsymbol{\eta}, \boldsymbol{\chi}), \quad (3.2)$$

[†] Sets of parameters (as opposed to single parameters) will henceforth be written using bold face.

[§] This important difference is why the likelihood is written here as $L(\boldsymbol{\phi})$ instead of the equally common $L(\mathbf{x}|\boldsymbol{\phi})$.

[‡] While searches for BSM physics using unbinned distributions also exist, only binned searches are considered in the following.

where ν_{csb} is the expected sample rate in a given bin of a given channel. The sample-wise rates are in general a function of the model parameters ϕ that can be either *free parameters* η or *constrained parameters* χ . Possible modifications of the expected sample rates due to model parameters are considered to be either multiplicative or additive changes to the nominal estimate ν_{csb}^0 of the form

$$\nu_{csb}(\eta, \chi) = \left(\prod_i f_{csb}^i(\eta, \chi) \right) \left(\nu_{csb}^0 + \sum_j \Delta_{csb}^j(\eta, \chi) \right). \quad (3.3)$$

Here, $f(\phi)$ and $\Delta(\phi)$ are the multiplicative and additive *rate modifiers*, respectively, modifying the nominal estimates. Although in practice often only a function of a single model parameter, the rate modifiers can in general be a function of a set of model parameters.

Free parameters directly determined by the data observations are called *normalisation factors*. The constrained parameters represent the systematic uncertainties considered in the model, which—in frequentist statistics—have fixed but unknown true values. The degree to which they cause a deviation of the expected event rates from the nominal event rates is limited through *constraint terms* $c_\chi(a_\chi|\chi)$ that can be viewed as *auxiliary measurements* with global observed data \mathbf{a} .

For a given observation $\mathbf{x} = (\mathbf{n}, \mathbf{a})$ of observed events \mathbf{n} and auxiliary data \mathbf{a} , the likelihood then reads

$$L(\eta, \chi) = \prod_{c \in \text{channels}} \prod_{b \in \text{bins}_c} \text{Pois}(n_{cb} | \nu_{cb}(\eta, \chi)) \prod_{\chi \in \chi} c_\chi(a_\chi | \chi), \quad (3.4)$$

where, given a certain integrated luminosity, n_{cb} and ν_{cb} refer to the corresponding observed and expected rate of events, respectively [162]. Most of the systematic uncertainties are so-called *interpolation parameters* α representing either normalisation uncertainties or correlated shape uncertainties. Their constraint terms $c_\alpha(a_\alpha|\alpha)$ are parametrised by a Gaussian[†] with mean $a = 0$ and variance $\sigma = 1$, with $\alpha = 0$ representing the nominal value. The *up* and *down* variations are then given by $\alpha = \pm 1$, thereby representing $\pm 1\sigma$ variations. The impact of any given value of the parameter on the event rates is subsequently evaluated through polynomial interpolation and exponential extrapolation[§], a method that avoids discontinuous first and second derivatives at $\alpha = 0$ and ensures positive values for the predicted event rates [163].

Sample rates derived directly from theory calculations (i.e. Monte Carlo (MC) simulation), are scaled to the integrated luminosity corresponding to the observed data. As discussed in section 2.1.2, the integrated luminosity is itself a measurement that is subject to uncertainties, requiring an additional constraint term in the likelihood. It is parametrised by a Gaussian with mean corresponding to the nominal integrated luminosity measurement and standard deviation equal to the integrated luminosity measurement uncertainty. Uncertainties arising from the finite size of the MC datasets used to derive estimated event rates are modelled by bin-wise scale factors γ_b . The constraint terms are Gaussian distributions with central value equal to unity and standard deviations calculated from the individual statistical uncertainties of the samples defined in the respective channel.

As the event rate in a given bin can depend on multiple parameters, and likewise, a single parameter can affect the expected event rate in multiple bins across different channels, correlations between the model parameters ϕ can occur.

[†] Other parameterisations are also possible and discussed in Ref. [163], but not used in the following.

[§] Different interpolation and extrapolation strategies are discussed in Ref. [163] but not mentioned herein as they will not be used in the following.

The above prescription for building binned likelihoods is called the HISTFACTORY template [163]. In this work, two independent implementations of the HISTFACTORY template are used. The first implementation, predominantly used in part II, relies on RooFIT [164] (using the Minuit [165] package) and RooStats [166] for model parameter estimation and hypothesis tests, and is fully integrated into the ROOT data analysis framework [167, 168]. The user interface and the steering of statistical fits, as well as the bookkeeping of their results, is provided by HISTFITTER [169]. The second implementation, used in part III, makes use of pyhf [170, 171], a recent pure-python implementation of HISTFACTORY that is independent of the ROOT environment. The pyhf implementation of HISTFACTORY relies on NUMPY [172] and uses computational graph libraries like PYTORCH [173], TENSORFLOW [174] and JAX [175] to significantly speed up the parameter estimation process by leveraging the computational advantages of tensor algebra and automatic differentiation.

Apart from separating the model parameter set into free and constrained parameters $\phi = (\eta, \chi)$, a separate partition $\phi = (\psi, \theta)$ is frequently used in the context of hypothesis testing. Here, ψ are so-called *parameters of interests* of the model for which hypothesis tests are performed, and θ are *nuisance parameters* that are not of immediate interest but need to be accounted for to correctly model the data. In the search presented in this work, the only Parameter of Interest (POI) is the *signal strength* parameter μ , representing the ratio of the signal process cross section to its reference cross section as expected from theory. The expected event rate v_i in each bin i can then be parametrised through

$$v_b = \mu S_b + B_b, \quad (3.5)$$

where S_b and B_b are the bin-wise expected signal and background rates, respectively. Fixing $\mu = 0$ thus yields an expected event rate containing only Standard Model of particle physics (SM) processes, which is why this is also called a *background-only* configuration. Setting $\mu = 1$ represents a *signal-plus-background* description at nominal signal cross section. Scanning multiple values of μ allows to set limits on the visible cross sections of the signal models considered in the search.

3.2 Parameter estimation

Given a likelihood $L(\phi)$ for a fixed set of observations \mathbf{x} , a measurement can be understood as a parameter estimation. In general, an estimator $\hat{\phi}$ is a function of the observed data used to estimate the true value of the model parameter ϕ .

In particle physics, the most commonly used estimator is the maximum likelihood estimator (MLE). The MLEs for the model parameters $\hat{\phi}$ are defined to be the parameter values that maximise $L(\phi)$, or equivalently, maximise $\ln L(\phi)$ and minimise $-\ln L(\phi)$. The logarithm of the likelihood is used for computational reasons, as it not only reduces the computational complexity by avoiding exponentials and products, but also avoids potential problems arising from finite floating point precision. As the logarithm is a monotonically increasing function, $\ln L(\phi)$ has maxima at the same parameter values as $L(\phi)$. The negative logarithm of the likelihood is chosen in order to stick to the convention of optimisers in statistical packages typically minimising the result of a *loss function*.

The MLEs $\hat{\phi}$ can, in general, be found by solving the system of equations

$$\frac{\partial \ln L}{\partial \phi_i} = 0, \quad (3.6)$$

where the index i runs over all parameters. Due to the complexity of the likelihood, a solution typically needs to be found numerically using minimisation algorithms. In the following, the parameter estimation is referred to as a *fit* of the model to data, and the maximum likelihood estimates of the parameters are consequently called *best-fit values*.

3.3 Statistical tests

In addition to estimating the values of model parameters, searches for Supersymmetry (SUSY) are naturally interested in claiming discovery (or exclusion) of hypothesised signal models. In the frequentist approach, this can be formulated in terms of hypothesis tests, evaluating a *null hypothesis* H_0 against an *alternative hypothesis* H_1 , with the goal of rejecting the null hypothesis. For discovering a new signal process, H_0 is defined to describe only known SM processes and thus called *background-only hypothesis*. The alternative hypothesis H_1 is then the *signal-plus-background hypothesis* describing both SM background processes as well as the signal process considered. When excluding a signal model, the signal-plus-background hypothesis takes over the role of H_0 and is tested against the background-only hypothesis.

The degree of agreement of observed data with a certain hypothesis H is quantified by calculating a p -value, representing the probability of finding data of greater or more extreme incompatibility under assumption of H . The hypothesis can then be considered to be excluded if its observed p -value is below a specified threshold. It is common to convert the p -value into a *significance* Z , defined in such a way that a Gaussian distributed observable with measured value Z standard deviations above its mean gives a one-sided upper tail probability equal to p . This yields the expression

$$Z = \Phi^{-1}(1 - p), \quad (3.7)$$

where Φ^{-1} is the quantile of the standard Gaussian. In HEP, claiming discovery of a signal conventionally requires a significance of at least $Z = 5$. If the significance is lower but still $Z > 3$, it is classified as a hint or evidence. For exclusion of a signal hypothesis at 95% confidence level, a p -value of 0.05, i.e. $Z = 1.64$, is required [161].

The p -values are calculated using a *test statistic* that parameterises the compatibility between the hypothesis and data in a single value. At the LHC experiments, the test statistics used for hypothesis testing are based on the *profile likelihood ratio* $\lambda(\mu)$, defined to be

$$\lambda(\mu) = \frac{L(\mu, \hat{\hat{\theta}}(\mu))}{L(\hat{\mu}, \hat{\theta})}, \quad (3.8)$$

where the conditional maximum likelihood estimators (CMLEs) $\hat{\hat{\theta}}$ are the values of θ that maximise the likelihood with μ fixed. The distribution of the profile likelihood ratio depends explicitly on μ , and implicitly on $\mathbf{x} = (\mathbf{n}, \mathbf{a})$, but is asymptotically (i.e. in the limit of a large number of events) independent of the nuisance parameters θ^\dagger in the case where the tested value of μ is the true value μ' [160]. The asymptotic independence from θ follows from Wilks' theorem [176] and is one of the main motivations for using the profile likelihood ratio, as it avoids the problem of having to compute p -values for all possible values of θ . A generalisation to tested values of μ not corresponding to the true value μ' can

[†] Eliminated by choosing specific values of the nuisance parameters for a given \mathbf{x} and μ , often referred to as *profiling*.

be derived using Wald's theorem [177], allowing to obtain the distribution $f(\lambda(\mu)|\mu', \theta)$. The profile likelihood ratio takes values between 0 and 1, with $\lambda(\mu) = 1$ corresponding to cases where the tested value of μ is in good agreement with the observed data. In eq. (3.8), the nuisance parameters result in a broadening of the profile likelihood distribution, reflecting the loss of information about μ due to systematic uncertainties [161].

As the rate of signal processes considered in the following is in general non-negative, an estimator for μ should satisfy $\hat{\mu} \geq 0$. In order to avoid the formal complications of having a boundary at $\mu = 0$, it is convenient to consider an effective estimator $\hat{\mu}$ that is allowed to become negative, provided that the respective Poisson terms for $\mu S_b + B_b$ remain positive. Imposing a constraint equivalent to requiring $\mu \geq 0$ on the test statistic itself, leads to the alternative definition of the profile likelihood as

$$\tilde{\lambda}(\mu) = \begin{cases} \frac{L(\mu, \hat{\theta}(\mu))}{L(\hat{\mu}, \hat{\theta})}, & \hat{\mu} \geq 0, \\ \frac{L(\mu, \hat{\theta}(\mu))}{L(0, \hat{\theta}(0))}, & \hat{\mu} < 0, \end{cases} \quad (3.9)$$

where $\hat{\theta}(0)$ and $\hat{\theta}(\mu)$ are the CMLEs of θ given a signal strength parameter of 0 and μ , respectively.

Discovery

For the important special case where $\mu = 0$ is tested in a model with $\mu \geq 0$, i.e. discovery of a non-negative signal (rejection of the background-only hypothesis), the profile likelihood $\tilde{\lambda}(\mu)$ is used to build the test statistic

$$q_0 = -2 \ln \tilde{\lambda}(0) = \begin{cases} -2 \ln \lambda(0), & \hat{\mu} \geq 0, \\ 0, & \hat{\mu} < 0. \end{cases} \quad (3.10)$$

This definition ensures that the background-only hypothesis is not rejected due to a downward fluctuation in data, causing $\hat{\mu} < 0$. In case more events are seen in data than expected based on the background-only hypothesis, eq. (3.10) produces increasingly large values of q_0 , corresponding to an increasing incompatibility between data and the background-only hypothesis. The p -value quantifying the disagreement between the $\mu = 0$ hypothesis and data can then be computed using

$$p_0 = \int_{q_{0,\text{obs}}}^{\infty} f(q_0|0) dq_0, \quad (3.11)$$

with $q_{0,\text{obs}}$ the observed value of the test statistic q_0 in data and $f(q_0|0)$ the pdf of q_0 under assumption of the background-only hypothesis. In the asymptotic limit [161] with a single POI, the test statistic q_0 can be written as

$$q_0 = \begin{cases} \hat{\mu}^2 / \sigma^2, & \hat{\mu} \geq 0, \\ 0, & \hat{\mu} < 0, \end{cases} \quad (3.12)$$

where $\hat{\mu}$ has a Gaussian distribution with mean μ' and variance σ^2 . In the case of $\mu' = 0$, the pdf of q_0 has the form of a half χ^2 distribution with one degree of freedom, and its cumulative distribution is $F(q_0|0) = \Phi(\sqrt{q_0})$ [160]. Using eq. (3.7), the p -value obtained with eq. (3.11) can be expressed with the significance Z_0 as

$$Z_0 = \sqrt{q_0}. \quad (3.13)$$

Exclusion and upper limits

If the background-only ($\mu = 0$) hypothesis cannot be rejected, the hypotheses can be switched around and instead the signal-plus-background ($\mu = 1$) hypothesis can be tested against a hypothesis where signal events are produced at a rate smaller than μ . For excluding the signal-plus-background hypothesis and setting upper limits on the signal strength μ , the test statistic is defined as

$$\tilde{q}_\mu = \begin{cases} -2 \ln \tilde{\lambda}(\mu), & \hat{\mu} \leq \mu \\ 0, & \hat{\mu} > \mu \end{cases} = \begin{cases} -2 \ln \frac{L(\mu, \hat{\theta}(\mu))}{L(\hat{\mu}, \hat{\theta})}, & \hat{\mu} < 0, \\ -2 \ln \frac{L(\mu, \hat{\theta}(\mu))}{L(0, \hat{\theta}(0))}, & 0 \leq \hat{\mu} \leq \mu, \\ 0 & \hat{\mu} > \mu. \end{cases} \quad (3.14)$$

Setting $\tilde{q}_\mu = 0$ in the case where $\hat{\mu} > \mu$ ensures that an overfluctuation of data is not considered as evidence against the signal hypothesis. This is opposed to the definition of q_0 , where an underfluctuation of data ($\hat{\mu} < \mu$) is not regarded to be evidence against the background-only hypothesis. It is worth highlighting that the discovery test statistic q_0 in eq. (3.11) is not just the special case of \tilde{q}_μ with $\mu = 0$, but hinges on a different definition.

The p -value, quantifying the level of agreement between data and the tested value of μ is then given by

$$p_\mu = \int_{\tilde{q}_{\mu, \text{obs}}}^{\infty} f(\tilde{q}_\mu | \mu) d\tilde{q}_\mu, \quad (3.15)$$

where, as before, $\tilde{q}_{\mu, \text{obs}}$ is the observed value of the test statistic in data and $f(\tilde{q}_\mu | \mu)$ is the pdf of \tilde{q}_μ given the hypothesis μ . In the asymptotic limit [161], the test statistic \tilde{q}_μ can be written as

$$\tilde{q}_\mu = \begin{cases} \mu^2 / \sigma^2 - 2\mu\hat{\mu} / \sigma^2, & \hat{\mu} < 0, \\ (\mu - \hat{\mu})^2 / \sigma^2, & 0 \leq \hat{\mu} \leq \mu, \\ 0 & \hat{\mu} > \mu, \end{cases} \quad (3.16)$$

which yields for the significance Z_μ the expression

$$Z_\mu = \begin{cases} \sqrt{\tilde{q}_\mu}, & 0 < \tilde{q}_\mu \leq \mu^2 / \sigma^2 \\ \frac{\tilde{q}_\mu + \mu^2 / \sigma^2}{2\mu / \sigma}, & \tilde{q}_\mu > \mu^2 / \sigma^2. \end{cases} \quad (3.17)$$

3.4 CL_s approach

In the CL_{s+b} method, a signal-plus-background model is excluded if $p_{s+b} < \alpha$, where α is defined by the desired confidence level, typically CL = 1 - α = 95%, and p_{s+b} can be calculated using the test statistic \tilde{q}_μ (with $\mu = 1$) introduced in eq. (3.14). If the experiment has very low sensitivity to a specific signal-plus-background model, e.g. because the production cross section of the signal process is too low, the distribution of the test statistic of the signal-plus-background model will be very close to that of the background-only model. In case of an underfluctuation in data, the $\mu = 1$ model can then be falsely excluded, even though no sensitivity is expected. Figure 3.1 illustrates this with a simple example. In fact, the exclusion of models to which the experiment has no sensitivity has a probability of at least α [178].

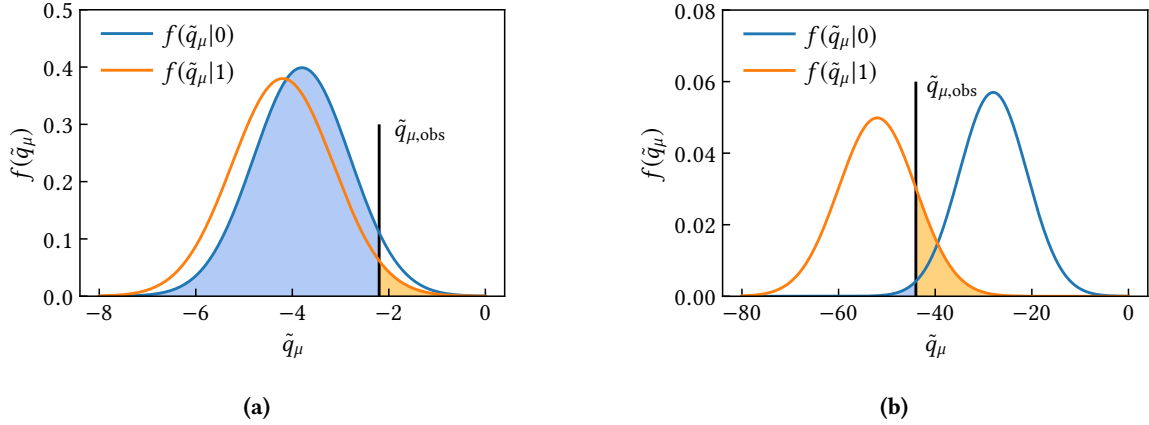


Figure 3.1: Distribution of the pdfs of the signal plus background (in orange) and background-only (in blue) models. The orange and blue coloured areas represent the p_{s+b} and p_b values, respectively. Figure (a) shows a case where both pdfs are close together, while figure (b) shows a case where they are well separated. Figures created by the author but based on Ref. [178].

This problem can be remedied by adopting the CL_s method [179], altering the threshold for excluding a model in a way to avoid exclusion of models to which the experiment has very low sensitivity. The CL_s value is defined as

$$\text{CL}_s = \frac{p_{s+b}}{1 - p_b}, \quad (3.18)$$

where p_b is the p -value of the background-only hypothesis[†]. If the distributions of the test statistics for the signal-plus-background and the background-only models are close to each other (as illustrated in fig. 3.1(a)) a small value of p_{s+b} due to an underfluctuation in data will entail a large value of p_b . Consequently, in the calculation of the CL_s value, p_{s+b} will be penalised by $1 - p_b$ (that will be close to 0), resulting in $\text{CL}_s > p_{s+b}$, preventing the exclusion of the signal-plus-background model. Conversely, in the case where the two test statistics are well-separated (see fig. 3.1(b)) and $p_{s+b} < \alpha$, then p_b will also be small and thus CL_s will be close to p_{s+b} obtained by the frequentist approach.

3.5 Asimov dataset

Searches for BSM physics are not only interested in the significance obtained using the dataset measured by the experiment, but also in the expected (or median) significance obtained for rejecting different values of μ . For example, for rejecting the $\mu = 1$ hypothesis, searches are interested in the expected significance obtained assuming data generated according to the $\mu = 0$ hypothesis.

The expected experimental sensitivity can be determined using an artificial dataset called the *Asimov dataset*, defined such that MLEs of all parameters determined using Asimov data correspond to the true parameter values. This is achieved by constructing a dataset where the number of events in each bin is exactly equal to the expected event rate in that bin. Using Asimov data, the Asimov likelihood L_A as well as the corresponding profile likelihood λ_A can be evaluated, and thus a median significance

[†] It is worth highlighting that p_b is equal to p_μ from eq. (3.15) with $\mu = 0$. This is strictly different from p_0 in eq. (3.11) as it relies on a different test statistic.

can be determined. Non-integer values for data counts are not an issue as factorial terms from the Poisson probabilities are canceled in the profile likelihood and can thus be dropped altogether.

3.6 Sensitivity estimation

When designing search regions for an analysis, it is necessary to achieve an optimal signal-to-background separation power. A significance metric is needed in order to quantify the separation power and to have a metric to optimise for. In the following, the expected discovery significance introduced in Ref. [180] is used. As the full statistical model is in general not yet known when designing the search regions, appropriate assumptions have to be made. In a *cut-and-count* selection where only the total number of events after a selection are relevant (and not e.g. their distribution), the significance is determined by the total number of signal events S , the total number of background events B and the uncertainty on the expected number of background events ΔB . This can be modelled as a so-called *on/off problem*[†] [180, 181], where the *cut-and-count* experiment uses two bins, a signal region (SR) enriched in signal events, and a control region (CR) containing only background events. In the background-only hypothesis, the parameter $\tau = n_{\text{CR}}/n_{\text{SR}}$ then denotes the ratio between the event rate in the CR, n_{CR} , and the event rate in the SR, n_{SR} .

If τ is known, then the likelihood of this simple configuration can be written in terms of the expected background event rate

$$L(\mu, B) = \text{Pois}(n_{\text{SR}}|\mu S + B) \cdot \text{Pois}(n_{\text{CR}}|\tau B), \quad (3.19)$$

where μ is again the signal strength parameter. The relative background uncertainty can thus be treated as coming from a Poisson-distributed auxiliary measurement containing only background (i.e. in the CR) with corresponding uncertainty $\sqrt{\tau B}$, leading to the approximation

$$\tau = \frac{B}{\Delta B^2}. \quad (3.20)$$

As n_{SR} and n_{CR} are each drawn from a Poisson probability with unknown means ν_{SR} and ν_{CR} , the background-only hypothesis corresponds exactly to the case where the ratio of Poisson means $\lambda = \nu_{\text{CR}}/\nu_{\text{SR}}$ is equal to τ [180]. The two Poisson terms can then be written as the product of a single Poisson term with mean $n_{\text{tot}} = n_{\text{SR}} + n_{\text{CR}}$ and the binomial probability $B(n_{\text{SR}}|\rho, n_{\text{tot}})$ of picking n_{SR} events out of n_{tot} with probability $\rho = \nu_{\text{SR}}/\nu_{\text{tot}} = 1/(1 + \lambda)$. The likelihood can thus be written as

$$\begin{aligned} L(\mu, B) &= \text{Pois}(n_{\text{tot}}|\lambda_{\text{tot}}) \cdot B(n_{\text{SR}}|\rho, n_{\text{tot}}) \\ &= \frac{e^{-\lambda_{\text{tot}}} \lambda_{\text{tot}}^{n_{\text{tot}}}}{n_{\text{tot}}!} \cdot \binom{n_{\text{tot}}}{n_{\text{SR}}} \rho^{n_{\text{SR}}} (1 - \rho)^{n_{\text{tot}} - n_{\text{SR}}}. \end{aligned} \quad (3.21)$$

Since the background-only hypothesis cannot only be expressed as $\mu = 0$ but also as $\nu_{\text{SR}} = \nu_B$, $\lambda = \tau$, and especially also as $\rho = 1/(1 + \tau)$ [180], its p -value can be calculated using the well-known frequentist

[†] The *on/off* nomenclature originates from gamma ray astronomy where *on* refers to the telescope pointing on-source (measuring signal and background photons), while *off* refers to it pointing off-source (measuring only background photons). This problem is an exact analog to the HEP problem herein, where the off-source measurement typically corresponds to some *sideband* measurement, i.e. a measurement of events in a region of a parameter disjoint from the parameter range where the signal might exist.

binomial test,

$$p_B = \sum_{j=n_{\text{SR}}}^{n_{\text{tot}}} B(j|n_{\text{tot}}, \rho). \quad (3.22)$$

The significance corresponding to p_B can be derived using eq. (3.7) and is computable in a numerically fast way using the incomplete beta function. The algorithm used for calculating Z_B in this work is implemented in the `RooStats::NumberCountingUtils` methods in ROOT [167, 168].

Part II

The 1-lepton analysis

Part III

Reinterpretation

Part IV

Summary and Outlook

Part V

Appendices

Abbreviations

BSM beyond the Standard Model. [55](#), [61](#)

CMLE conditional maximum likelihood estimator. [58](#), [59](#)

CR control region. [62](#)

HEP high energy physics. [55](#), [58](#), [62](#)

MC Monte Carlo. [56](#)

MLE maximum likelihood estimator. [57](#), [61](#)

pdf probability density function. [55](#), [59–61](#)

POI Parameter of Interest. [57](#), [59](#)

SM Standard Model of particle physics. [57](#), [58](#)

SR signal region. [62](#)

SUSY Supersymmetry. [58](#)

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