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WIP: Work in Progress Title

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LUDWIG-MAXIMILIANS-UNIVERSITY MUNICH  
FACULTY OF PHYSICS

DISSERTATION

Eric Schanet

December 2020



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FAKULTÄT FÜR PHYSIK

DISSERTATION

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Supervisor: Prof. Dr. Dorothee Schaile

## **Abstract**

My abstract



## **Zusammenfassung**

Meine Zusammenfassung





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# Introduction

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Here is my introduction

Natural  
units and  
Minkowski  
metric



# Chapter 1

1

## Theory

2

This chapter starts with an outline of the basic principles and concepts of the Standard Model of Particle Physics (SM), the theoretical framework describing nature on the level of elementary particles. This is followed by an introduction to supersymmetry, a promising class of theories aiming to solve some of the shortcomings of the SM.

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By no means intended to be a full description, this chapter merely tries to highlight the important relations and consequences of the SM and supersymmetry. The mathematical description of this chapter largely follows [1] for the SM and [2] for supersymmetry.

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### 1.1 The Standard Model of Particle Physics

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By the end of the 1920s, quantum mechanics and general relativity had been relatively well established and the consensus among physicists was that matter was made of nuclear atoms consisting of electrons and protons. During the 1930s, a multitude of new experimental discoveries and theoretical puzzles excited physicists in three main fields of research: nuclear physics, cosmic rays and relativistic quantum mechanics. The following years and decades saw particle physics emerge as a result of these currents ultimately flowing together.

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Since these early times of particle physics research, physicists have made extraordinary progress in describing nature at the subatomic scale. Today, a century later, the resulting theoretical framework, the Standard Model of Particle Physics, is the most fundamental theory of nature to date. It provides an extremely precise description of the interactions of elementary particles and—using the Large Electron Positron collider (LEP)—has been tested and verified to an unprecedented level of accuracy up to the electroweak (EWK) scale. Given the unprecedented success of SM, it is not surprising that its history is paved with numerous awards for both experimental and theoretical work. In 1964, the Nobel prize was awarded to Feynman, Schwinger and Tomonaga for their fundamental work in quantum electrodynamics (QED). This quantum field theory allows to precisely

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**Table 1.1:** Names, electric charges and masses (rounded to three significant digits if known to that precision) of all observed fermions in the SM [4].

	generation	particle	electric charge [ $e$ ]	mass
leptons	1	electron ( $e$ )	$-1$	511 keV
		electron neutrino ( $\nu_e$ )	$0$	$< 2$ eV
	2	muon ( $\mu$ )	$-1$	106 MeV
		muon neutrino ( $\nu_\mu$ )	$0$	$< 0.19$ MeV
	3	tau ( $\tau$ )	$-1$	1.78 GeV
		tau neutrino ( $\nu_\tau$ )	$0$	$< 18.2$ MeV
quarks	1	up ( $u$ )	$\frac{2}{3}$	2.3 MeV
		down ( $d$ )	$-\frac{1}{3}$	4.8 MeV
	2	charm ( $c$ )	$\frac{2}{3}$	1.28 GeV
		strange ( $s$ )	$-\frac{1}{3}$	95 MeV
	3	top ( $t$ )	$\frac{2}{3}$	173 GeV
		bottom ( $b$ )	$-\frac{1}{3}$	4.18 GeV

calculate fundamental processes as e.g. the anomalous magnetic moment of the electron to a relative experimental uncertainty of  $2.3 \times 10^{-10}$  [3]. In 1979, Glashow, Weinberg and Salam were awarded with the Nobel prize for their work towards electroweak unification. The most prominent recent progress is undoubtedly the discovery of the Higgs boson, not only resulting in the Nobel prize being awarded to Englert and Higgs, but also completing the SM, roughly 50 years after the existence of the Higgs boson had been theorised.

Couplings and masses are measured from experiment

### 1.1.1 Particle content of the SM

The SM successfully describes ordinary matter as well as their interactions, namely the electromagnetic, weak and strong interactions. Gravity is the only fundamental force not described within the SM. The particles in the SM are classified into two main categories, depending on their spin. Particles with half-integer spin follow Fermi-Dirac statistics and are called fermions. As they are subject to the Pauli exclusion principle, they make up ordinary matter. Particles with integer spin follow Bose-Einstein statistics and mediate the fundamental interactions between fermions.

Neutrino masses not in SM!

Fermions are further divided into leptons and quarks, which each come in three generations with increasing masses<sup>†</sup>. The three electrically charged leptons are each associated with a corresponding neutral neutrino (more on this *association* in chapter). While the SM assumes massless neutrinos, the observation of neutrino oscillations [5] implies the existence of at least two massive neutrinos. By extending the SM to allow non-vanishing neutrino masses, neutrino oscillations can be introduced through lepton generation mixing, described by the Pontecorvo-Maki-Nakagawa-Sakata (PMNS) matrix [6]. Apart from an

Need ref

<sup>†</sup> Neutrinos might not exist in a normal mass hierarchy but could also have an inverted mass hierarchy.



**Table 1.2:** Names, electric charges and masses (rounded to three significant digits if known to that precision) of all observed bosons in the SM [4].

particle	spin	electric charge [ $e$ ]	mass
photon ( $\gamma$ )	1	0	0
gluon ( $g$ )	1	0	0
$W^\pm$	1	$\pm 1$	80.4 GeV
$Z^0$	1	0	91.2 GeV
Higgs boson ( $H$ )	0	0	125 GeV

electric charge, the six quarks also carry a colour charge. There are three types of colour charge: *red*, *green* and *blue* as well as their respective anti-colours. The mixing in the quark sector through the weak interaction can be described by the Cabibbo-Kobayashi-Maskawa (CKM) matrix [7]. Finally, each fermion comes with its own anti-particle with same mass and spin, but inverted charge-like quantum numbers<sup>†</sup>. All fermions in the SM are listed in table 1.1.

The fundamental forces described by the SM are propagated by bosons with spin  $1\hbar$ . The photon  $\gamma$  couples to electrically charged particles and mediates the electromagnetic interaction. As the photon is massless, the electromagnetic force has infinite range. The strong force is mediated by gluons carrying one unit of colour and one unit of anti-colour. Due to colour-confinement, colour charged particles like quarks and gluons cannot exist as free particles and instead will always form colour-neutral bound states. Although nine gluon states would theoretically be possible, only eight of them are realised in nature: the colour-singlet state  $\frac{1}{\sqrt{3}}(|r\bar{r}\rangle + |g\bar{g}\rangle + |b\bar{b}\rangle)$  would be colour-neutral result in long-range strong interactions, which have not been observed. Finally, the weak force is mediated by a total of three bosons, two charged  $W$ -bosons  $W^+$  and  $W^-$ , and a neutral  $Z$ -boson. The mediators of the weak force are massive, resulting in a finitely ranged interaction. The  $W^\pm$  and  $Z$  bosons gain their masses through the Higgs mechanism (discussed in chapter ), resulting in a massive spin-0 boson, called the Higgs boson. All bosons known to the SM are listed in table 1.2.

### 1.1.2 The SM as a gauge theory

Formally, the SM is a collection of a special type of quantum field theories, called gauge theories. Quantum field theory (QFT) is the application of quantum mechanics to dynamical systems of fields, just as quantum mechanics is the quantisation of dynamical systems of particles. QFT provides a uniform description of quantum mechanical particles and classical fields, while including special relativity.

<sup>†</sup> The exact nature of anti-neutrinos is still an open question and ties into whether or not the neutrino mass matrix contains non-vanishing Majorana mass terms.

need ref

Might want to explain this later once I introduced the gauge groups?

In classical mechanics, the fundamental quantity is the action  $S$ , which is the time integral of the Lagrangian  $L$ , a functional characterising the state of a system of particles in terms of generalised coordinates  $q_1, \dots, q_n$ . In field theory, the Lagrangian can be written as spatial integral of a Lagrangian density  $\mathcal{L}(\phi_i, \partial_\mu \phi_i)$ , that is a function of one or more fields  $\phi_i$  and their spacetime derivatives  $\partial_\mu \phi_i$ . For the action, this yields

$$S = \int L dt = \int \mathcal{L}(\phi_i, \partial_\mu \phi_i) d^4x. \quad (1.1)$$

In the following, the Lagrangian density  $\mathcal{L}$  will simply be referred to as the *Lagrangian*. Using the principle of least action  $\delta S = 0$ , the equation of motions for each field are given by the Euler-Lagrange-equation,

$$\partial_\mu \left( \frac{\partial \mathcal{L}}{\partial (\partial_\mu \phi_i)} \right) - \frac{\partial \mathcal{L}}{\partial \phi_i} = 0. \quad (1.2)$$

As opposed to the Hamiltonian formalism, the Lagrange formulation of field theory is especially well suited in this context, as it exhibits explicit Lorentz-invariance. This is a direct consequence of the principle of least action, since boosted extrema in the action will still be extrema for Lorentz-invariant Lagrangians.

Symmetries are of central importance in the SM. As Emmy Noether has famously shown in 1918 [8] for classical mechanics, every continuous symmetry of the action has a corresponding conservation law. In the context of classical field theory, each generator of a continuous internal or spacetime symmetry transformation leads to a conserved current, and thus to a conserved charge. In QFTs, quantum versions of Noether's theorem, called Ward–Takahashi identities [9, 10] for Abelian theories and Slavnov–Taylor identities [11–13] for non-Abelian theories relate the conservation of quantum currents and charge-like quantum numbers to continuous global symmetries of the Lagrangian.

From a theoretical point of view, the SM can be described by a non-Abelian Yang-Mills type gauge theory based on the symmetry group

$$SU(3)_C \otimes SU(2)_L \otimes U(1)_Y,$$

where  $U(n)$  ( $SU(n)$ ) describes (special) unitary groups, i.e. the Lie groups of  $n \times n$  unitary matrices (with determinant 1, if special).  $SU(3)_C$  generates quantum chromodynamics (QCD), i.e. the interaction of particles with colour charge through exchange of gluons, and  $SU(2)_L \otimes U(1)_Y$  generates the electroweak interaction. Here, the subscript  $Y$  represents the weak hypercharge, while the  $L$  indicates that  $SU(2)_L$  only couples to left-handed particles (right-handed antiparticles).

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Explicitly  
derive  
the Euler-  
Lagrange  
equa-  
tions? Cf.  
Peskins  
Ch.2.2.

Check  
correct-  
ness of  
formula-  
tion

**Gauge principle**

The gauge principle is fundamental to the SM and dictates that the existence of gauge fields is directly related to symmetries under local gauge transformations. QED, being the simplest gauge theory, can be taken to illustrate this important principle. The free Dirac Lagrangian for a single, non-interacting fermion with mass  $m$  is given by

$$\mathcal{L}_{\text{Dirac}} = \bar{\psi} (i\gamma^\mu \partial_\mu - m) \psi, \quad (1.3)$$

where  $\psi$  is a four-component complex spinor field,  $\bar{\psi} = \psi^\dagger \gamma^0$ , and  $\gamma^\mu$  with  $\mu = 0, 1, 2, 3$  are the Dirac matrices with the usual anticommutation relations generating a matrix representation of the Dirac algebra

$$\{\gamma^\mu, \gamma^\nu\} \equiv \gamma^\mu \gamma^\nu + \gamma^\nu \gamma^\mu = 2\eta^{\mu\nu} \mathbb{1}_4. \quad (1.4)$$

It is worth noting that the free Dirac Lagrangian is invariant under a global  $U(1)$  transformation

$$\psi \rightarrow e^{i\theta} \psi, \quad (1.5)$$

where the phase  $\theta$  is spacetime independent and real. In order to produce the physics of electromagnetism, the free Dirac Lagrangian however has to be invariant under *local*  $U(1)$  phase transformations of the form

$$\psi \rightarrow e^{i\theta(x)} \psi, \quad (1.6)$$

where the phase  $\theta(x)$  is a function of spacetime. It is however obvious, this is not the case as the transformed Lagrangian picks up an additional term from the spacetime derivative of the phase  $\partial_\mu \theta(x)$ , leading to

$$\mathcal{L} \rightarrow \mathcal{L} - (\partial_\mu \theta) \bar{\psi} \gamma^\mu \psi. \quad (1.7)$$

By introducing a new vector field  $A_\mu(x)$  that transforms under local phase transformations according to

$$A_\mu \rightarrow A_\mu - \frac{1}{e} \partial_\mu \theta(x), \quad (1.8)$$

and furthermore replacing the partial derivative  $\partial_\mu$  by the covariant derivative<sup>†</sup>

$$\partial_\mu \rightarrow D_\mu \equiv \partial_\mu + ieA_\mu, \quad (1.9)$$

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<sup>†</sup> The prescription of achieving local gauge invariance by replacing  $\partial_\mu$  with  $D_\mu$  is called *minimal coupling*.

yields for the Lagrangian in eq. (1.3) a modified version including a term for interactions between the gauge field and the fermion field

$$\begin{aligned}\mathcal{L} &= \mathcal{L}_{\text{Dirac}} + \mathcal{L}_{\text{int}} \\ &= \bar{\psi} (i\gamma^\mu \partial_\mu - m) \psi - (e\bar{\psi}\gamma^\mu \psi) A_\mu.\end{aligned}\tag{1.10}$$

It can be easily verified, that this modified Lagrangian is indeed invariant under a local phase transformation. Yet, it still cannot be complete as it is missing a free kinetic term for the gauge field  $A_\mu$  itself. For a vector field, the free term is described by the Proca Lagrangian

$$\mathcal{L}_{\text{Proca}} = -\frac{1}{4}F_{\mu\nu}F^{\mu\nu} + \frac{1}{2}m_A^2 A^\nu A_\nu,\tag{1.11}$$

where  $F^{\mu\nu} \equiv (\partial^\mu A^\nu - \partial^\nu A^\mu)$  is the field strength tensor that is invariant under the transformation in eq. (1.8). Since  $A^\nu A_\nu$  is not invariant under the same transformation, the only way to keep the full Lagrangian invariant under a local phase transformation is by requiring  $m_A = 0$ , i.e. the introduced gauge field  $A_\mu$  has to be massless, giving the Maxwell Lagrangian (ultimately generating the Maxwell equations)

$$\mathcal{L}_{\text{Maxwell}} = -\frac{1}{4}F_{\mu\nu}F^{\mu\nu}.\tag{1.12}$$

This finally yields the full Lagrangian

$$\begin{aligned}\mathcal{L}_{\text{QED}} &= \mathcal{L}_{\text{Dirac}} + \mathcal{L}_{\text{Maxwell}} + \mathcal{L}_{\text{int}} \\ &= \bar{\psi} (i\gamma^\mu \partial_\mu) \psi - m\bar{\psi}\psi - \frac{1}{4}F^{\mu\nu}F_{\mu\nu} - (e\bar{\psi}\gamma^\mu \psi) A_\mu \\ &= \bar{\psi} (i\gamma^\mu D_\mu - m) \psi - \frac{1}{4}F^{\mu\nu}F_{\mu\nu},\end{aligned}\tag{1.13}$$

which can be identified to be the full Lagrangian of QED. The introduced gauge field  $A_\mu$  is therefore nothing else but the electromagnetic potential with its associated massless particle, the photon. Thus, by applying the gauge principle on the free Dirac Lagrangian, i.e. forcing the Lagrangian to be invariant under local phase transformations, a new massless gauge field including interaction terms with the existing fields in the Lagrangian has to be introduced. In the case of the free Dirac Lagrangian, the requirement of phase invariance to hold locally, produces all of quantum electrodynamics.

As the phase transformation in eq. (1.6) is part of the unitary group  $U(1)$ , this symmetry is called  $U(1)$  *gauge symmetry*.

**Quantum chromodynamics**

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**1.1.3 Renormalisation and divergencies**

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**1.2 Supersymmetry**

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## **Chapter 2**

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## **The LHC and ATLAS**

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# Chapter 3

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## Data and Monte Carlo Simulation

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### 3.1 Data

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## Chapter 4

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## Statistical data analysis

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# Chapter 5

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## Analysis

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# Chapter 6

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## Summary

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Here be dragons/

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# Symbols

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## Acronyms / Abbreviations

2

CKM Cabibbo-Kobayashi-Maskawa, page 7

3

LEP Large Electron Positron Collider, page 5

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PMNS Pontecorvo–Maki–Nakagawa–Sakata, page 6

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QCD Quantum Chromodynamics, page 7

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QED Quantum Electrodynamics, page 5

7

QFT Quantum Field Theory, page 7

8

SM Standard Model of Particle Physics, page 5

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# Appendix A

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## A.1 N-1 plots for cut-scan results

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# Appendix B

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## B.1 Scatter plots comparing truth and reco yields in the SRs

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1

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## Selbstständigkeitserklärung

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Hiermit erkläre ich, die vorliegende Arbeit mit dem Titel

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**WIP: Work in Progress Title**

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WIP: Work in Progress Title

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selbständig verfasst zu haben und keine anderen als die in der Arbeit angegebenen  
Quellen und Hilfsmittel benutzt zu haben.

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Eric Schanet

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München, den 01. Mai 2021

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