

# Supplementary Materials for

# Scalable thermochromic smart windows with passive radiative cooling regulation

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#### The PDF file includes:

Materials and Methods Figs. S1 to S27 Tables S1 to S6 References

#### **Materials and Methods**

# Fabrication of VO<sub>2</sub>-PMMA multilayer structure

VO<sub>2</sub> NPs (Pure and 2 wt.% W-doped, Hangzhou Jikang New Material CO.,LTD), PMMA (Mw: ~120,000, Sigma-Aldrich), acetone (95%, Aik Moh), double side ITO coated glass (Winteck Technology) were used in this work without further purification. The ITO glass was cleaned by ethanol and dried before spin coating.

The PMMA was dissolved into acetone to spin coat the PMMA layer in multilayer structure. 0.5 g and 1 g PMMA were dissolved into 10 ml acetone respectively to form the PMMA solution with different concentration. In order to prepare PMMA thin film with different thickness, the PMMA solutions were coated on the ITO coated glass with different spinning speeds of up to 3000 rpm with the use of a spin coater (POLOS 150i, Specialty Coating Systems Inc.). For the deposition of VO<sub>2</sub> layer, VO<sub>2</sub> NPs and PMMA particles with different weight ratio (Table S6) was dispersed in 5 ml acetone to prepare the VO<sub>2</sub>-PMMA suspension. The suspension was firstly stirred at 500 rpm for 30 min to dissolve the PMMA. Subsequently, the suspension was sonicated in the ultrasonic bath for 1 hour to form the VO<sub>2</sub> NPs-PMMA mixture for spin coating. The VO<sub>2</sub> thin film was spin coated with the same spin coater used to prepared PMMA thin film. The spinning speed were set as 3000 rpm. The sample for the large-scale fabrication demonstration had the size of 5\*5 cm while the sample for optical properties measurement had the size of 2.5\*2.5 cm.

# Characterization of material

The morphology of VO<sub>2</sub> NPs was investigated scanning electron microscope (SEM, Carl Zeiss Supra 55). The crystal structure of VO<sub>2</sub> NPs was determined through x-ray diffraction (XRD, PANalytical Empyrean). Moreover, the bonding information of PMMA and VO<sub>2</sub> NPs were investigated thought FTIR (Perkin Elmer Frontier). The thickness of films was measured by a surface profiler (NanoMap, AEP Technology).

Optical and thermal properties characterization of VO<sub>2</sub>-PMMA multilayer structure The UV-Vis-NIR spectra for the samples were measured with the UV-Vis-NIR spectrometer (Avantes AvaSpec-ULS2048L StarLine Versatile Fiber-optic Spectrometer and AvaSpec-NIR256-2.5-HSC-EVO). To control the sample temperature, a heating/cooling stage (Linkam PE120) was installed. Spot size for UV-Vis spectrometer was 0.5\*0.5 cm. The  $T_{\text{lum}}$  and  $T_{\text{sol}}$  were calculated with the formula:

T<sub>lum/sol</sub> = 
$$\int \varphi_{lum/sol} T(\lambda) d\lambda / \int \varphi_{lum/sol} d\lambda$$

The  $T(\lambda)$  is the spectral transmittance (360 nm-780 nm for  $T_{\text{lum}}$  and 360 nm-2500 nm for  $T_{\text{sol}}$ ).  $\psi_{\text{lum}}(\lambda)$  is the standard luminous efficiency function of photopic vision for the wavelength of 380–780 nm.(34)  $\psi_{\text{sol}}(\lambda)$  is the solar irradiance spectra for air mass 1.5 (corresponding to the sun standing 37 ° above the horizon with 1.5 atmosphere thickness, corresponds to a solar zenith angle of 48.2°).(35) The  $\Delta T_{\text{sol}}$  was calculated with the formula:

$$\Delta T_{sol} = T_{sol,20^{\circ}\text{C}} - T_{sol,90^{\circ}\text{C}}$$

The hysteresis loop of  $VO_2$  was measured with the UV-Vis-NIR spectrometer with the heating/cooling stage installed. The transmittance of 1750 nm was recorded for plotting. The sample was firstly heated from 20 °C to 100 °C, and 100 °C back to 20 °C for a cooling process. The data interval for the hysteresis loop measurement was 5 °C. For each data point, the

transmittance of the sample was recorded after the temperature of the sample was stabilized. The  $\tau_c$  was determined by calculating the derivation of transmittance against temperature. The integrated  $\varepsilon_{LWIR}$  of the samples were measured by a dual-band emissivity measuring instrument (IR-2, Shanghai Chengbo Photoelectric Technology) with heating stage equipped.  $\varepsilon_{LWIR}$  value of 5 spots were recorded for every sample and the average value was used as the final  $\varepsilon_{LWIR}$ . The  $\Delta\varepsilon_{LWIR}$  were calculated with the formula:

$$\Delta \varepsilon_{LWIR} = \varepsilon_{LWIR-H} - \varepsilon_{LWIR-L}$$

Where the  $\varepsilon_{LWIR-H}$  was the integrated LWIR emissivity of sample that measured at high temperature while the  $\varepsilon_{LWIR-L}$  was the integrated LWIR emissivity of sample that measured at low temperature.

Meanwhile,  $\varepsilon_{LWIR}$  spectral curve was plotted according to the Kirchhoff's law of thermal radiation:  $\varepsilon(\lambda) = A(\lambda) = 1 - T(\lambda) - R(\lambda)$ . (36, 37) Where  $R(\lambda)$  is the spectral LWIR reflectance and  $T(\lambda)$  is the spectral LWIR transmittance that measured by FTIR spectrometer (Perkin Elmer Frontier) with an integration sphere attached. Spot size for FTIR spectrometer was 2\*2 cm. The sample temperature was controlled by a self-designed heating plate. The IR images of the multilayer structure and VO<sub>2</sub> on glass were taken by an IR camera (FLIR E4) with a copper background ( $\varepsilon_{LWIR}$ =0.5). The sample temperature was controlled by the same heating/cooling stage used in UV-Vis spectroscopy, while the color in IR image only represent the  $\varepsilon_{LWIR}$  difference between sample and background.

The relationship of  $\Delta \varepsilon_{LWIR}$  and spacer thickness was simulated based on FDTD method. The structure of the simulated multilayer structure consists of an intrinsic VO<sub>2</sub> thin layer with the thickness of 25 nm, PMMA spacer with the thickness from 1  $\mu$ m to 5  $\mu$ m, and double-sided ITO glass with the ITO thickness of 100 nm. The surface roughness and defects of the structure were ignored in the simulation. The optical constants of VO<sub>2</sub>, PMMA, ITO, and SiO<sub>2</sub> were obtained from reference (38-42), respectively.

#### Energy saving performance simulation

When investigating the sensitivity of the  $T_{\text{sol}}$  and  $\varepsilon_{\text{LWIR}}$  impacts on the building cooling and heating energy consumption, a single-story small office building has been proposed (Fig. S11). The heating and cooling energies are modeled from whole building energy simulation using EnergyPlus by applying "ideal-loads-air-systems" served with district cooling and heating sources, the results of which closely represent direct effects of the various  $T_{\rm sol}$  and  $\varepsilon_{\rm LWIR}$ characteristics to space cooling and heating loads. In particular, the building has a dimension of  $20m (L) \times 10m (W) \times 4m (H)$  and the building façade and HVAC specifications of the model are displayed in Table S2A, while the insulation meets the requirements of ASHRAE standard 90.1 (43). In the model, the glazing system has a gross window glass area of 72 m<sup>2</sup>, with a window to wall ratio of 30%, which is evenly distributed to four walls. Typical locations under seven climate zones for worldwide have been chosen for simulation (43): Honolulu, HI, U.S. (Zone 1), Cairo, Egypt (Zone 2), Shanghai, China (Zone 3), Albuquerque, NM, U.S. (Zone 4), Mannheim, Germany (Zone 5), Stockholm, Sweden (Zone 6), and Whitehorse, YT, Canada (Zone 7). In this mapping with single glaze window,  $T_{\text{sol}}$  and  $\varepsilon_{\text{LWIR-Front}}$  of the glass were tuned while  $\varepsilon_{\text{LWIR-Back}}$ was fixed at 0.1. The heating and cooling energy savings were evaluated by applying the site-tosource energy conversion factors of 1.28 and 1.05 for district heating and cooling, respectively.(44)

The building energy savings of the specimens are estimated from whole building energy simulation using a typical 12-story large office building with a floor dimension of 73m (240ft.,

L)  $\times$  49m (160ft., W)  $\times$  4m (13ft., H) as the prototype building that was developed by Pacific Northwest National Laboratory (PNNL) of the U.S. Department of Energy (DOE) (Fig. S19).(45) Derived from "DOE's Commercial Reference Building Models", this actual size prototype building model represented the commercial buildings in the U.S. and was accepted by building energy area as benchmark models. (46) This model follows applicable building codes and standards for energy efficiency requirements(43), adopted typical operation and occupancy schedule, and defined typical lighting/miscellaneous loads and HVAC systems. The building façade and HVAC specifications of the prototype are displayed in Table S2B. The building glazing system has a total window glass area of 4,636 m<sup>2</sup> (window to wall ratio: 40%). The EnergyPlus built-in thermochromic function was applied to model the thermochromic feature of the glass specimens in the simulation. The building energy saving performances are obtained by measuring the differences in values between various types of the specimens including commercial low-E glass, thermochromic glass without RC regulation, and clear glass specimen (baseline). The detailed optical properties of the glass specimens measured at 10 °C interval is updated in the prototype building model and summarized in Fig. S21. The glass surface temperature for the prototype building was modeled using EnergyPlus in which the glazing optical and thermal calculations are based on procedures from the WINDOW program developed by the U.S. Lawrence Berkeley Lab (LBL). (47) The typical locations under climate zones around the world were chosen for simulation (43): Honolulu, HI, U.S. (Zone 1), Cairo, Egypt (Zone 2), Shanghai, China (Zone 3), Albuquerque, NM, U.S. (Zone 4), Mannheim, Germany (Zone 5), Stockholm, Sweden (Zone 6), and Whitehorse, YT, Canada (Zone 7). The US prototype building model has been applied when the simulation is conducted at the selected cities under the corresponding climate zone. The site-to-source conversion factor varies with the countries and regions that have diverse energy sources and technologies. (48, 49) Thereby comprehensively considering these factors for electricity and natural gas in 17 countries to represent the energy utilizing situations worldwide, (44, 49-56) this work adopted 2.40 and 1.04 for electricity and natural gas, respectively. The results are shown in Fig. S23. Besides, additional cities around the world across different zones were adopted for predicting the heating and cooling energy savings (Fig. 3D): Abu Dhabi, U.A.E.; Bangkok, Thailand; Singapore, Singapore; Karachi, Pakistan; Rio de Janeiro, Brazil; New Delhi, India; Hong Kong, China; Lima, Peru; Adelaide, Australia; Atlanta, GA, U.S.; Auckland, New Zealand; Nairobi, Kenya; Cape Town, South Africa; Beijing, China; Lyon, France; Denver, CO, U.S.; Salt Lake City, UT, U.S.; Ottawa, ON, Canada; Calgary, AB, Canada; Ekaterinburg, Russia; Helsinki, Finland; International Falls, MN, U.S.; Tampere, Finland; Resolute, NU, Canada. The building energy savings per unit area is based on window glass area.

#### **Supplementary Text**

#### Characterizations of VO<sub>2</sub> NPs, PMMA, and ITO

Fig. S1 shows the UV-Vis-NIR spectrum (Fig. S1A) and FTIR spectrum (Fig. S1B) of PMMA thin film. The standard error of  $T_{\text{lum}}$  and  $T_{\text{sol}}$  value for all samples is less than 10%. The PMMA thin film has a  $T_{\text{lum}}$  of 89.4%, and a  $T_{\text{sol}}$  of 84.3%. The visible transmittance of ITO coated glass is shown in Fig. S2. ITO coated glass has a  $T_{\text{lum}}$  of 81.8%. Meanwhile, ITO coated glass has an  $\varepsilon_{\text{LWIR}}$  of 0.1 (Fig. S3).

The SEM image of VO<sub>2</sub> NPs is shown in Fig. S4, while its XRD pattern in Fig. S5 indicates the character XRD peak of VO<sub>2</sub> from the lattice planes (011), (-211), (-212), (-222), and (-213). Fig.

S6 is the FTIR transmittance spectrum for VO<sub>2</sub> NPs, the absorption peak at 422, 530, and 715 cm<sup>-1</sup> are due to the V–O–V octahedral bending modes and coupled vibration of V=O bond that belongs to VO<sub>2</sub> NPs.

Fig. S7 is the NIR spectrum of ITO coated glass. It can be observed that ITO coated glass has a low transmittance for light with wavelength longer than 1500 nm.  $T_{NIR}$  of ITO coated glass is 58.4%.

Fig. S8 is the derivate of transmittance for pure VO<sub>2</sub>. The largest derivation during heating appeared at 65 °C while the largest derivation during cooling appeared at 55 °C. As the result, the pure VO<sub>2</sub> NPs'  $\tau_c$  was determined as 62.5 °C by averaging the two values.

#### **ELWIR** switching performance regulation

Fig. S9 shows the relationship between PMMA thickness, VO<sub>2</sub> weight ratio and  $\varepsilon_{LWIR}$ . It can be observed that with fixed VO<sub>2</sub> weight ratio,  $\varepsilon_{LWIR-L}$  increases with the increasing of spacer thickness. On the other hand, the change of  $\varepsilon_{LWIR-H}$  differs from  $\varepsilon_{LWIR-L}$ . The change of  $\varepsilon_{LWIR-H}$  is affected by both VO<sub>2</sub> weight ratio and PMMA spacer thickness.

Meanwhile, Fig. S10 shows the comparison between experiment data and simulation data of  $\Delta \epsilon_{8-13\mu m}$  and PMMA spacer thickness with fixed VO<sub>2</sub> weight ratio of 20:1. The difference of experiment and simulation might be due to several reasons. In simulation, the defects of film were ignored to simplify the simulation. Meanwhile, in experiment VO<sub>2</sub>-PMMA composite layer was used while in simulation, pure VO<sub>2</sub> layer was used. The same trending indicates that there is an optimized spacer thickness for the best emissivity switching performance.

# Mapping of energy consumption vs $T_{\text{sol}}$ and $\varepsilon_{\text{LWIR}}$

The mapping of heating and cooling energy consumption vs  $T_{sol}$  (10-90%) and  $\varepsilon_{LWIR}$  (0.1-0.9) across seven climate zones are shown in Fig. 3B and Fig. S12-S17. In this simulation, a single-story small office building was used as prototype (Fig. S11). It is worth noting that in Zone 1, the heating energy consumption is negligible. Therefore, Fig. S12 only shows the cooling energy mapping.

Fig. S18 shows the energy consumption of optimized static  $\varepsilon$  window and optimized dynamic  $\varepsilon$  window. The energy consumption of static optimized  $\varepsilon$  window is derived from the point of minimum total energy consumption in 7 climate zones by fixing  $\varepsilon$ . The optimized dynamic  $\varepsilon$  window has a  $\varepsilon_{LWIR}$  of 0.9 for cooling, 0.1 for heating. Their  $T_{sol}$  were all fixed at 30% for studying  $\varepsilon_{LWIR}$  effect according to the recommendation of ASHARE standard. It can be observed that the optimized dynamic  $\varepsilon$  window has lower energy consumption than optimized static  $\varepsilon$  window.

# Characterizations of W-doped VO<sub>2</sub> NPs

Fig. S20 is the derivate of transmittance for W-doped VO<sub>2</sub>. The largest derivation during heating appeared at 30 °C while the largest derivation during cooling appeared at 25 °C. As the result, the W-doped VO<sub>2</sub> NPs'  $\tau_c$  was determined as 27.5 °C by averaging the two values.

Fig. S21 shows  $T_{\text{lum}}$ ,  $T_{\text{sol}}$  and  $\varepsilon_{\text{LWIR}}$  of W-doped VO<sub>2</sub> RCRT window at different temperature with an interval of 10 °C. The data was used in the building energy simulation.

# Additional energy consumption modelling for RCRT windows

The surface temperature of simulated eastern side window and ambient temperature was showed in Fig. S22. It can be observed that the window has a higher surface temperature than the ambient from 8:00 to 18:00 in Singapore.

Fig. S23 shows the energy savings of commercial low-E glass, W-doped Max  $\Delta\varepsilon$  sample (namely "current work") and W-doped VO<sub>2</sub> sample without RC modulation in climate zone 1 to 7 against normal glass. Their optical data used in simulation is listed in Table S5. The  $\varepsilon_{LWIR-Back}$ of the three glasses are fixed at 0.1 for comparison. It can be observed that, by combining the thermochromic window to low-E glass, the thermochromic window without RC has a better energy saving performance compared with commercial low-E glass. This observation indicates that  $\Delta T_{\rm sol}$  is effective for energy saving. Moreover, by adding the RC regulation, the RCRT window could further enhance the energy saving from zone 3 to 7. Therefore, in four-season regions, RC regulation is important as it works with solar modulation to improve energy efficiency. Moreover, with a commercial low-E glass as benchmark, tropical climate Honolulu gives the energy savings of 324.1 MJ m<sup>-2</sup>. On the other hand, in cold climate cities such as Stockholm and Whitehorse, RCRT window also shows reduced energy consumption (96.8 MJ m<sup>-</sup> <sup>2</sup> and 324.6 MJ m<sup>-2</sup>, respectively) compared with low-E window. The RCRT window shows an average global energy saving of 206.0 MJ m<sup>-2</sup>. It is worth noting that with application of RCRT window, the lighting energy will increase slightly compared to that of the commercial low-E glass, in a range of 0.7 - 2.2%. However, the additional energy savings achieved in HVAC's delivery system are much more than the increased lighting energy consumption.

Relationship of film thickness and spinning speed for PMMA spacer and VO<sub>2</sub>-PMMA layer The relationship of spinning speed and PMMA layer thickness was showed in Fig. S24. It can be observed that with the spinning speed increasing from 2000 to 4000 rpm, the spacer layer thickness decreases.

The relationship of spinning speed and VO<sub>2</sub>-PMMA layer was showed in Fig. S25. As the VO<sub>2</sub> film coated with 3000 rpm has the most stable film thickness across the different weight ratio, the spinning speed of 3000 rpm was chosen to fabricate the multilayer structure. For VO<sub>2</sub> sample without RC regulation, the sample was prepared through spin coating VO<sub>2</sub> NPs-PMMA suspension onto glass substrate with the spin speed of 3000 rpm.

#### Additional energy consumption simulation for double-glazed window

The energy saving for double glazed unit, double glazed low-E window, and double glazed RCRT window in Shanghai with the single panel normal glass as baseline is shown in Fig. S26. For double glazed RCRT window, RCRT layer is on the surface 1 while the low-E layer is on the surface 2. Optical properties of commercial low-E glass and W-doped Max  $\Delta\varepsilon$  sample listed in Table S5 were used in this simulation. Compared with double glazed unit (307.7 MJ m<sup>-2</sup>) and double glazed low-E window (386.5 MJ m<sup>-2</sup>), double glazed RCRT window shows the best energy saving performance of 540.7 MJ m<sup>-2</sup>.

#### Improving the emissivity difference between smaller temperature differences

To further improve the emissivity modulation ability between smaller temperature differences, the FDTD simulations with the same multi-layered structure used in Fig. S10 were conducted. In this simulation, Molybdenum (Mo) and Niobium (Nb) doped VO<sub>2</sub> based RCRT windows were employed, and pure VO<sub>2</sub> based RCRT window was used as a benchmark. The optical constant of pure and doped VO<sub>2</sub> at different temperatures was referred from reference. (57-59) It can be

observed that for pure VO<sub>2</sub>, the LWIR emissivity drastically increases from 0.1 to 0.62 from 20-70 °C, giving  $\Delta \epsilon_{LWIR}$  (20-70°C) = 0.52. In contrast, Nb-doped VO<sub>2</sub> shows an  $\Delta \epsilon_{LWIR}$  (20-40°C) = 0.47 (20 °C: 0.23, 40 °C: 0.70); while Mo-doped VO<sub>2</sub> achieves  $\Delta \epsilon_{LWIR}$  (30-35°C) = 0.44 (30 °C: 0.24, 35 °C: 0.68) as shown in Fig. S27. Therefore, a similar emissivity difference compared with pure VO<sub>2</sub> can be achieved with a relatively small temperature difference through doping.

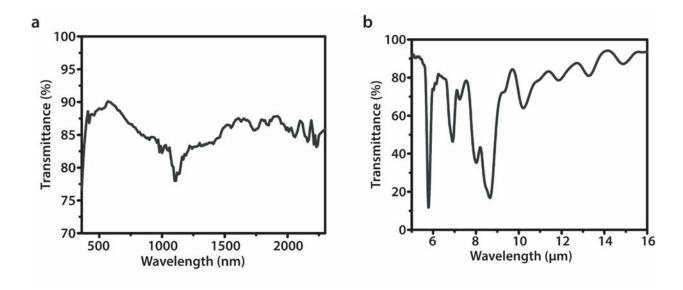
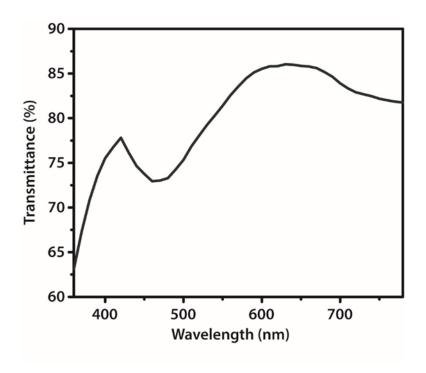
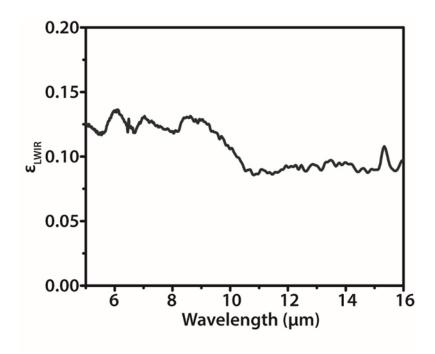


Fig. S1.

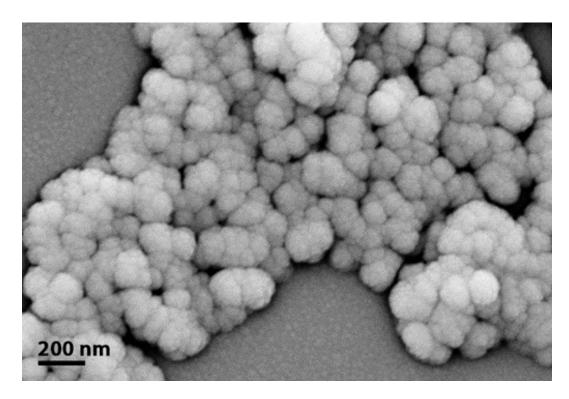
(A) UV-Vis-NIR spectrum of PMMA thin film. (B) FTIR spectrum of PMMA thin film.



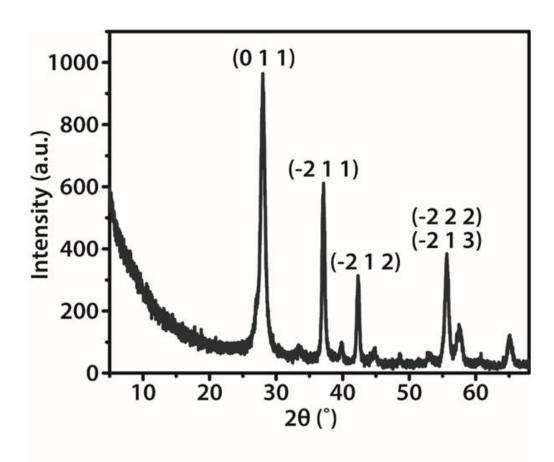
**Fig. S2.** Visible transmittance spectra of ITO.



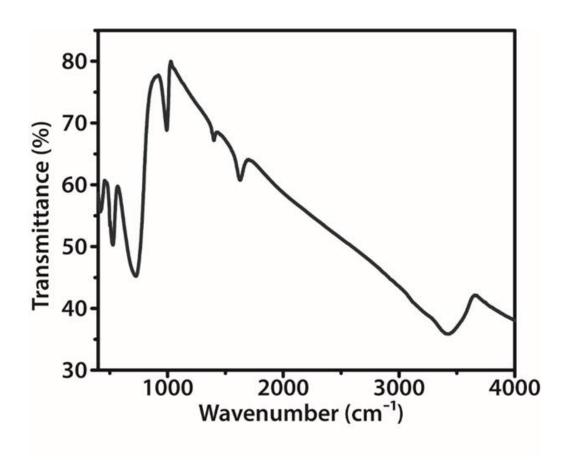
**Fig. S3.**  $\varepsilon_{LWIR}$  spectrum of ITO.



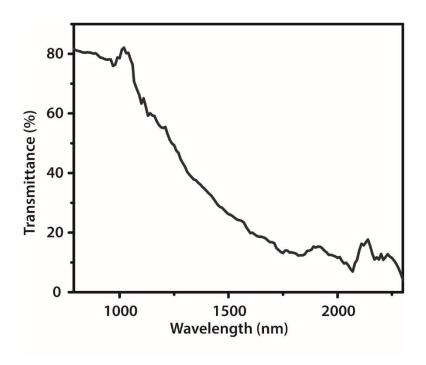
**Fig. S4.** SEM image of VO<sub>2</sub> NPs.



**Fig. S5.** XRD pattern of VO<sub>2</sub> NPs.



**Fig. S6.** FTIR spectrum of VO<sub>2</sub> NPs.



**Fig. S7.**NIR transmittance of ITO.

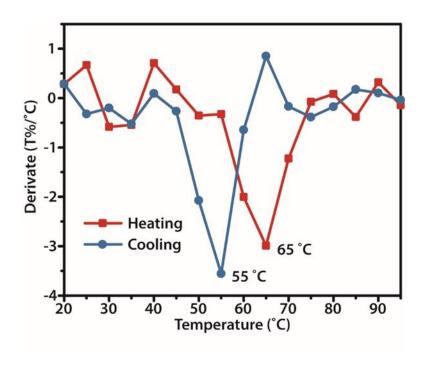


Fig. S8. Derivate of transmittance for pure  $VO_2$  to show its transition temperature.

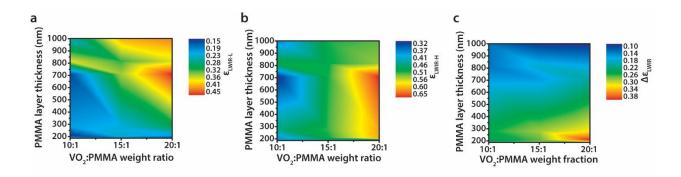


Fig. S9. Mapping results on the effects of PMMA spacer thickness and VO<sub>2</sub> weight ratio in the VO<sub>2</sub> layer to the (A)  $\varepsilon_{LWIR-L}$ , (B)  $\varepsilon_{LWIR-H}$ , (C)  $\Delta\varepsilon_{LWIR}$ .

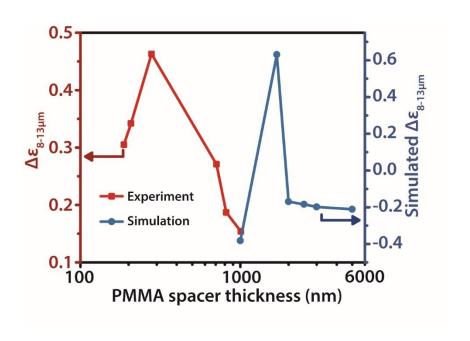
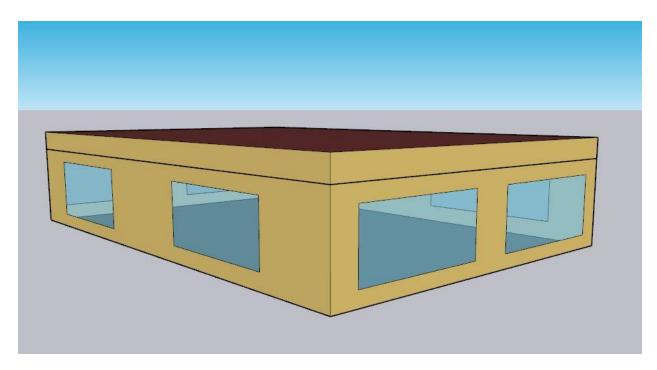


Fig. S10. Experiment (labelled in red) and simulation (labelled in blue) relationship of  $\Delta \epsilon_{8-13\mu m}$  and PMMA spacer thickness with fixed VO<sub>2</sub> weight ratio of 20:1.



**Fig. S11.** Geometrical model of the single-story prototype building for mapping simulation.

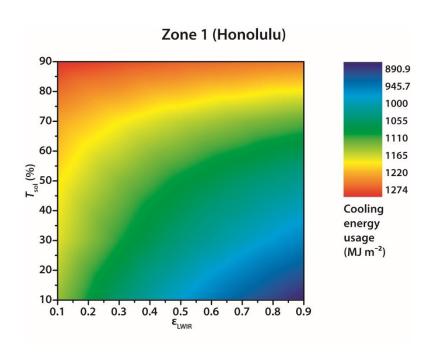
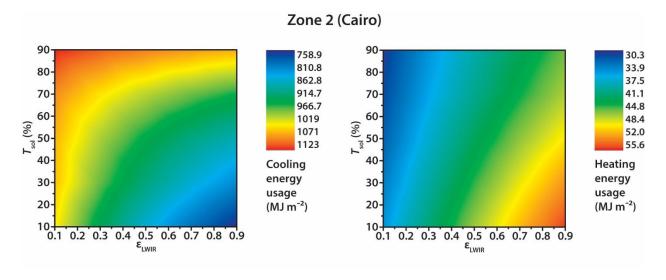
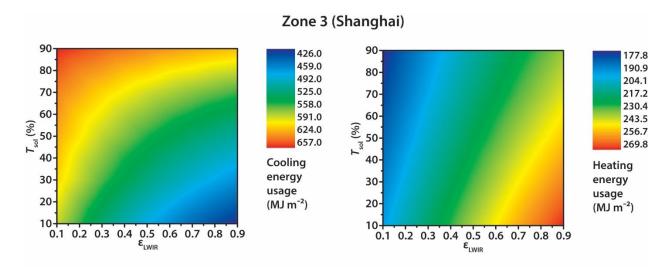


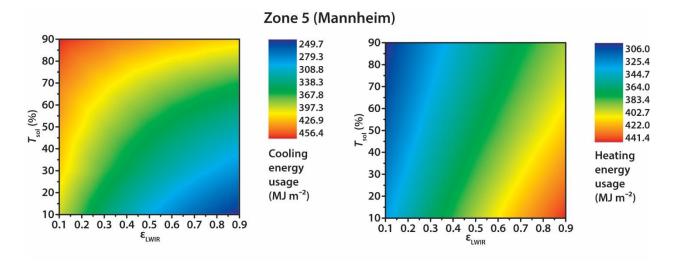
Fig. S12. Mapping result on the effects of  $T_{\rm sol}$  and  $\varepsilon_{\rm LWIR}$  to the cooling energy usage in zone 1. The heating energy consumption in zone 1 is negligible. Colors of the regions indicate the cooling energy usage of samples.



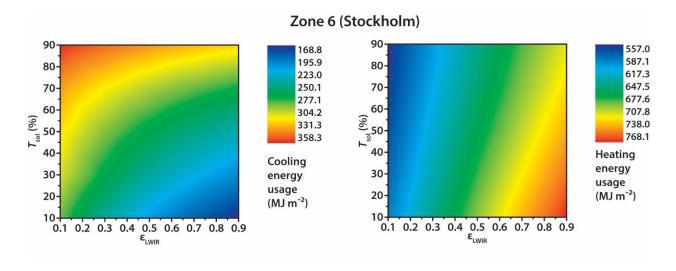
**Fig. S13.** Mapping results on the effect of  $T_{\text{sol}}$  and  $\varepsilon_{\text{LWIR}}$  to the cooling (left) and heating (right) energy usage in zone 2. Color of the regions indicates the energy usage of samples, respectively.



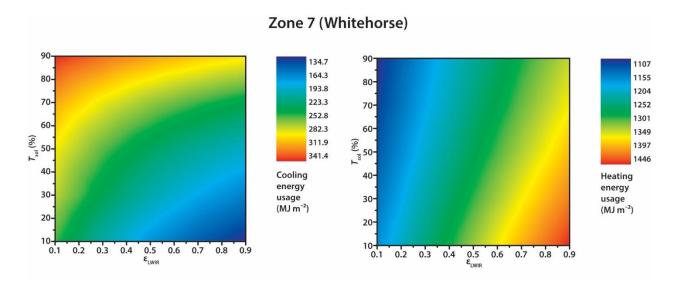
**Fig. S14.** Mapping results on the effect of  $T_{\text{sol}}$  and  $\varepsilon_{\text{LWIR}}$  to the cooling (left) and heating (right) energy usage in zone 3. Color of the regions indicates the energy usage of samples, respectively.



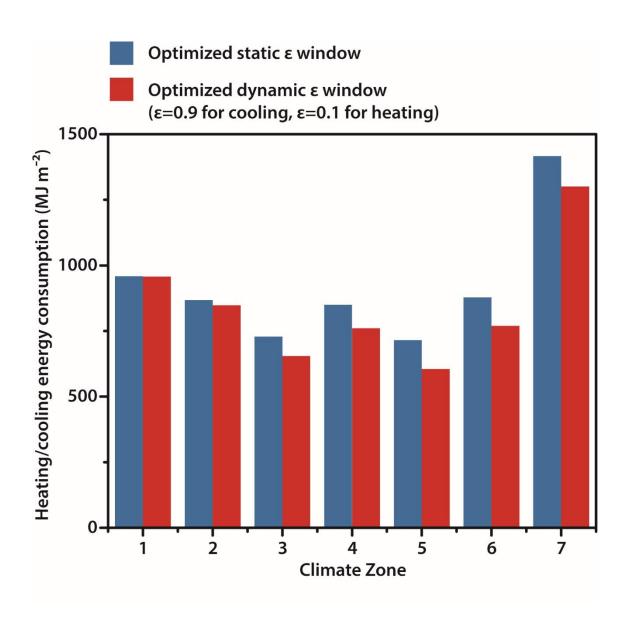
**Fig. S15.** Mapping results on the effect of  $T_{\text{sol}}$  and  $\varepsilon_{\text{LWIR}}$  to the cooling (left) and heating (right) usage in zone 5. Color of the regions indicates the energy usage of samples, respectively.



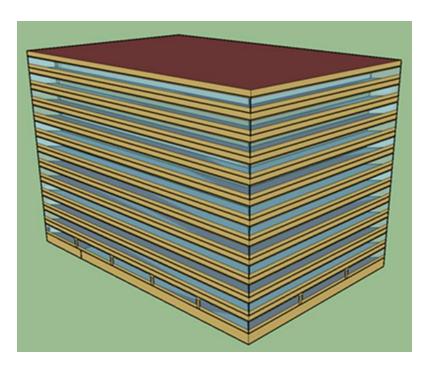
**Fig. S16.** Mapping results on the effect of  $T_{\text{sol}}$  and  $\varepsilon_{\text{LWIR}}$  to the cooling (left) and heating (right) energy usage in zone 6. Color of the regions indicates the energy usage of samples, respectively.



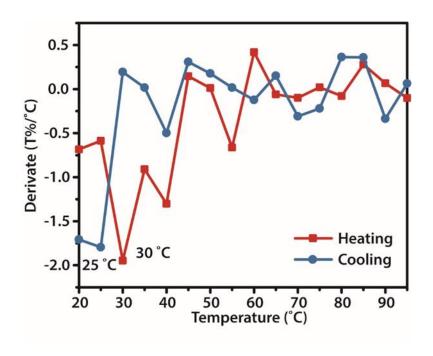
**Fig. S17.** Mapping results on the effect of  $T_{\text{sol}}$  and  $\varepsilon_{\text{LWIR}}$  to the cooling (left) and heating (right) energy usage in zone 7. Color of the regions indicates the energy usage of samples, respectively.



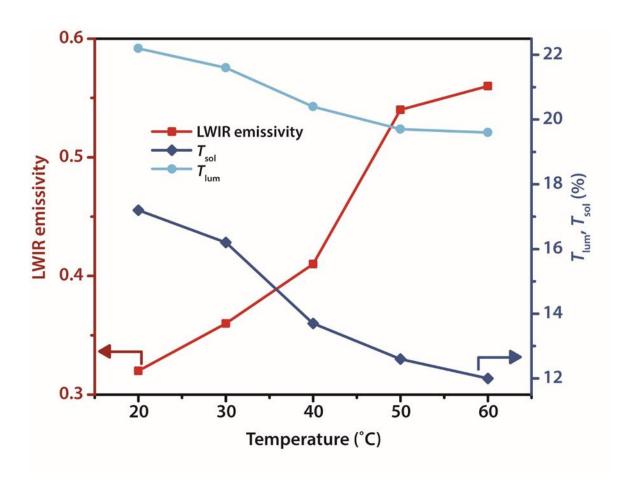
**Fig. S18.** Heating/cooling energy consumption of optimized static ε window and optimized dynamic ε window. The energy consumption of static optimized ε window is derived from the point of minimum total energy consumption in 7 climate zones with fixed 30% of  $T_{\rm sol}$ . The optimized dynamic ε window has a ε<sub>LWIR</sub> of 0.9 for cooling, 0.1 for heating, and a  $T_{\rm sol}$  of 30%.



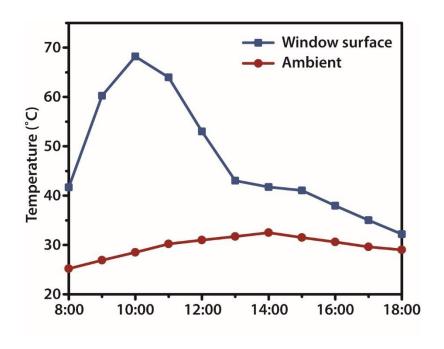
**Fig. S19.**Large office building model used in an actual-size building energy simulation. (46)



**Fig. S20.**Derivate of transmittance for W-doped VO<sub>2</sub> to show its transition temperature.



**Fig. S21.**  $T_{\text{lum}}$ ,  $T_{\text{sol}}$  and  $\varepsilon_{\text{LWIR}}$  of W-doped VO<sub>2</sub> RCRT window at different temperatures.



**Fig. S22.**Comparison of a simulated eastern window's surface temperature against the ambient temperature from 8:00 to 18:00 for high-rise office building in Singapore.

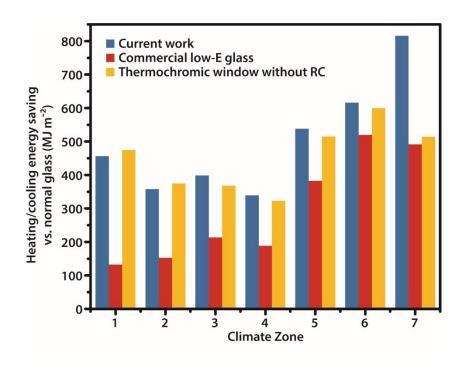
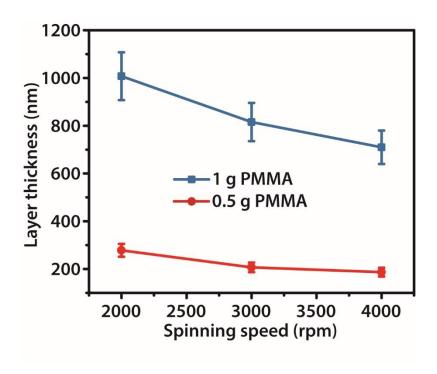


Fig. S23. Heating/cooling energy savings of commercial low-E glass, W-doped Max  $\Delta \varepsilon$  sample (namely "current work") and W-doped VO<sub>2</sub> sample without RC modulation in climate zone 1 to 7 against normal glass and the optical data used in simulation is listed in Table S5. The  $\varepsilon_{LWIR-Back}$  of the three glasses are fixed at 0.1 for comparison.



**Fig. S24.**Relationship of PMMA film thickness and spinning speed for PMMA-acetone solution with different PMMA content.

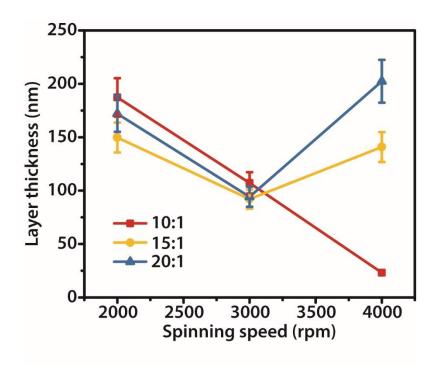


Fig. S25. Relationships of  $VO_2$  film thickness and spinning speed for different  $VO_2$  weight ratio suspensions.

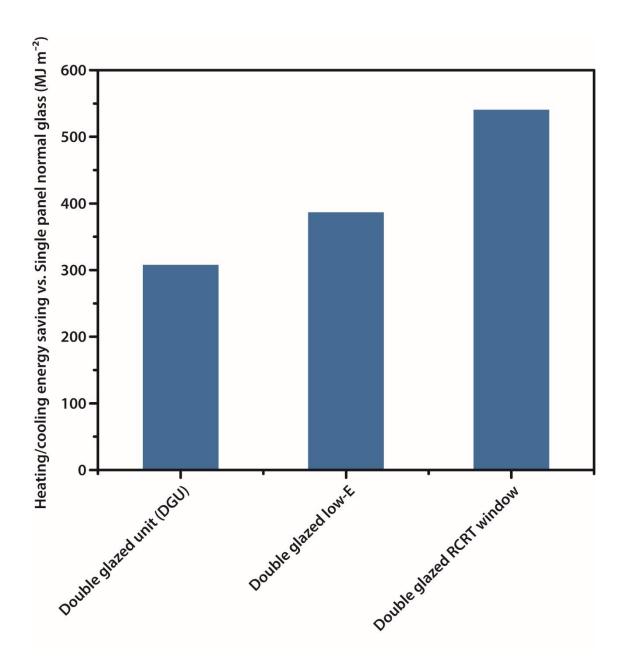


Fig. S26.

Heating and cooling energy saving for double glazed unit, double glazed low-E window, and double glazed RCRT window in Shanghai with the single panel normal glass as baseline. For double glazed RCRT window, RCRT layer is on the surface 1 while the low-E layer is on the surface 2. Optical properties of commercial low-E glass and W-doped Max  $\Delta\varepsilon$  sample listed in Table S5 were used in this simulation.

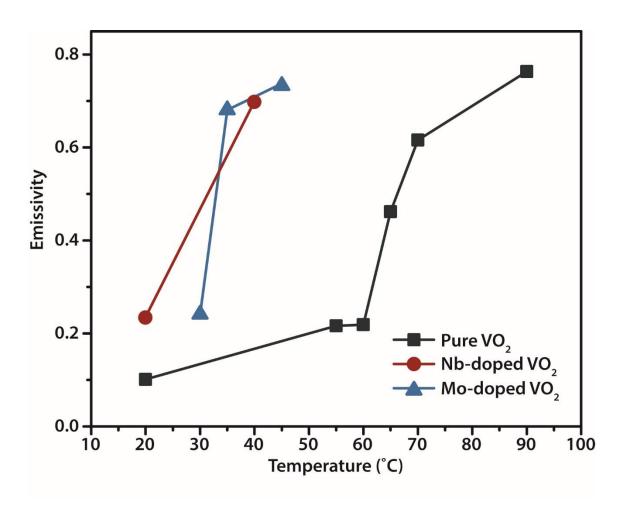


Fig. S27 FDTD simulated emissivity for pure  $VO_2$ , Nb-doped  $VO_2$ , and Mo-doped  $VO_2$  based RCRT windows at different temperatures.

**Table S1.** Summary of recent RC/emissivity regulation works.

Luminous transmission (380-780 nm)	Solar transmission (380-2500 nm)	Atmospheric window emissivity (8-13 µm)	Materials/Structure	Applications	Reference
27.8%	27.4% (20°C) 18.1% (90°C)	0.24 (20°C) 0.70 (90°C)	VO <sub>2</sub> -PMMA spacer-ITO	Smart window	This work
N/A* (highly reflective)	N/A (highly reflective)	~0.85	HfO <sub>2</sub> /SiO <sub>2</sub> multilayer	Daytime radiative cooler	S. Fan, et al., Nature, 2014 <sup>9</sup>
Highly transparent	N/A	~0.95	Silica photonic crystal	Transparent radiative cooler for solar panel	S. Fan, <i>et al.</i> , <i>Proc. Natl.</i> <i>Acad. Sci. U. S.</i> <i>A.</i> , 2015 <sup>10</sup>
N/A (highly reflective)	N/A (highly reflective)	~0.9	Si <sub>3</sub> N <sub>4</sub> /Si/Al on Si wafer	Radiative cooler	S. Fan <i>et al.</i> , <i>Nat. Commun.</i> , 2016 <sup>11</sup>
Translucent	N/A	>0.93	Polymer-based hybrid metamaterial with randomly distributed SiO <sub>2</sub> microsphere	Semi- transparent radiative cooling film	X. Yin et al., Science, 2017 <sup>15</sup>
N/A (black/white opaque emitter)	N/A (black/white opaque emitter)	~0.9	Black/white spray- painted copper emitter	Directional daytime radiative cooler Radiative	E. N. Wang et al., Nat. Commun., 2018 <sup>12</sup>
<5%	<5%	0.83	Delignificated hot pressed wood	cooling structural material	L. Hu <i>et al.</i> , Science, 2019 <sup>20</sup>
N/A (highly reflective)	N/A (highly reflective)	~0.95	PDMS coated metal (Al or Ag) film	All-day radiative cooling film	Q. Gan <i>et al.</i> , <i>Nature</i> <i>Sustainability</i> , 2019 <sup>14</sup>
N/A (coloured opaque painting)	N/A (coloured opaque painting)	0.95	Bilayer hierarchically porous polymer film	Coloured radiative cooling painting	Yang, Y. et al., Sci. Adv., 2020 <sup>60</sup>
N/A (white opaque film)	N/A (white opaque film)	0.98	Hierarchically structured PMMA film with a micropore array	Radiative cooling film	L. Wu et al., Nat. Commun., 2021 <sup>61</sup>
N/A	N/A	~0.2 (25°C) ~0.8 (70°C)	VO <sub>2</sub> on sapphire	IR absorber	F. Capasso <i>et al.</i> , <i>Appl. Phys. Lett.</i> , 2012 <sup>30</sup>

N/A (highly reflective)	N/A (highly reflective)	~0.1 (Amorphous) ~0.5 (Crystalline) Driven by electricity	Crystalline GST on Au coated glass	Data storage	M. Wuttig et al., Nat. Mater., 2008 <sup>62</sup>
N/A	N/A	~0.4 (Pristine) ~0.2 (H intercalation)	Perovskite on Si <sub>3</sub> N <sub>4</sub>	Optical memories	N. Yu et al., Adv. Mater., 2016 <sup>63</sup>
N/A	N/A	~0.3 (25°C) ~0.8 (100°C)	VO <sub>2</sub> -SiO <sub>2</sub> -Au multilayer structure	Thermal radiator	É. Haddad <i>et</i> al., <i>Appl. Phys. Lett.</i> , 2013 <sup>64</sup> O. L. Muskens
N/A	N/A	~0.3 (25°C) ~0.75 (80°C)	VO <sub>2</sub> -SiO <sub>2</sub> -Al-Al <sub>2</sub> O <sub>3</sub> on Si	Radiative cooler	et al., ACS Photonics 2018 <sup>65</sup>
N/A	61%	N/A	Simulation work for wasaving	rindow energy	J. Wang <i>et al.</i> , Appl. Energy, 2015 <sup>66</sup>
39.6%	~35% (20°C) ~30% (90°C)	~0.2	VO <sub>2</sub> on FTO	Smart window	Z. L. Wang et al., Energy Environ. Sci. 2011 <sup>67</sup>

<sup>\*</sup>N/A: not available

**Table S2.** A: Information of the building model applied in mapping simulation.

Items	Specifications
Window fraction (window-to-wall ratio)	30% of above-grade gross walls
Window locations	Even distribution among all four sides
Floor to ceiling height	3.00 m
Glazing sill height	0.70 m
Exterior walls	Stucco + wall insulation + gypsum board
Roof	Roof membrane + roof insulation + roof truss
Window	The window type is described accordingly
	Ideal-loads-air-system served by district
HVAC	cooling and heating sources; thermostat
пуас	setpoint 24 °C (75 °F) cooling/ 21 °C (70 °F)
	heating with 5.6 °C (10 °F) setback

B: Information of the building model applied in actual building energy simulation.

Items	Specifications
Window fraction (window-to-wall ratio)	40% of above-grade gross walls
Window locations	Even distribution among all four sides
Floor to floor height	3.96 m
Floor to ceiling height	2.74 m
Glazing sill height	0.91 m
Exterior walls	Mass (pre-cast concrete panel): heavy-weight concrete + wall insulation + gypsum board
Roof	Built-up roof: roof membrane + roof insulation + metal decking
Window	The window type is described accordingly
	Water-cooled centrifugal chillers + VAV
	terminal box with damper and hot-water
HVAC	reheating coil + gas-fired boiler; thermostat
	setpoint 24 °C (75 °F) cooling/ 21 °C (70 °F)
	heating with 5.6 °C (10 °F) setback

Table S3. PMMA spacer thickness and W-doped VO2 weight ratio to tune the  $\epsilon_{LWIR}$  (2.5-25  $\mu m)$  in the RCRT window

			ELWIR-L			
		PMMA spacer thickness (nm)				
W-VO <sub>2</sub> :PMMA	190	210	280	710	820	1000
weight ratio						
10:1	0.18	0.16	0.20	0.42	0.45	0.55
15:1	0.16	0.14	0.19	0.48	0.58	0.57
20:1	0.31	0.32	0.36	0.59	0.64	0.65
			€LWIR-H			
			PMMA space	er thickness (nn	n)	
W-VO <sub>2</sub> :PMMA	190	210	280	710	820	1000
weight ratio						
10:1	0.26	0.23	0.25	0.53	0.54	0.59
15:1	0.19	0.19	0.31	0.64	0.69	0.64
20:1	0.52	0.57	0.56	0.77	0.71	0.74
$\Delta arepsilon_{ m LWIR}$						
	PMMA spacer thickness (nm)					
W-VO <sub>2</sub> :PMMA	190	210	280	710	820	1000
weight ratio						
10:1	0.09	0.07	0.06	0.11	0.09	0.05
15:1	0.03	0.05	0.12	0.15	0.12	0.07
20:1	0.21	0.24	0.20	0.18	0.07	0.09

**Table S4.** Summary of the optimized  $\varepsilon_{LWIR}$  and heating/cooling energy consumption of static  $\varepsilon_{LWIR}$  window for different climate zone.

Climate zone	Optimized $\varepsilon_{ m LWIR}$	Heating/cooling energy consumption (MJ m <sup>-2</sup> )
Zone 1 (Honolulu)	0.9	958.9
Zone 2 (Cairo)	0.9	867.8
Zone 3 (Shanghai)	0.9	728.7
Zone 4 (Albuquerque)	0.9	849.8
Zone 5 (Mannheim)	0.7	715.2
Zone 6 (Stockholm)	0.1	878.1
Zone 7 (Whitehorse)	0.1	1416.5

**Table S5.** Optical properties for samples used in simulation

Optical properties	W-doped Max	W-doped VO <sub>2</sub> w/o	Commercial low-E	Normal
	$\Delta arepsilon$	RC modulation	glass	glass
ELWIR-L	0.32	0.82	0.84	0.84
€LWIR-H	0.56	0.84	0.84	0.84
$\Delta arepsilon_{ m LWIR}$	0.24	0.02	0	0
ELWIR-Back	0.1	0.1	0.1	0.84
$T_{\mathrm{lum}}$ (%)	22.2	25.5	85.0	88.1
$R_{\text{lum-Front}}$ (%)	9.1	7.9	5.6	8.0
$R_{\text{lum-Back}}$ (%)	11.6	11.3	7.9	8.0
$T_{\text{sol-L}}$ (%)	17.2	23.8	63.0	77.5
$R_{\text{sol-L-Front}}$ (%)	11.1	7.9	19.0	7.1
$R_{\text{sol-L-Back}}$ (%)	16.6	16.6	22.0	7.1
$T_{\text{sol-H}}$ (%)	12.0	16.1	63.0	77.5
$R_{\text{sol-H-Front}}$ (%)	7.7	6.5	19.0	7.1
$R_{\text{sol-H-Back}}$ (%)	16.5	16.7	22.0	7.1

**Table S6.** Summary of VO<sub>2</sub>-PMMA mixed suspension used in this work.

VO <sub>2</sub> /PMMA weight ratio	Weight of VO <sub>2</sub> (g)	Weight of PMMA
10:1	0.5	0.05
15:1	0.75	0.05
20:1	1	0.05

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