

# Fatgraphs of $M_{1,1}$

Automatically generated by FatGHoL 5.4  
(See: <http://fatghol.googlecode.com/>)

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There are a total of 2 undecorated fatgraphs in the Kontsevich graph complex of  $M_{1,1}$ , originating 2 marked ones.

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## Notation

We denote  $G_{m,j}$  the  $j$ -th graph in the set of undecorated fatgraphs with  $m$  edges; the symbol  $G_{m,j}^{(k)}$  denotes the  $k$ -th inequivalent marking of  $G_{m,j}$ .

Fatgraph vertices are marked with lowercase latin letters “a”, “b”, “c”, etc.; edges are marked with an arabic numeral starting from “1”; boundary cycles are denoted by lowercase greek letters “ $\alpha$ ”, “ $\beta$ ”, etc.

Automorphisms are specified by their action on the set of vertices, edges, and boundary cycles: for each automorphism  $A_k$ , a table line lists how it permutes vertices, edges and boundary cycles relative to the identity morphism  $A_0$ . The automorphism table is printed only if the automorphism group is non-trivial.

Automorphisms that reverse the orientation of the unmarked fatgraph are indicated with a “†” symbol in the automorphism table; those that reverse the orientation of the marked fatgraphs are distinguished with a “‡” sign.

If a fatgraph is orientable, a “Markings” section lists all the inequivalent ways of assigning distinct numbers  $\{0, \dots, n-1\}$  to the boundary cycles; this is of course a set of representatives for the orbits of  $\mathfrak{S}_n$  under the action of  $\text{Aut}(G)$ .

A separate section lists the differential of marked fatgraphs; graphs with null differential are omitted. If no marked fatgraph has a non-zero differential, the entire section is dropped.

Boundary cycles are specified using a “sequence of corners” notation: each corner is represented as  ${}^pL^q$  where  $L$  is a latin letter indicating a vertex, and  $p, q$  are the attachment indices of the incoming and outgoing edges, respectively. Attachment indices match the Python representation of the vertex: e.g., if `a=Vertex([0,0,1])`, the two legs of edge 0 have attachment indices 0 and 1, and the boundary cycle enclosed by them is represented by the (single) corner  ${}^0a^1$ .

## Fatgraphs with 2 edges / 1 vertex

There is 1 unmarked fatgraph in this section, originating 1 non-orientable marked fatgraph.

### The Fatgraph $G_{2,0}$ (non-orientable, no orientable markings)



```
Fatgraph([
  Vertex([1, 0, 1, 0]),# a
])
```

Boundary cycles

$$\alpha = ({}^3a^0 \rightarrow {}^2a^3 \rightarrow {}^1a^2 \rightarrow {}^0a^1)$$

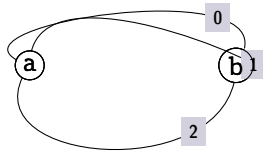
Automorphisms

$A_0$	a	0	1	$\alpha$
$A_1^\dagger$	a	1	0	$\alpha$
$A_2$	a	0	1	$\alpha$
$A_3^\dagger$	a	1	0	$\alpha$

## Fatgraphs with 3 edges / 2 vertices

There is 1 unmarked fatgraph in this section, originating 1 orientable marked fatgraph.

### The Fatgraph $G_{3,0}$ (1 orientable marking)



```
Fatgraph([
  Vertex([1, 0, 2]),# a
  Vertex([2, 1, 0]),# b
])
```

### Boundary cycles

$$\alpha = ({}^2a^0 \rightarrow {}^1a^2 \rightarrow {}^0a^1 \rightarrow {}^0b^1 \rightarrow {}^2b^0 \rightarrow {}^1b^2)$$

### Automorphisms

$A_0$	a	b	0	1	2	$\alpha$
$A_1$	a	b	2	0	1	$\alpha$
$A_2$	a	b	1	2	0	$\alpha$
$A_3$	b	a	1	2	0	$\alpha$
$A_4$	b	a	0	1	2	$\alpha$
$A_5$	b	a	2	0	1	$\alpha$