# **Binary Search Trees**

Scurtu Estera Daniela May 30, 2016

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#### 1 Problem statement

A library for binary search trees (BST).

The library should provide operations for: creating an empty tree, inserting a node into a tree, deleting a node and at least two different traversal strategies; the traversal functions must accept a function which will be passed the current element.

# 2 Application Design

Binary Search Tree, is a node-based binary tree data structure which has the following properties:

- The left sub-tree of a node contains only nodes with keys less than the nodes key.
- The right sub-tree of a node contains only nodes with keys greater than the nodes key.
- The left and right sub-tree each must also be a binary search tree.
- There must be no duplicate nodes.

Binary Search Tree can be implemented as a linked data structure in which each node is an object with two pointer fields and an information field. The two pointer fields left and right point to the nodes corresponding to the left child, right child. NULL in any pointer field signifies that there exists no corresponding child.

#### 2.1 Inputs

Input data is read from a file named test.in.txt which has the following structure:

- the first line contains the number of nodes that are initially in the tree
- the second line contain the number of tests to be made
- the next nrTeste lines, has each two values, one for the nodes to be inserted in the tree and one for the nodes to be deleted from the tree.

Here is an example of inputs for this algorithm:

70 123 125 213

# 2.2 Outputs

First output is the number of nodes of the tree followed by a traversal of the tree, breadth first tree traversal. The rest output consists in nrTeste tests which include inserting nrNodeAdd in the tree and deleting nrNodeDel from the tree.

This image is a part of output, the test number 5.

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33	27	13	39	45	41	40	53	53	48	
58	48	37	70	79	73	73	66	85 101	81	
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143 175 193	155	102 139 156	162	165	166	167	166	157	173	
175	174	172	156	137	101	188	197	200	200	
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307	284	264 320	320	324	326	322	320	313	291 282	
251	217	65 349	329	331	335	330	337	336	329	
340	344	349	345	342	341	351	355	362	351	
340	373	375	372	385	389	388	146 166 197 225 235 277 292 320 337 355 388 412	381	379	
371	371	375 395 414	397	403 202	397 490	373	412	412	426 435	
441	435	427	390	366	447	449	447	445	445	
340 391 426 441 450 481 329	456	452	451	458	470	480	434 447 478	463	463	
481	460	492	494	499	495	492	491	450	443	
329	512	515	520	520	526	518	528	528	535	
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601 616	618	613	625	623	620	633	628	638	636	
639	641	640	639	626	620	647	667	667	665	
675 690 716 742 757 771 781 830 871	683	686	678	674	654	654	654	688	688	
69Ø	697	691	702	703	702	704	714	718	716 736	
742	749 749	907 943	743	743	752	734	758	261	757	
757	756	751	771	775	752 775 785 816 858 894 608	779	780	777 799 819 830 886	777	
771	735	794	793	795	785	798	799	799	785	
781	720	647	804	804	816	824	826	819	833	
830	837	837	854	864	858	849	839	830	802 881	
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nrNod	eDel = 2:									
28	33	33 92 246	34	35	40	65	66 143	81 165	81	
85 170	87 217	92	101	101	102	11b	143 200	263	166 264	
264	221	270	270	277	279	279	282	282	284	
291	307	277 313	322	324	337	345	351	362	372	
28 85 178 264 291 388	391	393 445 520	395	35 101 251 277 324 397 451 528 6183 743	40 102 251 279 337 397 460	65 116 251 279 345 403	259 282 351 404	414	434	
435 508	435	445	445	451	460	463	480	481	495	
508	515	520	528	528	541 620 686	541	541 625 688	546	548 639	
654	654	566 654	667	683	686	688	688	636 704	716	
720	720	724	742	743	743	755	771 804	771 804	775	
553 654 720 775 830	271 307 391 435 515 558 654 720 777 830	724 777 868	780	793 899	743 795 900	463 541 623 688 755 798 900	804	804	826	
830	830	868	34 101 246 277 322 395 445 528 613 667 742 780 881	899	900	900				_
	<u> </u>	<u> </u>	<u> </u>	<u> </u>			<u> </u>	<u> </u>		

If we were to run again the program, the numbers would be different because the program would generate different numbers for each run.

## 2.3 Operations on Binary Search Trees

#### 1. Create an element

This operation can be seen in the procedure "getNode" which have a parameter of type int, that represent the value we want to store in the created node. Firstly I allocate memory for one element of type "bstNode" using the "malloc" function, next step is to store the value key in the data field. The last step to be taken is to initialize the right and left fields of the node to NULL.

I will use this function in the procedure "insert\_bst" to create the node to be inserted in the tree.

#### 2. Insertion of a node in the tree

For this operation I used a function named "insert\_bst" with two parameters one of type bstNode which is the adress of the root, and an integer which represents the value to be inserted. Insertion begins as a search would begin; if the key is not equal to that of the root, we search the left or right subtrees as before. Eventually, we will reach an external node and add the new key-value pair as its right or left child, depending on the node's key. In other words, we examine the root and recursively insert the new node to the left subtree if its key is less than that of the root, or the right subtree if its key is greater than or equal to the root

#### 3. Deletion of a node of the tree

This operation is described in the procedure "deleteNode" with two parameters, one that represent the adress of the root and another one that takes the value to be deleted. Deletion also begins as a search, we try to find where the node that has the value we want to delete is, if the key is lesser than the root(the actual node) value we use recursion and call the function to move in the left sub-tree and take the steps from the beginning, else if is greater we move in the right sub-tree, else we find the wanted value and from here three cases can be distinguished:

- Case 1: the node has no child this case is the simple one because
  the wanted node already points to NULL so all we have to do is
  to deallocate the node using the function free and make it NULL.
- Case 2: the node has one child here there can be two cases, the node can have either the left child or the right child. If the node has only a left child, we put all the left sub-tree int the place of the node to be deleted. I made this using an auxiliary variable named temp which will copy the address of the root, and make the root point to its left child, while the auxiliary variable will be deallocated. The case for the right child is similar the only difference is where the root node will point.

• Case 3: the node has two children - to solve this case I will use a function "findMin" which goes to the most left child of the tree, which is the minimum value and return its address. I will use the auxiliary variable again, this time it will store the address of the minimum value in the right sub-tree, we copy this value to the node we want to delete. Now there will be two nodes that store the same value, because we don't know in which one of the cases we are we will call the function with the parameters root-¿right and root-¿data, which is the minimum value in the right sub-tree.

#### 4. Traversal of a tree.

There are two known types of traversal for a Binary Search Tree:

- (a) Depth First Search which can be
  - Pre-order Traversal
  - In-order Traversal
  - Post-order Traversal
- (b) Breadth First Search to implement this traversal we will use three functions which take as a parameter the address of the root: "height" which compute the height of the tree the number of nodes along the longest path from the root node down to the farthest leaf node, "printGivenLevel" which print the node of a given level, "level" is a parameter of the procedure and the last function is printLevelOrder print all the nodes in level order.

#### 5. Search for a given value in the tree

The procedure for this task is named "search\_node" and takes two parameters, one of type bstNode, which is the adress of the root, and one integer which is the value we want to find. First we compare the given value with the data stored in the node, if it is greater than the node's data we move the search in the right subtree, else we are looking for the value in the left sub-tree. Once we find the value we retuen its adress.

#### 6. Add elements in the tree

The procedure used for this operation is create\_bst. This function use the function radomize which generate random numbers that are inserted in the tree using the insert\_bst function. To prevent the insertion of the same number I used the goto function which force the algorithm to reread a number if it exists in the tree.

#### 7. Delete elements from the tree

The procedure used for this operation is nodeDelete. This function generate random numbers which are delete from the tree using

the deleteNode function. Because I can not know which are the current numbers of the tree and also the numbers generated randomly I check if the data is in the tree first, if it is it will be deleted, it it is not the program will generate another number to be deleted.

## 3 Pseudocode

• The procedure insert\_bst

procedure insert\_bst (var root :struct bstNode; var key: integer): struct bstNode 1. begin 2. **if** root = NULL **then** 3. root := getNode(var root ; var key) 4. 5. else if  $root \rightarrow data < key$  then 6.  $root \rightarrow left := insert\_node(root \rightarrow left, key)$ 7. end 8. else if  $root \rightarrow data > key$  then  $root \rightarrow right := insert\_node(root \rightarrow right, key)$ 7. 8. end 9. return root 10. end insert\_node

• The procedure deleteNode

procedure deleteNode (var root :struct bstNode;

```
var key: integer): struct bstNode
1.
           begin
2.
              var temp: bstNode
3.
              if root = NULL then
4.
                 return root;
5.
              end
6.
              if root \rightarrow data < key then
7.
                 root \rightarrow left := deleteNode(root \rightarrow left, key)
b.
              end
9.
              else if root \rightarrow data > key then
                  root \rightarrow right := deleteNode(root \rightarrow right, key)
10.
11.
               else if ! root \rightarrow left and ! root \rightarrow right then
12.
13.
                  free root
14.
                  root := NULL
15.
               else if root \rightarrow left = NULL then
16.
```

```
17.
                    temp := root
18.
                    root \coloneqq root \to right
19.
                   free temp
20.
                 end
21.
                else if root \rightarrow left = NULL then
22.
                    temp := root
23.
                    root \coloneqq root \to right
24.
                   free temp
25.
                else if root \rightarrow left and root \rightarrow right then
26.
27.
                    temp:=findMin(root \rightarrow right)
28.
                   root \rightarrow data \coloneqq temp \rightarrow data
29.
                   root \rightarrow right := deleteNode(root \rightarrow right, root \rightarrow data)
30.
                 end
31.
              end deleteNode
```

• The procedure search\_node

```
procedure search_node (var root :struct bstNode;
```

```
var key: integer): struct bstNode
1.
      begin
2.
              if root = NULL then
3.
                return false
4.
              end
5.
              if root \rightarrow data = key then
6.
                return true
7.
              else if root \rightarrow data < key then
8.
9.
                return search\_node(root \rightarrow left, key)
10.
               else if root \rightarrow data > key then
11.
                  return search\_node(root \rightarrow roght, key)
12.
13.
               end
14.
            end insert_node
```

# 4 Conclusions

Only using linked lists may not be enough in some applications, for example if we want a description of a product, we would need an hierarchical description of its components. Hierarchical organisation of data is used in various fields and we can say that every physical entity can be represented as trees. The binary search tree is a different way of structuring data in hierarchical way so that it can still be binary searched (or a very similar procedure can be used), but it's easier to add and remove elements. The implementation based on dynamic programming makes the code clear and easily understandable and reduce the complexity of the algorithm.

The algorithm I made presents the most important operations that can be made on binary search trees, operations like insertion, deletion, traversals and binary search. The most challenging part of the project was to write the procedure for deletion because it is very complex and it took a lot of time to realise which was my mistake.

### 5 References

### References

- [1] Sara Baase, Computer Algorithms, Introduction to Design and Analysis *Edison-Wesley Publishing Company*. Edison Wesley, 2nd Edition,
- [2] Ellis Horowitz, Fundamentals of Programming Languages, *Computer Science Press*. Computer Science Press, 2nd Edition,
- [3] site url http://www.geeksforgeeks.org/category/binary-search-tree/,.

### 6 Source Code

Here are all the function I described above implemented in C

```
#ifndef BST_H_HINCLUDED
#define BST_H_HINCLUDED
#include "bst_c.c"

struct bstNode *getNode(int key);

struct bstNode *insert_bst(struct bstNode *root,int key);

bool search_node(struct bstNode *root, int key);

struct bstNode *create_bst(struct bstNode *root, int nrNode);

int bstSrd(struct bstNode *root);

int bstRsd(struct bstNode *root);

int bstSdr( struct bstNode *root);

struct bstNode *findMin(struct bstNode *root);

struct bstNode *deleteNode(struct bstNode *root, int key);

int printGivenLevel(struct bstNode* root, int level);
```

```
int height(struct bstNode* root);
void printLevelOrder(struct bstNode* root);
void freeTree(struct bstNode *root);
void nodeDelete(struct bstNode *root, int n);
#endif // BST_H_H_INCLUDED
#include < stdio.h>
#include < stdlib.h>
#include < stdbool.h>
#include <time.h>
#include "bst_h.h"
int randomize();
struct bstNode {
    int data;
    struct bstNode *left;
    struct bstNode *right;
struct bstNode *getNode(int key){
    struct bstNode *node = (struct bstNode *) malloc( sizeof ( struct bstNode));
    node \rightarrow data = key;
    node \rightarrow left = node \rightarrow right = NULL;
    return node;
}
struct bstNode *insert_bst(struct bstNode *root, int key){
    if (root == NULL){
        root = getNode(key);
    else if ( key < root -> data) {
        root -> left = insert_bst( root -> left, key);
    else {
        root -> right = insert_bst( root -> right, key);
    return root;
}
bool search_node(struct bstNode *root, int key){
    if (root == NULL){
        return false;
    }
```

```
else if (root \rightarrow data == key)
        return true;
    }
    else if (key < root -> data) {
        return search_node(root->left, key);
    }
    else {
        return search_node(root->right, key);
}
struct bstNode *create_bst(struct bstNode *root, int nrNode){
    int i, data;
    for (i = 0; i < nrNode; i++)
        data = rand() \% 900 + 1;
pas0:
        if (search_node(root, data)){
             goto pas0;
        }
        else {
             root = insert_bst(root, data);
    }
}
int bstSrd(struct bstNode *root){
    if(root == NULL)
             return 0;
    bstSrd(root \rightarrow left);
    printf("%d\t", root->data);
    bstSrd(root->right);
}
int bstRsd(struct bstNode *root){
    if (root == NULL){
             return 0;
    printf("%d\t", root->data);
    bstRsd(root->left);
    bstRsd(root->right);
}
int bstSdr( struct bstNode *root){
    if(root == NULL)
```

```
return 0;
    }
        bstSdr(root->left);
        bstSdr(root->right);
         printf("%d \ t", root \rightarrow data);
}
int height(struct bstNode* root)
{
    if (root == NULL)
        return 0;
    e l s e
/** compute the height of each subtree */
        int leftHeight = height(root->left);
        int rightHeight = height(root->right);
/** use the larger one */
        if (leftHeight > rightHeight){
             return(leftHeight+1);
        }
        else {
                 return (rightHeight+1);
        }
    }
}
int printGivenLevel(struct bstNode* root, int level)
    if (root == NULL)
        return;
    if (level == 1)
         printf("%d \setminus t", root->data);
    else if (level > 1)
    {
         printGivenLevel(root->left, level-1);
        printGivenLevel(root->right, level-1);
    }
}
void printLevelOrder(struct bstNode* root)
    int h = height(root);
    int i;
```

```
for (i=1; i \le h; i++)
         printGivenLevel(root, i);
    }
}
struct bstNode *findMin(struct bstNode *root){
    if (root == NULL){
         printf("the tree is empty");
         return 0;
    }
    else if (root \rightarrow left == NULL)
         return root;
    return findMin(root->left);
}
struct bstNode *deleteNode(struct bstNode *root, int key) {
    struct bstNode * temp;
    if (root == NULL) {
         return root;
    if (key < root -> data) {
         root->left = deleteNode(root->left, key);
    }
    else {
         if(root \rightarrow left == NULL \&\& root \rightarrow right == NULL)
              free (root);
             root = NULL;
         else if (root \rightarrow left == NULL) {
                  temp = root;
                  root = root -> right;
                  free (temp);
         else if (root->right == NULL) {
                       temp = root;
                       root = root \rightarrow left;
                       free (temp);
         else if (root->left != NULL && root->right != NULL) {
                  temp = findMin(root->right);
                  root \rightarrow data = temp \rightarrow data;
                  root -> right = deleteNode(root -> right, root -> data);
             }
```

```
}
    return root;
}
void freeTree(struct bstNode *root) {
    if (root == NULL) {
        return;
    freeTree(root -> left);
    freeTree(root->right);
    free (root);
}
void nodeDelete(struct bstNode *root, int n){
    int i;
    int data;
    for (i = 0; i < n; i++)
pas1:
        data = rand() % 900;
        if (search_node (root, data)) {
            root = deleteNode(root, data);
        }
        else {
            goto pas1;
    }
}
#include "bst_h.h"
int main()
{
    srand(time(NULL));
    FILE *test;
    test = fopen("test.in.txt","r");
    int nrTeste;
    int nrNode;
    int nrNodeAdd;
    int nrNodeDel;
    struct bstNode *root = NULL;
    root = insert_bst(root, 500);
    fscanf(test,"%d",&nrNode);
    fscanf(test,"%d",&nrTeste);
    printf ("Numarul de elemente din arbore este %d\n", nrNode);
```

```
create_bst(root, nrNode);
    printLevelOrder(root);
    printf("\langle n \rangle n \rangle");
    while (nrTeste != 0){
         printf("\nnTESTUL: %d\n", nrTeste);
        fscanf(test,"%d %d",&nrNodeAdd, &nrNodeDel);
         printf("\nnrNodeAdd = %d\n", nrNodeAdd);
         create_bst(root, nrNodeAdd);
        bstSdr(root);
         printf("\n\nnrNodeDel = %d\n", nrNodeDel);
        nodeDelete(root, nrNodeDel);
        bstSrd(root);
        nrTeste --;
    freeTree(root);
    fclose(test);
}
```

Here is the code in Python3.5 for the algorithm. I must say that this code does not work entirely, it is a problem when trying to delete more numbers. I tried to fix this problem but I could not do that.

```
class Node:
    def __init__(root, val):
        root.right = None
        root.left = None
        root.data = val
def insert (root, data):
    if root.data:
        if data < root.data:
            if root.left is None:
                root.left = Node(data)
            else:
               insert (root.left, data)
        elif data > root.data:
            if root.right is None:
                 root.right = Node(data)
            else:
                insert(root.right, data)
    else:
        root.data = data
def SRD(root):
    if root is None:
```

```
return
   SRD(root.left)
    print (root.data)
   SRD(root.right)
def RSD(root):
    if root is None:
        return
    print (root.data)
   RSD(root.left)
   RSD(root.right)
def bin_search(root, data):
    if root is None:
        return 0
    elif root.data is data:
        return 1
    elif data < root.data:
        return bin_search (root.left, data)
    else:
        return bin_search (root.right, data)
def find_min(root):
    if root is None:
        print ("the tree is empty")
    elif root.left is None:
        return root
    return find_min(root.left)
def delete_node(root, data):
    if root is None:
        return root
    if data < root.data:
        root.left = delete_node(root.left, data)
    elif data > root.data:
        root.right = delete_node(root.right, data)
    else:
        if root.left is None and root.right is None:
            del root
            root = None
        if root.left is None:
            temp = root.right
            root = None
            return temp
        elif root.right is None:
```

```
temp = root.left
             root = None
             return temp
        temp = find_min(root.right)
        root.data = temp.data
        root.right = delete_node(root.right , temp.data)
    return root
def create_bst(root,n):
   for i in range (1,n):
       a = randint(0,300)
       insert (root, a)
def delete_bst(root,n):
   for i in range (1,n):
       a = randint(0,300)
       delete_node (root, a)
from random import randint
root = Node(110)
create_bst(root,150)
SRD(root)
delete_bst(root,50)
RSD(root)
```

# 7 Experiments and results

To check the correctness of the algorithm I made 10 tests, each consisting in inserting a number of nrNodeAdd nodes in the tree and deleting a number nrNodeDel from the tree, the nrNodeAdd and nrNodeDel are two variables read from a file. The results were displayed using three traversal functions: level order traversal, to display the initial tree, in-order traversal, to print the tree after the insertion and post-order traversal for printing the remaining nodes after deletion.