#### Q1: Numpy array

- 1. Write a Python program to create a 5x5 array with random values and find the minimum and maximum values.
- 2. Write a Python program to create a random 10x4 array and extract the first five rows of the array and store them into a variable.
- 3. Write a Python program to create a random vector of size 10 and sort it.
- 4. Write a Python program to find the most frequent value in an one-dimensional array

```
In []:
         # 01.1
         import numpy as np
         arr = np.random.rand(5, 5)
         min_val = np.min(arr)
         max val = np.max(arr)
         print("Array:")
         print(arr)
         print("Minimum value:", min val)
         print("Maximum value:", max val)
         #01.2
         arr = np.random.rand(10, 4)
         first five rows = arr[:5, :]
         print("Array:")
         print(arr)
         print("First five rows:")
         print(first five rows)
         #Q1.3
         vec = np.random.rand(10)
         # Sort the vector
         sorted vec = np.sort(vec)
         print("Vector:")
         print(vec)
         print("Sorted vector:")
         print(sorted vec)
         #01.4
         arr = np.array([1, 2, 3, 4, 1, 2, 3, 1, 2, 1])
         # Find the most frequent value
         most freq val = np.bincount(arr).argmax()
         print("Array:")
         print(arr)
         print("Most frequent value:", most freq val)
        Array:
        [[0.65343859 0.40131901 0.80661201 0.90827084 0.97253937]
         [0.44195564 0.61107106 0.47778849 0.7143094 0.26731692]
         [0.89224649 0.45709448 0.13227858 0.51015184 0.09533194]
         [0.95958318 0.15137788 0.06036099 0.99900175 0.5688955 ]
         [0.15263539 0.096094 0.08682336 0.99681491 0.08379173]]
        Minimum value: 0.060360990638355316
        Maximum value: 0.9990017454256855
        Array:
```

```
[[0.61534186 0.7844447 0.2236946 0.30965475]
 [0.26641308 0.1646026 0.93738371 0.01441015]
 [0.17661365 0.00721641 0.37762121 0.95725058]
 [0.74279005 0.71745329 0.30281841 0.25159635]
 [0.79785256 0.79049072 0.27525058 0.63279884]
 [0.80495615 0.41445176 0.44004392 0.54583671]
 [0.24307926 0.48612474 0.6985225 0.2237292 ]
 [0.73929606 0.59157316 0.78229287 0.94939461]
 [0.50962642 0.80929789 0.83278139 0.40127202]
 [0.98691956 0.05726697 0.81321345 0.20202481]]
First five rows:
[[0.61534186 0.7844447 0.2236946 0.30965475]
 [0.26641308 0.1646026 0.93738371 0.01441015]
 [0.17661365 0.00721641 0.37762121 0.95725058]
 [0.74279005 0.71745329 0.30281841 0.25159635]
 [0.79785256 0.79049072 0.27525058 0.63279884]]
[0.86891569 0.95587306 0.65261503 0.42963711 0.73198988 0.77590815
 0.55669227 0.54507453 0.8306748 0.5986303 ]
Sorted vector:
[0.42963711 0.54507453 0.55669227 0.5986303 0.65261503 0.73198988
 0.77590815 0.8306748 0.86891569 0.95587306]
Array:
[1 2 3 4 1 2 3 1 2 1]
Most frequent value: 1
```

Q2. Linear Algebra (40pts) Bob invested 10000 dollars on two mutual funds one year ago. After one year, the overall yield rates for these two mutual funds are +2% and +4%. His yearend account showed \$10,250. How much did he initially put onto two mutual funds?

Let's represent the initial amount invested in mutual fund 1 by x, and the initial amount invested in mutual fund 2 by y. So we have the equation: x + y = 10000 After one year, the overall yield rates for these two mutual funds are +2% and +4%. His yearend account showed \$10,250.

The amount he earned on the first mutual fund is 0.02x and the amount he earned on the second mutual fund is 0.04y. So, we have the equation: x + y + 0.02x + 0.04y = 10250; 1.02x + 1.04y = 10250 We have this:  $x + y = 10000 \cdot 1.02x + 1.04y = 10250$  let's multiplying the first equation by 1.02, we get: 1.02x + 1.02y = 10200, then we get we get: 0.02y = 50, thus we get 0.02y = 50.

Therefore, Bob put 7500 on one mutual fund and \$2500 on the other mutual fund.

Q3. K-means Clustering Load the data from attached file "Assignment\_table.csv". • Create a histogram for the first and second column respectively (20 points) • Conduct a clustering algorithm on these two columns. Try out 3,4,5 clusters respectively. What do you think is the right number of clusters for this dataset? (40 points)

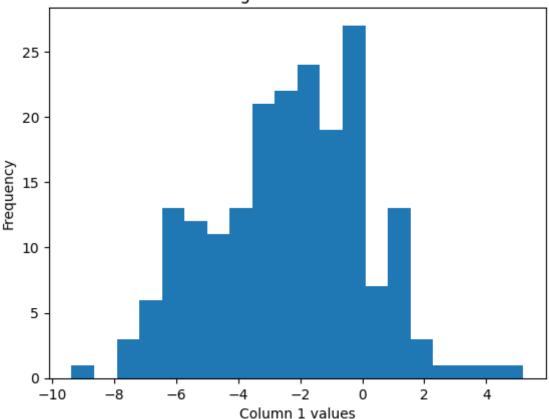
```
import pandas as pd
import numpy as np
from matplotlib import pyplot as plt
from sklearn.cluster import KMeans

data = pd.read_csv("Assignment_table.csv")

# Create histograms for first and second columns
```

```
plt.hist(data.iloc[:, 0], bins=20)
plt.title("Histogram for Column 1")
plt.xlabel("Column 1 values")
plt.ylabel("Frequency")
plt.show()
plt.hist(data.iloc[:, 1], bins=20)
plt.title("Histogram for Column 2")
plt.xlabel("Column 2 values")
plt.ylabel("Frequency")
plt.show()
# do clustering
X = data.iloc[:, [0, 1]].values
for n clusters in range(3, 6):
    kmeans = KMeans(n_clusters=n_clusters, random_state=0)
    kmeans.fit(X)
    labels = kmeans.labels_
    centroids = kmeans.cluster_centers_
    # show the results
   plt.scatter(X[:, 0], X[:, 1], c=labels)
   plt.scatter(centroids[:, 0], centroids[:, 1], marker='*', s=300, c='r')
    plt.title(f'K-means Clustering Results (n_clusters={n_clusters})')
   plt.xlabel('Column 1')
    plt.ylabel('Column 2')
    plt.show()
```

#### Histogram for Column 1

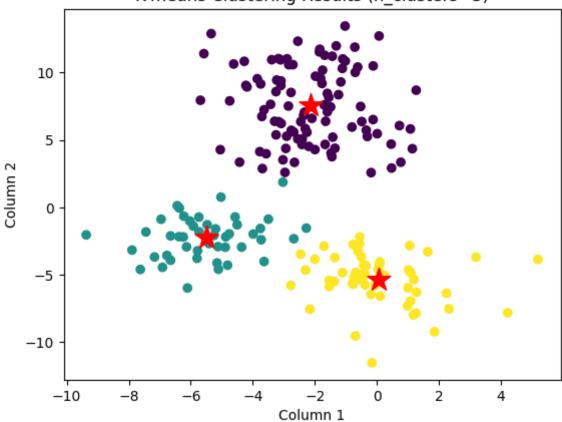


# Histogram for Column 2 20.0 17.5 15.0 Frequency 12.5 10.0 7.5 5.0 2.5 0.0 -5 -100 5 10

/Library/Frameworks/Python.framework/Versions/3.11/lib/python3.11/site-packages/sklearn/cluster/\_kmeans.py:870: FutureWarning: The default value of `n\_init` wil 1 change from 10 to 'auto' in 1.4. Set the value of `n\_init` explicitly to suppr ess the warning warnings.warn(

Column 2 values

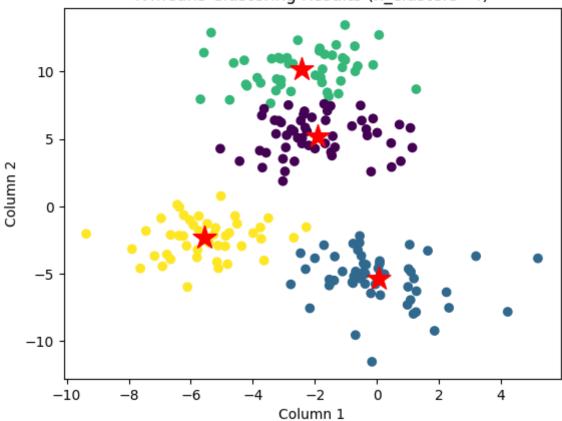
## K-means Clustering Results (n\_clusters=3)



/Library/Frameworks/Python.framework/Versions/3.11/lib/python3.11/site-packages/ sklearn/cluster/\_kmeans.py:870: FutureWarning: The default value of `n\_init` wil 1 change from 10 to 'auto' in 1.4. Set the value of `n\_init` explicitly to suppr ess the warning

warnings.warn(

## K-means Clustering Results (n\_clusters=4)



/Library/Frameworks/Python.framework/Versions/3.11/lib/python3.11/site-packages/sklearn/cluster/\_kmeans.py:870: FutureWarning: The default value of `n\_init` wil 1 change from 10 to 'auto' in 1.4. Set the value of `n\_init` explicitly to suppr ess the warning warnings.warn(

# K-means Clustering Results (n\_clusters=5)

