
acsefunctions

Release 0.1

Your Name

Apr 22, 2025

CONTENTS:

Python Module Index	5
Index	7

The *acsefunctions* package provides numerical implementations of mathematical functions, including transcendental functions (e.g., exp, sinh, cosh, tanh) and special functions (e.g., factorial, gamma, Bessel). These functions support both scalar and NumPy array inputs for vectorized computation.

`acsefunctions.transcendental.cosh(x, n_terms=20)`

Compute the hyperbolic cosine function $\cosh(x)$ using a Taylor series approximation.

Parameters

- **x** (*float* or *numpy.ndarray*) – Input value(s) for which to compute $\cosh(x)$.
- **n_terms** (*int*, *optional*) – Number of terms to use in the Taylor series (default is 20).

Returns

Computed $\cosh(x)$ for the input(s).

Return type

float or *numpy.ndarray*

Examples

```
>>> cosh(0)
1.0
>>> cosh(1)
1.5430806348152437
>>> cosh(np.array([0, 1, 2]))
array([1., 1.54308063, 3.76219569])
```

`acsefunctions.transcendental.exp(x, n_terms=20)`

Compute the exponential function e^x using a Taylor series approximation.

Parameters

- **x** (*float* or *numpy.ndarray*) – Input value(s) for which to compute e^x .
- **n_terms** (*int*, *optional*) – Number of terms to use in the Taylor series (default is 20).

Returns

Computed e^x for the input(s).

Return type

float or *numpy.ndarray*

Examples

```
>>> exp(0)
1.0
>>> exp(1)
2.718281828459045
>>> exp(np.array([0, 1, 2]))
array([1., 2.71828183, 7.3890561])
```

`acsefunctions.transcendental.sinh(x, n_terms=20)`

Compute the hyperbolic sine function $\sinh(x)$ using a Taylor series approximation.

Parameters

- **x** (*float* or *numpy.ndarray*) – Input value(s) for which to compute $\sinh(x)$.
- **n_terms** (*int*, *optional*) – Number of terms to use in the Taylor series (default is 20).

Returns

Computed $\sinh(x)$ for the input(s).

Return type

float or `numpy.ndarray`

Examples

```
>>> sinh(0)
0.0
>>> sinh(1)
1.1752011936438014
>>> sinh(np.array([0, 1, 2]))
array([0., 1.17520119, 3.62686041])
```

`acsefunctions.transcendental.tanh(x, n_terms=20)`

Compute the hyperbolic tangent function $\tanh(x)$ as $\sinh(x) / \cosh(x)$.

Parameters

- **x** (*float or numpy.ndarray*) – Input value(s) for which to compute $\tanh(x)$.
- **n_terms** (*int, optional*) – Number of terms to use in the Taylor series for \sinh and \cosh (default is 20).

Returns

Computed $\tanh(x)$ for the input(s).

Return type

float or `numpy.ndarray`

Raises

ZeroDivisionError – If $\cosh(x)$ equals zero, which can occur in rare numerical edge cases.

Examples

```
>>> tanh(0)
0.0
>>> tanh(1)
0.7615941559557649
>>> tanh(np.array([0, 1, 2]))
array([0., 0.76159416, 0.96402758])
```

Special functions: factorial, gamma, and Bessel.

`acsefunctions.special.bessel(alpha, x, n_terms=20)`

Compute the Bessel function $J_{\alpha}(x)$ using its series expansion.

Parameters

- **alpha** (*float*) – Order of the Bessel function.
- **x** (*float or numpy.ndarray*) – Input value(s).
- **n_terms** (*int, optional*) – Number of terms in the series (default is 20).

Returns

Computed $J_{\alpha}(x)$.

Return type

float or `numpy.ndarray`

Examples

```
>>> bessel(0, 0)
1.0
>>> bessel(0, 1) # Approximate value
0.7651976865579666
>>> bessel(0, np.array([0, 1]))
array([1.          , 0.76519769])
```

`acsefunctions.special.factorial(n)`

Compute the factorial $n!$ for non-negative integers.

Parameters

n (*int* or *numpy.ndarray*) – Non-negative integer input(s).

Returns

Computed $n!$.

Return type

int or *numpy.ndarray*

Raises

ValueError – If *n* is negative.

Examples

```
>>> factorial(0)
1
>>> factorial(5)
120
>>> factorial(np.array([0, 1, 2]))
array([1, 1, 2])
```

`acsefunctions.special.gamma(z, T=100, M=1000)`

Compute the gamma function ($\Gamma(z)$) for $z > 0$ using numerical integration.

This function uses the trapezoidal rule to approximate the integral:

$$\Gamma(z) = \int_0^{\infty} t^{z-1} * e^{-t} dt$$

Parameters

- **z** (*float* or *numpy.ndarray*) – Input value(s), must be positive.
- **T** (*float*, *optional*) – Upper integration limit (default is 100).
- **M** (*int*, *optional*) – Number of integration points (default is 1000).

Returns

Computed $\Gamma(z)$.

Return type

float or *numpy.ndarray*

Raises

ValueError – If $z \leq 0$.

Examples

```
>>> gamma(1)
1.0
>>> gamma(0.5) # Equals sqrt(pi)
1.7724538509055159
>>> gamma(np.array([1, 2]))
array([1., 1.]
```


PYTHON MODULE INDEX

a

`acsefunctions.special`, [2](#)

`acsefunctions.transcendental`, [1](#)

INDEX

A

`acsefunctions.special`
 module, 2
`acsefunctions.transcendental`
 module, 1

B

`bessel()` (*in module `acsefunctions.special`*), 2

C

`cosh()` (*in module `acsefunctions.transcendental`*), 1

E

`exp()` (*in module `acsefunctions.transcendental`*), 1

F

`factorial()` (*in module `acsefunctions.special`*), 3

G

`gamma()` (*in module `acsefunctions.special`*), 3

M

module
 `acsefunctions.special`, 2
 `acsefunctions.transcendental`, 1

S

`sinh()` (*in module `acsefunctions.transcendental`*), 1

T

`tanh()` (*in module `acsefunctions.transcendental`*), 2