acsefunctions

Release 0.1

Your Name

Apr 22, 2025

CONTENTS:

The *acsefunctions* package provides numerical implementations of mathematical functions, including transcendental functions (e.g., exp, sinh, cosh, tanh) and special functions (e.g., factorial, gamma, Bessel). These functions support both scalar and NumPy array inputs for vectorized computation.

acsefunctions.transcendental.**cosh**(*x*, *n_terms=20*)

Compute the hyperbolic cosine function cosh(x) using a Taylor series approximation.

Parameters

- **x** (*float or numpy.ndarray*) – Input value(s) for which to compute cosh(x).
- **n_terms** (*int, optional*) – Number of terms to use in the Taylor series (default is 20).

Returns

Computed cosh(x) for the input(s).

Return type

float or numpy.ndarray

Examples

```
>>> cosh(0)
1.0
>>> cosh(1)
1.5430806348152437
>>> cosh(np.array([0, 1, 2]))
array([1., 1.54308063, 3.76219569])
```

acsefunctions.transcendental.**exp**(*x*, *n_terms=20*)

Compute the exponential function e^x using a Taylor series approximation.

Parameters

- **x** (*float or numpy.ndarray*) – Input value(s) for which to compute e^x.
- **n_terms** (*int, optional*) – Number of terms to use in the Taylor series (default is 20).

Returns

Computed e^x for the input(s).

Return type

float or numpy.ndarray

Examples

```
>>> exp(0)
1.0
>>> exp(1)
2.718281828459045
>>> exp(np.array([0, 1, 2]))
array([1., 2.71828183, 7.3890561])
```

acsefunctions.transcendental.**sinh**(*x*, *n_terms=20*)

Compute the hyperbolic sine function sinh(x) using a Taylor series approximation.

Parameters

- **x** (*float or numpy.ndarray*) – Input value(s) for which to compute sinh(x).
- **n_terms** (*int, optional*) – Number of terms to use in the Taylor series (default is 20).

Returns
Computed sinh(x) for the input(s).

Return type
float or numpy.ndarray

Examples

```
>>> sinh(0)
0.0
>>> sinh(1)
1.1752011936438014
>>> sinh(np.array([0, 1, 2]))
array([0., 1.17520119, 3.62686041])
```

acsefunctions.transcendental.**tanh**(*x*, *n_terms=20*)

Compute the hyperbolic tangent function tanh(x) as sinh(x) / cosh(x).

Parameters

- **x** (*float or numpy.ndarray*) – Input value(s) for which to compute tanh(x).
- **n_terms** (*int, optional*) – Number of terms to use in the Taylor series for sinh and cosh (default is 20).

Returns
Computed tanh(x) for the input(s).

Return type
float or numpy.ndarray

Raises
ZeroDivisionError – If cosh(x) equals zero, which can occur in rare numerical edge cases.

Examples

```
>>> tanh(0)
0.0
>>> tanh(1)
0.7615941559557649
>>> tanh(np.array([0, 1, 2]))
array([0., 0.76159416, 0.96402758])
```

Special functions: factorial, gamma, and Bessel.

acsefunctions.special.**bessel**(*alpha*, *x*, *n_terms=20*)

Compute the Bessel function J_alpha(x) using its series expansion.

Parameters

- **alpha** (*float*) – Order of the Bessel function.
- **x** (*float or numpy.ndarray*) – Input value(s).
- **n_terms** (*int, optional*) – Number of terms in the series (default is 20).

Returns
Computed J_alpha(x).

Return type
float or numpy.ndarray

Examples

```
>>> bessel(0, 0)
1.0
>>> bessel(0, 1)  # Approximate value
0.7651976865579666
>>> bessel(0, np.array([0, 1]))
array([1.        , 0.76519769])
```

acsefunctions.special.**factorial**(*n*)

Compute the factorial n! for non-negative integers.

Parameters
n (*int or numpy.ndarray*) – Non-negative integer input(s).

Returns
Computed n!.

Return type
int or numpy.ndarray

Raises
ValueError – If n is negative.

Examples

```
>>> factorial(0)
1
>>> factorial(5)
120
>>> factorial(np.array([0, 1, 2]))
array([1, 1, 2])
```

acsefunctions.special.**gamma**(*z*, *T=100*, *M=1000*)

Compute the gamma function (Gamma(z)) for z > 0 using numerical integration.

Uses trapezoidal rule on (Gamma(z) = int_0^infty t^{z-1} e^{-t} , dt).

Parameters

- **z** (*float or numpy.ndarray*) – Input value(s), must be positive.
- **T** (*float, optional*) – Upper integration limit (default is 100).
- **N** (*int, optional*) – Number of integration points (default is 1000).

Returns
Computed gamma(z).

Return type
float or numpy.ndarray

Raises
ValueError – If z <= 0.

Examples

```
>>> gamma(1)
1.0
>>> gamma(0.5)  # Equals sqrt(pi)
1.7724538509055159
>>> gamma(np.array([1, 2]))
array([1., 1.])
```

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