Parser Operators with Haskell

- Haskell lab assignment 3 –
 D7012E Declarative languages –
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1 Introduction

This assignment was originally written by Lennart Andersson while he was working at Luleå University of Technology. When he moved to Lund University around the year 2000, he introduced the assignment there. As a result, the assignment was (and still is) used both in Luleå and in Lund¹

There have been minor changes in the actual lab instruction over the years but the assignment has essentially remained the same. It is described in two documents that I have appended.

- 1. The actual instruction. This is the most recent version I could find (from Spring 2016) and was on the course webpage at Lund University (currently maintained by Jacek Malec). It is the instruction used previous years in D7012E and I have just extracted the text and edited it a bit.
- 2. The 16 page text Parsing with Haskell by Lennart Andersson.

Moreover, you are given a set of Haskell source files to start with and add your code to. These are briefly described in the instruction. A zip-file containing all files can be downloaded from the course homepage from which this document could be downloaded.

¹As a side-note, I know that Lennart's assignment is also used at Dartmouth College because of my stay there in 2007.

2 Assignment

- First complete the original assignment as described in the appended documents.
- When you are done with that (and it all works) you should add a **repeat** statement so that this program reads an integer n and computes the sum $1 + 2 + \cdots + n$ (assuming $n \ge 1$).

```
read n;
s := 0;
repeat
begin
s := s + n;
n := n - 1;
end
until (0-n)+1;
write s;
```

A repeat statement works mush like a while statement. However, the statement within is always executed at least once and the test is at the end (after the statement) rather than at the beginning (before the statement). A crucial difference is also that a repeat goes on *until*, and not *while*, the condition is true.

Adding this new statement means extending the type **Statement** with a new constructor and adding

```
'repeat' statement 'until' expr ';'
```

to the grammar for statements. Some functions also have to be rewritten so they can handle this new statement.

Once you have completed the original assignment, this addition is straight-forward and takes very little time to do.

Lab assignment H3 in D7012E

In this assignment you will create a parser and an interpreter for a small imperative language. The main goal is to get acquainted with a monadic way of solving a classical problem in computer science. The assignment is to be solved individually.

Introduction

The following program is written in the programming language to be parsed and interpreted in this assignment.

```
read k;
read n;
m := 1;
while n-m do
  begin
    if m - m/k*k then
       skip;
  else
       write m;
  m := m + 1;
end
```

The language has just one data type, integer, and variables are not declared. In the while and if statements a positive expression value is interpreted as true while 0 and negative values mean false.

The program above reads two integers, k and n, and writes all integers between 1 and n that are multiples of k.

The grammar for the language is given by

An explanation of this grammar and a parser for an expression, expr, can be found in the document *Parsing with Haskell* by Lennart Andersson. The intended semantics for the language should be obvious from the keywords for anybody familiar with the Java language.

Program structure

You are given the stub of a solution:

```
CoreParser.hs
```

defines the Parser type and implements the three elementary parsers, char, return and fail, and the basic parser operators #, !, ?, #>, and >->, described in Lennart Andersson's

description.

The class Parse with signatures for parse, tostring, and fromstring with an implementation for the last one is introduced.

The representation of the Parser type is visible outside the module, but this visibilty should not be exploited.

Parser.hs

contains a number of derived parsers and parser operators.

Expr.hs

contains a data type for representing an arithmetic expression, an expression parser, an expression evaluator, and a function for converting the representation to a string.

Dictionary.hs

contains a data type for representing a dictionary.

Statement.hs

contains a data type for representing a statement, a statement parser, a function to interpret a list of statements, and a function for converting the representation to a string.

Program.hs

contains a data type for representing a program, a program parser, a program interpreter, and a function for converting the representation to a string.

Test*.hs

contain test data.

In a test using the program in the introduction with the following definitions

```
src = "read k; read n; m:=1; ... "
p = Program.fromString src
```

the expression Program.exec p [3,16] should return [3,6,9,12,15].

Assignment and hints

1. In Parser.hs implement the following functions. All the implementations should use other parsers and parser operators. No implementation may rely on the fact that the parsers return values of type Maybe(a, String). This means e.g. that the words Just and Nothing may not appear in the code.

```
letter :: Parser Char.
```

letter is a parser for a letter as defined by the Prelude function isAlpha.

spaces :: Parser String.

spaces accepts any number of whitespace characters as defined by the Prelude function isSpace.

```
chars :: Int -> Parser String.
```

The parser chars n accepts n characters.

```
require :: String -> Parser String.
```

The parser require waccepts the same string input as accept wbut reports the missing string using err in case of failure.

```
-# :: Parser a -> Parser b -> Parser b.
```

The parser m -# n accepts the same input as m # n, but returns just the result from the n parser. The function should be declared as a left associative infix operator with precedence 7. Example:

```
(accept "read" -# word) "read count;" -> Just ("count", ";")
```

```
#- :: Parser a -> Parser b -> Parser a.
```

The parser m #- n accepts the same input as m # n, but returns the result from the m parser.

- 2. Implement the function value in Expr. The expression value e dictionary should return the value of e if all the variables occur in dictionary and there is no division by zero. Otherwise an error should be reported using error.
- 3. Implement the type and the functions in the Statement module. Some hints:
 - a. The data type T should have seven constructors, one for each kind of statement.
 - b. Define a parsing function for each kind of statement. If the parser has accepted the first reserved word in a statement, you should use require rather than accept to parse other reserved words or symbols in order to get better error messages in case of failure. An example:

- c. Use these functions to define parse.
- d. The function exec :: [T] -> Dictionary.T String Integer -> [Integer] -> [Integer] takes a list of statements to be executed, a dictionary containing variable/value pairs, and a list of integers containing numbers that may be read by read statements and the returned list contains the numbers produced by write statements. The function exec is defined using pattern matching on the first argument. If it is empty an empty integer list is returned. The other patterns discriminate over the first statement in the list. As an example the execution of a conditional statement may be implemented by

```
exec (If cond thenStmts elseStmts: stmts) dict input =
   if (Expr.value cond dict)>0
   then exec (thenStmts: stmts) dict input
   else exec (elseStmts: stmts) dict input
```

For each kind of statement there will be a recursive invocation of exec. A write statement will add a value to the returned list, while an assignment will make a recursive call with a new dictionary.

- 4. In the Program module you should represent the program as a Statement list. Use the parse function from the Statement module to define the parse function in this module. Use the exect function in the Statement module to execute a program.
- 5. Implement tostring :: T -> String in Statement and Program. A newline character should be inserted after each statement and some keywords, but no indentation of lines is required. However, it will be appreciated. No spurious empty lines should appear in the output.

Grading etc

The grading will take place in the lab and be carried out pretty much like the grading of assignment 1 and 2. You will also be asked to hand in your code.

Parsing with Haskell

Lennart Andersson Computer Science Lund University

October 28, 2001

Introduction

This will be an extended example that will provide the basis for a small program project resulting in an interpreter for an imperative language. The example will show how abstraction and higher order functions can be used to make the parsing program look like the grammar for the imperative language.

The example will decompose a nontrivial problem into a large number of very small problems. Most of them can be solved with almost trivial functions. Actually, the longest function in the example has just 7 lines of code. To do this decomposition requires a fair amount of experience; it should be a lot easier to understand the functions and the program. We believe it is a good programming strategy to decompose a nontrivial problem into problems that are small and almost trivial.

The programming language will have statements and integer expressions as its main building stones. Expressions will be represented in the interpreter with the following data type.

```
data Expr = Num Int | Var String | Add Expr Expr | Sub Expr Expr | Mul Expr Expr | Div Expr Expr |

As an example the expression 2*(x+3) will be represented by Mul (Num 2) (Add (Var "x") (Num 3))

Statements will be represented using data Statement = Assignment String Expr | ....

so that the assignment statement count := count + 1 is represented by
```

Assignment "count" (Add (Var "count") (Num 1))

We are going to define parsing functions that takes such strings as arguments and returns the corresponding representation. We are going to introduce a few very simple parsers and some operators for combining parsers that may be used to construct complex parsers.

A parsing function will usually not parse all of the input string, but just a prefix. The remainder of the string will be the input to another parser. Suppose that we have a parser which accepts an identifier consisting of letters, another one accepting the string ":=" and a third one accepting an expression and returning a pair with some representation of the accepted string and a remainder string:

```
ident "count:=count+1;" -> ("count", ":=count+1;")
becomes ":=count+1:" -> (":=", "count+1;")
expr "count+1;" -> (Add (Var "count") (Num 1), ";")
```

The arrow -> denotes evaluation. We can combine these parsers to a parser for an assignment statement:

```
assignment str = (Assignment id e, rest3) where
  (id, rest1) = ident str
  (_, rest2) = becomes rest1
  (e, rest3) = expr rest2
```

The type of such parsers would be

```
type Parser a = String -> (a, String)
```

A Parser a takes a string argument and returns a pair. We will call the first component the result of the parser and second the remainder string. Thus we have

```
ident :: Parser String
becomes :: Parser String
expr :: Parser Expr
assignment :: Parser Statement
```

A parser should either accept or reject its input. The Prelude defines a data type for handling two such alternatives.

```
data Maybe a = Nothing | Just a
```

This type can be used in any context where a computation either fails or returns some valid result. We redefine our parser type

```
type Parser a = String -> Maybe (a,String)
and the parsers so that e.g.
ident "count:=count+1;" -> Just("count",":=count+1;")
ident "123:=count+1;" -> Nothing
```

The type definitions just give synonyms to type expressions; there are no constructors as in the case of data definitions.

```
Exercise 1 Define semicolon :: Parser Char so that semicolon "; skip" -> Just(';', " skip") semicolon "skip" -> Nothing
```

Exercise 2 Define becomes.

Exercise 3 Define a parser char :: Parser Char which accepts one character. The solution appears on the next page, don't look!

Basic parsers

The basic parsers are almost trivial. The first one will accept one character and is defined by

```
char :: Parser Char
char (c:cs) = Just(c,cs)
char [] = Nothing
```

Parser Char is a synonym for String -> Maybe(Char, String). The function fails if the input string is empty. Some examples

```
char "" -> Nothing
char "1" -> Just('1',"")
char "abc" -> Just('a',"bc")
```

The next parser is even simpler.

```
fail :: Parser a
fail cs = Nothing
```

This parser will never accept any input, so it seems to be useless. Actually we will later define a similar parser which will print an error message and abort the computation. The name fail is defined in the Prelude so we have hide it when importing the Prelude. If you test fail by applying it to a string the system refuses to print Nothing:

```
> fail "abc"
ERROR: Cannot find "show" function for:
*** expression : fail "abc"
*** of type : Maybe (a,[Char])
```

In order to print (show) the result the Haskell system must know how to print values of type a which occurs in Maybe (a,[Char]) even if no such value is present in Nothing. Supplying a printable type fixes the problem:

```
> fail "abc" :: Maybe(Int,String)
Nothing
```

The same error is reported if you enter an empty list to the system:

```
> []
ERROR: Cannot find "show" function for:
*** expression : []
*** of type : [a]
```

While fail is extreme in one way the next parser, return, is extreme in opposite sense; it will always succeed without inspecting the input string. It returns its first argument that may be of any type.

```
return :: a -> Parser a
return a cs = Just(a,cs)
```

Examples

```
return 0 "abc" -> Just(0,"abc")
return (Add (Var "count") (Num 1)) ";" -> Just(Add (Var "count") (Num 1)), ";")
```

The return function is defined in the Prelude for a similar but different purpose.

Parser operators

The first parser operator will be an infix operator denoted by ?. If m :: Parser a is a parser and p :: a -> Bool is a predicate then (m ? p) is a parser which applies m to the input string and tests if the result satisfies p.

```
infix 7 ?
(?) :: Parser a -> (a -> Bool) -> Parser a
(m ? p) cs =
  case m cs of
   Nothing -> Nothing
  Just(a,cs) -> if p a then Just(a,cs) else Nothing
```

The infix directive declares? to be an infix operator with precedence 7. The precedence levels for the parser operators will be chosen so that most parentheses may be omitted.

The Prelude contains a predicate for deciding if a character is a digit, isDigit. We can define a parser accepting one digit

```
digit :: Parser Char
digit cs = (char ? isDigit) cs
```

Examples

```
digit "123" -> Just('1',"23")
digit "abc" -> Nothing
```

If the right member of a function definition applies an expression not containing the last argument to the last argument than this argument may be removed from both sides of the definition.

```
digit = char ? isDigit
```

The second parser operator corresponds to alternatives in the grammar. We will use an infix operator, !, for this parser combinator. If m and n are parsers of the same type then (m ! n) will be a parser which first applies m to the input string which will be the result unless m fails. In that case n is applied to the input.

The definition is simple:

```
infixl 3 !
(!) :: Parser a -> Parser a -> Parser a
(m ! n) cs =
  case m cs of
   Nothing -> n cs
  mcs -> mcs
```

The infixl directive tells the Haskell system! will be an infix operator which associates to the left. Left association means that m! n! k is evaluated as (m!n)! k. Some examples:

```
(char ! digit) "abc" -> Just('a', "bc")
(digit ! char) "abc" -> Just('a', "bc")
(digit ! return '0') "abc" -> Just('0', "abc")
(digit ! char) "" -> Nothing
```

We have assigned precedences to the operators so that m ? p ! n will mean (m ? p) ! n and not m ? (p ! n) which would give a type mismatch error.

Exercise 4 The Prelude defines the predicates isAlpha, isSpace:: Char -> Bool which decide if a character is a letter or space character (blank, tab, newline). Define parsers accepting a letter and a space character, letter, space :: Parser Char.

Exercise 5 Define a parser alphanum :: Parser Char which accepts a letter or a digit.

A parser accepting a given character is easily defined.

```
lit :: Char -> Parser Char
lit c = char ? (==c)
```

The operator section (==c) is equivalent to the predicate ($x \rightarrow x==c$). The predicate decides if the given character is the the same as the one accepted by char.

```
lit 'a' "abc" -> Just ('a', "bc")
lit 'b' "abc" -> Nothing
```

Exercise 6 Redefine semicolon :: Parser Char using lit. The definition should not include the string argument.

The next parser combinator applies two parsers in sequence where the remainder string from the first one is fed into the other. The results of the two parsers are combined into a pair.

```
infix1 6 #
(#) :: Parser a -> Parser b -> Parser (a, b)
(m # n) cs =
    case m cs of
     Nothing -> Nothing
    Just(p, cs') ->
          case n cs' of
          Nothing -> Nothing
     Just(q, cs'') -> Just((p,q), cs'')
```

A parser accepting two characters follows.

```
(char # char) ":=1" -> Just((':', '='), "1")
```

We may name it:

```
twochars :: Parser (Char, Char)
twochars = char # char
```

Exercise 7 Redefine becomes :: Parser (Char, Char) using twochars and the ? operator. The definition should not include the string argument.

Sometimes we would like to transform the result of a parser. This may be done with

```
infixl 5 >->
(>->) :: Parser a -> (a -> b) -> Parser b
(m >-> k) cs =
  case m cs of
    Just(a,cs') -> Just(k a, cs')
    Nothing -> Nothing
```

The right operand of >-> named k is the function defining the transformation. The result of the operation is a new parser. We may use it to define a parser which accepts a digit and returns an Int using digitToInt from the Prelude.

```
digitVal :: Parser Int
digitVal = digit >-> digitToInt
```

Example

```
digitVal "123" -> Just(1, "23")
digitVal "abc" -> Nothing
```

Exercise 8 Define a parser that accepts a letter and returns an upper case letter. The Prelude function toUpper :: Char -> Char transforms any letter to its uppercase form.

Exercise 9 Define sndchar :: Parser Char which accepts two characters and returns the second one. Use twochars and the transformation operator. Examples

```
sndchar "abc" -> Just('b', "c")
sndchar "a" -> Nothing
```

Exercise 10 Redefine twochars :: Parser String so that it returns a String with two characters instead of a pair of characters.

Exercise 11 Define an operator (-#) :: Parser a -> Parser b -> Parser b which applies two parsers in sequence as # but throws away the result from the first one. Use # and >-> in the definition. Examples

```
(char -# char) "abc" -> Just('b', "c")
(char -# char) "a" -> Nothing
```

Exercise 12 Define a similar operator (#-) :: Parser a -> Parser b -> Parser a which applies two parsers in sequence as # but throws away the result from the second one.

It is useful to be able to apply a parser iteratively to the input string. First we define $iterate\ m$ i which will apply the parser m to the input string i times with the result in a list with i elements. Example

```
iterate digitVal 3 "123456" \rightarrow Just([1, 2, 3], "456") iterate letter 3 "a123" \rightarrow Nothing
```

The definition uses primitive recursion over natural numbers.

```
iterate :: Parser a -> Int -> Parser [a]
iterate m 0 = return []
iterate m i = m # iterate m (i-1) >-> cons
```

where

```
cons :: (a, [a]) -> [a]
cons (hd, tl) = hd:tl
```

The name iterate is defined in the Prelude so it is necessary to hide it or to rename the new function.

It is even more useful to be able to iterate a parser as long as it succeeds. Assuming that iter does this we could use it like follows

```
iter digitVal "123abc" -> Just([1, 2, 3], "abc")
iter digit "123abc" -> Just(['1', '2', '3'], "abc") -> Just("123", "abc")
iter digit "abc" -> Just([], "abc") -> Just("", "abc")
```

The definition will again be recursive but termination will be signaled by the failure of the recursive branch. In that case we just return the empty list.

```
iter :: Parser a -> Parser [a]
iter m = m # iter m >-> cons ! return []
```

Inserting parentheses to indicate precedences of the operators we get

```
iter m = ((m # (iter m)) >-> cons) ! (return [])
```

Exercise 13 Why is it an error to take the alternatives in the opposite order?

```
iter m = return [] ! m # iter m >-> cons
```

We can use iter to define a parser for a string of letters. Our first attempt is

```
letters :: Parser String
letters = iter letter
```

This is OK provided we are willing to accept an empty string. If this is not the case we define it as

```
letters = letter # iter letter >-> cons
```

We now consider the problem of whitespace, i.e. blanks and newline characters, in the input. We define token which for a given parser will return a parser which will remove any whitespace after the accepted string.

```
token :: Parser a -> Parser a
token m = m #- iter space
```

We now define two very useful parsers.

```
word :: Parser String
word = token letters

accept :: String -> Parser String
accept w = token (iterate char (size w) ? (==w))

Examples

word "count := count+1" -> Just("count", ":= count+1")
word ":= count+1" -> Nothing
accept "while" "while x do x:=x-1" -> Just("while", "x do x:=x-1")
accept "if" "while x do x:=x-1" -> Nothing
```

Sometimes we need to make the result from one parser available to another. The following operator provides the means.

```
infix 4 #>
(#>) :: Parser a -> (a -> Parser b) -> Parser b
(m #> k) cs =
    case m cs of
    Nothing -> Nothing
    Just(a,cs') -> k a cs'
```

After applying the parser m to the input string both the result and the remainder input string are given to the second operand, $k :: a \rightarrow Parser b$.

This operator is very useful for parsing numbers and arithmetic expressions with operators that associate to the left like – and /. These parsers will be nontrivial so we start with a simpler and not so useful parser. It will accept two characters provided they are equal and returning just one character.

```
double :: Parser Char
double = char #> lit
```

Remember that lit:: Char -> Parser Char needs on argument to become a parser which will accept this character. The character is provided as the result of the first parser. Examples

```
double "aab" -> Just('a', "b")
double "abb" -> Nothing
```

In order to construct a number parser we define three functions, bldNumber, number' and number.

```
bldNumber :: Int -> Int -> Int
bldNumber n d = 10*n+d
```

bldNumber n d just "appends" the digit d after n.

```
bldNumber 123 4 -> 1234

number' :: Int -> Parser Int
number' n =
   digitVal >-> bldNumber n #> number'
   ! return n

number :: Parser Int
number = token (digitVal #> number')
```

The argument in number' will serve as an accumulator which will be returned when no more input can be consumed. Otherwise the next digit is "appended" to the accumulator and recursively given to number'. The number parser accepts the first digit with digitVal and sends it to number' and finally removes any trailing whitespace. Examples

```
number' 1 "abc" -> Just(1, "abc")
number' 1 "23 abc" -> Just(123, " abc")
number "123 abc" -> Just(123, "abc")
```

Exercise 14 Define the operator # using #>. The solution should not contain Just or Nothing.

An expression parser

We are going to construct a parser for arithmetic expressions with integer numbers, variables, additions, subtractions, multiplications, divisions and parentheses with the usual laws for operator precedence. A grammar is given by

```
expr ::= term expr'
expr' ::= addOp term expr' | empty
term ::= factor term'
term' ::= mulOp factor term' | empty
factor::= num | var | "(" expr ")"
addOp ::= "+" | "-"
mulOp ::= "*" | "/"
```

The word empty denotes the empty string. In the definition of factor, num is a string of digits and var a string of letters. There are several grammars describing ordinary expressions. The current one has been chosen since it will be possible to define a parser which is very similar. The result of the parser will be a value of the following type.

```
data Expr =
  Num Int | Var String | Add Expr Expr |
  Sub Expr Expr | Mul Expr Expr | Div Expr Expr
```

We are going to build the parser from the bottom starting with parsers for mulOp and addOp. mulOp will accept either * or / and will return Mul or Div. These parsers are trivial to define without our parser operators:

```
mulOp ('*':rest) = Just(Mul, rest)
mulOp ('/':rest) = Just(Div, rest)
mulOp _ = Nothing
```

We prefer, however, to make the definition on the abstract level. The reason is that if we do not exploit the fact that the representation by the Maybe type is visible outside the Parser module then we may change it without changing any module using the Parser module. Such a change is suggested at the end of this paper.

```
mulOp, addOp :: Parser ((Expr, Expr) -> Expr)
mulOp = lit '*' >-> (\_ -> Mul)
    ! lit '/' >-> (\_ -> Div)
```

Examples

```
mulOp "*2*3" -> Just(Mul, "2*3")
mulOp "/2*3" -> Just(Div, "2*2")
mulop "+2*3" -> Nothing
```

The addOp parser is analogous.

The num and var parsers are simple; we just give the result from word and number to the relevant Expr constructor.

```
var :: Parser Expr
var = word >-> Var
num :: Parser Expr
num = number >-> Num
```

Examples

```
var "count + 1" -> Just(Var "count", "+ 1")
num "123*456" -> Just(Num 123, "*456")
```

The expr, term and factor parsers are going to be mutually recursive. It may be simpler to define and test such functions if one temporarily eliminates the recursion. We do it by simplifying the factor production.

```
factor :: num | var | "(" var ")"
```

We already have parsers for the two first alternatives. A parser for the last alternative is given by

```
lit '(' -# var #- lit ')'
```

We conclude with

```
factor :: Parser Expr
factor = num ! var ! lit '(' -# var #- lit ')'
```

A straightforward implementation of the rule for terms would parse e.g. the expression 6/3/2 as 6/(3/2) contrary to the ordinary rules. In order to get the interpretation (6/3)/2 we may use the same technique as in the definition of number' with a parameter to accumulate the result.

```
term' :: Expr -> Parser Expr
term' e =
  mulOp # factor >-> bldOp e #> term' !
  return e
```

The parameter e will be the result of the previous parser. If the input doesn't start with a mulOp we just return e. Otherwise mulOp # factor results in a pair which is given to bldOp e. The transformed result is given recursively to term'. The transformation bldOp is defined by

```
bldOp :: Expr -> (Expr -> Expr -> Expr, Expr) -> Expr
bldOp e (oper,e') = oper e e'
```

Example

```
bldOp (Num 1) (Mul, Num 2) -> Mul Num 1 Num 2
```

The result of all this is given recursively to term' which will find a new mulOp or terminate.

```
term' (Num 1) "*2" ->
  (mulOp # factor >-> bldOp (Num 1) #> term') "*2" ->
  (term' (bldOp (Num 1) (Mul, Num 2))) "" ->
  (term' (Mul (Num 1) (Num 2))) "" ->
  Just(Mul (Num 1) (Num 2), "")
```

The definition of term is simple; parse a factor and send the result to term'.

```
term :: Parser Expr
term = factor #> term'
```

Examples

```
term' (Num 1) "" -> Just(Num 1, "")
term "1*2" -> Just(Mul (Num 1) (Num 2), "")
term "6/3/2" -> Just(Div (Div (Num 6) (Num 3)) (Num 2), "")
```

The definitions of expr' and expr are analogous.

```
expr' :: Expr -> Parser Expr
expr' e =
    addOp # term >-> bldOp e #> expr' !
    return e
expr :: Parser Expr
expr = term #> expr'
```

We may now compose the factor, term and expr parsers resetting the first one to make them mutually recursive.

```
factor =
    num !
    var !
    lit '(' -# expr #- lit ')' !
    err "illegal factor"

term' e =
    mulOp # factor >-> bldOp e #> term' !
    return e

term = factor #> term'
expr' e =
    addOp # term >-> bldOp e #> expr' !
    return e

expr = term #> expr'
```

We have added another alternative parser in factor in order to get an informative message for illegal input. Without it, any invalid string argument will just return Nothing.

The err parser is defined by

```
err :: String -> Parser a
err message cs = error (message ++ " near " ++ cs ++ "\n")
```

It will print the message and the offending input and abort the computation.

Exercise 15 Define a parser require :: String -> Parser a that behaves as accept but emits an error message instead of returning Nothing.

Program structure

The program parts that we have developed so far should be divided into two parser modules and one expression module. The first parser module should contain the parser type, the basic parsers and parser operators, while the second one contains derived parsers and parser operators. The representation of parsers as values of type String -> Maybe(a, String) will not be exploited outside the first parser module.

Since we are going to define parsers for more than one data type it is useful to have a type class declaring the names parse and toString and defining fromString. We can then use these names for all the data types and the relevant one will be chosen using the context where the name is used. We use the name Parse for the type class.

It is inconvenient to use qualified import for the parser module, so we refrain from giving the parser type the conventional name T.

```
module CoreParser(Parser, char, return, fail, (#), (!), (?), (#>), (>->),
                  Parse, parse, toString, fromString) where
import Prelude hiding (return, fail)
infixl 3 !
infixl 7 ?
infixl 6 #
infixl 5 >->
infixl 4 #>
class Parse a where
    parse :: Parser a
    fromString :: String -> a
    fromString cs =
        case parse cs of
               Just(s, []) -> s
               Just(s, cs) -> error ("garbage '"++cs++"'")
               Nothing -> error "Nothing"
    toString :: a -> String
type Parser a = String -> Maybe (a, String)
char :: Parser Char
char [] = Nothing
char (c:cs) = Just (c, cs)
return :: a -> Parser a
return a cs = Just (a, cs)
fail :: Parser a
fail cs = Nothing
```

```
(!) :: Parser a -> Parser a -> Parser a
(m ! n) cs = case m cs of
              Nothing -> n cs
             mcs -> mcs
(?) :: Parser a -> (a -> Bool) -> Parser a
(m ? p) cs =
    case m cs of
    Nothing -> Nothing
    Just(r, s) -> if p r then Just(r, s) else Nothing
(#) :: Parser a -> Parser b -> Parser (a, b)
(m # n) cs =
    case m cs of
    Nothing -> Nothing
    Just(a, cs') ->
        case n cs' of
        Nothing -> Nothing
        Just(b, cs'') -> Just((a, b), cs'')
(>->) :: Parser a -> (a -> b) -> Parser b
(m \rightarrow -> b) cs =
    case m cs of
    Just(a, cs') -> Just(b a, cs')
    Nothing -> Nothing
(#>) :: Parser a -> (a -> Parser b) -> Parser b
(p \#> k) cs =
    case p cs of
    Nothing -> Nothing
    Just(a, cs') -> k a cs'
The derived parsers appear in Parser.hs.
module Parser(module CoreParser, digit, digitVal, chars, letter, err,
             lit, number, iter, accept, require, token,
             spaces, word, (-#), (#-)) where
import Prelude hiding (return, fail)
import CoreParser
infixl 7 -#, #-
type T a = Parser a
err :: String -> Parser a
err message cs = error (message++" near "++cs++"\n")
iter :: Parser a -> Parser [a]
iter m = m # iter m >-> cons ! return []
cons(a, b) = a:b
. . .
```

The expression module will have a few other functions not mentioned previously. We rename the main type to T. The value function should evaluate an expression. It will need a "dictionary" to find the values of the variables.

The expression module will make heavy use of the parser functions so it is convenient to import the parser module without qualification.

Parsing with ambiguous grammars

This description is mainly inspired by an article by Phil Wadler, [4]. He uses an elegant trick to code the failure and the success of a parser and finding all possible parses of a string. The Maybe data type may be viewed as a special case of the list type, but with the list either being empty, Nothing, or having one element, Just a. Failure will be represented by the empty list while a nonempty list contains all possible successes. He defines the parser type by

```
type Parser a = String -> [(a,String)]
```

As an example the number parser will find

```
number "123abc" -> [(123, "abc"), (12, "3abc"), (1, "23abc")]
number "abc" -> []
```

A few modifications are needed in the Parser module. The basic parser must be changed to return lists instead of Maybe values.

```
char [] = []
char (c:cs) = [(c,cs)]
return a cs = [(a,cs)]
fail cs = []
```

The operators must also be adapted. Using list comprehension they become "one-liners"

```
(m ? p) cs = [(a,cs') | (a,cs') <- m cs, p a]
(m ! n) cs = (m cs) ++ (n cs)
```

```
(m # n) cs = [((a,b),cs'') | (a,cs') <- m cs, (b,cs'') <- n cs']

(m >-> b) cs = [(b a, cs') | (a,cs') <- m cs]

(p #> k) cs = [(b,cs'') | (a,cs') <- p cs, (b,cs'') <- k a cs']
```

The err and hence the require parsers can no longer be used in Expr and Program to give adequate error messages.

Parsec

There is a "industrial stength" parser library called *Parsec*, [2]. It uses basically the same technique as above, but is larger and uses do notation extensively. An expression parser using this library follows.

```
import Parsec
import ParsecExpr
data Expr = Num Int | Var String | Add Expr Expr
       | Sub Expr Expr | Mul Expr Expr | Div Expr Expr
         deriving Show
        :: Parser Expr
expr
        = buildExpressionParser table factor
expr
        <?> "expression"
        = [[op "*" Mul AssocLeft, op "/" Div AssocLeft],
table
           [op "+" Add AssocLeft, op "-" Sub AssocLeft]]
        where
          op s f assoc
             = Infix (do{ string s; return f}) assoc
factor = do{ char '('
            ; x <- expr
            ; char ')'
            ; return x}
       <|> number
       <|> variable
       <?> "simple expression"
number :: Parser Expr
number = do{ ds<- many1 digit</pre>
            ; return (Num (read ds))}
       <?> "number"
variable :: Parser Expr
variable = do{ ds<- many1 letter</pre>
            ; return (Var ds)}
       <?> "variable"
```

The library has special support for parsing expressions. Operator precedences and associativities are given using a table. do notation is used to express sequential composition of parsers. Alternatives are separated by <|> and <?> is used as our err parser.

References

- [1] Hutton, G. and Meier, E., *Monadic Parser Combinators*, Technical report NOTTCS-TR-96-4, Department of Computer Science, University of Nottingham, 1996.
- [2] Leijen, D., *Parsec, a fast combinator parser*, Oct 2001, http://www.cs.ruu.nl/~daan/parsec.html.
- [3] Wadler P., How to replace failure by a list of successes, 2nd International Conference on Functional Programming Languages and Computer Architecture, Springer-Verlag, Nancy France, September 1985. http://cm.bell-labs.com/cm/cs/who/wadler/.
- [4] Wadler, P., *Monads for functional programming*, Marktoberdorf Summer School on Program Design Calculi, Springer Verlag, NATO ASI Series F: Computer and systems sciences, Volume 118, August 1992. http://cm.bell-labs.com/cm/cs/who/wadler/.