

# IMAGE PROCESSING

## Lecture-8

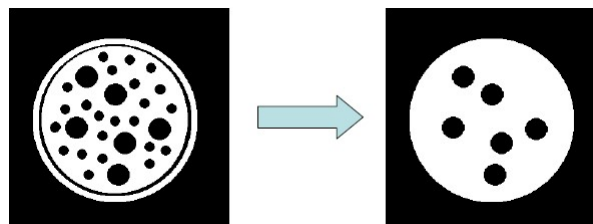
Morphological Image Processing

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### Morphology

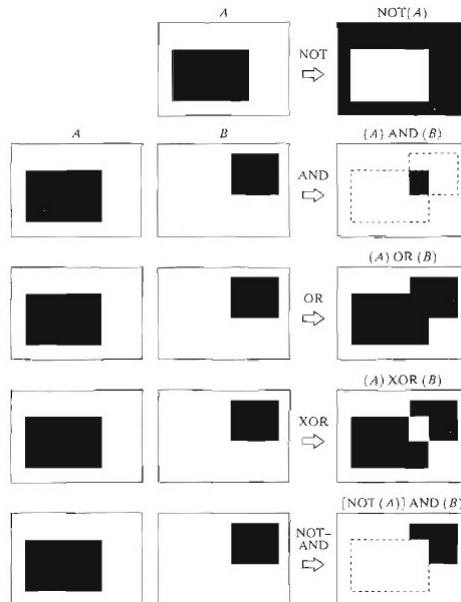
- Morphology: Shape and Structure (TR: biçim bilim)
- Mathematical Morphology based on cluster operations.
- Possible Applications: extract shape borders/skeletons, define shapes, reduce noise, segment images
- Basic Operations: Erosion (TR: aşındırma) and Dilation (TR: yayma)
- Usually binary morphology.



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## Logic Operations in Binary Images



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## Erosion and Dilations



- Erosion: shape boundaries are eroded



- Dilation: shape boundaries are expanded

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## Dilation

- Two inputs:
  - Image
  - Structure element (yapı elemanı)

$$A \oplus B = \left\{ z \mid \left( \hat{B} \right)_z \cap A \neq \emptyset \right\}$$

Dilation operand

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MATLAB: **imdilate**

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## Dilation

- Structure Element defines expansion approach.

1	1	1
1	1	1
1	1	1



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## Dilation



Input image

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



Output Image

	1								
--	---	--	--	--	--	--	--	--	--

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## Dilation



Input image

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



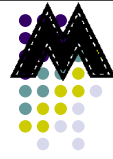
Output Image

	1	0							
--	---	---	--	--	--	--	--	--	--

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## Dilation



Input image

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



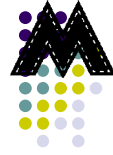
Output Image

	1	0	1						
--	---	---	---	--	--	--	--	--	--

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## Dilation



Input image

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



Output Image

	1	0	1	1					
--	---	---	---	---	--	--	--	--	--

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## Dilation



Input image

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



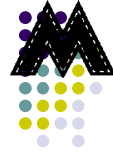
Output Image

	1	0	1	1	1				
--	---	---	---	---	---	--	--	--	--

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## Dilation



Input image

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



Output Image

	1	0	1	1	1	1			
--	---	---	---	---	---	---	--	--	--

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## Dilation



Input image

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



Output Image

	1	0	1	1	1	1	1		
--	---	---	---	---	---	---	---	--	--

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## Dilation



Input image

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



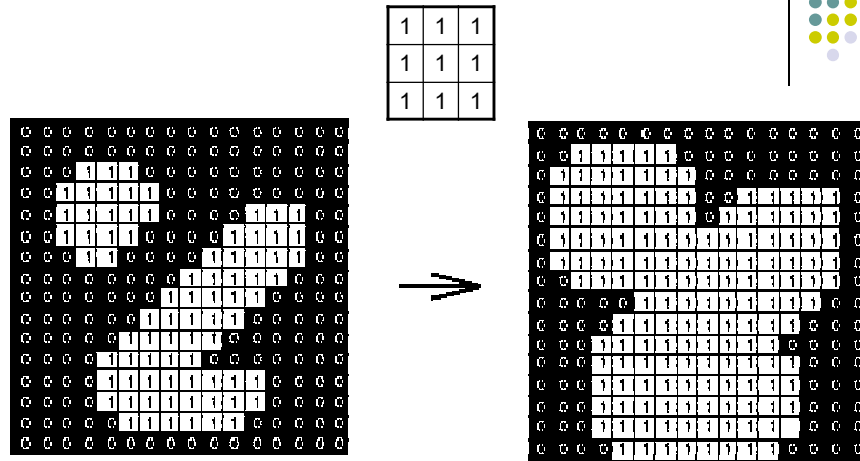
Output Image

	1	0	1	1	1	1	1	1	
--	---	---	---	---	---	---	---	---	--

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## Dilation

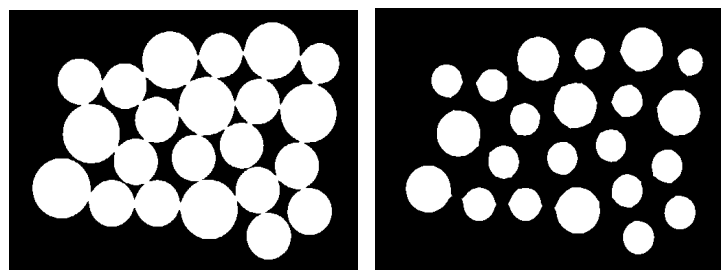


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## Erosion

$$A \ominus B = \{z \mid (B)_z \subseteq A\}$$



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MATLAB: `imerode`

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## Erosion



Input image

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



Output Image

	0								
--	---	--	--	--	--	--	--	--	--

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## Erosion



Input image

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



Output Image

	0	0							
--	---	---	--	--	--	--	--	--	--

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## Erosion



Input image

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



Output Image

	0	0	0						
--	---	---	---	--	--	--	--	--	--

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## Erosion



Input image

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



Output Image

	0	0	0	0					
--	---	---	---	---	--	--	--	--	--

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## Erosion



Input image

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



Output Image

	0	0	0	0	1				
--	---	---	---	---	---	--	--	--	--

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## Erosion



Input image

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---

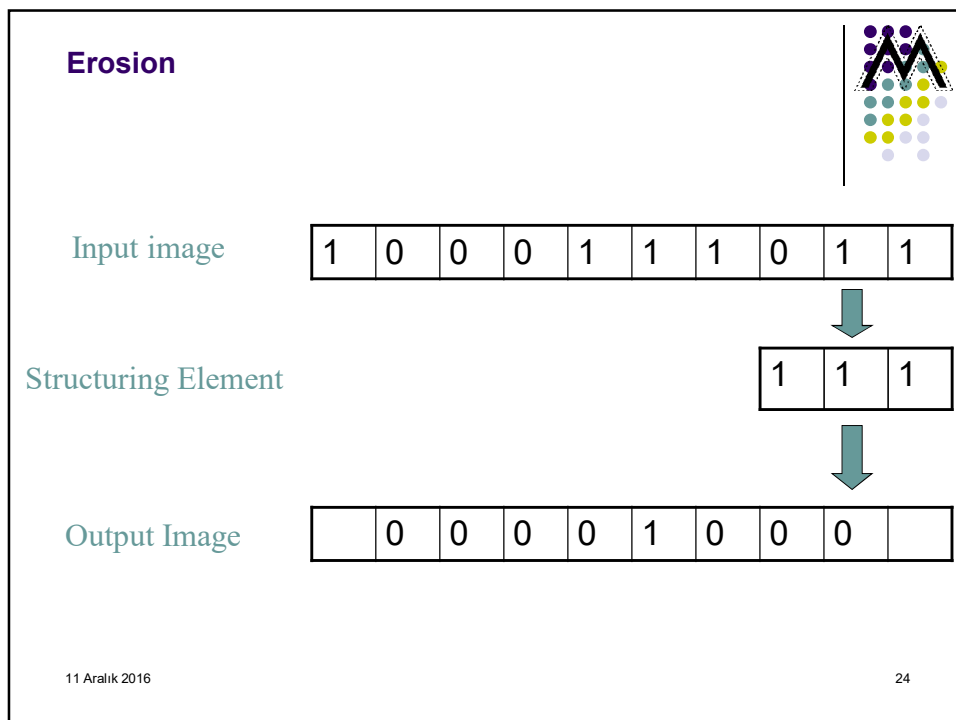
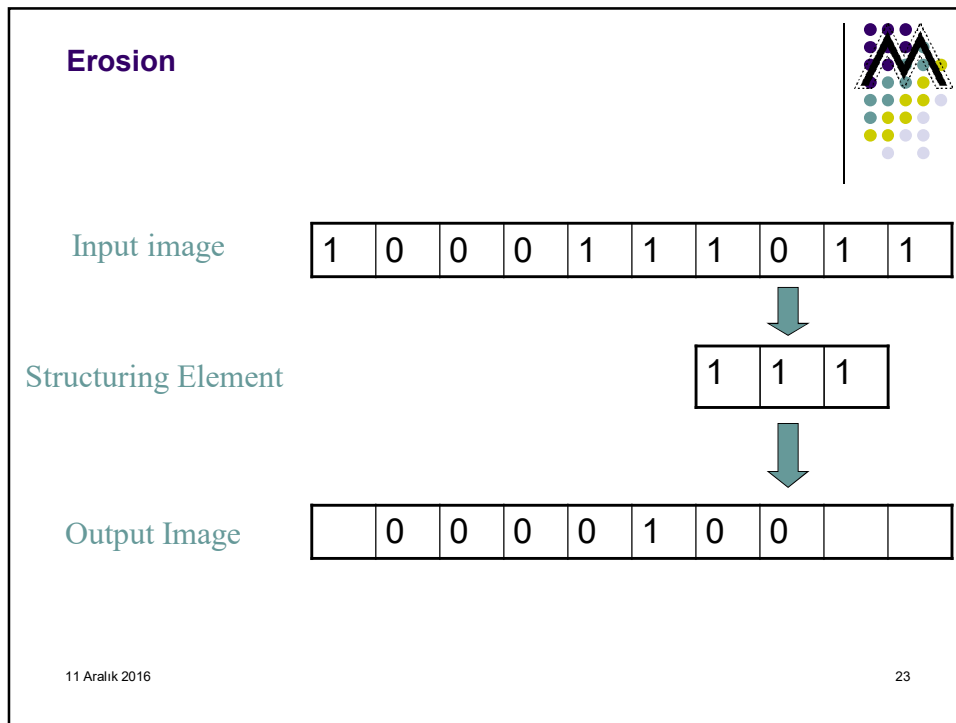


Output Image

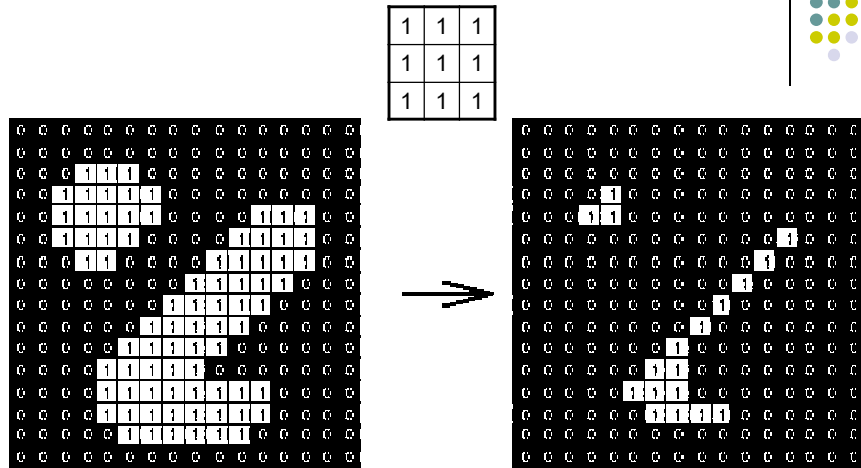
	0	0	0	0	1	0			
--	---	---	---	---	---	---	--	--	--

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## Erosion



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## Opening and Closing

- Opening:

$$A \circ B = (A \ominus B) \oplus B$$

- Closing:

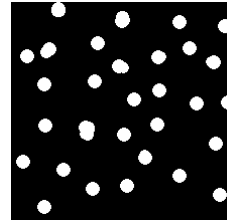
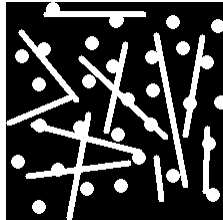
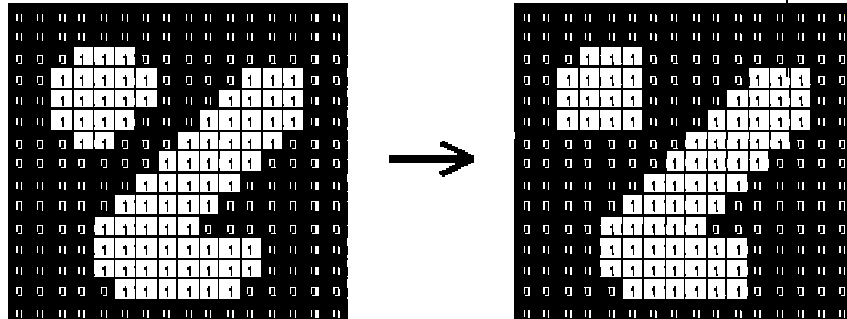
$$A \bullet B = (A \oplus B) \ominus B$$

MATLAB: `imopen`, `imclose`

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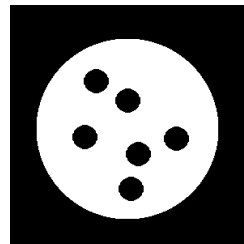
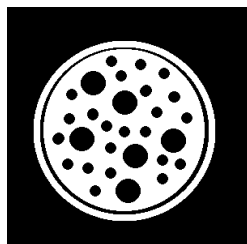
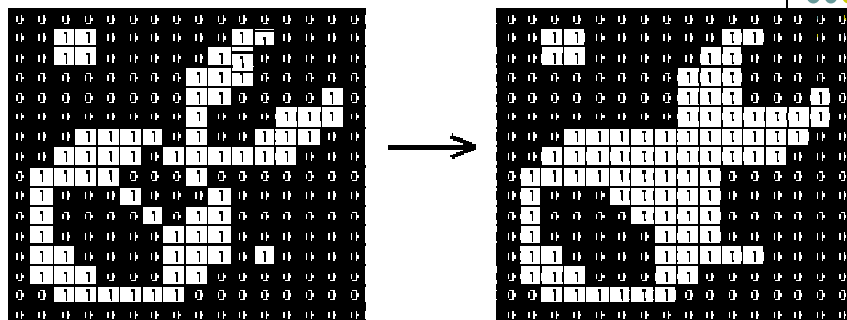
## Opening



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## Closing



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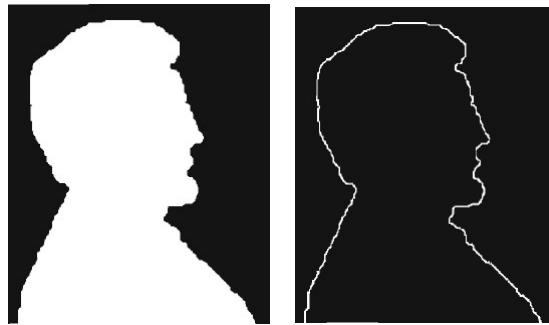
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## Boundary Extraction



$$\beta(A) = A - (A \ominus B)$$

Boundary



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## Application



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## Application

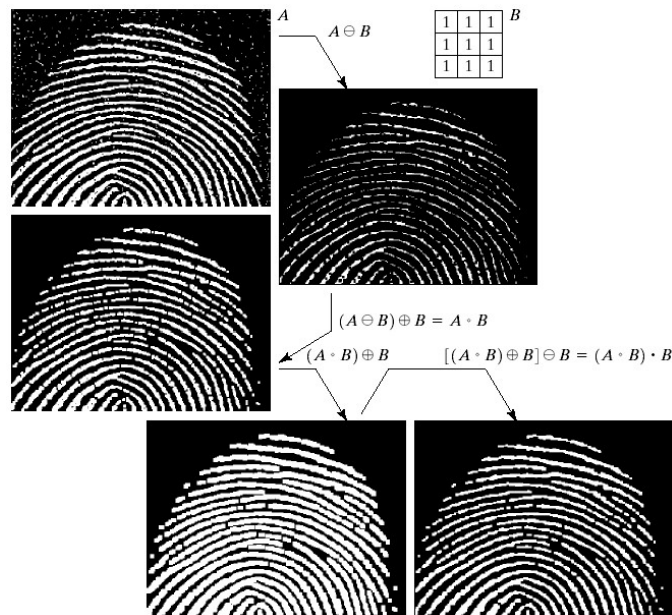


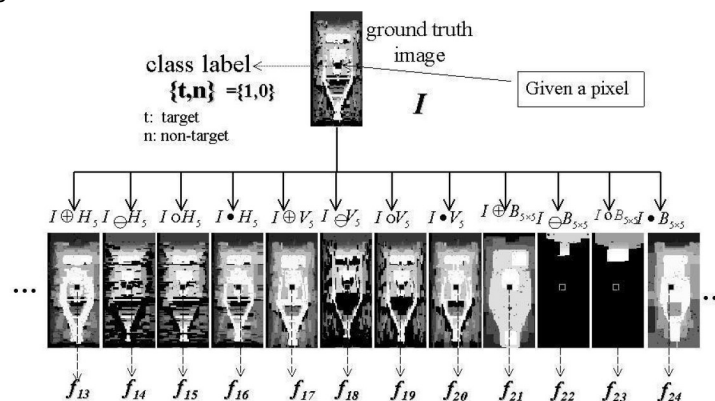
FIGURE 9.11

(a) Noisy image.  
(c) Eroded image.  
(d) Opening of  $A$ .  
(e) Closing of the opening. (Original image for this example courtesy of the National Institute of Standards and Technology.)

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## Application

Target Detection:



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