

## EX 5.2. b)

Maximum energy:

$$\begin{aligned} \rho &= 3 \text{ Km} \\ B &= 16 \text{ T} \end{aligned} \rightarrow \frac{p}{e} = B\rho \rightarrow p = 3 \times 10^3 \text{ m} \times 16 \text{ T} \times e \times 3 \times 10^8 \frac{\text{m}}{\text{s}} = 14,4 \frac{\text{TeV}}{c}$$

and so the energy is  $\boxed{E = 14,4 \text{ TeV}}$

Synchrotron radiation:

$$\gamma(14,4 \text{ TeV}) = 15,3 \times 10^3$$

now the majority of the photons is emitted at the critical energy

$$\boxed{E_c = \hbar \omega_c = \hbar \frac{2}{3} \frac{c}{\rho} \gamma^3 = 158,5 \text{ eV}}$$

so in the UV.

The energy lost per turn ~~is~~ by one proton is:

$$\boxed{U_0 (\text{KeV}) = 6,03 \frac{E^4 (\text{TeV})}{\rho (\text{m})} = 86,4 \text{ KeV}}$$

this means that for an 1 A beam the power irradiated is

$$\boxed{P (\text{KW}) = U_0^{(\text{KeV})} \cdot I (\text{A}) = 86,4 \text{ KW}}$$

so this means:

- the vacuum is stressed a lot by the synchrotron emission, the beam pipe will probably need proper conditioning. Also the working of getters and ion pump. has to be verified carefully because ad- and ab-sorption of gasses is reduced by radiation. (smaller capture time on the surfaces of the residual gas)

- the RF system has to be designed to transfer to the beam at least 86.4 kW of power. And ~~atop~~ ~~also~~ this just to maintain the energy at f<sub>top</sub>.

Compared to the LHC at 7 TeV, where just 3.7 kW are irradiated per beam [1], this means to require a much higher performance of the RF systems.

[1] LHC project report 316, 1.12.1999

- In general such high radiation level is stressing for all the instrumentation, in particular the electronics.