

# Review of Continuous Adaptation Via Meta-Learning in Nonstationary and Competitive Environments

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April 17, 2018

## 1 A Probabilistic View of Model-Agnostic Meta-Learning (MAML)

Assume that we are given a distribution over tasks,  $\mathcal{D}(T)$ , where each task,  $T$ , is a tuple:

$$T := (L_T, P_T(\mathbf{x}), P_T(\mathbf{x}_{t+1}|\mathbf{x}, \mathbf{a}_t), H) \quad (1)$$

$L_T$  is a task specific loss function that maps a trajectory,  $\boldsymbol{\tau} := (\mathbf{x}_0, \mathbf{a}_1, \mathbf{x}_1, R_1, \dots, \mathbf{a}_H, \mathbf{x}_H, R_H) \in \mathcal{T}$ , to a loss value, i.e.,  $L_T : \mathcal{T} \rightarrow \mathbb{R}$ ;  $P_T\mathbf{x}$  and  $P_T(\mathbf{x}_{t+1}|\mathbf{x}_t, \mathbf{a}_t)$  define the Markovian dynamics of the environment in task  $T$ ;  $H$  denotes the horizon; observations,  $\mathbf{x}_t$ , and actions,  $\mathbf{a}_t$ , are elements (typically, vectors) of the observation space,  $\mathcal{X}$ , and action space,  $\mathcal{A}$ , respectively. The loss of a trajectory,  $\boldsymbol{\tau}$ , is the negative cumulative reward,  $L_T(\boldsymbol{\tau}) := -\sum_{t=1}^H R_t$ .