### RNA STRUCTURE ANALYSIS VIA THE RIGID BLOCK MODEL

by
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A dissertation submitted to the
Graduate School—New Brunswick
Rutgers, The State University of New Jersey
in partial fulfillment of the requirements
for the degree of
Doctor of Philosophy
Graduate Program in Chemistry and Chemical Biology

Written under the direction of
Wilma K. Olson
and approved by

ABSTRACT OF THE DISSERTATION

RNA Structure Analysis via the Rigid Block Model

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RNA structure is at the forefront of our understanding of the origin of life, and the mechanisms of life

regulation and control. RNA plays a primordial role in some viruses. Our knowledge of the importance

of RNA in cellular regulation is relatively new, and this knowledge, along with the detailed structural

elucidation of the transcription machine, the ribosome, has propelled interest in understanding RNA to

a level which starts to closely resemble that given to proteins and DNA.

In the process of progressively understanding the landscape of functionality of such a complex

polymer as RNA, one practical task left to the structural chemist is to understand the details of how

structure relates to large-scale polymer processes. With this in mind the fundamental problems which

fuel the work described in this thesis are those of the conformations which RNA's assume in nature,

and the aim to understand how RNA folds.

The RNA folding problem can be understood as a mechanical problem. Therefore efforts to deter-

mine its solution are not foreign to the use of statistical mechanical methods combined with detailed

knowledge of atomic level structure. Such methodology is mainly used in this work in a long-term effort

to understand the intrinsic structural features of RNA, and how they might relate to its folding.

ii

As a thing among things, each thing is equally insignificant; as a world each one equally significant. If I have been contemplating the stove, and then am told; but now all you know is the stove, my result does indeed sound trivial. For this represents the matter as if I had studied the stove as one among the many, many things in the world. But if I was contemplating the stove, it was my world, and everything else colorless by contrast with it ...

For it is equally possible to take the bare present image as the worthless momentary picture in the whole temporal world, and as the true world among shadows.

**Ludwig Wittgenstein** 

As a molecule among molecules, each molecule is equally insignificant; as a world each one equally significant.

If I have been contemplating RNA, and then am told; but now all you know is RNA, my result does indeed sound trivial. For this represents the matter as if I had studied RNA as one among the many, many molecules in the world. But if I was contemplating RNA, it was my world, and everything else colorless by contrast with it ...

For it is equally possible to take the bare present image as the worthless momentary picture in the whole temporal world, and as the true world among shadows.

**Anonymous Chemist** 

### **Acknowledgements**

I would first like to give a special thanks to Dr. Yurong Xin, whose patience, help, and collaboration since the very beginning of my joining of the Olson lab have been fundamental for the development of this work. I would like to thank Dr. Olson's extreme patience, and room for freedom on carrying out this research. Finally I thank all colleagues at the Olson lab.

I would like to dedicate this thesis to David and Stella Case, without them these words would not exist.

# **Table of Contents**

ΑŁ	strac	t		ii
Ac	know	ledgem	nents	iv
Li	st of	Tables		vii
Li	st of	Figures	S	ix
1.	Intro	oductio	on	1
	1.1.	RNA c	chemistry	1
	1.2.	RNA f	olding	3
	1.3.	Is RN	A folding a hard or easy problem?	5
	1.4.	Experi	imental folding techniques	7
	1.5.	RNA s	simulations	7
		1.5.1.	Local nucleotide interactions	8
		1.5.2.	RNA secondary structure algorithms and the lack of tertiary ones	9
		1.5.3.	RNA overall fold	9
		1.5.4.	RNA motifs	11
	1.6.	Overv	iew	12
Re	eferen	ices .		14
2.	RNA	A Base	Steps	21
	2.1.	Conse	ensus Clustering of Single Stranded Base Step Parameters	24
		2.1.1.	Combining Fourier Averaging Results and Clustering Analysis	24
		2.1.2.	Selection of a Clustering Methodology	28
Re	eferen	ices .		40
3.	RNA	A Base-	Pairing	42
	2 1	Canor	nical and Nancanonical Rase-nairs	12

	3.2. Clustering of Yurong's Classification	42
Re	eferences	44
4.	RNA Base Pair Steps	45
	4.1. Analysis (Albany Poster) and Django Webserver	45
	4.2. Persistence Length of RNA	45
	4.3. AMBER: Persistence Length of Base-Pair Step Patterns	46
Re	eferences	47
5.	RNA Motifs	47
	5.1. GNRA tetraloop	47
	5.1.1. 3DNA-Parser	47
	5.1.2. Overlap Scores	48
	5.2. Triplets on RNA (comparison to Laing et al.)	48
Re	eferences	51
6.	RNA Helical Regions and Graph Theory	52
Αŗ	ppendix A. Standard reference frame and local parameters	53
	A.1. Base-pair and base-step parameters	53
	A.2. Local helical parameters	56
Re	eferences	59
Αŗ	ppendix B. Clustering Analysis (CA)	60
	B.1. General Methodology	60
	B.2. Hierarchical methods	61
Re	eferences	65
Αp	ppendix C. Dimension Reduction	66
	C.1. Principal Component Analysis	66
Re	eferences	68
Αp	ppendix D. Persistence Length	69
	D.1. Persistence Lenght Definitions	69

D.2. end-to-end	. 72
D.3. Models	. 73
D.3.1. Kuhn - Freely Jointed Chain (FJC)	. 73
D.3.2. Porod-Kratky - Worm Like Chain (WLC)	. 73
D.3.3. Olson - Realistic	. 73
D.4. Suggested Reads	. 73
References	. 74
Supplement A. Figure Supplements	. 75
Curriculum Vitae	72

# **List of Tables**

2.1.	Some large RNA structures (>300 bases) elucidated in the last decade	23
2.2.	Number of base-steps with RMSD values less than or equal to 10 Å between the refer-	
	ence base-step vectors from the four groups of non-A-type RNA dinucleotide conforma-	
	tions and all base-step vectors found in the 23S strand of Haloarcula marismortui. The	
	percentage is calculated with respect to a total of 2753 base-steps present in the 23S	
	chain of the 50S subunit of the ribosome.	28
2.3.	Base step parameters for common DNA and RNA conformations. The base-step pa-	
	rameters are computed for a single-stranded base-step rather than a double-stranded	
	base-pair step	33
3.1.	Classification of RNA Types in Non-Redundant Dataset at less than 3.5 Å (For Base-Pairs	
	in Helices of 3 base-pairs or more).	43
B.1.	Example of structures, considered as bidimensional vectors, to be clustered using the	
	average linkage method and the Manhattan distance	63
D.1.	Persistence lengths for some biopolymers with filament structures	72

# List of Figures

1.1.	A single strand of RNA drawn in the 5' to 3' sense showing the three chemical entities	
	which compose it, base, sugar, and phosphate. The four bases (A, G, C, U) are colored	
	according to the NDB (Nucleic Acid Database) convention [18], the phosphate is colored	
	gray, and the sugars black. The bases G, and C, and the furanose sugar attached to the	
	G are numbered according to the IUPAC rules [19]. This figure is an adaptation of Figure	
	2.1, in Wolfram Saenger's book, "Principles of Nucleic Acid Structure" [20]	2
1.2.	Saenger base-pairing classes, reproduced from his book, "Principles of Nucleic Acid	
	Structure". [20]	4
1.3.	Left: Sugar, and sugar-phosphate backbone torsion angles. Right: The most common	
	sugar pucker conformations in RNA, that is, $C_{3'-\mathrm{endo}}$ and $C_{2'-\mathrm{endo}}$ , reproduced from	
	Wolfram Saenger's, "Principles of Nucleic Acid Structure". [20]	5
1.4.	Separation of secondary and tertiary interaction in RNA [39]. Double helical secondary	
	structure represented by individual cylinders and tertiary interactions by association of	
	cylinders. Color coding stands for separate helical regions of RNA, and the connecting	
	black strings represent single stranded loop structures	6
1.5.	Ribbon-coil schematic illustraring the fold and intermolecular units of a dimer of prealbu-	
	min (PDB_ID:2pab), or transthyretin, taken from Richardson et al. [90]	10
1.6.	Images of the Haloharcula marismortui's large ribosomal subunit NDB_ID:RR0033 (left)	
	and the hammerhead ribozyme (right) NDB_ID:UR0029. The figures were taken directly	
	from the NDB web pages, and show a 3DNA generated [91] ribbon representation of	
	the phosphate backbone, and a block representation for the nucleotide bases. From	
	the figures it's clear that, whereas the ribozyme fold can be clearly understood with this	
	representation, the ribosome fold cannot.	11
2.1.	Left: Total number of RNA bases added to the PDB database between 2000 and 2010	
	(Exponential fit line in blue). Right: Total number of RNA structures solved yearly by	
	X-Ray crystallography between 2000 and 2010 (Exponential fit line in red).	21

۷.۷.	Frequency of nucleotide bases in ANA molecules lound in the FDB classified by the size	
	of RNA molecules. We define the size as the total number of nucleotide bases present	
	per molecule	23
2.3.	Figure taken from Richardson et al. [11] where the blue and green dots in a) mean very	
	accurate van der Waals distances, and in b) the red and orange dots mean steric clashes,	
	that is, distances outside the acceptable van der Waals range	24
2.4.	Dendrogram showing the results of consensus clustering of 20 non-Atype rRNA dinu-	
	cleotides according to their hexadimensional base-step parameter vectors	26
2.5.	RNA dinucleotide structures organized by clusters obtained from consensus clustering of	
	their hexadimensional base-step parameter vectors. The structures have been centered	
	on the reference frame of the first step, that is, the adenine base, and the minor groove	
	face of the rigid block parameter associated to adenine is facing the viewer	27
2.6.	Root mean square deviation of the main four groups show in Figure 2.5. The color of the	
	histograms is the same as that of the boxes surrounding the structures of Figure 2.5	29
2.7.	Root mean square deviation histograms for the subgroups present in group IV. Since sub-	
	group IVb is composed of A-RNA like conformations we see in the upper left histogram	
	that the highest proportion of small RMSD values belongs to this group	30
2.8.	Rigid block representation of dinucleotide steps. The major groove side of the first nu-	
	cleotide block is oriented towards the viewer and shaded gray. Left: Drawn in blue, the	
	block representing the Group I cluster from Figure 2.5. Superimposed to the Group I	
	cluster are three structures whose step-parameter RMSD's with respect to the Group I	
	cluster are less than or equal to 10 Å. Right: With an RMSD less than or equal to 15	
	Å we "identify" a total of seven structures from the ribosome. We clearly see that three of	
	them (encircled in cyan blobs) are farther apart from the original Group I main structure	
	of Figure 2.5 which is drawn in blue	31
2.9.	Pairs scatterplot for base-step parameters, shift, slide, rise, tilt, roll, and twist, for the	
	non-ARNA dataset colored according to purine-pyrimidine (black), purine-purine (red),	
	pyrimidine-pyrimidine (green), and pyrimidine-purine (blue) steps	32

2.10	. Cluster validity scores for internal measures. Notice now the hierarchical method, labeled	
	as 1 in black color, behaves better for the whole range of Connectivity (smaller values)	
	and Dunn (higher values), and it also outperforms all others after $k=12$ for Silhoutte	
	(higher values) scores	34
2.11	.Cluster validity scores for stability measures.	35
2.12	RMSD values between base-step parameters of the 23S subunit of ribosomal RNA and	
	the standard base-step parameters derived from Arnott and collaborators [24] work	36
2.13	.Cluster validity scores for the non-ARNA dataset. It can be seen clearly that the optimal	
	method for clustering is the hierarchical one, as measured by lower values in the con-	
	nectivity scores, and higher values in the Dunn score. The optimal number of clusters	
	given by the dunn score is 67, we also see shoulders at $k=67$ , for the connectivity and	
	silhouette scores.	38
2.14	.17 out of the 67 groups clustered using the hierarchical clustering algorithm are drawn	
	in a photograph contact sheet fashion. Each group is centered on the base reference	
	frame of the adenine block drawn in red. In the lower right corner of the "contact sheet"	
	the full space of 797 reconstructed steps is shown, along with the 20 steps derived from	
	schneider et al. work. Notice how the only "hollow" side of the "onion" formed by the full	
	space of base-step conformations is that corresponding to the watson-crick base-pairing	
	region	39
5.1.	GNRA Tetraloop from <i>Thermus Thermophilus</i> 23S Ribosomal RNA PDB-ID:1ffk	48
5.2.	Normalized histograms showing the distribution of overlap values in the 23S subunit or	
	Thermus Thermophilus rRNA, PDB-ID:1jjk. In histogram (a) all values are included, but in	
	histogram (b) only values greater than zero are included. Notice the high preponderance	
	of zero values, exactly 897 out of a total of 2705	49
5.3.	Dendrogram for consensus clustering of overlap scores in the ribosome. Zero values	
	filtered out and remaining data normalized	50

A.1.	Standard reference frame of an A-1 base-pair [4]. The y-axis (dashed green line) is	
	chosen to be parallel to the line connecting the C1 of adenine and the C1 of thymine	
	associated in an ideal Watson-Crick base-pair. The x-axis is the perpendicular bisector	
	of the $C1'$ - $C1'$ line, and the origin is located at the intersection of the <i>x</i> -axis and the line	
	connecting the C8 atom of adenine and the C6 atom of thymine. The z-axis is the cross	
	product of the $\hat{x}$ and $\hat{y}$ unit vectors	54
A.2.	Illustration of base pair and base step parameters [1]	57
B.1.	Clustering tree for 5 bidimensional vectors using the Manhattan distance definition and	
	the average linkage clustering method.	64
S1.	Non A-RNA Type base steps centered on the standard reference frame of Adenine. Top	
	view with the Minor Groove side of Adenine pointing down the page and the Major Groove	
	pointing up	76
S2.	The total number of structures available in the pdb up to the end of year 2009. The scale	
	of the axis in the left (in black), is ten times that in the right (in green). The black y-axis	
	sets the scale for the number of protein structures available in the PDB up to the end of	
	the year 2009. The green y-axis sets the scale for the number of molecular structures	
	containing, rna only (in red), dna only (in blue), and protein plus nucleic acid (in green).	
	One can clearly see that the total number of protein, rna, and protein plus nucleic acid	
	structures is growing exponentially. It is also clear that the number of DNA structures	
	is perhaps tending toward a constant number, that is, it might not be growing. It is also	
	interesting to see how the number of RNA structures really lifts off in the middle of the	
	nineties, whereas for DNA the growth started earlier and is settling down	77

### **Chapter 4**

### **RNA Base Pair Steps**

#### 4.1 Analysis (Albany Poster) and Django Webserver

Results shown in Albany and steps part of methods paper.

This gives us the force constant matrices per base-step which are used in the next section.

### 4.2 Persistence Length of RNA

A quantity commonly used to quantify the stiffness of polymers is the so-called persistence length *a*. To determine this quantity for DNA or RNA a variety of theoretical and experimental techniques are used. Some common experimental techniques to determine *a* are Electron Microscopy (EM), gel electrophoresis, sedimentation velocities, electrical birefringence Atomic Force Microscopy (AFM), Magnetic Tweezers, and Small Angle X-Ray Scattering (SAXS). For reviews of such techniques applied to the determination of RNA persistence length, we refer the reader to Hagerman [?], Abels et al. [1], and Caliskan et al. [2]. We will use their results for comparison with those coming from the "realistic" model developed by Olson and collaborators [3] to describe DNA. The "realistic" model is dependent on high resolution crystallographic data. Initial studies started with small numbers of data for the deformabilities of the ten unique base-pair steps [3]. A more complete picture applied to the study of DNA sequence dependent deformability became available in 1998 [4]. The base-pair step deformability data for DNA has been constantly refined as more high resolution DNA and DNA-protein structures have been added to the Nucleic Acid Database (NDB) [5]. Although such data has been available for DNA since 1998, it had not been so for RNA, until now [6].

A detailed description of the "realistic model" along with the scheme of the C++ code developed by Czapla and Zheng to implement it, and a brief account of various definitions of persistence length and models from which a can be derived are included in Appendix D

# 4.3 AMBER: Persistence Length of Base-Pair Step Patterns

I guess it needs some input here in order to work on latex compilation.

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### Appendix D

### **Persistence Length**

Nucleic Acids and other polymers can be understood as mechanical objects [1, 2] and therefore engineering approaches can be used for their understanding. Usually the methods followed by the engineering approach consider the polymer as a long continuous rod, and are known as continuum elastic theory. This type of approach leaves little space for taking into account the nature of the subunits which make up the polymer, that is, it is mainly applicable to homopolymers made up of identical subunits. In nucleic acids this is not necesarily the case, a more general approach should take into account the possibility of having different subunits making up the polymer. Olson and collaborators have developed a sequence dependent model, refered to as the "realistic" model [3]. Such model is harmonic and depends on determination of force-constant analogs derived from X-Ray cristallographic data taken from the Nucleic Acid Database (NDB) [4, 5]. Within the context of the "realistic" model Czapla et al. [6] have suggested a gaussian sampling methodology which allows the determination of global polymer properties like the persistence length a following a matrix approach suggested by Flory [7] and expanded upon by Olson et al. [?, ?]

In what follows we summarize various definitions of persistence length and how it's computed using different models.

### **D.1 Persistence Lenght Definitions**

There are two parallel perspectives which can be used to define the persistence length of nucleic acids. One is a more mathematical, or physical one, where it is understood as the resistence to deformation of a curve in space, or thin rod, a physical object. The other one is a stochastic one where it is understood as "a measure of the distance over which the direction of the DNA is maintained [8]" and has the classical formulation by Flory which states that the persistence length is:

"the average sum of the projections of all bonds  $j \ge i$  on bond i in an indefinetely long chain. The bond i is taken to be remote from either end of the chain, i.e.,  $1 \ll i \ll n$ ". Paul J. Flory, Statistical

Mechanics of Chain Molecules. 1969

This perspective has a more chemically flavored tone, since it assumes some type of bonded connectivity between polymeric units, whether the bond is a "real" one, or a "virtual" one.

### "Bend-persistence length:

A length scale beyond which the elastic cost of bending is totally negligible" Philip Nelson, Yearbook of Science and Technology, McGraw Hill 1999

"In a randomly shaken rod any particular point in the rod will be pointing in a random direction, but nearby points will be pointing in roughly the same direction, that is, these nearby points are persistent. Points farther away than the bend-persistence length are said to be uncorrelated." Philip Nelson, Yearbook of Science and Technology, McGraw Hill 1999

#### "twist-persistence length:

that is, a rubber rod not only resists bending but also twisting"

"basic mechanical property that quantifies stiffness" Abels et al, Biophysical Journal, 2005, 2737-2744

"Classical elasticity tells us that a thin, straight rod that is bent into an arc has a bending energy  $E=Bl/2R^2$ , where B is the bending elastic constant of the rod, l is the length of the rod and R is the radius of arc. Setting R=l gives us the energy of a 1 radian bend along the rod, and solving for when  $E\kappa_BT$  gives us the length of rod along which a thermally excited bend of 1 radian typically occurs:  $lB/\kappa_BT$ . This is called the persistence length..." John F. Marko and Simona Cocco, Physics World, March 2003

$$E = \frac{Bl}{2R^2} \tag{D.1}$$

$$R = l ag{D.2}$$

$$E \sim k_B T l \sim \frac{B}{k_B T}$$
 (D.3)

"The persistence length a is a measure of the stiffness of a polymer chain and is related to the limiting value of the characteristic ratio at infinite chain length

$$a = \frac{\nu}{2}(C_{\infty} + 1) \tag{D.4}$$

71

"length at which the orientation of the sequential bonds which make up a polymer chain, stop being

correlated. That is, if you have just two bonds, or a few, they will be correlated, which is the case in

most molecules, but, in polymers, you have a long chain of sequential bonds. At some length, bonds will

become uncorrelated, but up to that length they were correlated, this is what is meant by persistence

length, and, in this context it's obvious that is an exclusive property of polymers." My understanding so

far.

Biopolymers can be either rigid or flexible.

They can be classified according to whether their persistence length (a) is greater, smaller, or similar

to the contour length (L) of the polymer.

Model Type Polymer Characteristic a to L relation  $a \gg \overline{L}$ Rigid Rod Rigid Gaussian chain Flexible  $a \ll L$ Worm-like chain Semi-flexible  $a \approx L$ 

Notice that for  $a \gg L$ , there is a definition problem, since L has to be large enough to be a good

approximation to the definition of persistence length, which is defined for an infinite chain length.

Worm-like-chain = Porod-Kratky = Freely Rotating Chain in limit I=0 and n=infinity

Rigid biopolymers: actin, microtubules

Flexible biopolymers:

Semi-flexible biopolymers: High force extension DNA.

If the persistence length is of the same order of the length of the polymer, then the polymer is

classified as semi-flexible

Think about the "energy" based perspective of Nicolas, and the stochastic based perspective of

Flory and others.

Polymer	a (nm)
$\alpha$ -helix	80-100
coiled-coil	150-300
Ideal DNA	51
Ideal RNA	70-80

Table D.1: Persistence lengths for some biopolymers with filament structures.

#### D.2 end-to-end

The end-to-end vector r is the vector which connects the ends of a polymer chain. It can be defined as the sum of the vectors connecting the monomer units in a chain. These connecting vectors are sometimes called virtual bond vectors l.

From the end-to-end vector the quantity which is usually of interest is it's magnitude.

$$r = \sum_{i=1}^{n} l_i \tag{D.5}$$

$$r^2 = r \cdot r = \sum_{i,j} l_i \cdot l_j \tag{D.6}$$

Equation D.5, can also be written:

$$r^{2} = \sum_{i} l_{i}^{2} + 2 \sum_{i \neq j} l_{i} \cdot l_{j}$$
 (D.7)

To describe a polymer it's necessary to think about the various conformations it can adopt due to its flexibility, therefore, it is important to think of polymer related quantities in terms of the average of their possible conformations. For the end-to-end vector the average of its values is denoted as < r >, and the average of its norm, also called the second moment of the end-to-end distribution, is denoted by  $< r^2 >$ :

$$< r^2 > = \sum_{i} < l_i^2 > +2 \sum_{i < j} < l_i \cdot l_j >$$
 (D.8)

When there is no correlation between succesive bonds we can write:

$$\langle l_i \cdot l_j \rangle = 0 \tag{D.9}$$

So that equation D.8 keeps only the bond auto-correlation term:

$$< r^2 > = \sum_i < l_i^2 > = n < l^2 >$$
 (D.10)

This equation is used to describe a so-called freely-jointed chain.

#### D.3 Models

Nelson in book says:

$$dE = \frac{1}{2}K_BT[A\beta^2 + Bu^2 + C\omega^2 + 2Du\omega]ds \tag{D.11}$$

 $A\kappa\beta$  T = Bend stiffness  $B\kappa\beta$  T = Stretch stiffness  $C\kappa\beta$  T = Twist stiffness  $D\kappa\beta$  T = Twist-stretch coupling

If only the bend stiffness survives then the model is called an inextensible model, also Porod-Kratky, or WLC.

#### D.3.1 Kuhn - Freely Jointed Chain (FJC)

### D.3.2 Porod-Kratky - Worm Like Chain (WLC)

#### D.3.3 Olson - Realistic

The Hamiltonian for a [9]

#### D.4 Suggested Reads

From Equilibrium Statistics of Plischke and Bergersen they suggest to read: Des Cloiseaoux and Janik () Rubinstein and Colby (Polymer Physics)

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