#### RNA STRUCTURE ANALYSIS VIA THE RIGID BLOCK MODEL

by
MAURICIO ESGUERRA NEIRA

A dissertation submitted to the
Graduate School—New Brunswick
Rutgers, The State University of New Jersey
in partial fulfillment of the requirements
for the degree of
Doctor of Philosophy
Graduate Program in Chemistry and Chemical Biology

Written under the direction of
Wilma K. Olson
and approved by

ABSTRACT OF THE DISSERTATION

RNA Structure Analysis via the Rigid Block Model

by Mauricio Esquerra Neira

Dissertation Director: Wilma K. Olson

RNA structure is at the forefront of our understanding of the origin of life, and the mechanisms of life

regulation and control. RNA plays a primordial role in some viruses. Our knowledge of the importance

of RNA in cellular regulation is relatively new, and this knowledge, along with the detailed structural

elucidation of the transcription machine, the ribosome, has propelled interest in understanding RNA to

a level which starts to closely resemble that given to proteins and DNA.

In the process of progressively understanding the landscape of functionality of such a complex

polymer as RNA, one practical task left to the structural chemist is to understand the details of how

structure relates to large-scale polymer processes. With this in mind the fundamental problems which

fuel the work described in this thesis are those of the conformations which RNA's assume in nature,

and the aim to understand how RNA folds.

The RNA folding problem can be understood as a mechanical problem. Therefore efforts to deter-

mine its solution are not foreign to the use of statistical mechanical methods combined with detailed

knowledge of atomic level structure. Such methodology is mainly used in this work in a long-term effort

to understand the intrinsic structural features of RNA, and how they might relate to its folding.

ii

As a thing among things, each thing is equally insignificant; as a world each one equally significant. If I have been contemplating the stove, and then am told; but now all you know is the stove, my result does indeed sound trivial. For this represents the matter as if I had studied the stove as one among the many, many things in the world. But if I was contemplating the stove, it was my world, and everything else colorless by contrast with it ...

For it is equally possible to take the bare present image as the worthless momentary picture in the whole temporal world, and as the true world among shadows.

**Ludwig Wittgenstein** 

As a molecule among molecules, each molecule is equally insignificant; as a world each one equally significant.

If I have been contemplating RNA, and then am told; but now all you know is RNA, my result does indeed sound trivial. For this represents the matter as if I had studied RNA as one among the many, many molecules in the world. But if I was contemplating RNA, it was my world, and everything else colorless by contrast with it ...

For it is equally possible to take the bare present image as the worthless momentary picture in the whole temporal world, and as the true world among shadows.

**Anonymous Chemist** 

## Acknowledgements

I would first like to give a special thanks to Dr. Yurong Xin, whose patience, help, and collaboration since the very beginning of my joining of the Olson lab have been fundamental for the development of this work. I would like to thank Dr. Olson's extreme patience, and room for freedom on carrying out this research. Finally I thank all colleagues at the Olson lab.

## **Table of Contents**

Αk	strac	t		ii
Ac	know	ledgem	nents	iv
Li	st of	Tables		vii
Li	st of	Figures	S	ix
1.	Intro	oductio	on	1
	1.1.	RNA c	chemistry	1
	1.2.	RNA f	olding	3
	1.3.	Is RN	A folding a hard or easy problem?	5
	1.4.	Experi	imental folding techniques	7
	1.5.	RNA s	simulations	7
		1.5.1.	Local nucleotide interactions	8
		1.5.2.	RNA secondary structure algorithms and the lack of tertiary ones	9
		1.5.3.	RNA overall fold	9
		1.5.4.	RNA motifs	11
	1.6.	Overv	iew	12
Re	eferen	ices .		14
2.	RNA	A Base	Steps	21
	2.1.	Conse	ensus Clustering of Single Stranded Base Step Parameters	24
		2.1.1.	Combining Fourier Averaging Results and Clustering Analysis	24
		2.1.2.	Selection of a Clustering Methodology	28
Re	eferen	ices .		40
3.	RNA	A Base-	Pairing	42
	2 1	Canor	nical and Nancanonical Rase-nairs	12

	3.2. Clustering of Yurong's Classification	42
Re	eferences	44
4.	RNA Base Pair Steps	45
	4.1. Analysis (Albany Poster) and Django Webserver	45
	4.2. Persistence Length vs. Hagerman	45
	4.3. AMBER: Persistence Length of Base-Pair Step Patterns	45
Re	eferences	46
5.	RNA Motifs	47
	5.1. GNRA tetraloop	47
	5.1.1. 3DNA-Parser	47
	5.1.2. Overlap Scores	48
	5.2. Triplets on RNA (comparison to Laing et al.)	48
Re	eferences	51
6.	RNA Helical Regions and Graph Theory	52
Αŗ	ppendix A. Standard reference frame and local parameters	53
	A.1. Base-pair and base-step parameters	53
	A.2. Local helical parameters	56
Re	eferences	59
Αŗ	ppendix B. Clustering Analysis (CA)	60
	B.1. General Methodology	60
	B.2. Hierarchical methods	61
Re	eferences	65
Αŗ	ppendix C. Dimension Reduction	66
	C.1. Principal Component Analysis	66
Re	eferences	68
Sι	upplement A. Figure Supplements	69

# **List of Tables**

2.1.	Some large RNA structures (>300 bases) elucidated in the last decade	23
2.2.	Number of base-steps with RMSD values less than or equal to 10 Å between the refer-	
	ence base-step vectors from the four groups of non-A-type RNA dinucleotide conforma-	
	tions and all base-step vectors found in the 23S strand of Haloarcula marismortui. The	
	percentage is calculated with respect to a total of 2753 base-steps present in the 23S	
	chain of the 50S subunit of the ribosome.	28
2.3.	Base step parameters for common DNA and RNA conformations. The base-step pa-	
	rameters are computed for a single-stranded base-step rather than a double-stranded	
	base-pair step	33
3.1.	Classification of RNA Types in Non-Redundant Dataset at less than 3.5 Å (For Base-Pairs	
	in Helices of 3 base-pairs or more)	43
B.1.	Example of structures, considered as bidimensional vectors, to be clustered using the	
	average linkage method and the Manhattan distance	63

# List of Figures

1.1.	A single strand of RNA drawn in the 5' to 3' sense showing the three chemical entities	
	which compose it, base, sugar, and phosphate. The four bases (A, G, C, U) are colored	
	according to the NDB (Nucleic Acid Database) convention [18], the phosphate is colored	
	gray, and the sugars black. The bases G, and C, and the furanose sugar attached to the	
	G are numbered according to the IUPAC rules [19]. This figure is an adaptation of Figure	
	2.1, in Wolfram Saenger's book, "Principles of Nucleic Acid Structure" [20]	2
1.2.	Saenger base-pairing classes, reproduced from his book, "Principles of Nucleic Acid	
	Structure". [20]	4
1.3.	Left: Sugar, and sugar-phosphate backbone torsion angles. Right: The most common	
	sugar pucker conformations in RNA, that is, $C_{3'-\mathrm{endo}}$ and $C_{2'-\mathrm{endo}}$ , reproduced from	
	Wolfram Saenger's, "Principles of Nucleic Acid Structure". [20]	5
1.4.	Separation of secondary and tertiary interaction in RNA [39]. Double helical secondary	
	structure represented by individual cylinders and tertiary interactions by association of	
	cylinders. Color coding stands for separate helical regions of RNA, and the connecting	
	black strings represent single stranded loop structures	6
1.5.	Ribbon-coil schematic illustraring the fold and intermolecular units of a dimer of prealbu-	
	min (PDB_ID:2pab), or transthyretin, taken from Richardson et al. [90]	10
1.6.	Images of the Haloharcula marismortui's large ribosomal subunit NDB_ID:RR0033 (left)	
	and the hammerhead ribozyme (right) NDB_ID:UR0029. The figures were taken directly	
	from the NDB web pages, and show a 3DNA generated [91] ribbon representation of	
	the phosphate backbone, and a block representation for the nucleotide bases. From	
	the figures it's clear that, whereas the ribozyme fold can be clearly understood with this	
	representation, the ribosome fold cannot.	11
2.1.	Left: Total number of RNA bases added to the PDB database between 2000 and 2010	
	(Exponential fit line in blue). Right: Total number of RNA structures solved yearly by	
	X-Ray crystallography between 2000 and 2010 (Exponential fit line in red).	21

۷.۷.	Frequency of nucleotide bases in ANA molecules lound in the FDB classified by the size	
	of RNA molecules. We define the size as the total number of nucleotide bases present	
	per molecule	23
2.3.	Figure taken from Richardson et al. [11] where the blue and green dots in a) mean very	
	accurate van der Waals distances, and in b) the red and orange dots mean steric clashes,	
	that is, distances outside the acceptable van der Waals range	24
2.4.	Dendrogram showing the results of consensus clustering of 20 non-Atype rRNA dinu-	
	cleotides according to their hexadimensional base-step parameter vectors	26
2.5.	RNA dinucleotide structures organized by clusters obtained from consensus clustering of	
	their hexadimensional base-step parameter vectors. The structures have been centered	
	on the reference frame of the first step, that is, the adenine base, and the minor groove	
	face of the rigid block parameter associated to adenine is facing the viewer	27
2.6.	Root mean square deviation of the main four groups show in Figure 2.5. The color of the	
	histograms is the same as that of the boxes surrounding the structures of Figure 2.5	29
2.7.	Root mean square deviation histograms for the subgroups present in group IV. Since sub-	
	group IVb is composed of A-RNA like conformations we see in the upper left histogram	
	that the highest proportion of small RMSD values belongs to this group	30
2.8.	Rigid block representation of dinucleotide steps. The major groove side of the first nu-	
	cleotide block is oriented towards the viewer and shaded gray. Left: Drawn in blue, the	
	block representing the Group I cluster from Figure 2.5. Superimposed to the Group I	
	cluster are three structures whose step-parameter RMSD's with respect to the Group I	
	cluster are less than or equal to 10 Å. Right: With an RMSD less than or equal to 15	
	Å we "identify" a total of seven structures from the ribosome. We clearly see that three of	
	them (encircled in cyan blobs) are farther apart from the original Group I main structure	
	of Figure 2.5 which is drawn in blue	31
2.9.	Pairs scatterplot for base-step parameters, shift, slide, rise, tilt, roll, and twist, for the	
	non-ARNA dataset colored according to purine-pyrimidine (black), purine-purine (red),	
	pyrimidine-pyrimidine (green), and pyrimidine-purine (blue) steps	32

2.10	. Cluster validity scores for internal measures. Notice now the hierarchical method, labeled	
	as 1 in black color, behaves better for the whole range of Connectivity (smaller values)	
	and Dunn (higher values), and it also outperforms all others after $k=12$ for Silhoutte	
	(higher values) scores	34
2.11	.Cluster validity scores for stability measures.	35
2.12	RMSD values between base-step parameters of the 23S subunit of ribosomal RNA and	
	the standard base-step parameters derived from Arnott and collaborators [24] work	36
2.13	.Cluster validity scores for the non-ARNA dataset. It can be seen clearly that the optimal	
	method for clustering is the hierarchical one, as measured by lower values in the con-	
	nectivity scores, and higher values in the Dunn score. The optimal number of clusters	
	given by the dunn score is 67, we also see shoulders at $k=67$ , for the connectivity and	
	silhouette scores.	38
2.14	.17 out of the 67 groups clustered using the hierarchical clustering algorithm are drawn	
	in a photograph contact sheet fashion. Each group is centered on the base reference	
	frame of the adenine block drawn in red. In the lower right corner of the "contact sheet"	
	the full space of 797 reconstructed steps is shown, along with the 20 steps derived from	
	schneider et al. work. Notice how the only "hollow" side of the "onion" formed by the full	
	space of base-step conformations is that corresponding to the watson-crick base-pairing	
	region	39
5.1.	GNRA Tetraloop from <i>Thermus Thermophilus</i> 23S Ribosomal RNA PDB-ID:1ffk	48
5.2.	Normalized histograms showing the distribution of overlap values in the 23S subunit or	
	Thermus Thermophilus rRNA, PDB-ID:1jjk. In histogram (a) all values are included, but in	
	histogram (b) only values greater than zero are included. Notice the high preponderance	
	of zero values, exactly 897 out of a total of 2705	49
5.3.	Dendrogram for consensus clustering of overlap scores in the ribosome. Zero values	
	filtered out and remaining data normalized	50

A.1.	Standard reference frame of an A-1 base-pair [4]. The y-axis (dashed green line) is	
	chosen to be parallel to the line connecting the C1 of adenine and the C1 of thymine	
	associated in an ideal Watson-Crick base-pair. The x-axis is the perpendicular bisector	
	of the $C1'$ - $C1'$ line, and the origin is located at the intersection of the $x$ -axis and the line	
	connecting the C8 atom of adenine and the C6 atom of thymine. The z-axis is the cross	
	product of the $\hat{x}$ and $\hat{y}$ unit vectors	54
A.2.	Illustration of base pair and base step parameters [1]	57
B.1.	Clustering tree for 5 bidimensional vectors using the Manhattan distance definition and	
	the average linkage clustering method.	64
S1.	Non A-RNA Type base steps centered on the standard reference frame of Adenine. Top	
	view with the Minor Groove side of Adenine pointing down the page and the Major Groove	
	pointing up.	70
S2.	The total number of structures available in the pdb up to the end of year 2009. The scale	
	of the axis in the left (in black), is ten times that in the right (in green). The black y-axis	
	sets the scale for the number of protein structures available in the PDB up to the end of	
	the year 2009. The green y-axis sets the scale for the number of molecular structures	
	containing, rna only (in red), dna only (in blue), and protein plus nucleic acid (in green).	
	One can clearly see that the total number of protein, rna, and protein plus nucleic acid	
	structures is growing exponentially. It is also clear that the number of DNA structures	
	is perhaps tending toward a constant number, that is, it might not be growing. It is also	
	interesting to see how the number of RNA structures really lifts off in the middle of the	
	nineties, whereas for DNA the growth started earlier and is settling down	71

#### **Chapter 3**

## **RNA Base-Pairing**

#### 3.1 Canonical and Noncanonical Base-pairs

As seen in Figure 1.2, there can be various base-pairing patterns between heterocyclic bases in nucleic acids due to a variety of possible hydrogen bonding interactions. The most prevalent hydrogen bonding pattern is known as canonical Watson-Crick, all other possible patterns are known as non-canonical base-pairs and are more common in RNA than in DNA. We used 3DNA to find all base-pairs in a non-redundant database of X-ray determined RNA structures from the PDB with resolutions less than or equal to 3.5 Å. We also constrained our search to helical regions in RNA. Such helical regions are composed of 3 consecutive base-pairs or more, and they need not be covalently bonded by the sugar-phosphate backbone between consecutive base-pairs. For more details the reader is referred to Olson et al. [1].

In the helical regions data we quantify:

Abundances (Counts) Deformabilites Helical Context

NON-REDUNDANT DATABASE AND CONSTRAIN TO HELICAL REGIONS.

We use a non-redundant dataset of RNA structures. By non-redundant we mean to say that, for the main source of RNA structural information, which is the ribosome, we used only one of the available structures per organism, that is, one for each of *Deinococus Radiodurans*, *Haloarcula marismortui*, *Escherichi coli*, and *Thermus thermophilus*.

#### 3.2 Clustering of Yurong's Classification

RNA Type	Counts	G	С	Α	U
small helices	78	891	753	404	442
drug-RNA	36	932	862	365	433
protein-RNA	207	4001	3457	1771	1731
protein-tRNA	9	175	155	98	87
rRNA	13	3866	2949	1939	1785
tRNA	13	205	159	124	112
ribozyme	113	2434	2086	1438	1150
Total	469	12504	10421	6139	5740

Table 3.1: Classification of RNA Types in Non-Redundant Dataset at less than 3.5  $\rm \mathring{A}$  (For Base-Pairs in Helices of 3 base-pairs or more).

### References

[1] Olson, W. K., Esguerra, M., Xin, Y., and Lu, X.-J. (2009) New Information Content in RNA Base Pairing Deduced from Quantitative Analysis of High-Resolution Structures. *Methods*, **47**, 177–186.