EE24BTECH11022 - Eshan Sharma

Question:

Area of the region in the first quadrant enclosed by the x - axis, the line y = x and the circle $x^2 + y^2 = 32$ is

Solution:

Symbol	Value	Description
С	$x^2 + y^2 = 32$	Circle
L	y = x	Line
A	(4 4)	Intersection1
В	$\begin{pmatrix} 4\sqrt{2} & 0 \end{pmatrix}$	Intersection2

TABLE 0: Variables Used

The given circle C can be expressed as

$$v = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}, u = 0, f = -32 \tag{0.1}$$

The given line L is

$$h = \begin{pmatrix} 1 \\ -1 \end{pmatrix} \tag{0.2}$$

$$\mathbf{A} = \begin{pmatrix} 4 \\ 4 \end{pmatrix} \text{ and } \mathbf{B} = \begin{pmatrix} 4\sqrt{2} \\ 0 \end{pmatrix} \tag{0.3}$$

$$\int_0^4 x \, dx + \int_4^{4\sqrt{2}} \sqrt{32 - x^2} \, dx = 4\pi \text{ square units}$$
 (0.4)

l

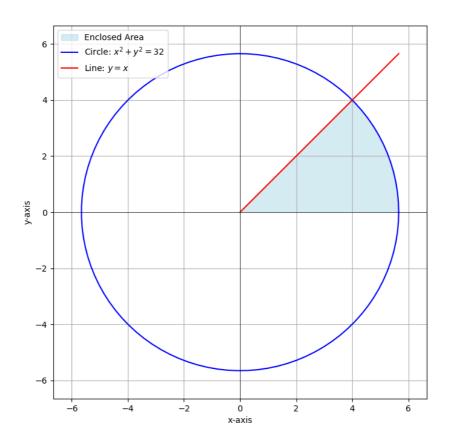


Fig. 0.1: Area enclosed in the first quadrant