

EE24BTECH11021 - Eshan Ray

- 1) If the functions are defined as $f(x) = \sqrt{x}$ and $g(x) = \sqrt{1-x}$, then what is the common domain of the following functions: $f+g, f-g, f/g, g/f, g-f$ where $(f \pm g)(x) = f(x) \pm g(x), (f/g)(x) = \frac{f(x)}{g(x)}$
- $0 < x \leq 1$
 - $0 \leq x < 1$
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- 2) Let α, β, γ be the roots of the equation, $x^3 + ax^2 + bx + c = 0, (a, b, c \in \mathbb{R} \text{ and } a, b \text{ and } a, b \neq 0)$. The system of equations (in u, v, w) given by $\alpha u + \beta v + \gamma w = 0; \beta u + \gamma v + \alpha w = 0; \gamma u + \alpha v + \beta w = 0$ has non-trivial solutions, then the value of $\frac{a^2}{b}$ is
- 5
 - 1
 - 0
 - 3
- 3) If the equation $a|z|^2 + \bar{\alpha}z + \alpha\bar{z} + d = 0$ represents a circle where a, d are real constants then which of the following conditions are correct?
- $|\alpha|^2 - ad \neq 0$
 - $|\alpha|^2 - ad > 0$ and $a \in \mathbb{R} - \{0\}$
 - $\alpha = 0, a, d \in \mathbb{R}^+$
 - $|\alpha|^2 - ad \geq 0$ and $a \in \mathbb{R}$
- 4) $\frac{1}{3^2-1} + \frac{1}{5^2-1} + \frac{1}{7^2-1} + \dots + \frac{1}{201^2-1}$ is equal to :
- $\frac{101}{404}$
 - $\frac{101}{408}$
 - $\frac{99}{400}$
 - $\frac{25}{101}$
- 5) The number of integral values of m so that the abscissa of point of intersection of lines $3x + 4y = 9$ and $y = mx + 1$ is also an integer, is:
- 3
 - 2
 - 1
 - 0
- 6) The solutions of the equation

$$\begin{vmatrix} 1 + \sin^2 x & \sin^2 x & \sin^2 x \\ \cos^2 x & 1 + \cos^2 x & \cos^2 x \\ 4 \sin 2x & 4 \sin 2x & 1 + 4 \sin 2x \end{vmatrix} = 0$$

, $(0 < x < \pi)$, are:

- a) $\frac{\pi}{6}, \frac{5\pi}{6}$
- b) $\frac{7\pi}{12}, \frac{11\pi}{12}$
- c) $\frac{5\pi}{12}, \frac{7\pi}{12}$
- d) $\frac{\pi}{12}, \frac{\pi}{6}$

7) If $f(x) = \begin{cases} \frac{1}{|x|} & ; |x| \geq 1 \\ ax^2 + b & ; |x| < 1 \end{cases}$ is differentiable at every point of the domain, then the values of a and b are respectively :

- a) $\frac{5}{2}, -\frac{3}{2}$
- b) $-\frac{1}{2}, \frac{3}{2}$
- c) $\frac{1}{2}, \frac{1}{2}$
- d) $\frac{1}{2}, -\frac{3}{2}$

8) A vector \mathbf{a} has components $3p$ and 1 with respect to a rectangular Cartesian system. This system is rotated through a certain angle about the origin in the counterclockwise sense. If with respect to the new system, \mathbf{a} has components $p + 1$ and $\sqrt{10}$, then a value of p is equal to:

- a) 1
- b) -1
- c) $\frac{4}{5}$
- d) $-\frac{5}{4}$

9) The sum of all the 4-digit distinct numbers that can be formed with the digits 1, 2, 2 and 3 is:

- a) 26664
- b) 122664
- c) 122234
- d) 22264

10) Choose the correct statement about two circles whose equations are given below:

$$x^2 + y^2 - 10x - 10y + 41 = 0$$

$$x^2 + y^2 - 22x - 10y + 137 = 0$$

- a) circles have no meeting point
- b) circles have two meeting points
- c) circles have only one meeting point
- d) circles have the same centre

11) If α, β are natural numbers such that $100^\alpha - 199\beta = (100)(100) + (99)(101) + (98)(102) + \dots + (1)(199)$, then the slope of the line passing through (α, β) and origin is:

- a) 510
- b) 550
- c) 540
- d) 530

12) The value of $3 + \frac{1}{4 + \frac{1}{3 + \frac{1}{4 + \frac{1}{3 + \dots}}}}$ is equal to :

- a) $3 + 2\sqrt{3}$
- b) $4 + \sqrt{3}$
- c) $2 + \sqrt{3}$
- d) $1.5 + \sqrt{3}$

13) The integral $\int \frac{(2x-1)\cos\sqrt{(2x-1)^2+5}}{\sqrt{4x^2-4x+6}} dx$ is equal to (where c is a constant of integration)

- a) $\frac{1}{2} \sin \sqrt{(2x+1)^2+5} + c$
- b) $\frac{1}{2} \sin \sqrt{(2x-1)^2+5} + c$
- c) $\frac{1}{2} \cos \sqrt{(2x+1)^2+5} + c$
- d) $\frac{1}{2} \cos \sqrt{(2x-1)^2+5} + c$

14) The differential equations satisfied by the system of parabolas $y^2 = 4a(x+a)$ is :

- a) $y\left(\frac{dy}{dx}\right) + 2x\left(\frac{dy}{dx}\right) - y = 0$
- b) $y\left(\frac{dy}{dx}\right)^2 + 2x\left(\frac{dy}{dx}\right) - y = 0$
- c) $y\left(\frac{dy}{dx}\right)^2 - 2x\left(\frac{dy}{dx}\right) - y = 0$
- d) $y\left(\frac{dy}{dx}\right)^2 - 2x\left(\frac{dy}{dx}\right) + y = 0$

15) The real-valued function $f(x) = \frac{\operatorname{cosec}^{-1}x}{\sqrt{x-[x]}}$, where $[x]$ denotes the greatest integer less than or equal to x , is defined for all x belonging to :

- a) all non- integers except the interval $[-1, 1]$
- b) all integers except $0, -1, 1$
- c) all reals except integers
- d) all reals except the interval $[-1, 1]$