

- 14) There are four electrons in  $3d$  shell of an isolated atom. The total magnetic moment of the atom in units in Bohr magneton is ...
- 15) Which of the following transitions is NOT allowed in the case of an atom, according to the electric dipole radiation selection rule?
- a)  $2s - 1s$
  - b)  $2p - 1s$
  - c)  $2p - 2s$
  - d)  $3d - 2p$
- 16) In the  $SU(3)$  quark model, the triplet of mesons  $(\pi^+, \pi^0, \pi^-)$  has
- a) Isospin=0, Strangeness =0
  - b) Isospin=1, Strangeness =0
  - c) Isospin= $\frac{1}{2}$ , Strangeness =+1
  - d) Isospin= $\frac{1}{2}$ , Strangeness =-1
- 17) The magnitude of the magnetic dipole moment associated with a square shaped loop carrying a steady current  $I$  is  $m$ . If this loop is changed to a circular shape with the same current  $I$  passing through it, the magnetic dipole moment becomes  $\frac{pm}{\pi}$ . The value of  $p$  is ...
- 18) The total power emitted by a spherical black body of Radius  $R$  at a temperature  $T$  is  $P_1$ . Let,  $P_2$  be the total power emitted by another spherical black body of radius  $\frac{R}{2}$  kept at an temperature  $2T$ . The ratio,  $\frac{P_1}{P_2}$  is ....  
(Give your answer upto two decimal places)
- 19) The entropy  $S$  of a system of  $N$  spins, which may align either in the upward or in the downward direction, is given by  $S = -k_B N [p \ln p + (1 - p) \ln (1 - p)]$ . Here,  $k_B$  is the Boltzmann constant. The probability of alignment in the upward direction is  $p$ . The value of  $p$ , at which the entropy is maximum, is ....  
(Give your answer upto one decimal place)
- 20) For a system at constant temperature and volume, which of the following statements is correct at equilibrium?
- a) The Helmholtz free energy attains a local minimum.
  - b) The Helmholtz free energy attains a local maximum.
  - c) The Gibbs free energy attains a local minimum.
  - d) The Gibbs free energy attains a local maximum.
- 21)  $N$  atoms of an ideal gas are enclosed in a container of volume  $V$ . The volume of the container is changed to  $4V$ , while keeping the total energy constant. The change in the entropy of the gas, in units of  $Nk_B \ln 2$ , is ..., where  $k_B$  is the Boltzmann constant.
- 22) Which of the following is an analytic function of  $z$  everywhere in the complex plane?

- a)  $z^2$
- b)  $(z')^2$
- c)  $|z|^2$
- d)  $\sqrt{z}$

- 23) In a Young's double slit experiment using light, the apparatus has two slits of unequal widths. When only *slit* – 1 is open, the maximum observed intensity on the screen is  $4I_0$ . When only *slit* – 2 is open, the maximum observed intensity is  $I_0$ . When both the slits are open, an interference pattern appears on the screen. The ratio of the intensity of principal maximum to that of the nearest minimum is ...
- 24) Consider a metal which obeys the Sommerfeld model exactly. If  $E_F$  is the Fermi energy of the metal at  $T = 0\text{ K}$  and  $R_H$  is the Hall coefficient, which of the following statements is correct ?
- a)  $R_H \propto E_F^{\frac{3}{2}}$
  - b)  $R_H \propto E_F^{\frac{3}{2}}$
  - c)  $R_H \propto E_F^{-\frac{3}{2}}$
  - d)  $R_H$  is independent of  $E_F$
- 25) A one-dimensional linear chain of atoms contains two types of atoms of masses  $m_1$  and  $m_2$  (where  $m_2 > m_1$ ), arranged alternately. The distance between successive atoms is the same. Assume that the harmonic approximation is valid. At the first Brillouin zone boundary, which of the following statements is correct?
- a) The atoms of mass  $m_2$  are at rest in optical mode, while they vibrate in acoustical mode.
  - b) The atoms of mass  $m_1$  are at rest in optical mode, while they vibrate in acoustical mode.
  - c) Both types of atoms vibrate with equal amplitudes in the optical as well as in the acoustical modes.
  - d) Both types of atoms vibrate, but with unequal, non-zero amplitudes in the optical as well as in the acoustical modes.
- 26) Which of the following operators is Hermitian?
- a)  $\frac{d}{dx}$
  - b)  $\frac{d^2}{dx^2}$
  - c)  $i \frac{d^2}{dx^2}$
  - d)  $\frac{d^3}{dx^3}$