

Homework 2
Due 11am, Friday, April 24, 2020

Download the starter code `PlayCard.java`. It should give you an idea of how we intend to use the class `MatchCardGame`. We may take off up to 20% of the total marks for poor style; make sure to name your variables reasonably, indent properly, and comment sufficiently. Put everything in the package `hw2`. Submit `PlayCard.java` and `MatchCardGame.java`.

Problem 1: (Pairs)

In a card game of *Pairs* the goal is to turn over pairs of matching cards.

[https://en.wikipedia.org/wiki/Concentration_\(game\)](https://en.wikipedia.org/wiki/Concentration_(game))

Here are the rules for the variation of Pairs we consider.

At the start of the game, there are n cards face-down, where n is a multiple of 4. There are 4 cards of each type, and the cards are labeled with letters `a`, `b`, For example, if $n=24$, there are 6 types of cards: `a`, `b`, `c`, `d`, `e`, and `f`. Say $1 \leq n$ and $n \leq 4 \cdot 26$.

At each turn, the player flips 2 cards, one at a time, that are face-down. If the 2 flips are of the same type, the matched cards are left face-up. If the 2 flips mismatch, the mismatched cards are returned to the face-down position. The game ends when all cards are matched, and the score is the total number of flips made. (Flipping a pair of cards counts as 2 flips, so the best possible score is n flips.)

Write a `public class` titled `MatchCardGame` with the following members that implement this game of Pairs. The starter code in `PlayCard.java` should give you an idea of how `MatchCardGame` is used.

`MatchCardGame` should have no other `public` fields, methods, and constructors aside from the ones specified. However, it may and should have additional `private` fields, methods, or constructors.

The field

```
public final int n;
```

is the size of the game set by the constructor.

The constructor

```
public MatchCardGame(int n);
```

initializes a card game with a total of n cards. Assume n is a multiple of 4 and that $4 \leq n$ && $n \leq 4 \cdot 26$. Without shuffling (explained in Problem 2) cards 0,1,2, and 3 should be `a`, cards 4,5,6, and 7 should be `b`, and so on.

The method

```
public String boardToString();
```

converts the state of the board to an appropriate `String` representation. You have freedom to choose your own representation, but it must reasonably represent the state of the game.

The method

```
public boolean flip(int i);
```

plays card number `i`. If card `i` cannot be played because it's face-up, or if `i` is an invalid card number, then return `false`. If `i` is a card number that can be played, play card `i` and return `true`.

The method

```
public boolean wasMatch();
```

returns `true` if the previous pair was a match and returns `false` otherwise. This method should be called only after `flip` has been successfully called an even number of times and before `flipMismatch` is called. (A successful call of `flip` is a call that results in a flip and returns `true`.)

The method

```
public char previousFlipIdentity();
```

returns the face of the previously flipped card as a `char`. This method should only be called after a card has been flipped.

The method

```
public void flipMismatch();
```

reverts the a mismatched pair to face-down position. This method should only be called after a 2 calls of `flip` results in a mismatch.

The method

```
public boolean gameOver();
```

returns `true` if all cards have been matched and the game is over and returns `false` otherwise.

The method

```
public int getFlips();
```

returns the total number of card flips that have been performed so far.

Remark. `MatchCardGame` represents the physical state of the game, not the player. `MatchCardGame` has nothing to do with game strategies a human or AI player might employ.

Remark. The problem specifies how these methods should be used. For example, the input `n` of `MatchCardGame`'s constructor needs to be a multiple of 4. You do not have to do any sort of error handling when these requirements are violated, although using `asserts` will help debugging. Note that `main` of `PlayCard.java` uses `MatchCardGame` in compliance to the specifications.

Remark. We will not use `PlayCard` or `MatchCardGame`'s `main` function in the grading.

Problem 2: (Shuffle)

For the class `MatchCardGame` write the method

```
public void shuffleCards();
```

This method shuffles the cards using the Fisher-Yates shuffle. This method should be called before any flips have been made.

Problem 3: (Game AIs)

Within the class `PlayCard`, write the following methods that automatically play the game.

The first method

```
public static int playRandom(MatchCardGame g);
```

plays the game by flipping a legal random card. I.e., at each turn, play one of face-down cards with equal probability independent of any past plays. (This “AI” is the least intelligent player.) The method plays until the game is over and **returns** the total number of flips.

The second method

```
public static int playGood(MatchCardGame g);
```

plays the game with perfect memory. After an even number of flips, if there is a known face-down pair, play the pair. Otherwise, randomly play, with equal probability, one of the unknown face-down cards. After an odd number of flips, if there is a known face-down match, play the match. Otherwise, randomly play, with equal probability, one of the unknown face-down cards. The method plays until the game is over and **returns** the total number of flips.

Remark. These AIs should perform the same whether or not the cards are shuffled.

Remark. When n is the board size, the good AI will always score $2n$ or better.

Problem 4: (Monte Carlo)

Within `PlayCard`, write the following methods that play the game many times with the AIs.

The first method

```
public static double randomMC(int N);
```

plays shuffled `MatchCardGames` of size 32 a total of N times using `playRandom` method. The method **returns** the average number of flips to complete the games.

The second method

```
public static double goodMC(int N);
```

plays shuffled `MatchCardGames` of size 32 a total of N times using `playGood` method. The method **returns** the average number of flips to complete the games.