# Verifying Forecasts of Land-Sea Breeze and Boundary Layer Mixing

2	Processes
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#### **ABSTRACT**

- This study presents a methodology for comparing the performance of Aus-
- tralian Bureau of Meteorology forecasts of the land-sea breeze with unedited
- model guidance products, such as those of the European Center for Medium-
- Range Weather Forecasting (ECMWF) and the Australian Community Cli-
- mate and Earth System Simulation (ACCESS). The methodology is applied
- to the 8 Australian capital city airports. The results indicate that at some air-
- ports, human intervention to model guidance products adds value to land-sea
- <sup>20</sup> breeze forecasts, whereas at other airports it does not.

#### 1. Introduction

Modern weather forecasts are produced by models in conjunction with human forecasters. For instance, a forecaster working for the Australian Bureau constructs a seven day forecast by first 23 loading model data into the Graphical Forecast Editor (GFE) software package, then manually editing this model data as they see fit. Forecasters can choose which model to base their forecast on, and refer to this as a choice of *model guidance*. Edits are typically made to account for processes that are underesolved at synoptic scale model resolutions, or to address known biases of 27 the models being used. 28 It is therefore important to assess not only the overall accuracy of weather forecasts, but also 29 the contribution human forecaster edits make to this accuracy. If effective, but routine, editing procedures can be identified they can be automated, freeing forecasters up to focus on other tasks. 31 One common edit involves changing the surface wind fields near coastlines to try to represent seabreezes more realistically. Forecasters invest time in making sea-breeze edits because accurate 33 predictions of near-surface winds are highly valued by a number of users, such as the aviation and energy (Smith et al. 2009) industries. Accurate sea-breeze forecasts are also valuable to environmental monitoring authorities, as these winds provide ventilation to coastal urban areas. Assessing the accuracy of a weather forecast is a task far more nuanced than it might first appear. 37

Assessing the accuracy of a weather forecast is a task far more nuanced than it might first appear.

For instance, attempting to assess the accuracy of a precipitation forecast by comparing the rainfall amounts measured at an individual weather station to the closest grid point of a model prediction will often give poor results. Although the synoptic drivers of convection are usually well predicted, excatly where convective cells form, and where the most rain falls, is highly unpredictable. As such, it is often appropriate to use "fuzzy" verification metrics which measure the agreement between prediction and observation in a more indirect way. For instance, one approach known as

"upscaling" is to first average forecast and observational data over a given spatial domain before
calculating verification scores. Ebert (2008) provided a review of current "fuzzy verification"
methodologies, and a framework for how they can be used to determine the spatial scales at which

a given forecast has predictive skill.

Relatively few forecast verification studies have focused on near-surface winds, and the ones
that have generally only considered wind speeds. Pinson and Hagedorn (2012) performed a verification study of the ECMWF 10 m wind speeds across western Europe over December, January,
February 2008/09. First, they interpolated ECMWF model data onto the locations of weather
stations across Europe, then they compared the interpolated model data at these stations with the
station observations themselves. They found that the worst performing regions were coastal and
mountainous areas, and attributed this poor performance to the small scale processes, e.g. sea
and mountain breezes, that are underesolved at ECMWF's coarse 50km spatial resolution. They
noted that future work could better identify the effect of diurnal cycles on verification statistics by
considering forecasts at different times of day.

Lynch et al. (2014) also performed a verification study of ECMWF 10 m wind speed data, with
the goal of assessing skill at lead times of between 14 to 20 days. They compared ECMWF 32day forecast model wind speeds with gridded ERA-Interim wind speeds between 2008-12, with
both datasets analysed at a six hour temporal resolution. Before conducting the comparison, the
wind speed data were transformed into wind-speed "anomaly" data by first calculating the mean
wind speed at 0000, 0600, 1200 and 1800 UTC for each calendar day from the entire ERA-Interim
record, and from a 20 year ECMWF 32-day model hindcast, then subtracting these means from the
ERA-Interim and ECMWF 32-day model data respectively. Wind speed anomaly data was used
so that stable seasonal and diurnal cycles did not contribute to verification scores. At the 14-20

- day timescale around western Europe, the greatest skill was found in the boreal winter (austral summer) months of December, January and February.
- Pinson and Hagedorn (2012) and Lynch et al. (2014) restricted their verification studies to wind speeds, but wind directions are also crucial to diagnosing whether land sea breezes and the diurnal wind cycle more generally are being forecast correctly. Furthermore, no previous published work has proposed a verification methodology to assess the accuracy of the diurnal wind cycle in forecasts, or of the contributions made to this accuracy by human forecaster edits of model output. Finally, no previously published work has considered the performance of ACCESS near surface winds, which together with ECMWF, are the model guidance products most widely used by Australian forecasters. Thus, the present study has two goals. First, to describe a methodology for comparing human edited forecasts of the land-sea breeze to unedited model guidance forecasts, in order to assess where and when human edits are producing an increase in accuracy. Second, to apply this methodology across Australia. The remainder of this paper is organised as follows. Section ?? describes the methodology in detail, section ?? provides results, and sections ?? and ?? provide a discussion and a conclusion, respectively.

#### 82 2. Data and Methods

- This study compares both edited and non-edited Australian Bureau of Meteorology forecast
  data with automatic weather station (AWS) data across Australia. The comparison is performed
  by first isolating the diurnal signals of each dataset, then comparing these signals on an hour-byhour basis. If the diurnal cycle cannot be resolved correctly using wind perturbations, it cannot be
  resolved correctly in the overall wind fields, which are subject to additional synoptic scale errors
- between the models and observations.

#### 89 a. Data

ficial wind forecast data, model data from the European Center for Medium Range Weather Fore-91 casting (ECMWF), model data from the Australian Community Climate and Earth System Simulator (ACCESS), and observational data from automatic weather stations. The Official, ECMWF and ACCESS data are at a ?, ? degree spatial resolution respectively. What are the resolutions of these datasets as they're used in Jive? Does the ACCESS model data in Jive Official, ACCESS and AWS data exists at each UTC hour. ECMWF data exists at a three hour resolution. To be consistent with the other data sets, ECMWF is therefore linearly interpolated to an hourly resolu-97 tion: this is also what happens in practice when forecasters load ECMWF wind data into the GFE. Two time periods are considered, the austral summer months (December, January, February) of 2017/18, and the austral winter months (June, July, August) of 2018. How is model/forecast data made consistent with AWS data in Jive - particularly regarding heights? Are all stations 10 m 101 above surface? Are all model/forecast data provided at the same height? 102 Only station data from the seven Australian capital city airport automatic weather stations are considered; Official, ECMWF and ACCESS data is (linearly?) interpolated to the coordinates 104 of the airport weather stations. Capital city airports have been chosen as the focus of this study 105 for a number of reasons. Automatic weather stations located at airports tend to provide the most accurate wind data, and wind forecasts at airports are important to the aviation industry. Moreover, 107 the capital city airports are all reasonably close to coastlines, resulting in a clear diurnal signal. 108 Finally, these airports are also all close to their respective capital cities, which are high priority regions for accurate forecasting. The datasets are hosted on the Bureau's Jive database, but are not 110 currently generally available, although the long term plan is for this to change. Can I extract and

Four datasets are considered in this study; they are the Australian Bureau of Meteorology's Of-

host the data I need myself? Can I obtain copies of the relevant Jive Functions so that I can post complete code online?

As described above, the Australian Bureau of Meteorology's official wind forecast is constructed out of model data, which is then edited by human forecasters using the Graphical Forecast Editor (GFE) software package. Australian forecasters typically construct wind forecasts out of model data either from the European Center for Medium Range Weather Forecasting (ECMWF), or the Australian Community Climate and Earth System Simulator (ACCESS). Testing whether the official forecast data conforms more closely to the AWS observations than ECMWF or ACCESS therefore provides a way to assess the extra accuracy gained by forecaster edits.

### b. Assessing Diurnal Cycles

Although close to coastlines the land-sea breeze is generally the dominant diurnal wind process,
the overall diurnal signal may also include mountain-valley breezes, boundary layer mixing processes, atmospheric tides, and urban heat island circulations. Forecasters typically edit model output to account for *both* unresolved sea-breezes *and* unresolved boundary layer mixing; attempting
to focus solely on sea-breezes without examining the entire diurnal cycle therefore risks erroneous
conclusions, with the effects of one category of edit mistaken for another. In general it is hard to
seperate boundary layer mixing edits from sea-breeze edits in the diurnal cycle composites, so this
point maybe needs to be reworked. Or could simply comment on this in the discussion.

Sea-breezes are therefore analysed by examining the overall diurnal signal in each dataset, with
the assumption that close to coastlines the land-sea breeze is the dominant diurnal process. The diurnal signal is identified by subtracting a twenty hour centred running mean *background wind* from
each zonal and meridional hourly wind data point. This provides a collection of zonal and meridional wind *perturbation* datasets. Note that thinking of land-sea breezes in terms of perturbations

from a background wind may require a conceptual shift from the usual operational definitions.

A forecaster would likely define a sea-breeze to be a reversal in wind direction from a primar-

ily offshore flow during the night and morning, to an onshore flow in the afternoon and evening.

However, even if the wind is offshore the entire day, sea-breeze perturbations are generally still

detectable as a weakening of the offshore flow throughout the afternoon and evening.

Note that subtracting background winds may raise concerns, because perturbations obviously depend on background winds. However, the forecaster does not have knowledge of the observations when they make the diurnal process edits. They are implicitly assuming that the true mean winds will be close enough to the predicted mean state - however this prediction is produced - to justify making diurnal edits on the basis of the predicted mean state.

Once the wind perturbation datasets have been constructed, the accuracy of the Official, ACCESS and ECMWF diurnal cycles are quantified by first calculating the Euclidean distances of
the perturbations at each hour from the corresponding AWS perturbations. For instance, to quantify how closely the Official forecast perturbations match the AWS observations, we calculate the
Euclidean distances  $|u_{AWS} - u_{O}|$  at each time step. The accuracy with which the Official and ACCESS datasets resolve the diurnal cycle can then be compared by defining the *Wind Perturbation*Index (WPI)

$$WPI_{OA} \equiv |\boldsymbol{u}_{AWS} - \boldsymbol{u}_{A}| - |\boldsymbol{u}_{AWS} - \boldsymbol{u}_{O}|. \tag{1}$$

At a given time, the Official forecast wind perturbation is closer to the AWS perturbation than that of ACCESS if and only if WPI > 0. Similarly, the WPI can used to provide a comparison of the Official and ECMWF datasets, or a comparison of the two model guidance datasets ACCESS and ECMWF.

To asses which dataset provides, in general, the most accurate representation of the diurnal cycle, we then take means of the WPI on an hourly basis; i.e. all the 00:00 UTC WPI values are

averaged, all the 01:00 UTC values are averaged, and so forth. The sampling distributions of 158 these means can then be modelled as Student's t-distributions, and from this we can calculate the 159 probability that WPI > 0 at each hour, where the bar denotes a temporal average. Temporal au-160 tocorrelations of WPI, i.e. correlations between WPI values at a particular hour from one day to 161 the next, are accounted for using the standard method of reducing the "effective" sample size to 162  $n(1-\rho_1)/(1+\rho_1)$ , where n is the actual sample size and  $\rho_1$  is the lag-1 autocorrelation (Zwiers 163 and von Storch 1995; Wilks 2011), although in practice temporal autocorrelations of WPI are ei-164 ther non-existant or very small. To assess how well the diurnal perturbations of an overall region are predicted, for instance those of the Victorian coastal station group (see Fig. ??), the perturba-166 tions across each station group are averaged before WPI values calculated. The temporal means 167 and sampling distributions of the WPI are then calculated as before, with each value of WPI cal-168 culated from the spatially averaged perturbations treated as a single observation. This provides a 169 conservative method for dealing with spatial correlation in the perturbations. 170

The advantage of the WPI method is it's clarity and simplicity: we are essentially just comparing 171 the magnitudes of vector differences, then applying a two sided t-test to determine whether one 172 dataset's perturbations are consistently closer to observations than another's. One factor that com-173 plicates interpretation of statistics of WPI, is that the near surface winds observed in AWS data are 174 consistently noisier than those of the Official, ECMWF and ACCESS forecasts. This is likely due 175 to unresolved subgrid scale turbulence in the Official, ECMWF and ACCESS model datasets. It 176 would be unreasonable to expect forecasters to be able to predict this essentially random additional observed variability, and so a direct comparison of observed and modelled diurnal cycles is overly 178 stringent. 179

To reduce the significance of unpredictable noise, we also compare temporal averages of the perturbations for each dataset. These comparisons have less operational significance: people gen-

erally care how well the actual weather forecast performed, not whether the average of a predicted quantity matched the average of an observed quantity. However, comparisons of averages arguably better represent what we can realistically expect from human forecaster edits, and from weather forecasts overall, particularly in regards to small scale processes like sea-breezes. Furthermore, when temporal averages of perturbations are considered, the diurnal signal becomes dramatically clearer, and structual differences become much easier to diagnose.

To quantify how closely the temporally averaged Official forecast perturbations match those of the AWS observations, we calculate  $|\overline{u}_{\rm AWS} - \overline{u}_{\rm O}|$  for each hour. To assess the performance of the Official temporally averaged perturbations against those ACCESS, we define the *Climatological Wind Perturbation Index* (CWPI)

$$CWPI_{OA} \equiv |\overline{u}_{AWS} - \overline{u}_{O}| - |\overline{u}_{AWS} - \overline{u}_{A}|. \tag{2}$$

As with the WPI, the CWPI can also be used to provide a comparison of the Official and ECMWF datasets, or a comparison of the two model guidance datasets ACCESS and ECMWF. Uncertainty in the CWPI is estimated through bootstrapping (Efron 1979). This is done by performing resampling with replacement on the underlying perturbation datasets, and calculating the CWPI multiple times using these resampled datasets. This provides a distribution of CWPI values, from which the probability that CWPI > 0 can be calculated. Similarly to with the WPI, performance over a particular region can be assessed by first averaging perturbation values over multiple stations before the CWPI is calculated.

Although the WPI and CWPI provide quantitive information on the accuracy of the diurnal cycle at different times of day, they do not provide much information about the structure of the diurnal wind cycles of each dataset, or provide insight into the reason one dataset is outperforming another.

Gille et al. (2005) obtained summary statistics on the observed structure of temporally averaged

diurnal wind cycles across the globe by using linear regression to calculate the coefficients  $u_i$ ,  $v_i$  i = 0, 1, 2, for the elliptical fit

where  $\omega$  is the angular frequency of the earth and t is the local solar time in seconds. Descriptive

$$u = u_0 + u_1 \cos(\omega t) + u_2 \sin(\omega t), \tag{3}$$

$$v = v_0 + v_1 \sin(\omega t) + v_2 \sin(\omega t), \tag{4}$$

quantities - like the angle the semimajor axis of the ellipse makes with the horizontal - were then calculated directly from the coefficients  $u_1$ ,  $u_2$ ,  $v_1$  and  $v_2$ . 208 Gille et al. (2005) applied this fit to satellite scatterometer wind observations, which after tem-209 poral averaging provided only four temporal datapoints at each  $0.25^{\circ} \times 0.25^{\circ}$  spatial grid cell. As such, their fit was very good, explaining over 90% of the wind variability in each spatial gridcell. 211 However, the choice of ellipse parametrisation in equations 5 and 6 assumes that datapoints lie on 212 the ellipse at equal intervals of time t. When observational or model data with an hourly or smaller timestep is considered, this assumption becomes too stringent, as heating asymmetries imply that 214 wind perturbations evolve much more rapidly during the day than at night (see Fig. XX). Note 215 I'm also basing this point on knowledge of the land vs sea breeze, and knowledge of heating vs cooling asymmetries (Brown et al. 2017, e.g.). 217

Thus, we model the climatological diurnal cycles with the equations

$$u = u_0 + u_1 \cos(\alpha(\psi, t)) + u_2 \sin(\alpha(\psi, t)), \tag{5}$$

$$v = v_0 + v_1 \sin(\alpha(\psi, t)) + v_2 \sin(\alpha(\psi, t)), \tag{6}$$

with lpha the function from  $[0,24) imes [0,2\pi) o [0,2\pi)$  given by

$$\alpha(\psi,t) \equiv \pi \left[ \sin \left( \frac{\pi(t-\psi) \bmod 24}{24} - \frac{\pi}{2} \right) + 1 \right],\tag{7}$$

where t is time in units of hours UTC, and  $\psi$  gives to the time when the wind perturbations vary least with time. Need to confirm whether least or most! For each climatological diurnal wind cycle, we solve for the seven parameters  $u_0$ ,  $u_1$ ,  $u_2$ ,  $v_0$ ,  $v_1$ ,  $v_2$  and  $\psi$  using nonlinear regression.

Descriptive quantities can then be calculated from these parameters. The value of  $\alpha$  at which the winds align with the semimajor axis,  $\alpha_M$ , satisfies

$$\alpha_M = \frac{1}{2} \arctan\left(\frac{2(u_1 u_2 + v_1 v_2)}{u_1^2 + v_1^2 - u_2^2 - v_2^2}\right) \bmod \pi, \tag{8}$$

The time at which the perturbations align with the major axis  $t_M$  can then be calculated by inverting equation (7), fixing  $\psi$  to the value obtained from the nonlinear regression. The lengths of the semimajor and semiminor axes, and the angle the semimajor axis makes with lines of latitude  $\phi$ , can then be calculated from  $\alpha_M$  using the same expressions as Gille et al. (2005).

#### 29 3. Results

In this section, the methods described in section ?? are applied to Australian forecast and station
data over the months of June, July and August (austral winter) 2018. First, error is assessed on
a daily basis using the Wind Perturbation Index (WPI) at three different spatial scales. Second,
overall seasonal biases during this time period are assessed using the Climatological Wind Perturbation Index CWPI, and by comparing quantities derived from ellipses fitted to the climatological
wind perturbations. Unless otherwise stated, values throughout this section are provided to two
significant figures.

#### 237 a. Daily Comparison

Figure 2 provides the mean wind perturbation index values  $\overline{\text{wpi}}$  and confidence scores  $P(\overline{\text{WPI}} > 0)$  for the coastal station groups for  $\overline{\text{wpi}}_{\text{OA}}$ ,  $\overline{\text{wpi}}_{\text{OE}}$  and  $\overline{\text{wpi}}_{\text{EA}}$ , which represent the the Official versus ACCESS, Official versus ECMWF, and ECMWF versus ACCESS comparisons,

respectively. Values of  $\overline{\mathrm{wpi}}_{\mathrm{OA}}$  and  $\overline{\mathrm{wpi}}_{\mathrm{OE}}$  are negative for the majority of station groups and hours, and often both  $P\left(\overline{\mathrm{WPI}}_{\mathrm{OA}}>0\right)<5\%$  and  $P\left(\overline{\mathrm{WPI}}_{\mathrm{OE}}>0\right)<5\%$ . This implies that at this level of spatial aggregation, there is often high confidence that both the unedited ACCESS and ECMWF models outperform the Official forecast. The lowest  $\overline{\mathrm{wpi}}$  values of -0.9 kn occur for the NT station group at 23:00 and 00:00 UTC for both  $\overline{\mathrm{wpi}}_{\mathrm{OA}}$  and  $\overline{\mathrm{wpi}}_{\mathrm{OE}}$ , with  $\overline{\mathrm{wpi}}_{\mathrm{EA}}=0$  kn. Comparatively low values also occur at 08:00 UTC with  $\overline{\mathrm{wpi}}_{\mathrm{OA}}=\overline{\mathrm{wpi}}_{\mathrm{OE}}=-0.6$  kn, but  $\overline{\mathrm{wpi}}_{\mathrm{EA}}=0$  kn. This suggests the Official forecast may be performing particularly poorly over the NT station group.

Although Official outperforms at least one of ACCESS or ECMWF with high confidence at a few dozen times and station groups, there is only one group and time where it outperforms both. At 05:00 UTC over the South WA station group,  $\overline{\text{wpi}}_{\text{OA}} = 0.2 \text{ kn}$  and  $\overline{\text{wpi}}_{\text{OE}} = 0.1 \text{ kn}$ , both with confidence scores  $\geq 95\%$ , although the actual  $\overline{\text{wpi}}$  values are comparatively small. Note that ECMWF generally outperforms ACCESS from 10:00 - 14:00 UTC, with the South WA station group being the main exception.

Using the NT and South WA station groups as case studies, Figures 3 a) and b) provide time series of wpi<sub>OA</sub> and wpi<sub>OE</sub> for, a), the NT station group at 23:00 UTC, and b), the South WA station group at 05:00 UTC. The wpi<sub>OA</sub> and wpi<sub>OE</sub> values for the NT station group show significant temporal variability over the three month period, exceeding –2 kn on at least 10 days each, and occasionally becoming positive. The wpi values for the South WA station at 05:00 UTC also show significant temporal variability, with wpi<sub>OA</sub> and wpi<sub>OE</sub> each exceeding 1 kn on at least 9 seperate days, despite wpi<sub>OA</sub> and wpi<sub>OE</sub> being small.

Fig. 3 a) shows that there are four days where wpi<sub>OA</sub> and wpi<sub>OE</sub> are both less than -2 kn: the 8<sup>th</sup> of June and the 3<sup>rd</sup>, 9<sup>th</sup> and 10<sup>th</sup> of July. Figures 3 c) and d) show hodographs of the winds and wind perturbations, respectively, at each hour UTC for the AWS observations, Official forecast, and ACCESS and ECMWF model datasets on the 3<sup>rd</sup> of July, which provides an interest-

ing example. Figure 3 e) shows that the Official wind forecast on this day was likely based on edited ACCESS from 00:00 to 06:00 UTC, then edited ECMWF from 07:00 to 13:00 UTC, then 266 unedited ACCESS from 15:00 to 21:00 UTC. The final two hours of the forecast show the Official 267 winds acquiring a stronger east-northeasterly component than either the AWS observations, AC-CESS, or ECMWF; this rapid, exaggerated change is even clearer in the perturbation hodograph shown in Fig. 3 f). Note that at this time of year the prevailing winds throughout the NT are east-270 southeasterly, and 22:00 UTC corresponds to  $\approx$  08:30 LST in this region, so the rapid departure of the Official forecast from ACCESS at this time likely represents an edit made by a forecaster to capture boundary layer mixing processes. Figure 4 a) shows the first ten values from wind 273 soundings at Darwin Airport - the nearest station to issue vertical wind soundings - at 12:00 UTC on July 3<sup>rd</sup> and 00:00 UTC on July 4<sup>th</sup>. In both instances the winds are indeed east-southeasterly, and so the rapidly changing wind perturbations at 22:00 UTC in the Official forecast likely reflect 276 a boundary layer mixing edit that has been applied either too early, or has strengthened the southeasterly component of the winds too much. The 8th of June and 9th and 10th of July examples are all similar in this respect. 279

Considering now the South WA station group, Fig. 3 b) shows that  $wpi_{OA}$  and  $wpi_{OE}$  both exceed 1 kn on the 9<sup>th</sup> of June and the 3<sup>rd</sup> of August. Figures 3 c) and d) show hodographs of the winds and wind perturbations, respectively, at each hour UTC for the AWS observations, Official forecast, and ACCESS and ECMWF model datasets on the 9<sup>th</sup> of June, which is the more interesting example. The perturbation hodograph shows both ECMWF and ACCESS underpredicting the amplitude of the diurnal wind cycle on this day. In each dataset the 05:00 UTC perturbations are westerly to northwesterly, and given the orientation of the South WA coastline (see Fig. 1) and the fact that 05:00 UTC corresponds to  $\approx$  13:00 local solar time (LST) in this region, the perturbations likely indicate boundary layer mixing processes, rather than the land-sea breeze. Furthermore, the

AWS perturbations rapidly become northwesterly between 01:00 and 02:00 UTC,  $\approx$  09:00 - 10:00 LST, which would be about three hours after the sun has risen, consistent with a boundary layer mixing mechanism.

Figure 4 provides hodographs of wind with height throughout the first two km of the atmosphere 292 between 12:00 UTC on the 8<sup>th</sup> June and 12:00 UTC on the 9<sup>th</sup> June; the soundings were taken at 293 Perth Airport, which is the nearest station to the South WA station group to provide wind sound-294 ings. The 8<sup>th</sup> June 12:00 UTC hodograph shows surface northerlies of  $\approx$  6 kn, becoming west to northwesterlies of over 20 km 2.4 km above the surface. A forecaster basing a model edit of the following days winds on this sounding would therefore gradually strengthen the westerly compo-297 nent of the surface winds in the hours after sunrise. However, the subsequent sounding at 00:00 UTC on the 9<sup>th</sup> of June shows that the winds acquire a strong northerly component of 30 kn in the first 500 m of the atmosphere, with the final sounding indicating a strong northwesterly wind at 300 725 m persisting until 12:00 UTC. In Fig. 3 d), the Official perturbations from 04:00 to 07:00 UTC 301 show stronger westerly perturbations than either ACCESS or ECMWF, improving the amplitude of Official's diurnal wind cycle. However, the AWS perturbations are more northerly than those of 303 Official, and so the Official forecast winds have been strengthened in a slightly incorrect direction. 304 An explanation for this discrepancy is that the Official forecast for the southwest region of WA has been edited based on the June 8<sup>th</sup> 12:00 UTC Perth Airport sounding, with the winds above the 306 surface changing direction in the subsequent 12 hours. Note that the 3<sup>rd</sup> of August example is sim-307 ilar, although in this case the Official forecast slightly improves both the magnitude and direction of the 05:00 UTC wind perturbations. 309

Figure 5 presents the  $\overline{\text{wpi}}$  values and confidence scores for the Official versus ECMWF comparisons, i.e.  $\overline{\text{wpi}}_{\text{OE}}$  and  $P(\overline{\text{WPI}}_{\text{OE}} > 0)$ , for the airport stations, and airport station groups. The in Figures 2 c) and d), although they do share some similarities. Official outperforms ECMWF at 01:00 and 02:00 UTC at both the Darwin airport station and the NT station group, although ECMWF outperforms Official between 08:00 and 14:00 UTC at Darwin and Brisbane airports, and the corresponding NT and QLD station groups, with the exception of the QLD station group at 12:00 UTC where  $\overline{\text{wpi}}_{\text{OE}} = 0$ . ECMWF also outperforms Official at Hobart airport at almost all hours of the day, and at Adelaide and Canberra airports from 11:00 to 14:00 UTC.

For the remaining stations and times, only the Perth airport station at 06:00 UTC and the Mel-319 bourne airport station at 01:00 UTC exhibit  $\overline{\text{wpi}}_{OE} > 0$  with  $P(\overline{\text{WPI}}_{OE} > 0) \ge 95\%$ . However, in both cases  $\overline{\text{wpi}}_{OE} = 0.3$ , which is small compared to the maximum value of 1.0 which occurs 321 at the Darwin airport station at 02:00 UTC. Furthermore, in both cases there is no clear pattern 322 to the  $\overline{\mathrm{wpi}}_{\mathrm{OE}}$  values over the rest of the day. Given the random appearance of the  $\overline{\mathrm{wpi}}_{\mathrm{OE}}$  values, 323 the multiplicity problem (Wilks 2011, p. 178) requires care be taken before giving meaning to 324 these two examples: i.e., given that we are calculating twenty four confidence scores for eight 325 stations, then assuming WPI were uncorrelated across each station and hour we would expect to find  $0.05 \times 24 \times 8 \approx 10$  instances where  $P(\overline{WPI}_{OE} > 0) \geq 95\%$ , even if  $\overline{WPI}_{OE}$  was in fact equal 327 to zero. Comment on performance versus ACCESS. 328

For the airport station groups, ECMWF outperforms Official for the majority of station groups and times. The main exception is the Darwin airport station group, where Official outperforms ECMWF at 02:00 UTC, and there is ambiguity as to whether Official or ECMWF performs better at 01:00, 03:00 and 04:00 UTC, and from 15:00 to 22:00 UTC. In the analogous comparisons of Official and ACCESS (not shown), the airport station results are similarly noisy, although the airport station group results are slightly more favourable to Official, with Official outperforming ACCESS from 10:00 to 12:00 UTC at the Brisbane station group, and fewer occasions overall where ACCESS outperforms Official than ECMWF does.

Figure 5 shows the  $\overline{\text{wpi}}$  values and confidence scores for the ECMWF versus ACCESS comparisons, i.e.  $\overline{\text{wpi}}_{\text{EA}}$  and  $P(\overline{\text{WPI}}_{\text{EA}} > 0)$ , for the airport stations, and airport station groups. As with the Official versus ECMWF comparison in Fig. 5, the results for the airport stations are noisy, but more often than not show that ECMWF outperforms ACCESS. The results for the airport station group show ECMWF usually outperforms ACCESS, the main exceptions being the Darwin and Canberra airport station groups.

At face value, the fact that ECMWF generally outperforms ACCESS at these scales is surprising, 343 as ACCESS runs at a higher spatiotemporal resolution than ECMWF, and is calibrated for Australian conditions, so one would expect ACCESS would better resolve small scale processes like 345 the land-sea breeze and boundary layer mixing processes. However, these results are unsurprising 346 if one considers the scales at which predictable atmospheric motion occurs, and the scales being resolved by AWS, ACCESS and ECMWF. The AWS data resolves motion with time scales as low 348 as 10 minutes, and arbitrarily small spatial scales: it therefore includes highly unpredictable eddy 349 turbulence. This explains why the results for the airport stations are noisier than for the airport sta-350 tion groups or coastal station groups. Furthermore, because ACCESS runs at a higher resolution 351 than ECMWF, it includes additional scales of motion, and therefore adds additional variability to 352 the wind fields. Unless this additional variability in ACCESS is perfectly correlated with observations, the average of  $|u_{AWS} - u_A|$  will therefore increase, unless this additional variability is 354 compensated for by a reduction in bias, i.e.  $|\overline{u}_{AWS} - \overline{u}_A|$  decreases. These ideas are discussed in 355 greater detail in section 4. Note finally that the results for the Official versus ECMWF compari-356 son in Fig. 5 largely mirror those of the ECMWF versus ACCESS comparison in Fig. 5, e.g. for the Darwin airport station and station group, Official outperforms ECMWF at the same times that 358 ACCESS does, suggesting that either the Official forecast at these spatial scales is largely based on ACCESS, or that ECMWF is highly biased at these scales and times.

#### b. Seasonal Comparison

Figure 5 provides the climatological wind perturbation index values, cwpi, and confidence scores, P(CWPI > 0), for the coastal station groups for  $\text{cwpi}_{OA}$ ,  $\text{cwpi}_{OE}$  and  $\text{cwpi}_{EA}$ , which represent the Official versus ACCESS, Official versus ECMWF, and ECMWF versus ACCESS com-364 parisons, respectively. At the NT station group Official outperforms both ACCESS and ECMWF 365 at 03:00 UTC with  $\text{cwpi}_{OA} = \text{cwpi}_{OE} = 0.4$ ,  $P(\text{cwpi}_{OA} > 0) = 94\%$  and  $P(\text{cwpi}_{OE} > 0) = 93\%$ . However, both ACCESS and ECMWF outperform Official at 23:00 and 00:00 UTC, consistent 367 with the wpi results in Fig. 2. The NT station group results are discussed in more detail in section 368 4. 369 At the North WA station group at 01:00, 03:00 and 04:00, Official outperforms ACCESS with 370 confidence scores of 77, 78 and 90%, respectively; Official also outperforms ECMWF at 01:00 371 and 02:00 UTC with confidence scores above 99%. Figure 6 a) shows that ECMWF's poor performance at 01:00 and 02:00 UTC is simply due to its linear interpolation at these times, whereas 373 Official's outperformance of ACCESS at 01:00, 03:00 and 04:00 is due to ACCESS's climatolog-374 ical diurnal cycle being slightly out of phase with that of the AWS observations, and the Official forecast appearing to correct for this somewhat. Both Official and ECMWF slightly exaggerate 376 the magnitude of the climatological sea-breeze with ACCESS doing a good job in this regard. 377 At the South WA station group from 01:00 to 05:00 UTC, cwpi<sub>OE</sub> is positive with confidence 378 scores of at least 88%, although cwpi<sub>OA</sub> is negative or zero at these times. Figure 6 b) shows that 379 ECMWF underestimates the westerly perturbations at these times, with these perturbations likely 380 associated with boundary layer mixing processes, as discussed in section a. Each of Official, ACCESS and ECMWF underestimate the amplitude of the diurnal cycle between 02:00 and 10:00 UTC, including both the westerly perturbations and the southerly sea-breeze perturbations.

At the NSW station group from 17:00 to 19:00 UTC, cwpi<sub>OA</sub> and cwpi<sub>OE</sub> are at least 0.4 and 0.1 kn, respectively, with confidence scores of at least 95% and 75%, respectively. Figure 6 c) shows that these times correspond to a strange "dimple" in perturbation hodograph that is present in all four datasets. The Official hodograph closely resembles that of ACCESS, except for this dimple, which has been exaggerated relative to ACCESS. Don't know what is going on here. Figure 6 c) also shows that although ECMWF exaggerates the amplitude of the easterly sea-breeze perturbations, it captures the narrower shape of the AWS hodograph better than Official or ACCESS.

At the SA station group from 01:00 to 05:00 UTC and 09:00 to 11:00 UTC both cwpi<sub>OA</sub> and cwpi<sub>OE</sub> are positive, with maximum values of 0.4 and 0.1 kn, although confidence scores do not exceed 88% and 65% respectively. Figure 6 shows that the Official forecast captures the amplitude of the perturbations from 01:00 to 05:00 UTC almost perfectly, matching the amplitude of the AWS perturbations better than both ACCESS and ECMWF. However, the Official diurnal cycle is slightly out of phase with the AWS cycle during this period, explaining why Official only slightly outperforms ACCESS in the results of Figures 5 a) and b).

While the cwpi values and confidence scores of Fig. 5 provide detailed information on which
dataset's climatological diurnal cycle best matches those of the AWS observations, cwpi on it's
own reveals little about the structure of the diurnal cycle, and provides little insight into forecast
accuracy could be improved. Note that the hodographs in Fig. 6 are roughly elliptical in shape,
suggesting that descriptive quantities can be estimated by fitting equations (5) and (6) to the zonal
and meridional climatological perturbations, then calculating these quantities from the fit, as described in section 2.

Figure 7 provides the  $R^2$  values for the fits of the zonal and meridional perturbations to equations (5) and (6), respectively. The fit performs best at the coastal station group spatial scale, with  $R^2$  generally above 95%. It also performs well at the airport station and airport station group

scales, with a few exceptions, including the ACCESS and Official meridional perturbations at the
Canberra airport station group, and the ECMWF zonal perturbations at Melbourne airport.

The ellipse fits are used to derive four descriptive quantities: amplitude (half the length of the 410 semi-major axis), eccentricity, orientation (the angle the semi-major axis makes with lines of latitude) and the time of the peak in the diurnal cycle (the time at which the perturbations align with 412 the semi-major axis, ignoring translational coefficients). Figure 8 provides these four quantities 413 for each dataset and location across the three spatial scales. A variety of structural differences are apparent at a number of locations and scales. For example, Fig. 8 a) shows that at Brisbane airport, the amplitude of the AWS diurnal cycle is at least 1 kn greater than Official, ACCESS 416 and ECMWF, and Fig. 8 c) shows that the orientation of the AWS diurnal cycle hodograph is at least 20 degrees (anti-clockwise) from the other datasets. Figures 9 a) and b) show hodographs of 418 the Brisbane airport perturbation climatology and ellipse fit, respectively. Although the ellipse fit 419 suppresses some of the asymmetric details, it captures the amplitudes and orientations of the real 420 climatological diurnal cycles well. In this case the results show that the average AWS sea-breeze 421 approaches from the northeast, whereas the forecast and model sea-breezes approach more from 422 the east-northeast. To check whether this just represents a direction bias of the Brisbane Airport 423 station, Fig. 8 shows the climatological perturbations at the nearby Spitfire Channel station (see 424 Fig. ?? for the location of this station, and other stations referred to in this section). While the 425 amplitude bias is smaller at Spitfire Channel than Brisbane Airport, the directional bias is at least 426 as high; a similar directional bias is evident at the nearby Inner Beacon station, although the bias 427 is smaller than at Spitfire Channel and Brisbane Airport. Thus, the directional bias in Official, 428 ACCESS and ECMWF at these stations is likely genuine, and not just a consequence of biased 429 AWS observations. Figure 1 x) shows there are two small islands to the east of Brisbane airport; the more northwesterly orientation of the Brisbane Airport sea-breeze suggests these islands may 431

be channelling winds between the east coast of Brisbane and the west coasts of these islands, and
that this local effect is not being captured in Official, ACCESS or ECMWF.

Another example is the Hobart Airport station. Figure 8 c) shows that the ellipse fits for the 434 AWS perturbations are oriented 31, 35 and 62 degrees anti-clockwise from the ECMWF, Official and ACCESS ellipse fits, respectively. Figures 7 a) and b) show that the ellipse fit for the AWS perturbations at Hobart airport only achieve  $R^2$  values of 59% and 68% for the u and v components, 437 respectively, although figures 9 d) and e) show that the fit still captures the orientation accurately; 438 the deficiency is more with the amplitude of the AWS diurnal cycle. Figure 7 c) shows the climatological perturbations at the Hobart (city) station, which also show a large difference in orientation 440 between ACCESS and AWS. Given the timing of the westerly perturbations in ACCESS, and the fact that the prevailing winds around Tasmania are Hobart, these results suggest that ACCESS is exaggerating the boundary layer mixing processes involved in the diurnal cycle, whereas ECMWF 443 better captures the southerly sea-breeze component of the cycle.

The South WA station group also provides an interesting example. Here the ACCESS and 445 Official ellipse fits are oriented at least 49 degrees anti-clockwise from those of AWS and ECMWF, 446 and the time of the peak in the diurnal cycles of ACCESS and Official is at least 4.3 hours earlier 447 than AWS and ECMWF. This occurs because eccentricity values are low for this station group, and Figure 6 b) shows that the westerly perturbations associated with boundary layer mixing are 449 slightly faster than the corresponding southerly sea-breeze perturbations, which peak later, for 450 both ACCESS and Official, but slightly slower for ECMWF and Official. A similar issue affects the VIC station group, explaining why the AWS ellipse fit is oriented at least 49 degrees anti-452 clockwise from those of the other datasets. 453

Finally, figure 8 suggests that at the Darwin Airport, Darwin Airport station group, and NT station group, the AWS wind perturbations align with the semi-major axis after those of the other

datasets, and in the case of the NT station group alignment occurs at least 2.3 hours later; furthermore, the amplitude of the Official ellipse fit is in each case higher than those of the other
datasets. "Alignment" is probably the wrong word here. Figure 10 shows that these biases are
indeed evident in the perturbation climatologies themselves, with the exception of the Darwin
Airport amplitude bias, where the asymmetric hodograph shapes lead to the ellipse fit underestimating the amplitude of the AWS diurnal cycle Needs to be clarified to better distinguish between
"ellipse" amplitude and diurnal cycle amplitude. Furthermore, should we interpret the NT station
group results as genuine evidence of a timing bias?

#### 464 4. Discussion

The most important results of section 3 to explain are the substantial changes in the performance of the Official forecast at the different spatial and temporal scales. To do this in a systematic way, consider first the zonal components of the AWS and Official wind perturbations, denoted by  $u_{\text{AWS}}$  and  $u_{\text{O}}$  respectively. Considering just the values at a particular hour UTC, at a particular station, over the entire June, July, August time period, the mean square error  $\text{mse}(u_{\text{AWS}}, u_{\text{O}}) = \overline{(u_{\text{AWS}} - u_{\text{O}})^2}$  can be decomposed

$$\operatorname{mse}(u_{\mathrm{AWS}}, u_{\mathrm{O}}) = \underbrace{\operatorname{var}(u_{\mathrm{AWS}}) + \operatorname{var}(u_{\mathrm{O}}) - 2 \cdot \operatorname{covar}(u_{\mathrm{AWS}}, u_{\mathrm{O}})}_{\operatorname{var}(u_{\mathrm{AWS}} - u_{\mathrm{O}})} + \underbrace{\left(\overline{u}_{\mathrm{AWS}} - \overline{u}_{\mathrm{O}}\right)^{2}}_{\operatorname{bias}^{2}}$$
(9)

where var, covar and over-bars denote the sample variance, covariance and mean respectively. The first three terms are just the variance of  $u_{AWS} - u_{O}$ , whereas the last term is the square of the bias between  $u_{AWS}$  and  $u_{O}$ . This decomposition can also be applied to wind perturbations that have first been spatially averaged over a station group, and to  $mse(u_{AWS}, u_{E})$  and  $mse(u_{AWS}, u_{A})$ , where  $u_{E}$  and  $u_{A}$  are the ECMWF and ACCESS zonal perturbations, respectively.

- Figure 11 shows each term in the mean square error decomposition of equation 9 for both
- mse  $(u_{AWS}, u_{O})$  and mse  $(u_{AWS}, u_{E})$ , where  $u_{E}$  denotes the ECMWF zonal perturbations, for the
- Darwin Airport, Darwin station group, and NT station groups.

#### 5. Conclusion

We have

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- 509 1175/1520-0442(1995)008(0336:TSCIAI)2.0.CO;2.

## 510 LIST OF FIGURES

511 512	Fig. 1.	Locations of the automatic weather stations used in this study. Stars indicate capital city airport stations. Height and depth shading intervals every 200 and 1000 m, respectively		26
513 514 515 516 517 518	Fig. 2.	Heatmaps of $\overline{WPI}$ values and confidence scores for each coastal station group and hour of the day: a) and b), Official versus ACCESS, c) and d) Official versus ECMWF, e) and f) ECMWF versus ACCESS. Positive $\overline{WPI}$ values mean that the former dataset in each pair is on average closer to observations than the latter dataset. Confidence scores provide the probability the population $\overline{WPI}$ is greater than zero. Values within the heatmaps are accurate to two significant figures.		27
519 520 521 522	Fig. 3.	Time series, a) and b), of $\overline{wpi}_{OA}$ and $\overline{wpi}_{OE}$ for, a), the NT station group at 23:00 UTC, and b), the south WA station group at 05:00 UTC. Hodographs, c) to f), showing change in winds, c) and e), and wind perturbations, d) and f), for the NT station group, c) and d), and south WA station group, e) and f)		28
523 524	Fig. 4.	Hodographs showing change in winds with height at, a), Darwin Airport, and b), Perth Airport	•	29
525 526	Fig. 5.	The $\overline{wpi}_{OE}$ (Official versus ECMWF comparison) values, a) and c), and confidence scores, b) and d), for the airport stations, a) and b), and airport station groups, c) and d), respectively.		30
527	Fig. 6.	Climatological hodographs		33
528 529 530	Fig. 7.	Could also provide an analogous figure showing the use of the function $\alpha$ provides a significant improvement over the basic ellipse fit - or instead just quote some numbers? Or maybe these figures are entirely unnecessary?		34
531 532 533 534 535 536	Fig. 8.	Ellipse fits. If we were to include any analysis for alternative time periods (e.g. summer 2017/18 for contrast; or could do 18/19 if I were to go back to BoM to get the data) a copy of this figure could be a good choice. Could explain changes in diurnal cycle properties, e.g. amplitude, with seasonal changes to background winds, heating, etc. Note some issues with timing and amplitude values due to asymmetry - could instead just show eccentricity and orientation values?		35
537	Fig. 9.	Ellipse fits. Could instead just provide one example		36
538	Fig. 10.	Ellipse fits. Could instead not include the ellipses		37
539 540	Fig. 11.	Actual perturbation standard deviation values. Note that official performs the worst at this scale!		38
541 542	Fig. 12.	Actual perturbation standard deviation values. Note that official performs the worst at this scale!		39

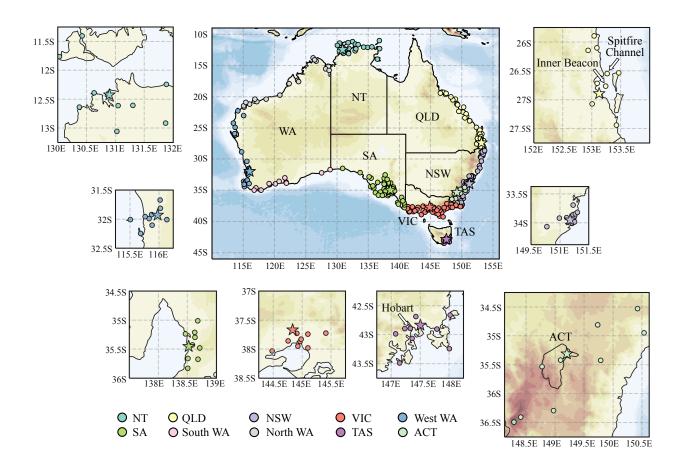


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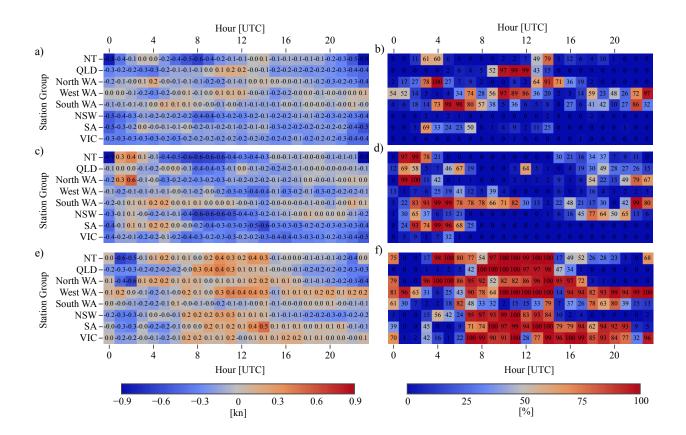


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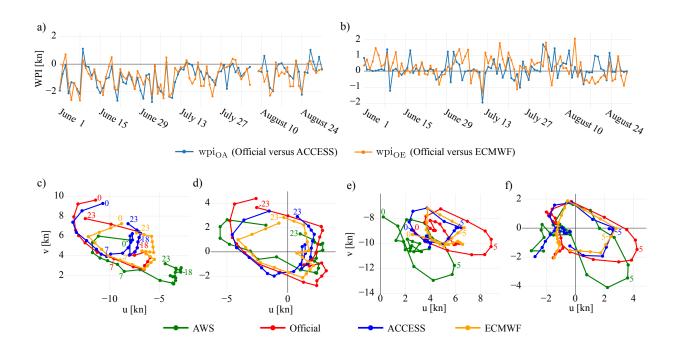


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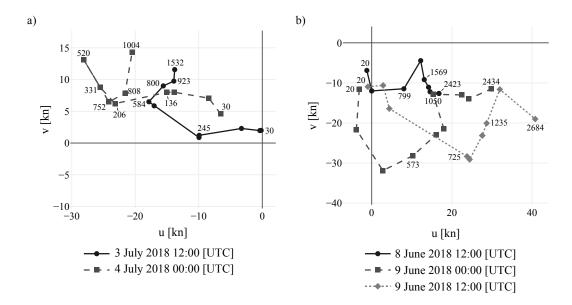


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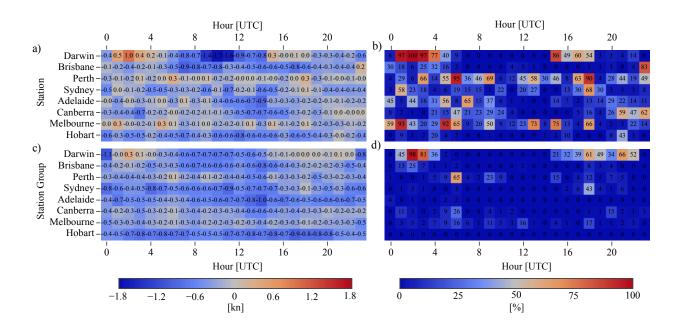
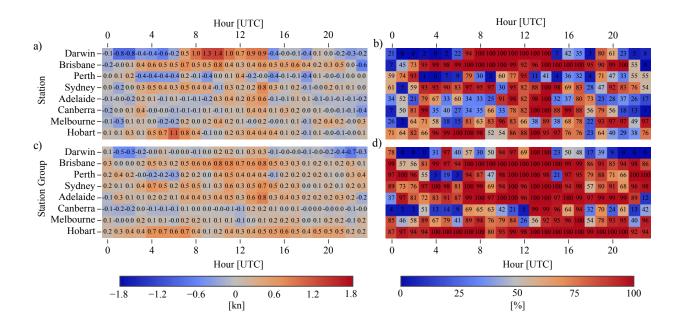
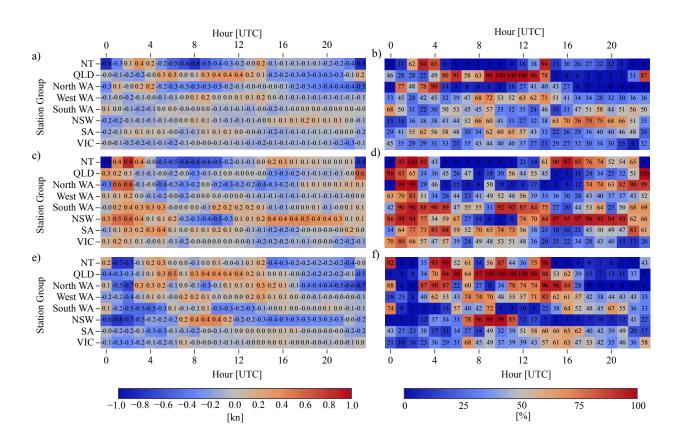


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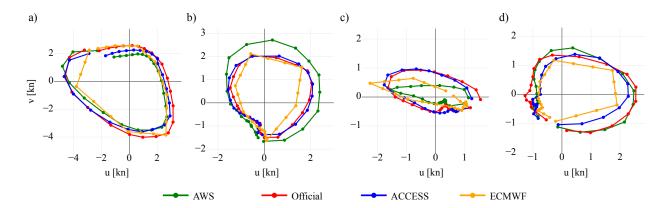


FIG. 6. Climatological hodographs.

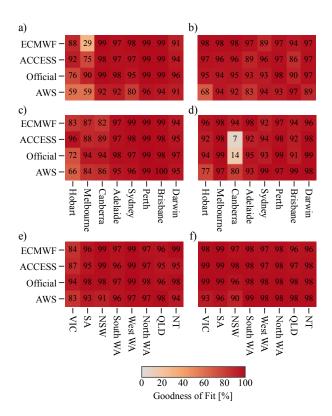


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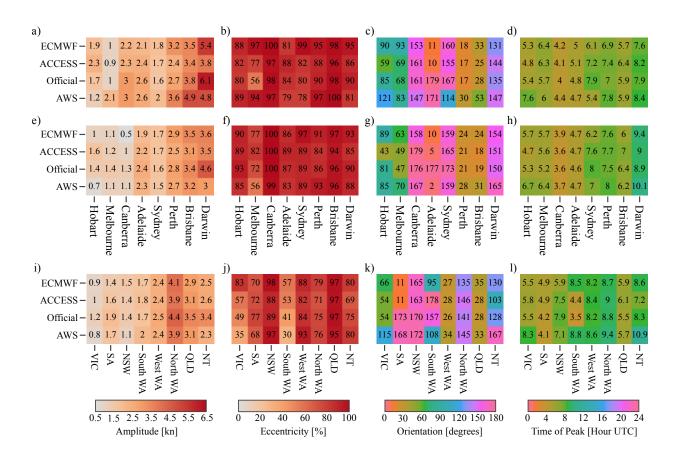


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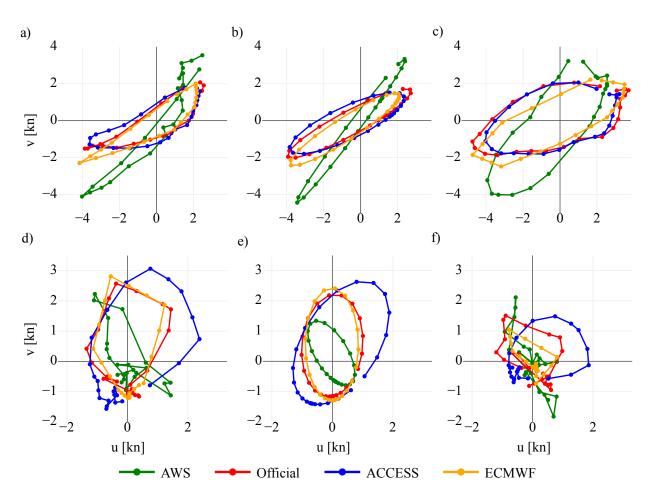


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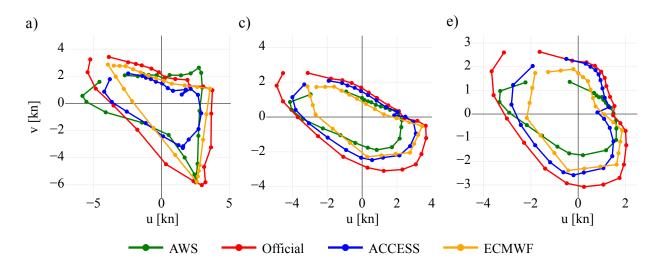


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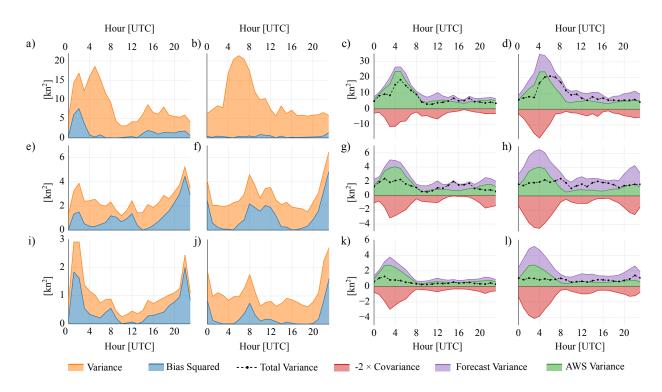


FIG. 11. Actual perturbation standard deviation values. Note that official performs the worst at this scale!

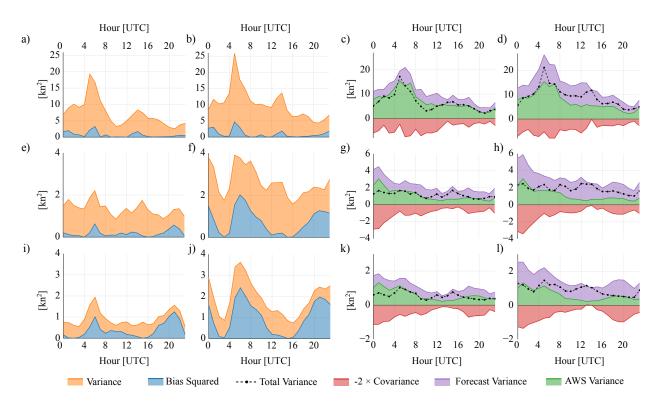


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