

# Relazione ROOT 2025

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## 1 Introduzione

Lo scopo di questo esperimento è studiare, attraverso la simulazione di un campione di particelle di vario tipo, le proprietà di una particella ignota e instabile che decade troppo velocemente per poter essere osservata direttamente. Poiché la particella iniziale è neutra, i prodotti del decadimento avranno carica discorde; inoltre, la massa invariante segue una distribuzione gaussiana con media pari alla massa della particella madre e deviazione standard pari alla sua larghezza di risonanza. Di conseguenza, si misurano le masse invarianti dal campione di particelle che contiene anche quelle derivanti dal decadimento separando per coppie di carica concorde e discorde, e si isola l'effetto delle sole particelle figlie rimuovendo il rumore di fondo dai dati. Per ridurre il fondo più efficientemente si può ripetere l'analisi considerando il campione composto dalle sole particelle ottenibili teoricamente dal decadimento.

## 2 Struttura del Codice

Il codice che gestisce le particelle è stato organizzato creando tre classi: `ParticleType`, `ResonanceType` e `Particle`. Come il nome suggerisce, le prime due vogliono rappresentare dei tipi di particelle (protone, antiprotone, kaone, pione, ...), mentre la terza rappresenta una particella di per sé. `ParticleType` descrive un tipo di particella che possiede una massa e una carica, e alla quale viene assegnato un nome. La classe, inoltre, espone anche due metodi virtuali, `GetWidth` e `Print`, che possono essere sovrascritti dalle classi figlie per implementare la larghezza di risonanza di una particella o per modificare la stampa a schermo delle proprietà della particella. `ResonanceType` fa uso di questa possibilità ereditando pubblicamente da `ParticleType`, in quanto vuole rappresentare un tipo di particella che può decadere e che, di conseguenza, oltre alle proprietà di una particella base, necessita anche della descrizione della sua larghezza di risonanza. La classe `Particle`, infine, funge da rappresentazione di una particella di un dato tipo con una quantità di moto. Sapendo che nel programma il numero di tipi di particelle sarà minuscolo rispetto al numero di particelle che verranno create si è preferito utilizzare, rispetto all'ereditarietà, che avrebbe portato a una ripetizione degli stessi dati (nome, massa, carica e larghezza di risonanza)

fra molte particelle, uno `std::vector` statico di puntatori a `ParticleType` (che di conseguenza, per il polimorfismo dinamico, possono puntare anche a `ResonanceType`). Quest'ultimo racchiude tutti i tipi di particelle che sono presenti nella simulazione, i quali vengono aggiunti a run-time: si è preferito questo approccio per accomodare anche l'eventualità in cui non si dovesse conoscere il numero di tipi di particelle a compile-time, come avverrebbe se questi volessero essere specificati in un file invece che nel codice. In questo modo ad ogni particella saranno associati solo tre float, per descrivere la quantità di moto, e un indicatore del tipo di particella, per il quale è stato scelto un int, che funge da indice nell'`std::vector` di tipi di particelle.

### 3 Generazione

Il codice prevede la generazione di  $10^5$  eventi, ciascuno dei quali considera molte particelle suddivise in un numero limitato di tipi. Nel nostro caso, in ogni evento vengono generate, una alla volta, 100 particelle che possono appartenere a sette tipi differenti, ognuno dei quali ha una fissa percentuale di probabilità di essere generato: le proporzioni prevedono 40% di pioni positivi, 40% di pioni negativi, 5% di kaoni positivi, 5% di kaoni negativi, 4.5% di protoni, 4.5% di antiprotoni e 1% di una particella instabile che chiamiamo  $K^*$ , che decade in una coppia di carica discorde composta da un pione e un kaone, con uguale probabilità di ottenere coppie  $\pi + K^-$  o  $\pi - K^+$ . Ad ogni particella generata sono associate sia proprietà di base (nome, massa, carica, larghezza di risonanza) sia proprietà cinematiche, cioè una quantità di moto sulle tre dimensioni, che può variare da particella a particella e da evento a evento. Per generare quest'impulso in maniera casuale abbiamo utilizzato i metodi Monte Carlo implementati da ROOT per generare una distribuzione esponenziale con media 1 per il modulo, due distribuzioni uniformi, rispettivamente tra 0 e  $2\pi$  e tra 0 e  $\pi$ , per gli angoli phi (azimutale) e theta (polare), che definiscono la direzione dell'impulso nello spazio, e abbiamo poi convertito questi dati da coordinate sferiche a cartesiane, ottenendo le tre componenti Px, Py e Pz della quantità di moto.

### 4 Analisi

L'istogramma della distribuzione dei tipi delle particelle generate segue coerentemente la distribuzione a tratti costanti che ci si aspetta: la probabilità della creazione di ciascun tipo corrisponde alla proporzione in cui è effettivamente osservato (Tab. 1). La distribuzione degli impulsi è coerente con un'esponenziale, e al fit corrisponde correttamente un  $\tilde{\chi}^2 \simeq 1$  (Tab. 2). Gli angoli polari e azimutali sono distribuiti uniformemente nei domini previsti, come confermano i fit a cui corrispondono nuovamente dei  $\tilde{\chi}^2 \simeq 1$  (Tab. 2). Questi quattro grafici sono riportati in Fig. 1.

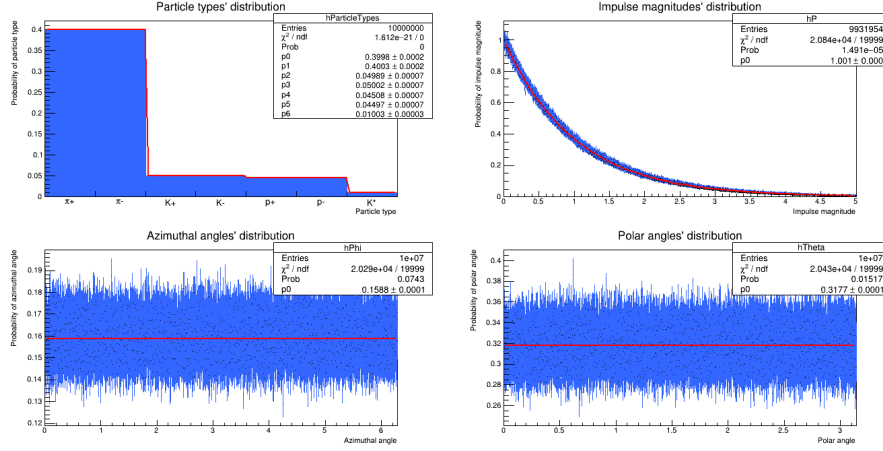


Figure 1: In alto a sx la distribuzione dei tipi di particelle generati, in alto a dx la distribuzione del modulo dell'impulso, in basso le distribuzioni degli angoli azimutale ( $\phi$ ) e polare ( $\theta$ ).

Per la distribuzione della massa invariante relativa alle coppie di figlie di  $K^*$  si osserva, come ci si aspetta, una gaussiana con media e deviazione standard pari rispettivamente a massa e lunghezza di risonanza della  $K^*$  (Tab. 3). Essendo la  $K^*$  molto instabile e rara, per estrarre il suo segnale è occorso seguire un approccio per sottrazione: a partire dalla distribuzione della massa invariante delle particelle generate, rimuovendo il rumore di fondo si riesce a osservare il segnale della particella di risonanza. Ovvero, dalla distribuzione della massa invariante delle particelle di segno discorde, che comprendono le combinazioni accidentali (fondo) e quelle effettivamente generate a partire dal decadimento di  $K^*$ , è stata rimossa quella della massa invariante delle particelle di segno concorde, che possono essere solo fondo ( $K^*$  decade in  $\pi^+$  e  $K^-$  o in  $\pi^-$  e  $K^+$ ). Per un'ulteriore distinzione più efficace è stata eseguita la stessa operazione, ma prendendo in considerazione solo i pioni  $\pi$  e i kaoni  $K$ , poiché  $K^*$  può decadere solo in questi, e quindi riducendo il rumore di fondo (i protoni  $P$  sono circa il 9% delle particelle generate). Le distribuzioni risultanti, analogamente alla precedente (tutte in Fig. 2), corrispondono a delle gaussiane la cui media risulta essere la massa della  $K^*$ , e la cui sigma la larghezza di risonanza: si è quindi riuscito ad estrarre il segnale dalle distribuzioni delle masse invarianti (Tab. 3).

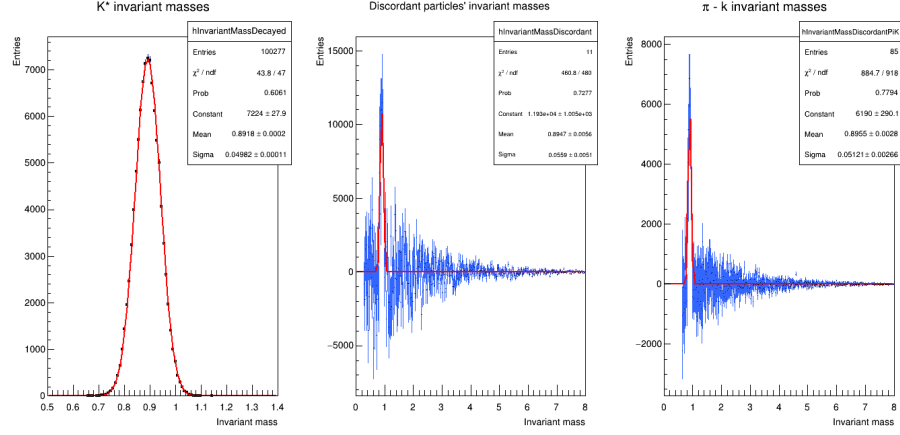


Figure 2: A sinistra la distribuzione delle masse invarianti solo fra particelle figlie, al centro la differenza degli istogrammi di masse invarianti fra particelle discordi e concordi, a destra come al centro ma solo considerando coppie  $\pi K$

Specie	Occorrenze osservate ( $10^6$ )	Occorrenze attese ( $10^6$ )
$\pi^+$	$3.998 \pm 0.002$	$4.0000 \pm 0.0015$
$\pi^-$	$4.003 \pm 0.002$	$4.0000 \pm 0.0015$
$K^+$	$0.4989 \pm 0.0007$	$0.5000 \pm 0.0007$
$K^-$	$0.5002 \pm 0.0007$	$0.5000 \pm 0.0007$
$p^+$	$0.4508 \pm 0.0007$	$0.4500 \pm 0.0007$
$p^-$	$0.4497 \pm 0.0007$	$0.4500 \pm 0.0007$
$K^*$	$0.1003 \pm 0.0003$	$0.1000 \pm 0.0003$

Table 1: Tabella delle occorrenze osservate e attese dei diversi tipi di particelle.

Distribuzione	Parametro del fit	$\chi^2$	DOF	$\tilde{\chi}^2$
Fit a distribuzione angolo $\phi$ (azi)	$0.15883 \pm 0.00005$	20288.6	19999	1.01
Fit a distribuzione angolo $\theta$ (pol)	$0.31766 \pm 0.00010$	20434.6	19999	1.02
Fit a distribuzione modulo impulso (expo)	$1.0007 \pm 0.0002$	20844.9	19999	1.04

Table 2: Risultati dei fit per diverse distribuzioni.

Distribuzione e fit	$\mu$	$\sigma$	Ampiezza	$\tilde{\chi}^2$
Massa invariante vere $K^*$	$0.89185 \pm 0.00016$	$0.04982 \pm 0.00011$	$7220 \pm 30$	0.932
Massa invariante ottenuta da differenza delle combinazioni di carica discorde e concorde	$0.895 \pm 0.006$	$0.056 \pm 0.005$	$(11.9 \pm 1.0) \cdot 10^3$	0.960
Massa invariante ottenuta da differenza delle combinazioni di carica discorde e concorde $\pi K$	$0.051 \pm 0.003$	$0.051 \pm 0.003$	$(6.2 \pm 0.3) \cdot 10^3$	0.964

Table 3: Parametri di fit per le masse invarianti in diverse combinazioni.

# Selected files

## 11 printable files

ParticleType.hpp  
ParticleType.cpp  
ResonanceType.hpp  
ResonanceType.cpp  
Particle.hpp  
Particle.cpp  
compile.C  
ParticleGenerator.cpp  
Analysis.cpp  
testParticleType.cpp  
testParticle.cpp

## ParticleType.hpp

```
1  #ifndef PARTICLE_TYPE_HPP
2  #define PARTICLE_TYPE_HPP
3
4  namespace kape {
5  class ParticleType
6  {
7  public:
8      explicit ParticleType(const char* name, double mass, int charge);
9      explicit ParticleType();
10     virtual ~ParticleType();
11
12     const char* GetName() const;
13     double GetMass() const;
14     int GetCharge() const;
15
16     virtual double GetWidth() const;
17     virtual void Print() const;
18
19 private:
20     const char* fName;
21     const double fMass;
22     const int fCharge;
23 };
24 } // namespace kape
25
26 #endif
```

## ParticleType.cpp

```
1  #include "ParticleType.hpp"
2  #include <iostream>
3  #include <stdexcept>
4
5  namespace kape {
6  ParticleType::ParticleType(const char* name, double mass, int charge)
7      : fName{name}
```

```
8      , fMass{mass}
9      , fCharge{charge}
10 {
11     if (mass <= 0.) {
12         throw std::invalid_argument{"mass can't be negative or null"};
13     }
14
15     if (name == nullptr) {
16         throw std::invalid_argument{"name can't point to nullptr"};
17     }
18 }
19
20 ParticleType::ParticleType()
21     : ParticleType("", 1, 0)
22 {}
23
24 ParticleType::~~ParticleType()
25 {}
26
27 const char* ParticleType::GetName() const
28 {
29     return fName;
30 }
31
32 double ParticleType::GetMass() const
33 {
34     return fMass;
35 }
36
37 int ParticleType::GetCharge() const
38 {
39     return fCharge;
40 }
41
42 double ParticleType::GetWidth() const
43 {
44     return 0.;
45 }
46
47
48 void ParticleType::Print() const
49 {
50     std::cout << "Name:\t" << fName << '\n';
51     std::cout << "Mass:\t" << fMass << '\n';
52     std::cout << "Charge:\t" << fCharge << '\n';
53 }
54 } // namespace kape
```

## ResonanceType.hpp

```
1 #ifndef RESONANCE_TYPE_HPP
2 #define RESONANCE_TYPE_HPP
```

```
3 #include "ParticleType.hpp"
4
5 namespace kape {
6 class ResonanceType : public ParticleType
7 {
8 public:
9     explicit ResonanceType(const char* name, double mass, int charge,
10                             double width);
11     explicit ResonanceType();
12
13     virtual double GetWidth() const override;
14     void Print() const override;
15
16 private:
17     const double fWidth;
18 };
19 } // namespace kape
20
21 #endif
```

## ResonanceType.cpp

```
1 #include "ResonanceType.hpp"
2 #include <iostream>
3 #include <stdexcept>
4
5 namespace kape {
6 ResonanceType::ResonanceType(const char* name, double mass, int charge,
7                               double width)
8     : ParticleType(name, mass, charge)
9     , fWidth{width}
10 {
11     if (width <= 0) {
12         throw std::invalid_argument{"width can't be negative or null"};
13     }
14 }
15
16 ResonanceType::ResonanceType()
17     : ParticleType()
18     , fWidth{}
19 {}
20
21 double ResonanceType::GetWidth() const
22 {
23     return fWidth;
24 }
25
26 void ResonanceType::Print() const
27 {
28     ParticleType::Print();
29     std::cout << "Width:\t" << fWidth << '\n';
30 }
```



```
31 } // namespace kape
32
```

## Particle.hpp

```
1  #ifndef PARTICLE_HPP
2  #define PARTICLE_HPP
3
4  #include "ParticleType.hpp"
5  #include "ResonanceType.hpp"
6  #include <vector>
7
8  namespace kape {
9  class Particle
10 {
11 public:
12     static int GetNParticleType();
13     static void AddParticleType(const char* name, double mass, int charge,
14                                double width = 0);
15     static void PrintParticleType();
16
17     Particle(const char* name = DEFAULT_NAME, double px = 0., double py = 0.,
18             double pz = 0.);
19     int Decay2body(Particle& dau1, Particle& dau2) const;
20     int GetIndex() const;
21     double GetPx() const;
22     double GetPy() const;
23     double GetPz() const;
24     double GetMass() const;
25     double GetEnergy() const;
26     double GetCharge() const;
27     void SetIndex(int index);
28     void SetIndex(const char* name);
29     void SetP(double px, double py, double pz);
30     double InvMass(Particle const& p) const;
31
32     void Print() const;
33
34 private:
35     static inline const char* DEFAULT_NAME{"DEFAULT_NAME"};
36     static inline std::vector<ParticleType*> fParticleType{};
37     //returns the index of the first particle type named "name"
38     //if not found it returns the number of particle types
39     static int FindParticle(const char* name);
40     void Boost(double bx, double by, double bz);
41
42     int fIndex;
43     double fPx;
44     double fPy;
45     double fPz;
46 };
47
```

```
48 } // namespace kape
49
50 #endif
```

## Particle.cpp

```
1  #include "Particle.hpp"
2  #include <cmath>
3  #include <cstdlib> //for RAND_MAX
4  #include <cstring> //for strcmp
5  #include <iostream>
6  #include <stdexcept>
7
8  namespace kape {
9  int Particle::GetNParticleType()
10 {
11     return static_cast<int>(fParticleType.size());
12 }
13
14 Particle::Particle(const char* name, double px, double py, double pz)
15     : fPx{px}
16     , fPy{py}
17     , fPz{pz}
18 {
19     fIndex = FindParticle(name);
20     // not found
21     if (fIndex == static_cast<int>(fParticleType.size())
22         && name != DEFAULT_NAME) {
23         std::cout << name << " is not a defined type of particle\n";
24         throw std::runtime_error{"it is not a defined type of particle. Check "
25                                 "terminal output for the name."};
26     }
27 }
28
29 int Particle::Decay2body(Particle& dau1, Particle& dau2) const
30 {
31     if (GetMass() == 0.0) {
32         printf("Decayment cannot be preformed if mass is zero\n");
33         return 1;
34     }
35
36     double massMot = GetMass();
37     double massDau1 = dau1.GetMass();
38     double massDau2 = dau2.GetMass();
39
40     if (fIndex > -1) { // add width effect
41
42         // gaussian random numbers
43
44         float x1, x2, w, y1;
45
46         double invnum = 1. / RAND_MAX;
```

```
47     do {
48         x1 = 2.0 * rand() * invnum - 1.0;
49         x2 = 2.0 * rand() * invnum - 1.0;
50         w = x1 * x1 + x2 * x2;
51     } while (w >= 1.0);
52
53     w = sqrt((-2.0 * log(w)) / w);
54     y1 = x1 * w;
55
56     massMot += fParticleType[fIndex]->GetWidth() * y1;
57 }
58
59 if (massMot < massDau1 + massDau2) {
60     printf("Decayment cannot be preformed because mass is too low in this "
61           "channel\n");
62     return 2;
63 }
64
65 double pout =
66     sqrt(
67         (massMot * massMot - (massDau1 + massDau2) * (massDau1 + massDau2))
68         * (massMot * massMot - (massDau1 - massDau2) * (massDau1 - massDau2))
69         / massMot * 0.5;
70
71 double norm = 2 * M_PI / RAND_MAX;
72
73 double phi = rand() * norm;
74 double theta = rand() * norm * 0.5 - M_PI / 2.;
75 dau1.SetP(pout * sin(theta) * cos(phi), pout * sin(theta) * sin(phi),
76           pout * cos(theta));
77 dau2.SetP(-pout * sin(theta) * cos(phi), -pout * sin(theta) * sin(phi),
78           -pout * cos(theta));
79
80 double energy = sqrt(fPx * fPx + fPy * fPy + fPz * fPz + massMot * massMot);
81
82 double bx = fPx / energy;
83 double by = fPy / energy;
84 double bz = fPz / energy;
85
86 dau1.Boost(bx, by, bz);
87 dau2.Boost(bx, by, bz);
88
89 return 0;
90 }
91
92 void Particle::AddParticleType(const char* name, double mass, int charge,
93                               double width)
94 {
95     int index = FindParticle(name);
96     if (index == GetNParticleType()) // it's a new Particle Type
97     {
98         if (width == 0.) { // it's a ParticleType
99             fParticleType.push_back(new ParticleType(name, mass, charge));
```

```
100     } else {
101         fParticleType.push_back(new ResonanceType(name, mass, charge, width));
102     }
103 } else // we're updating a Particle Type
104 {
105     delete fParticleType[index];
106     if (width == 0.) { // it's a ParticleType
107         fParticleType[index] = new ParticleType(name, mass, charge);
108     } else {
109         fParticleType[index] = new ResonanceType(name, mass, charge, width);
110     }
111 }
112 }
113
114 void Particle::PrintParticleType()
115 {
116     std::cout << "Particle types:\n";
117     for (auto const& p : fParticleType) {
118         p->Print();
119     }
120 }
121
122 int Particle::GetIndex() const
123 {
124     return fIndex;
125 }
126 double Particle::GetPx() const
127 {
128     return fPx;
129 }
130 double Particle::GetPy() const
131 {
132     return fPy;
133 }
134 double Particle::GetPz() const
135 {
136     return fPz;
137 }
138
139 double Particle::GetMass() const
140 {
141     return fParticleType[fIndex]->GetMass();
142 }
143
144 double Particle::GetEnergy() const
145 {
146     double m{fParticleType[fIndex]->GetMass()};
147     return std::sqrt(m * m + fPx * fPx + fPy * fPy + fPz * fPz);
148 }
149
150 double Particle::GetCharge() const
151 {
152     return fParticleType[fIndex]->GetCharge();
```

```
153 }
154
155 void Particle::SetIndex(int index)
156 {
157     if (index >= GetNParticleType() || index < 0) {
158         std::cout << "it is not a defined type of particle\n";
159         throw std::runtime_error{"it is not a defined type of particle."};
160     }
161
162     fIndex = index;
163 }
164
165 void Particle::SetIndex(const char* name)
166 {
167     SetIndex(FindParticle(name));
168 }
169
170 void Particle::SetP(double px, double py, double pz)
171 {
172     fPx = px;
173     fPy = py;
174     fPz = pz;
175 }
176
177 double Particle::InvMass(Particle const& p) const
178 {
179     return sqrt(std::pow(GetEnergy() + p.GetEnergy(), 2)
180                 - (std::pow(fPx + p.fPx, 2) + std::pow(fPy + p.fPy, 2)
181                   + std::pow(fPz + p.fPz, 2)));
182 }
183
184 void Particle::Print() const
185 {
186     std::cout << "Index: " << fIndex << '\n';
187     std::cout << "Name: " << fParticleType[fIndex]->GetName() << '\n';
188     std::cout << "P = (" << fPx << ", " << fPy << ", " << fPz << ") " << '\n';
189 }
190
191 int Particle::FindParticle(const char* name)
192 {
193     int i{0};
194     for (; i != static_cast<int>(fParticleType.size()); ++i) {
195         if (std::strcmp(fParticleType[i]->GetName(), name) == 0) {
196             break;
197         }
198     }
199     return i;
200 }
201
202 void Particle::Boost(double bx, double by, double bz)
203 {
204     double energy = GetEnergy();
205 }
```

```

206 // Boost this Lorentz vector
207 double b2      = bx * bx + by * by + bz * bz;
208 double gamma   = 1.0 / sqrt(1.0 - b2);
209 double bp      = bx * fPx + by * fPy + bz * fPz;
210 double gamma2  = b2 > 0 ? (gamma - 1.0) / b2 : 0.0;
211
212 fPx += gamma2 * bp * bx + gamma * bx * energy;
213 fPy += gamma2 * bp * by + gamma * by * energy;
214 fPz += gamma2 * bp * bz + gamma * bz * energy;
215 }
216 } // namespace kape

```

## compile.C

```

1 void compile(){
2     gROOT->LoadMacro("ParticleType.cpp+");
3     gROOT->LoadMacro("ResonanceType.cpp+");
4     gROOT->LoadMacro("Particle.cpp+");
5     gROOT->LoadMacro("ParticleGenerator.cpp+");
6 }

```

## ParticleGenerator.cpp

```

1 #include "Particle.hpp"
2 #include "TFile.h"
3 #include "TH1.h"
4 #include "TRandom.h"
5 #include "TRandom3.h"
6 #include <array>
7 #include <cmath> //for M_PI
8 #include <iostream>
9
10 enum ParticlesIndexes
11 {
12     PI_PLUS = 0,
13     PI_MINUS,
14     K_PLUS,
15     K_MINUS,
16     P_PLUS,
17     P_MINUS,
18     K_STAR
19 };
20
21 void RunSimulation()
22 {
23     kape::Particle::AddParticleType("pi+", 0.13957, +1); // pione +
24     kape::Particle::AddParticleType("pi-", 0.13957, -1); // pione -
25     kape::Particle::AddParticleType("K+", 0.49367, +1); // kaone +
26     kape::Particle::AddParticleType("K-", 0.49367, -1); // kaone -
27     kape::Particle::AddParticleType("p+", 0.93827, +1); // protone
28     kape::Particle::AddParticleType("p-", 0.93827, -1); // antiprotone
29     kape::Particle::AddParticleType("K*", 0.89166, 0, 0.050); // K*

```

```
30
31 // for a longer period of the random number generator
32 delete gRandom;
33 gRandom = new TRandom3();
34 gRandom->SetSeed(
35     136279841); // it's the exponent of the biggest mersenne
36                // prime found to this day :D (from GIMPS on 21/10/2024)
37
38 // chose 300 because all 100 particles could (in principle) be a k* and decay
39 // in two more particles
40 std::array<kape::Particle, 300> eventParticles;
41
42 // creating histograms
43 TH1F* hParticleTypes =
44     new TH1F("hParticleTypes", "Generated particle types", 7, -0.5, 6.5);
45 TH1F* hPhi = new TH1F("hPhi", "Generated phi angles", 1e5, 0., 2. * M_PI);
46 TH1F* hTheta = new TH1F("hTheta", "Generated theta angles", 1e5, 0., M_PI);
47 TH1F* hP = new TH1F("hP", "Generated p magnitudes", 1e5, 0., 5.);
48 TH1F* hPTrasverse =
49     new TH1F("hPTrasverse", "Generated p trasverses", 1e5, 0., 5.);
50 TH1F* hEnergy =
51     new TH1F("hEnergy", "Generated particle energies", 1000, 0., 6.);
52 TH1F* hInvariantMass =
53     new TH1F("hInvariantMass", "Generated invariant masses", 1e5, 0., 8.);
54 TH1F* hInvariantMassDiscordant =
55     new TH1F("hInvariantMassDiscordant",
56             "Generated discordant invariant masses", 1e4, 0., 8.);
57 TH1F* hInvariantMassConcordant =
58     new TH1F("hInvariantMassConcordant",
59             "Generated concordant invariant masses", 1e4, 0., 8.);
60 TH1F* hInvariantMassDiscordantPiK =
61     new TH1F("hInvariantMassDiscordantPiK",
62             "Generated discordant invariant masses pi/K", 1e4, 0., 8.);
63 TH1F* hInvariantMassConcordantPiK =
64     new TH1F("hInvariantMassConcordantPiK",
65             "Generated concordant invariant masses pi/K", 1e4, 0., 8.);
66 TH1F* hInvariantMassDecayed =
67     new TH1F("hInvariantMassDecayed", "Generated decayed invariant masses",
68             100, 0.5, 1.4);
69
70 // sumw2 for correct errors
71 hParticleTypes->Sumw2();
72 hPhi->Sumw2();
73 hTheta->Sumw2();
74 hP->Sumw2();
75 hPTrasverse->Sumw2();
76 hEnergy->Sumw2();
77 hInvariantMass->Sumw2();
78 hInvariantMassDiscordant->Sumw2();
79 hInvariantMassConcordant->Sumw2();
80 hInvariantMassDiscordantPiK->Sumw2();
81 hInvariantMassConcordantPiK->Sumw2();
82 hInvariantMassDecayed->Sumw2();
```

```
83
84 // generating 10^5 events
85 for (int eventIndex = 0; eventIndex != 1e5; ++eventIndex) {
86     // index for the next free space where decayed particles can be placed
87     int arrayEnd = 100;
88     // generating the 100 particles of each event
89     for (int arrayIndex = 0; arrayIndex < 100; ++arrayIndex) {
90         Double_t phi = gRandom->Uniform(0., 2. * M_PI);
91         Double_t theta = gRandom->Uniform(0., M_PI);
92         Double_t p = gRandom->Exp(1.);
93
94         eventParticles[arrayIndex].SetP(p * std::sin(theta) * std::cos(phi),
95                                         p * std::sin(theta) * std::sin(phi),
96                                         p * std::cos(theta));
97
98         // choose particle type following proportions
99         Double_t randomChoice = gRandom->Rndm();
100         if (randomChoice < 0.40) {
101             // pi+
102             eventParticles[arrayIndex].SetIndex(PI_PLUS);
103         } else if (randomChoice < 0.80) {
104             // pi-
105             eventParticles[arrayIndex].SetIndex(PI_MINUS);
106         } else if (randomChoice < 0.85) {
107             // k+
108             eventParticles[arrayIndex].SetIndex(K_PLUS);
109         } else if (randomChoice < 0.90) {
110             // k-
111             eventParticles[arrayIndex].SetIndex(K_MINUS);
112         } else if (randomChoice < 0.945) {
113             // p+
114             eventParticles[arrayIndex].SetIndex(P_PLUS);
115         } else if (randomChoice < 0.99) {
116             // p-
117             eventParticles[arrayIndex].SetIndex(P_MINUS);
118         } else {
119             // k* -> decays
120             eventParticles[arrayIndex].SetIndex(K_STAR);
121
122             // choose decayed particle types randomly
123             if (gRandom->Rndm() <= 0.5) {
124                 eventParticles[arrayEnd].SetIndex(PI_PLUS);
125                 eventParticles[arrayEnd + 1].SetIndex(K_MINUS);
126             } else {
127                 eventParticles[arrayEnd].SetIndex(PI_MINUS);
128                 eventParticles[arrayEnd + 1].SetIndex(K_PLUS);
129             }
130
131             int error = eventParticles[arrayIndex].Decay2body(
132                 eventParticles[arrayEnd], eventParticles[arrayEnd + 1]);
133             if (error != 0) {
134                 std::cout << "decayed to body failed with error " << error << '\n';
135                 throw std::runtime_error{
```



```
136         "decayed to body failed, check terminal for more info.\n");
137     }
138
139     // the next free space is two places after the last free space (2
140     // daughters)
141     arrayEnd += 2;
142 }
143
144 // filling histograms
145 hParticleTypes->Fill(eventParticles[arrayIndex].GetIndex());
146 hPhi->Fill(phi);
147 hTheta->Fill(theta);
148 hP->Fill(p);
149 hPTTrasverse->Fill(
150     std::sqrt(std::pow(eventParticles[arrayIndex].GetPx(), 2)
151         + std::pow(eventParticles[arrayIndex].GetPy(), 2)));
152 hEnergy->Fill(eventParticles[arrayIndex].GetEnergy());
153 }
154
155 // calculating invariant masses between all pairs of particles
156 for (int i = 0; i != arrayEnd - 1; ++i) {
157     if (eventParticles[i].GetIndex() == K_STAR) { // ignore k_star
158         continue;
159     }
160     for (int j = i + 1; j != arrayEnd; ++j) {
161         if (eventParticles[j].GetIndex() == K_STAR) { // ignore k_star
162             continue;
163         }
164
165         // calculate invariant mass of the pair
166         Double_t invMass = eventParticles[i].InvMass(eventParticles[j]);
167         hInvariantMass->Fill(invMass);
168
169         int i_type = eventParticles[i].GetIndex();
170         int j_type = eventParticles[j].GetIndex();
171
172         // discordant
173         if (eventParticles[i].GetCharge() * eventParticles[j].GetCharge() < 0) {
174             hInvariantMassDiscordant->Fill(invMass);
175
176             // PiK pair
177             if ((i_type == PI_PLUS && j_type == K_MINUS)
178                 || (i_type == PI_MINUS && j_type == K_PLUS)
179                 || (j_type == PI_PLUS && i_type == K_MINUS)
180                 || (j_type == PI_MINUS && i_type == K_PLUS)) {
181                 hInvariantMassDiscordantPiK->Fill(invMass);
182             }
183         } else { // concordant
184             hInvariantMassConcordant->Fill(invMass);
185
186             // PiK pair
187             if ((i_type == PI_PLUS && j_type == K_PLUS)
188                 || (i_type == PI_MINUS && j_type == K_MINUS))
```

```

189         || (j_type == PI_PLUS && i_type == K_PLUS)
190         || (j_type == PI_MINUS && i_type == K_MINUS)) {
191             hInvariantMassConcordantPiK->Fill(invMass);
192         }
193     }
194 }
195 }
196
197 // filling the histogram with the invariant masses from only pairs of
198 // decayed particles
199 int i = 100;
200 while (i < arrayEnd) {
201     hInvariantMassDecayed->Fill(
202         eventParticles[i].InvMass(eventParticles[i + 1]));
203     i += 2;
204 }
205 }
206
207 //save to file
208 TFile* file = new TFile("histo.root", "RECREATE");
209
210 hParticleTypes->Write();
211 hPhi->Write();
212 hTheta->Write();
213 hP->Write();
214 hPTrasverse->Write();
215 hEnergy->Write();
216 hInvariantMass->Write();
217 hInvariantMassDiscordant->Write();
218 hInvariantMassConcordant->Write();
219 hInvariantMassDiscordantPiK->Write();
220 hInvariantMassConcordantPiK->Write();
221 hInvariantMassDecayed->Write();
222
223 file->Close();
224 }

```

## Analysis.cpp

```

1  #include "TCanvas.h"
2  #include "TF1.h"
3  #include "TFile.h"
4  #include "TH1.h"
5  #include "TStyle.h"
6  #include <iostream>
7  #include <string>
8
9  std::string ExpectedWithError(Int_t nTot, Double_t probability)
10 {
11     return std::string{
12         std::to_string(nTot * probability) + " ± "
13         + std::to_string(std::sqrt((1. - probability) * (nTot)*probability))};

```

```
14 }
15
16 enum ParticlesIndexesAnalysis
17 {
18     PI_PLUS = 0,
19     PI_MINUS,
20     K_PLUS,
21     K_MINUS,
22     P_PLUS,
23     P_MINUS,
24     K_STAR
25 };
26
27 void Analysis()
28 {
29     TFile* file = new TFile("histo.root");
30
31     // read the data from file
32     TH1F* hParticleTypes      = (TH1F*)file->Get("hParticleTypes");
33     TH1F* hPhi                = (TH1F*)file->Get("hPhi");
34     TH1F* hTheta              = (TH1F*)file->Get("hTheta");
35     TH1F* hP                  = (TH1F*)file->Get("hP");
36     TH1F* hPTrasverse         = (TH1F*)file->Get("hPTrasverse");
37     TH1F* hEnergy             = (TH1F*)file->Get("hEnergy");
38     TH1F* hInvariantMass      = (TH1F*)file->Get("hInvariantMass");
39     TH1F* hInvariantMassDiscordant = (TH1F*)file->Get("hInvariantMassDiscordant");
40     TH1F* hInvariantMassConcordant = (TH1F*)file->Get("hInvariantMassConcordant");
41     TH1F* hInvariantMassDiscordantPiK =
42         (TH1F*)file->Get("hInvariantMassDiscordantPiK");
43     TH1F* hInvariantMassConcordantPiK =
44         (TH1F*)file->Get("hInvariantMassConcordantPiK");
45     TH1F* hInvariantMassDecayed = (TH1F*)file->Get("hInvariantMassDecayed");
46
47     // rebinning
48     hPhi->Rebin(5);
49     hTheta->Rebin(5);
50     hP->Rebin(5);
51     hInvariantMassDiscordant->Rebin(20);
52     hInvariantMassConcordant->Rebin(20);
53     hInvariantMassDiscordantPiK->Rebin(10);
54     hInvariantMassConcordantPiK->Rebin(10);
55
56     // check histo entries
57     if (hParticleTypes->GetEntries() != 1e7)
58         std::cout << "hParticleTypes has the wrong number of entries \n";
59     if (hPhi->GetEntries() != 1e7)
60         std::cout << "hPhi has the wrong number of entries \n";
61     if (hTheta->GetEntries() != 1e7)
62         std::cout << "hTheta has the wrong number of entries \n";
63     if (hP->GetEntries() != 1e7)
64         std::cout << "hP has the wrong number of entries \n";
65     if (hPTrasverse->GetEntries() != 1e7)
66         std::cout << "hPTrasverse has the wrong number of entries \n";
```

```

67  if (hEnergy->GetEntries() != 1e7)
68      std::cout << "hEnergy has the wrong number of entries \n";
69
70  // particle types proportions
71  std::cout
72      << "check that the expected number of particles generated for each type "
73      << "corresponds to the number of generated particles of that type within "
74      << "errors:\n";
75  std::cout << "|Particle Type\t| Expected\t\t\t\t\t| Generated\t\t\t|\n";
76  std::cout << "-----"
77      << "-----\n";
78  std::cout << "|pi+\t\t|" << ExpectedWithError(1e7, 0.400) << "\t\t|"
79      << hParticleTypes->GetBinContent(PI_PLUS + 1) << " ± "
80      << hParticleTypes->GetBinError(PI_PLUS + 1) << "\t|\n";
81  std::cout << "|pi-\t\t|" << ExpectedWithError(1e7, 0.400) << "\t\t|"
82      << hParticleTypes->GetBinContent(PI_MINUS + 1) << " ± "
83      << hParticleTypes->GetBinError(PI_MINUS + 1) << "\t|\n";
84  std::cout << "|K+ \t\t|" << ExpectedWithError(1e7, 0.050) << "\t\t|"
85      << hParticleTypes->GetBinContent(K_PLUS + 1) << " ± "
86      << hParticleTypes->GetBinError(K_PLUS + 1) << "\t|\n";
87  std::cout << "|K- \t\t|" << ExpectedWithError(1e7, 0.050) << "\t\t|"
88      << hParticleTypes->GetBinContent(K_MINUS + 1) << " ± "
89      << hParticleTypes->GetBinError(K_MINUS + 1) << "\t|\n";
90  std::cout << "|p+ \t\t|" << ExpectedWithError(1e7, 0.045) << "\t\t|"
91      << hParticleTypes->GetBinContent(P_PLUS + 1) << " ± "
92      << hParticleTypes->GetBinError(P_PLUS + 1) << "\t|\n";
93  std::cout << "|p- \t\t|" << ExpectedWithError(1e7, 0.045) << "\t\t|"
94      << hParticleTypes->GetBinContent(P_MINUS + 1) << " ± "
95      << hParticleTypes->GetBinError(P_MINUS + 1) << "\t|\n";
96  std::cout << "|K* \t\t|" << ExpectedWithError(1e7, 0.010) << "\t\t|"
97      << hParticleTypes->GetBinContent(K_STAR + 1) << " ± "
98      << hParticleTypes->GetBinError(K_STAR + 1) << "\t|\n";
99
100 // add all parameters to the output in the figures
101 gStyle->SetOptStat(11);
102 gStyle->SetOptFit(1111);
103
104 // Figure 1: particle types, p, phi,
105 // theta-----
106 TCanvas* Figure1 = new TCanvas("Figure1", "Figure1", 0, 0, 800, 600);
107 Figure1->Divide(2, 2);
108
109 // particle types-----
110 Figure1->cd(1);
111
112 // normalize
113 hParticleTypes->Scale(1. / hParticleTypes->Integral(), "width");
114
115 // fitting
116 TF1* particleTypesDistr = new TF1("particleTypesDistr",
117     "[0]*(x<0.5) + "
118     "[1]*(0.5<x && x<1.5) + "
119     "[2]*(1.5<x && x<2.5) + "

```

```
120         "[3]*(2.5<x && x<3.5) + "  
121         "[4]*(3.5<x && x<4.5) + "  
122         "[5]*(4.5<x && x<5.5) + "  
123         "[6]*(5.5<x && x<6.5)",  
124         -0.5, 6.5);  
125  
126 hParticleTypes->Fit(particleTypesDistr);  
127  
128 // fit output  
129 std::cout << "\nParticle Types Distribution Fit: \n"  
130         "y = \t A if (x<0.5) \n"  
131         "\t B if (0.5<x and x<1.5)\n "  
132         "\t C if (1.5<x and x<2.5)\n "  
133         "\t D if (2.5<x and x<3.5)\n "  
134         "\t E if (3.5<x and x<4.5)\n "  
135         "\t F if (4.5<x and x<5.5)\n "  
136         "\t G if (5.5<x and x<6.5)\n";  
137  
138 std::cout << "Parameter A: " << particleTypesDistr->GetParameter(0) << " ± "  
139         << particleTypesDistr->GetParError(0) << '\n';  
140 std::cout << "Parameter B: " << particleTypesDistr->GetParameter(1) << " ± "  
141         << particleTypesDistr->GetParError(1) << '\n';  
142 std::cout << "Parameter C: " << particleTypesDistr->GetParameter(2) << " ± "  
143         << particleTypesDistr->GetParError(2) << '\n';  
144 std::cout << "Parameter D: " << particleTypesDistr->GetParameter(3) << " ± "  
145         << particleTypesDistr->GetParError(3) << '\n';  
146 std::cout << "Parameter E: " << particleTypesDistr->GetParameter(4) << " ± "  
147         << particleTypesDistr->GetParError(4) << '\n';  
148 std::cout << "Parameter F: " << particleTypesDistr->GetParameter(5) << " ± "  
149         << particleTypesDistr->GetParError(5) << '\n';  
150 std::cout << "Parameter G: " << particleTypesDistr->GetParameter(6) << " ± "  
151         << particleTypesDistr->GetParError(6) << '\n';  
152  
153 std::cout << "Reduced Chi Square: "  
154         << particleTypesDistr->GetChisquare() / particleTypesDistr->GetNDF()  
155         << "\n";  
156 std::cout << "Chi Square Probability: " << particleTypesDistr->GetProb()  
157         << "\n\n";  
158  
159 // graphics  
160 hParticleTypes->SetTitle("Particle types' distribution");  
161 hParticleTypes->GetXaxis()->SetBinLabel(1, "#pi+");  
162 hParticleTypes->GetXaxis()->SetBinLabel(2, "#pi-");  
163 hParticleTypes->GetXaxis()->SetBinLabel(3, "K+");  
164 hParticleTypes->GetXaxis()->SetBinLabel(4, "K-");  
165 hParticleTypes->GetXaxis()->SetBinLabel(5, "p+");  
166 hParticleTypes->GetXaxis()->SetBinLabel(6, "p-");  
167 hParticleTypes->GetXaxis()->SetBinLabel(7, "K*");  
168 hParticleTypes->GetXaxis()->SetLabelSize(0.065);  
169 hParticleTypes->GetXaxis()->SetTitleOffset(1.2);  
170 hParticleTypes->GetXaxis()->SetTitle("Particle type");  
171 hParticleTypes->GetYaxis()->SetTitle("Probability of particle type");  
172 hParticleTypes->SetFillColor(kAzure - 2);
```

```
173 hParticleTypes->SetLineColor(kAzure - 2);
174 hParticleTypes->SetBarWidth(0.2);
175 hParticleTypes->SetBarOffset(0.8);
176 // if sumw2 is set to true the histogram doesn't get filled in
177 hParticleTypes->Sumw2(kFALSE);
178 hParticleTypes->Draw("b same");
179
180 // p-----
181 Figure1->cd(2);
182
183 // normalize
184 hP->Scale(1. / hP->Integral(), "width");
185
186 // fitting
187 TF1* pDistr = new TF1("pDistr", "TMath::Exp(-x/[0])", 0., 5.);
188 pDistr->SetParameter(0, 1);
189 pDistr->SetParameter(1, 1);
190 hP->Fit(pDistr);
191
192 // fit output
193 std::cout << "\nP Distribution Fit: y = e^(-x/A)\n";
194
195 std::cout << "Parameter A: " << pDistr->GetParameter(0) << " ± "
196           << pDistr->GetParError(0) << "\n";
197
198 std::cout << "Reduced Chi Square: "
199           << pDistr->GetChisquare() / pDistr->GetNDF() << "\n";
200 std::cout << "Chi Square Probability: " << pDistr->GetProb() << "\n\n";
201
202 // graphics
203 hP->SetTitle("Impulse magnitudes' distribution");
204 hP->GetXaxis()->SetTitle("Impulse magnitude");
205 hP->GetYaxis()->SetTitle("Probability of impulse magnitude");
206 hP->GetXaxis()->SetTitleOffset(1.2);
207 hP->SetLineColor(kAzure - 2);
208 hP->Draw();
209
210 // phi-----
211 Figure1->cd(3);
212
213 // normalize
214 hPhi->Scale(1. / hPhi->Integral(), "width");
215
216 // fitting
217 TF1* phiDistr = new TF1("phiDistr", "[0]", 0, 2 * TMath::Pi());
218
219 hPhi->Fit(phiDistr);
220
221 // fit output
222 std::cout << "\nPhi Distribution Fit: y = A\n";
223 std::cout << "Parameter A: " << phiDistr->GetParameter(0) << " ± "
224           << phiDistr->GetParError(0) << "\n";
225
```

```
226     std::cout << "Reduced Chi Square: "
227             << phiDistr->GetChisquare() / phiDistr->GetNDF() << "\n";
228     std::cout << "Chi Square Probability: " << phiDistr->GetProb() << "\n\n";
229
230     // graphics
231     hPhi->SetTitle("Azimuthal angles' distribution");
232     hPhi->GetXaxis()->SetTitle("Azimuthal angle");
233     hPhi->GetYaxis()->SetTitle("Probability of azimuthal angle");
234     hPhi->GetXaxis()->SetTitleOffset(1.2);
235     hPhi->SetLineColor(kAzure - 2);
236     hPhi->Draw();
237
238     // theta-----
239     Figure1->cd(4);
240
241     // normalize
242     hTheta->Scale(1. / hTheta->Integral(), "width");
243
244     // fitting
245     TF1* thetaDistr = new TF1("thetaDistr", "[0]", 0, TMath::Pi());
246     hTheta->Fit(thetaDistr);
247
248     // fit output
249     std::cout << "\nTheta Distribution Fit: y = A\n";
250     std::cout << "Parameter A: " << thetaDistr->GetParameter(0) << " ± "
251             << thetaDistr->GetParError(0) << "\n";
252
253     std::cout << "Reduced Chi Square: "
254             << thetaDistr->GetChisquare() / thetaDistr->GetNDF() << "\n";
255     std::cout << "Chi Square Probability: " << thetaDistr->GetProb() << "\n\n";
256
257     // graphics
258     hTheta->SetTitle("Polar angles' distribution");
259     hTheta->GetXaxis()->SetTitle("Polar angle");
260     hTheta->GetYaxis()->SetTitle("Probability of polar angle");
261     hTheta->GetXaxis()->SetTitleOffset(1.2);
262     hTheta->SetFillColor(kAzure - 2);
263     hTheta->SetLineColor(kAzure - 2);
264     hTheta->Draw();
265
266     // Figure 2: invariant masses graphs -----
267     TCanvas* Figure2 = new TCanvas("Figure2", "Figure2", 0, 0, 800, 600);
268     Figure2->Divide(3, 1);
269
270     // Only K*-----
271     Figure2->cd(1);
272
273     // fitting
274     TF1* invariantMassDecayedDistr =
275         new TF1("invariantMassDecayedDistr", "gaus(0)", 0., 8.);
276     hInvariantMassDecayed->Fit(invariantMassDecayedDistr);
277
278     // fit output
```



```
279 std::cout << "\nK* Invariant mass fit:  $y = A \cdot \exp(-0.5 \cdot ((x-M)/D)^2)$ \n";
280 std::cout << "Parameter A: " << invariantMassDecayedDistr->GetParameter(0)
281       << "  $\pm$  " << invariantMassDecayedDistr->GetParError(0) << "\n";
282 std::cout << "Parameter M: " << invariantMassDecayedDistr->GetParameter(1)
283       << "  $\pm$  " << invariantMassDecayedDistr->GetParError(1) << "\n";
284 std::cout << "Parameter D: " << invariantMassDecayedDistr->GetParameter(2)
285       << "  $\pm$  " << invariantMassDecayedDistr->GetParError(2) << "\n";
286 std::cout << "Reduced Chi Square: "
287       << invariantMassDecayedDistr->GetChisquare()
288       << " / invariantMassDecayedDistr->GetNDF()
289       << "\n";
290 std::cout << "Chi Square Probability: "
291       << invariantMassDecayedDistr->GetProb() << "\n\n";
292
293 // graphics
294 hInvariantMassDecayed->SetTitle("K* invariant masses");
295 hInvariantMassDecayed->GetXaxis()->SetTitle("Invariant mass");
296 hInvariantMassDecayed->GetYaxis()->SetTitle("Entries");
297 hInvariantMassDecayed->SetMarkerStyle(kFullSquare);
298 hInvariantMassDecayed->SetMarkerSize(0.5f);
299 hInvariantMassDecayed->Draw();
300
301 // Difference of discordant particles' invariant masses-----
302 // subtract
303 TH1F* hDiffMass = new TH1F(*hInvariantMassDiscordant);
304 hDiffMass->Add(hInvariantMassConcordant, -1);
305
306 Figure2->cd(2);
307
308 // fitting
309 TF1* diffMassDistr = new TF1("diffMassDistr", "gaus(0)", 0., 8.);
310 hDiffMass->Fit(diffMassDistr);
311
312 // fit output
313 std::cout
314   << "\nK* discordant invariant mass fit:  $y = A \cdot \exp(-0.5 \cdot ((x-M)/D)^2)$ \n";
315 std::cout << "Parameter A: " << diffMassDistr->GetParameter(0) << "  $\pm$  "
316       << diffMassDistr->GetParError(0) << "\n";
317 std::cout << "Parameter M: " << diffMassDistr->GetParameter(1) << "  $\pm$  "
318       << diffMassDistr->GetParError(1) << "\n";
319 std::cout << "Parameter D: " << diffMassDistr->GetParameter(2) << "  $\pm$  "
320       << diffMassDistr->GetParError(2) << "\n";
321 std::cout << "Reduced Chi Square: "
322       << diffMassDistr->GetChisquare() / diffMassDistr->GetNDF() << "\n";
323 std::cout << "Chi Square Probability: " << diffMassDistr->GetProb() << "\n\n";
324
325 // graphics
326 hDiffMass->SetTitle("Discordant particles' invariant masses");
327 hDiffMass->GetXaxis()->SetTitle("Invariant mass");
328 hDiffMass->GetYaxis()->SetTitle("Entries");
329 hDiffMass->SetLineColor(kAzure - 2);
330 hDiffMass->Draw();
331
```



```

332 // Difference of discordant PiK particles' invariant masses-----
333 // subtract
334 TH1F* hDiffMassPiK = new TH1F(*hInvariantMassDiscordantPiK);
335 hDiffMassPiK->Add(hInvariantMassConcordantPiK, -1);
336
337 Figure2->cd(3);
338
339 // fitting
340 TF1* diffMassPiKDistr = new TF1("diffMassPiKDistr", "gaus(0)", 0., 8.);
341 hDiffMassPiK->Fit(diffMassPiKDistr);
342
343 // fit output
344 std::cout << "\nK* discordant PiK invariant mass fit: y = "
345             << "A*exp(-0.5*((x-M)/D)**2)\n";
346 std::cout << "Parameter A: " << diffMassPiKDistr->GetParameter(0) << " ± "
347             << diffMassPiKDistr->GetParError(0) << "\n";
348 std::cout << "Parameter M: " << diffMassPiKDistr->GetParameter(1) << " ± "
349             << diffMassPiKDistr->GetParError(1) << "\n";
350 std::cout << "Parameter D: " << diffMassPiKDistr->GetParameter(2) << " ± "
351             << diffMassPiKDistr->GetParError(2) << "\n";
352 std::cout << "Reduced Chi Square: "
353             << diffMassPiKDistr->GetChisquare() / diffMassPiKDistr->GetNDF()
354             << "\n";
355 std::cout << "Chi Square Probability: " << diffMassPiKDistr->GetProb()
356             << "\n\n";
357
358 // graphics
359 hDiffMassPiK->SetTitle("#pi - k invariant masses");
360 hDiffMassPiK->GetXaxis()->SetTitle("Invariant mass");
361 hDiffMassPiK->GetYaxis()->SetTitle("Entries");
362 hDiffMassPiK->SetLineColor(kAzure - 2);
363 hDiffMassPiK->Draw();
364 }

```

## testParticleType.cpp

```

1  #define DOCTEST_CONFIG_IMPLEMENT_WITH_MAIN
2  #include "ParticleType.hpp"
3  #include "ResonanceType.hpp"
4  #include "doctest.h"
5  #include <cstring> //for strcmp()
6  #include <iostream>
7
8  TEST_CASE("Testing ParticleType")
9  {
10     SUBCASE("Testing Getter methods")
11     {
12         kape::ParticleType a{"a", 0.5, 1};
13         CHECK(std::strcmp(a.GetName(), "a") == 0);
14         CHECK(a.GetMass() == 0.5);
15         CHECK(a.GetCharge() == 1);
16     }

```

```
17
18 SUBCASE("Testing Print method")
19 {
20     kape::ParticleType a{"a", 0.5, 1};
21
22     std::cout << "\nPlease check that the 2 printed outputs are the same: \n\n";
23     std::cout << "Name:\ta\n";
24     std::cout << "Mass:\t0.5\n";
25     std::cout << "Charge:\t1\n\n";
26     a.Print();
27 }
28 }
29
30 TEST_CASE("Testing ResonanceType")
31 {
32     SUBCASE("Testing Getter methods")
33     {
34         kape::ResonanceType b{"b", 0.5, 1, 1.};
35         CHECK(std::strcmp(b.GetName(), "b") == 0);
36         CHECK(b.GetMass() == 0.5);
37         CHECK(b.GetCharge() == 1);
38         CHECK(b.GetWidth() == 1.);
39     }
40
41     SUBCASE("Testing Print method")
42     {
43         kape::ResonanceType b{"b", 0.5, 1, 1.};
44
45         std::cout << "\nPlease check that the 2 printed outputs are the same: \n\n";
46         std::cout << "Name:\tb\n";
47         std::cout << "Mass:\t0.5\n";
48         std::cout << "Charge:\t1\n";
49         std::cout << "Width:\t1\n\n";
50         b.Print();
51     }
52
53     SUBCASE("Testing Print override")
54     {
55         kape::ParticleType* particles[2];
56         particles[0] = new kape::ParticleType("ParticleType", 0.5, 1);
57         particles[1] = new kape::ResonanceType("ResonanceType", 1., -1, 1.);
58
59         std::cout << "\nPlease check that the 2 printed outputs are the same: \n\n";
60         std::cout << "Name:\tParticleType\n";
61         std::cout << "Mass:\t0.5\n";
62         std::cout << "Charge:\t1\n";
63
64         std::cout << "Name:\tResonanceType\n";
65         std::cout << "Mass:\t1\n";
66         std::cout << "Charge:\t-1\n";
67         std::cout << "Width:\t1\n\n";
68
69         for (int i = 0; i < 2; i++) {
```

```
70     particles[i]->Print();
71 }
72 }
73 }
```

## testParticle.cpp

```
1  #define DOCTEST_CONFIG_IMPLEMENT_WITH_MAIN
2  #include "Particle.hpp"
3
4  #include "doctest.h"
5
6  TEST_CASE("Testing Particle class")
7  {
8      SUBCASE("Testing AddParticleType()")
9      {
10         CHECK(kape::Particle::GetNParticleType() == 0);
11         kape::Particle::AddParticleType("kape", 70., -1);
12         CHECK(kape::Particle::GetNParticleType() == 1);
13         kape::Particle::AddParticleType("samu", 63., 4, 1.);
14         CHECK(kape::Particle::GetNParticleType() == 2);
15         kape::Particle::AddParticleType("lele", 56., 18);
16         CHECK(kape::Particle::GetNParticleType() == 3);
17         kape::Particle::AddParticleType("nick", 79., -100, 0.40);
18         CHECK(kape::Particle::GetNParticleType() == 4);
19
20         kape::Particle gebbi{"kape", 10., -3., 0.};
21         CHECK(gebbi.GetIndex() == 0);
22         CHECK(gebbi.GetMass() == 70.);
23         gebbi.Print();
24         gebbi.SetIndex(1);
25         CHECK(gebbi.GetIndex() == 1);
26         CHECK(gebbi.GetMass() == 63.);
27         gebbi.Print();
28
29         kape::Particle::AddParticleType("nick", 79., +100, 0.40);
30         CHECK(kape::Particle::GetNParticleType() == 4);
31
32         kape::Particle::PrintParticleType();
33     }
34
35     SUBCASE("testing with array")
36     {
37         kape::Particle::AddParticleType("pi+", 0.13957, +1); // pione +
38         kape::Particle::AddParticleType("pi-", 0.13957, -1); // pione -
39         kape::Particle::AddParticleType("K+", 0.49367, +1); // kaone +
40         kape::Particle::AddParticleType("K-", 0.49367, -1); // kaone -
41         kape::Particle::AddParticleType("p+", 0.93827, +1); // protone +
42         kape::Particle::AddParticleType("p-", 0.93827, -1); // protone -
43         kape::Particle::AddParticleType("K*", 0.89166, 0, 0.050); // K*
44
45         std::array<kape::Particle, 300> eventParticles;
```

```
46 |   }  
47 | }
```