Relazione

Samuele Bellini, Francesco Caprara, Gabriele Introna, Niccolò Lugli Dicembre 2024

1 Introduzione

Lo scopo di questo esperimento è studiare, attraverso la simulazione di un campione di particelle di vario tipo, le proprietà di una particella ignota e instabile che decade troppo velocemente per poter essere osservata direttamente. Poiché la particella iniziale è neutra i prodotti del decadimento avranno carica discorde; inoltre, la massa invariante segue una distribuzione gaussiana con media pari alla massa della particella madre e deviazione standard pari alla sua larghezza di risonanza. Di conseguenza, si misurano le masse invarianti dal campione di particelle che contiene anche quelle derivanti dal decadimento separando per coppie di carica concorde e discorde, e si isola l'effetto delle sole particelle figlie rimuovendo il rumore di fondo dai dati. Per ridurre il fondo più efficientemente si può ripetere l'analisi considerando il campione composto dalle sole particelle ottenibili teoricamente dal decadimento.

2 Struttura del Codice

Il codice che gestisce le particelle è stato organizzato creando tre classi: ParticleType, ResonanceType e Particle. Come il nome suggerisce, le prime due vogliono rappresentare dei tipi di particelle (protone, antiprotone, kaone, pione, ...), mentre la terza rappresenta una particella di per sé. ParticleType descrive un tipo di particella che possiede una massa e una carica, e alla quale viene assegnato un nome. La classe, inoltre, espone anche due metodi virtuali, GetWidth e Print, che possono essere sovrascritti dalle classi figlie per implementare la larghezza di risonanza di una particella o per modificare la stampa a schermo delle proprietà della particella. ResonanceType fa uso di questa possibilità ereditando pubblicamente da ParticleType, in quanto vuole rappresentare un tipo di particella che può decadere e che, di conseguenza, oltre alle proprietà di una particella base, necessita anche della descrizione della sua larghezza di risonanza. La classe Particle, infine, funge da rappresentazione di una particella di un dato tipo con una quantità di moto. Sapendo che nel programma il numero di tipi di particelle sarà minuscolo rispetto al numero di particelle che verranno create si è preferito utilizzare, rispetto all'ereditarietà, che avrebbe portato a una ripetizione degli stessi dati (nome, massa, carica e larghezza di risonanza) fra molte particelle, uno std::vector statico di puntatori a ParticleType (che di conseguenza, per il polimorfismo dinamico, possono puntare anche a Resonance-Type). Quest'ultimo racchiude tutti i tipi di particelle che sono presenti nella simulazione, i quali vengono aggiunti a run-time: si è preferito questo approccio per accomodare anche l'eventualità in cui non si dovesse conoscere il numero di tipi di particelle a compile-time, come avverrebbe se questi volessero essere specificati in un file invece che nel codice. In questo modo ad ogni particella saranno associati solo tre float, per descrivere la quantità di moto, e un indicatore del tipo di particella, per il quale è stato scelto un int, che funge da indice nell'std::vector di tipi di particelle.

3 Generazione

Il codice prevede la generazione di 10⁵ eventi, ciascuno dei quali considera molte particelle suddivise in un numero limitato di tipi. Nel nostro caso, in ogni evento vengono generate, una alla volta, 100 particelle che possono appartenere a sette tipi differenti, ognuno dei quali ha una fissa percentuale di probabilità di essere generato: le proporzioni prevedono 40% di pioni positivi, 40% di pioni negativi, 5% di kaoni positivi, 5% di kaoni negativi, 4.5% di protoni, 4.5% di antiprotoni e 1% di una particella instabile che chiamiamo K*, che decade in una coppia di carica discorde composta da un pione e un kaone, con uguale probabilità di ottenere coppie $\pi + K - o \pi - K +$. Ad ogni particella generata sono associate sia proprietà di base (nome, massa, carica, larghezza di risonanza) sia proprietà cinematiche, cioè una quantità di moto sulle tre dimensioni, che può variare da particella a particella e da evento a evento. Per generare quest'impulso in maniera casuale abbiamo utilizzato i motodi Monte Carlo implementati da ROOT per generare una distribuzione esponenziale con media 1 per il modulo, due distribuzioni uniformi, rispettivamente tra $0 e 2\pi$ e tra $0 e \pi$, per gli angoli phi (azimutale) e theta (polare), che definiscono la direzione dell'impulso nello spazio, e abbiamo poi convertito questi dati da coordinate sferiche a cartesiane, ottenendo le tre componenti Px, Py e Pz della quantità di moto.

4 Analisi

L'istogramma della distribuzione dei tipi delle particelle generate segue coerentemente la distribuzione a tratti costanti che ci si aspetta: la probabilità della creazione di ciascun tipo corrisponde alla proporzione in cui è effettivamente osservato (Tab. 1). La distribuzione degli impulsi è coerente con un'esponenziale, e al fit corrisponde correttamente un $\tilde{\chi}^2 \simeq 1$ (Tab. 2). Gli angoli polari e azimutali sono distribuiti uniformemente nei domini previsti, come confermano i fit a cui corrispondono nuovamente dei $\tilde{\chi}^2 \simeq 1$ (Tab. 2). Questi quattro grafici sono riportati in Fig. 1.

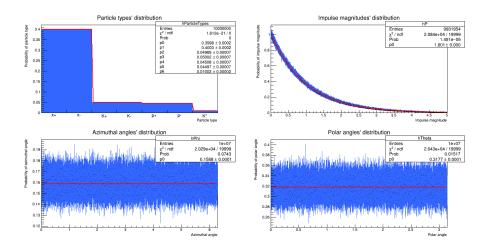


Figure 1: In alto a sx la distribuzione dei tipi di particelle generati, in alto a dx la distribuzione del modulo dell'impulso, in basso le distribuzioni degli angoli azimutale (ϕ) e polare (θ) .

Per la distribuzione della massa invariante relativa alle coppie di figlie di K* si osserva, come ci si aspetta, una gaussiana con media e deviazione standard pari rispettivamente a massa e lunghezza di risonanza della K* (Tab. 3). Essendo la K* molto instabile e rara, per estrarre il suo segnale è occorso seguire un approccio per sottrazione: a partire dalla distribuzione della massa invariante delle particelle generate, rimuovendo il rumore di fondo si riesce a osservare il segnale della particella di risonanza. Ovvero, dalla distribuzione della massa invariante delle particelle di segno discorde, che comprendono le combinazioni accidentali (fondo) e quelle effettivamente generate a partire dal decadimento di K*, è stata rimossa quella della massa invariante delle particelle di segno concorde, che possono essere solo fondo (K* decade in π + e K- o in π - e K+). Per un'ulteriore distinzione più efficace è stata eseguita la stessa operazione, ma prendendo in considerazione solo i pioni π e i kaoni K, poiché K* può decadere solo in questi, e quindi riducendo il rumore di fondo (i protoni P sono circa il 9% delle particelle generate). Le distribuzioni risultanti, analogamente alla precedente (tutte in Fig. 2), corrispondono a delle gaussiane la cui media risulta essere la massa della K*, e la cui sigma la larghezza di risonanza: si è quindi riuscito ad estrarre il segnale dalle distribuzioni delle masse invarianti (Tab. 3).

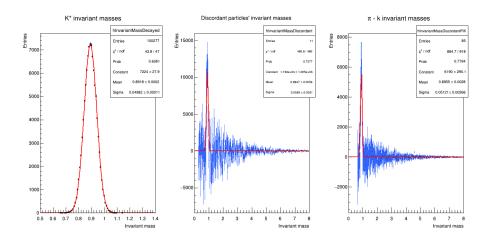


Figure 2: A sinistra la distribuzione delle masse invarianti solo fra particelle figlie, al centro la differenza degli istogrammi di masse invarianti fra particelle discordi e concordi, a destra come al centro ma solo considerando coppie πK

Specie	Occorrenze osservate (10^6)	Occorrenze attese (10^6)
π^+	3.998 ± 0.002	4.0000 ± 0.0015
π^-	4.003 ± 0.002	4.0000 ± 0.0015
K^+	0.4989 ± 0.0007	0.5000 ± 0.0007
K^-	0.5002 ± 0.0007	0.5000 ± 0.0007
p^+	0.4508 ± 0.0007	0.4500 ± 0.0007
p^-	0.4497 ± 0.0007	0.4500 ± 0.0007
K^*	0.1003 ± 0.0003	0.1000 ± 0.0003

Table 1: Tabella delle occorrenze osservate e attese dei diversi tipi di particelle.

Distribuzione	Parametro del fit	χ^2	DOF	$ ilde{\chi}^2$
Fit a distribuzione angolo ϕ (azi)	0.15883 ± 0.00005	20288.6	19999	1.01
Fit a distribuzione angolo θ (pol)	0.31766 ± 0.00010	20434.6	19999	1.02
Fit a distribuzione modulo impulso (expo)	1.0007 ± 0.0002	20844.9	19999	1.04

Table 2: Risultati dei fit per diverse distribuzioni.

Distribuzione e fit	μ	σ	Ampiezza	$ ilde{\chi}^2$
Massa invariante vere K^*	0.89185 ± 0.00016	0.04982 ± 0.00011	7220 ± 30	0.932
Massa invariante ot- tenuta da differenza delle combinazioni di carica discorde e con- corde	0.895 ± 0.006	0.056 ± 0.005	$(11.9 \pm 1.0) \cdot 10^3$	0.960
Massa invariante ottenuta da differenza delle combinazioni di carica discorde e concorde πK	0.051 ± 0.003	0.051 ± 0.003	$(6.2 \pm 0.3) \cdot 10^{3}$	0.964

Table 3: Parametri di fit per le masse invarianti in diverse combinazioni.

Selected files

11 printable files

```
ParticleType.hpp
ParticleType.cpp
ResonanceType.hpp
ResonanceType.cpp
Particle.hpp
Particle.cpp
compile.C
ParticleGenerator.cpp
Analysis.cpp
testParticleType.cpp
testParticle.cpp
```

ParticleType.hpp

```
#ifndef PARTICLE TYPE HPP
 2
   #define PARTICLE_TYPE_HPP
 3
 4
   namespace kape {
    class ParticleType
 6
    {
 7
     public:
8
      explicit ParticleType(const char* name, double mass, int charge);
9
      explicit ParticleType();
10
      virtual ~ParticleType();
11
12
      const char* GetName() const;
13
      double GetMass() const;
14
      int GetCharge() const;
15
16
     virtual double GetWidth() const;
17
      virtual void Print() const;
18
19
     private:
20
      const char* fName;
21
      const double fMass;
22
      const int fCharge;
23
   };
24
   } // namespace kape
25
26 #endif
```

ParticleType.cpp

```
1  #include "ParticleType.hpp"
2  #include <iostream>
3  #include <stdexcept>
4
5  namespace kape {
6  ParticleType::ParticleType(const char* name, double mass, int charge)
7  : fName{name}
```

```
8
        , fMass{mass}
9
        , fCharge{charge}
10
11
     if (mass <= 0.) {
12
        throw std::invalid_argument{"mass can't be negative or null"};
13
      }
14
15
      if (name == nullptr) {
        throw std::invalid argument{"name can't point to nullptr"};
16
17
   }
18
19
20
   ParticleType::ParticleType()
        : ParticleType("", 1, 0)
21
22
   {}
23
   ParticleType::~ParticleType()
24
25
   {}
26
27
   const char* ParticleType::GetName() const
28
29
      return fName;
30
   }
31
   double ParticleType::GetMass() const
32
33
   {
      return fMass;
34
35
   }
36
37
   int ParticleType::GetCharge() const
38
   {
39
      return fCharge;
40
   }
41
42
   double ParticleType::GetWidth() const
43
44
      return 0.;
45
   }
46
47
48
   void ParticleType::Print() const
49
     std::cout << "Name:\t" << fName << '\n';</pre>
50
      std::cout << "Mass:\t" << fMass << '\n';
51
      std::cout << "Charge:\t" << fCharge << '\n';</pre>
52
53
   }
54 } // namespace kape
```

ResonanceType.hpp

```
1 #ifndef RESONANCE_TYPE_HPP
2 #define RESONANCE_TYPE_HPP
```

```
#include "ParticleType.hpp"
3
 4
 5
   namespace kape {
   class ResonanceType : public ParticleType
 6
7
8
    public:
9
     explicit ResonanceType(const char* name, double mass, int charge,
10
                              double width);
     explicit ResonanceType();
11
12
13
     virtual double GetWidth() const override;
14
     void Print() const override;
15
16
    private:
     const double fWidth;
17
18
   };
   } // namespace kape
19
20
21 #endif
```

ResonanceType.cpp

```
#include "ResonanceType.hpp"
1
   #include <iostream>
   #include <stdexcept>
 4
5
   namespace kape {
   ResonanceType::ResonanceType(const char* name, double mass, int charge,
6
7
                                  double width)
        : ParticleType(name, mass, charge)
8
9
        , fWidth{width}
10
   {
     if (width <= 0) {
11
        throw std::invalid_argument{"width can't be negative or null"};
12
     }
13
   }
14
15
   ResonanceType::ResonanceType()
16
17
        : ParticleType()
        , fWidth{}
18
19
   {}
20
21
   double ResonanceType::GetWidth() const
22
23
      return fWidth;
24
   }
25
   void ResonanceType::Print() const
26
27
   {
28
     ParticleType::Print();
      std::cout << "Width:\t" << fWidth << '\n';</pre>
29
30 }
```

```
31 } // namespace kape 32
```

Particle.hpp

```
#ifndef PARTICLE HPP
 2
   #define PARTICLE HPP
3
 4 | #include "ParticleType.hpp"
  #include "ResonanceType.hpp"
 5
 6
   #include <vector>
7
8
  namespace kape {
9 class Particle
10
   {
11
    public:
12
      static int GetNParticleType();
      static void AddParticleType(const char* name, double mass, int charge,
13
                                   double width = 0);
14
15
     static void PrintParticleType();
16
17
     Particle(const char* name = DEFAULT_NAME, double px = 0., double py = 0.,
               double pz = 0.;
18
      int Decay2body(Particle& dau1, Particle& dau2) const;
19
      int GetIndex() const;
20
21
      double GetPx() const;
     double GetPy() const;
22
23
     double GetPz() const;
     double GetMass() const;
24
25
     double GetEnergy() const;
     double GetCharge() const;
26
27
     void SetIndex(int index);
     void SetIndex(const char* name);
28
29
     void SetP(double px, double py, double pz);
      double InvMass(Particle const& p) const;
30
31
     void Print() const;
32
33
34
     private:
35
      static inline const char* DEFAULT_NAME{"DEFAULT_NAME"};
     static inline std::vector<ParticleType*> fParticleType{};
36
     //returns the index of the first particle type named "name"
37
     //if not found it returns the number of particle types
38
39
      static int FindParticle(const char* name);
40
     void Boost(double bx, double by, double bz);
41
42
     int fIndex;
43
     double fPx;
      double fPy;
44
45
      double fPz;
46
   };
47
```

```
48 } // namespace kape
49
50 #endif
```

Particle.cpp

```
1 #include "Particle.hpp"
 2
   #include <cmath>
   #include <cstdlib> //for RAND MAX
   #include <cstring> //for strcmp
   #include <iostream>
   #include <stdexcept>
 7
   namespace kape {
 8
 9
   int Particle::GetNParticleType()
10
11
      return static cast<int>(fParticleType.size());
12
   }
13
14
   Particle::Particle(const char* name, double px, double py, double pz)
15
        : fPx{px}
16
        , fPy{py}
17
        , fPz{pz}
18
19
     fIndex = FindParticle(name);
20
     // not found
21
     if (fIndex == static cast<int>(fParticleType.size())
          && name != DEFAULT_NAME) {
22
        std::cout << name << " is not a defined type of particle\n";</pre>
23
        throw std::runtime_error{"it is not a defined type of particle. Check "
24
25
                                  "terminal output for the name."};
26
     }
   }
27
28
29
   int Particle::Decay2body(Particle& dau1, Particle& dau2) const
30
31
     if (GetMass() == 0.0) {
32
        printf("Decayment cannot be preformed if mass is zero\n");
33
        return 1;
34
      }
35
36
      double massMot = GetMass();
37
      double massDau1 = dau1.GetMass();
38
      double massDau2 = dau2.GetMass();
39
40
      if (fIndex > -1) { // add width effect
41
42
        // gaussian random numbers
43
44
        float x1, x2, w, y1;
45
        double invnum = 1. / RAND_MAX;
46
```

```
do {
47
48
          x1 = 2.0 * rand() * invnum - 1.0;
49
          x2 = 2.0 * rand() * invnum - 1.0;
50
         W = x1 * x1 + x2 * x2;
51
        } while (w >= 1.0);
52
53
        w = sqrt((-2.0 * log(w)) / w);
54
        y1 = x1 * w;
55
56
        massMot += fParticleType[fIndex]->GetWidth() * y1;
57
      }
58
59
      if (massMot < massDau1 + massDau2) {</pre>
60
        printf("Decayment cannot be preformed because mass is too low in this "
61
               "channel\n");
62
        return 2;
63
      }
64
65
      double pout =
          sqrt(
66
67
              (massMot * massMot - (massDau1 + massDau2) * (massDau1 + massDau2))
              * (massMot * massMot - (massDau1 - massDau2) * (massDau1 - massDau2)))
68
69
          / massMot * 0.5;
70
      double norm = 2 * M_PI / RAND_MAX;
71
72
73
      double phi = rand() * norm;
74
      double theta = rand() * norm * 0.5 - M PI / 2.;
75
      dau1.SetP(pout * sin(theta) * cos(phi), pout * sin(theta) * sin(phi),
76
                pout * cos(theta));
77
      dau2.SetP(-pout * sin(theta) * cos(phi), -pout * sin(theta) * sin(phi),
78
                -pout * cos(theta));
79
80
      double energy = sqrt(fPx * fPx + fPy * fPy + fPz * fPz + massMot * massMot);
81
82
      double bx = fPx / energy;
83
      double by = fPy / energy;
84
      double bz = fPz / energy;
85
86
      dau1.Boost(bx, by, bz);
87
      dau2.Boost(bx, by, bz);
88
89
      return 0;
90
   }
91
92
   void Particle::AddParticleType(const char* name, double mass, int charge,
93
                                    double width)
94
   {
95
      int index = FindParticle(name);
96
      if (index == GetNParticleType()) // it's a new Particle Type
97
98
        if (width == 0.) { // it's a ParticleType
99
          fParticleType.push back(new ParticleType(name, mass, charge));
```

```
100
         } else {
101
           fParticleType.push_back(new ResonanceType(name, mass, charge, width));
102
103
       } else // we're updating a Particle Type
104
105
        delete fParticleType[index];
         if (width == 0.) { // it's a ParticleType
106
107
           fParticleType[index] = new ParticleType(name, mass, charge);
         } else {
108
109
           fParticleType[index] = new ResonanceType(name, mass, charge, width);
110
         }
111
       }
112
    }
113
114
    void Particle::PrintParticleType()
115
      std::cout << "Particle types:\n";</pre>
116
117
      for (auto const& p : fParticleType) {
         p->Print();
118
119
       }
120
    }
121
    int Particle::GetIndex() const
122
123
124
      return fIndex;
125
    }
126
    double Particle::GetPx() const
127
128
       return fPx;
129
    }
130
    double Particle::GetPy() const
131
132
       return fPy;
133
    double Particle::GetPz() const
134
135
136
       return fPz;
137
    }
138
    double Particle::GetMass() const
139
140
141
       return fParticleType[fIndex]->GetMass();
142
    }
143
144
    double Particle::GetEnergy() const
145
    {
      double m{fParticleType[fIndex]->GetMass()};
146
       return std::sqrt(m * m + fPx * fPx + fPy * fPy + fPz * fPz);
147
148
    }
149
150
    double Particle::GetCharge() const
151
    {
152
       return fParticleType[fIndex]->GetCharge();
```

```
153 }
154
    void Particle::SetIndex(int index)
155
156
157
      if (index >= GetNParticleType() || index < 0) {</pre>
158
         std::cout << "it is not a defined type of particle\n";</pre>
         throw std::runtime_error{"it is not a defined type of particle."};
159
       }
160
161
162
      fIndex = index;
    }
163
164
    void Particle::SetIndex(const char* name)
165
166
      SetIndex(FindParticle(name));
167
168
    }
169
170
    void Particle::SetP(double px, double py, double pz)
171
172
      fPx = px;
173
      fPy = py;
174
      fPz = pz;
175
    }
176
177
    double Particle::InvMass(Particle const& p) const
178
    {
179
       return sqrt(std::pow(GetEnergy() + p.GetEnergy(), 2)
180
                   - (std::pow(fPx + p.fPx, 2) + std::pow(fPy + p.fPy, 2)
                      + std::pow(fPz + p.fPz, 2)));
181
182
    }
183
184
    void Particle::Print() const
185
186
       std::cout << "Index: " << fIndex << '\n';</pre>
       std::cout << "Name: " << fParticleType[fIndex]->GetName() << '\n';</pre>
187
188
       std::cout << "P = (" << fPx << ", " << fPy << ", " << fPz << ") " << '\n';
189
    }
190
191
    int Particle::FindParticle(const char* name)
192
    {
193
       int i{0};
194
       for (; i != static_cast<int>(fParticleType.size()); ++i) {
195
         if (std::strcmp(fParticleType[i]->GetName(), name) == 0) {
196
           break;
197
         }
198
       }
199
       return i;
200
201
202
    void Particle::Boost(double bx, double by, double bz)
203
    {
204
       double energy = GetEnergy();
205
```

```
206
      // Boost this Lorentz vector
207
      double b2 = bx * bx + by * by + bz * bz;
      double gamma = 1.0 / sqrt(1.0 - b2);
208
      double bp = bx * fPx + by * fPy + bz * fPz;
209
210
      double gamma2 = b2 > 0 ? (gamma - 1.0) / b2 : 0.0;
211
      fPx += gamma2 * bp * bx + gamma * bx * energy;
212
      fPy += gamma2 * bp * by + gamma * by * energy;
213
      fPz += gamma2 * bp * bz + gamma * bz * energy;
214
215
216 } // namespace kape
```

compile.C

```
void compile(){
    gR00T->LoadMacro("ParticleType.cpp+");

gR00T->LoadMacro("ResonanceType.cpp+");

gR00T->LoadMacro("Particle.cpp+");

gR00T->LoadMacro("ParticleGenerator.cpp+");

}
```

ParticleGenerator.cpp

```
1 #include "Particle.hpp"
 2
   #include "TFile.h"
   #include "TH1.h"
   #include "TRandom.h"
   #include "TRandom3.h"
   #include <array>
 7
   #include <cmath> //for M PI
 8
   #include <iostream>
 9
10
   enum ParticlesIndexes
11
   {
12
     PI_PLUS = 0,
13
     PI MINUS,
     K PLUS,
14
15
     K MINUS,
16
      P PLUS,
17
     P MINUS,
18
     K_STAR
19
   };
20
21
   void RunSimulation()
22
23
      kape::Particle::AddParticleType("pi+", 0.13957, +1);
                                                                 // pione +
                                                                 // pione -
24
      kape::Particle::AddParticleType("pi-", 0.13957, -1);
25
      kape::Particle::AddParticleType("K+", 0.49367, +1);
                                                                 // kaone +
26
      kape::Particle::AddParticleType("K-", 0.49367, -1);
                                                                 // kaone -
      kape::Particle::AddParticleType("p+", 0.93827, +1);
27
                                                                 // protone
28
      kape::Particle::AddParticleType("p-", 0.93827, -1);
                                                                 // antiprotone
      kape::Particle::AddParticleType("K*", 0.89166, 0, 0.050); // K*
29
```

```
30
31
      // for a longer period of the random number generator
32
      delete gRandom;
33
      gRandom = new TRandom3();
34
      gRandom->SetSeed(
          136279841); // it's the exponent of the biggest mersenne
35
36
                      // prime found to this day :D (from GIMPS on 21/10/2024)
37
      // chose 300 because all 100 particles could (in principle) be a k^* and decay
38
39
      // in two more particles
40
      std::array<kape::Particle, 300> eventParticles;
41
42
      // creating histograms
43
     TH1F* hParticleTypes =
          new TH1F("hParticleTypes", "Generated particle types", 7, -0.5, 6.5);
44
45
                   = new TH1F("hPhi", "Generated phi angles", 1e5, 0., 2. * M PI);
     TH1F* hTheta = new TH1F("hTheta", "Generated theta angles", 1e5, 0., M_PI);
46
47
                   = new TH1F("hP", "Generated p magnitudes", 1e5, 0., 5.);
48
      TH1F* hPTrasverse =
49
          new TH1F("hPTrasverse", "Generated p trasverses", 1e5, 0., 5.);
50
     TH1F* hEnergy =
51
          new TH1F("hEnergy", "Generated particle energies", 1000, 0., 6.);
52
      TH1F* hInvariantMass =
53
          new TH1F("hInvariantMass", "Generated invariant masses", 1e5, 0., 8.);
54
      TH1F* hInvariantMassDiscordant =
55
          new TH1F("hInvariantMassDiscordant",
56
                   "Generated discordant invariant masses", 1e4, 0., 8.);
57
     TH1F* hInvariantMassConcordant =
58
          new TH1F("hInvariantMassConcordant",
59
                   "Generated concordant invariant masses", 1e4, 0., 8.);
60
     TH1F* hInvariantMassDiscordantPiK =
61
          new TH1F("hInvariantMassDiscordantPiK",
62
                   "Generated discordant invariant masses pi/K", 1e4, 0., 8.);
     TH1F* hInvariantMassConcordantPiK =
63
64
          new TH1F("hInvariantMassConcordantPiK",
65
                   "Generated concordant invariant masses pi/K", 1e4, 0., 8.);
66
      TH1F* hInvariantMassDecayed =
          new TH1F("hInvariantMassDecayed", "Generated decayed invariant masses",
67
68
                   100, 0.5, 1.4);
69
70
      // sumw2 for correct errors
71
      hParticleTypes->Sumw2();
72
      hPhi->Sumw2();
73
      hTheta->Sumw2();
74
      hP -> Sumw2();
75
      hPTrasverse->Sumw2();
76
      hEnergy->Sumw2();
77
      hInvariantMass->Sumw2();
78
      hInvariantMassDiscordant->Sumw2();
79
      hInvariantMassConcordant->Sumw2();
80
      hInvariantMassDiscordantPiK->Sumw2();
81
      hInvariantMassConcordantPiK->Sumw2();
82
      hInvariantMassDecayed->Sumw2();
```

```
83
 84
       // generating 10<sup>5</sup> events
 85
       for (int eventIndex = 0; eventIndex != 1e5; ++eventIndex) {
 86
         // index for the next free space where decayed particles can be placed
 87
         int arrayEnd = 100;
88
         // generating the 100 particles of each event
 89
         for (int arrayIndex = 0; arrayIndex < 100; ++arrayIndex) {</pre>
 90
           Double t phi
                          = gRandom->Uniform(0., 2. * M_PI);
 91
           Double t theta = gRandom->Uniform(0., M PI);
 92
           Double_t p
                           = gRandom -> Exp(1.);
 93
 94
           eventParticles[arrayIndex].SetP(p * std::sin(theta) * std::cos(phi),
 95
                                             p * std::sin(theta) * std::sin(phi),
 96
                                             p * std::cos(theta));
 97
 98
           // choose particle type following proportions
99
           Double_t randomChoice = gRandom->Rndm();
100
           if (randomChoice < 0.40) {</pre>
101
             // pi+
102
             eventParticles[arrayIndex].SetIndex(PI PLUS);
103
           } else if (randomChoice < 0.80) {</pre>
104
             // pi-
             eventParticles[arrayIndex].SetIndex(PI_MINUS);
105
106
           } else if (randomChoice < 0.85) {</pre>
107
             // k+
108
             eventParticles[arrayIndex].SetIndex(K PLUS);
109
           } else if (randomChoice < 0.90) {
110
             // k-
111
             eventParticles[arrayIndex].SetIndex(K MINUS);
112
           } else if (randomChoice < 0.945) {
113
             // p+
114
             eventParticles[arrayIndex].SetIndex(P PLUS);
115
           } else if (randomChoice < 0.99) {
116
             // p-
117
             eventParticles[arrayIndex].SetIndex(P_MINUS);
118
           } else {
             // k* -> decays
119
120
             eventParticles[arrayIndex].SetIndex(K STAR);
121
122
             // choose decayed particle types randomly
             if (gRandom->Rndm() <= 0.5) {
123
124
               eventParticles[arrayEnd].SetIndex(PI_PLUS);
125
               eventParticles[arrayEnd + 1].SetIndex(K_MINUS);
126
             } else {
127
               eventParticles[arrayEnd].SetIndex(PI_MINUS);
128
               eventParticles[arrayEnd + 1].SetIndex(K_PLUS);
129
             }
130
131
             int error = eventParticles[arrayIndex].Decay2body(
132
                 eventParticles[arrayEnd], eventParticles[arrayEnd + 1]);
133
             if (error != 0) {
               std::cout << "decayed to body failed with error " << error << '\n';</pre>
134
135
               throw std::runtime error{
```

```
136
                   "decayed to body failed, check terminal for more info.\n"};
             }
137
138
139
             // the next free space is two places after the last free space (2
140
             // daughters)
141
             arrayEnd += 2;
           }
142
143
           // filling histograms
144
145
           hParticleTypes->Fill(eventParticles[arrayIndex].GetIndex());
146
           hPhi->Fill(phi);
147
           hTheta->Fill(theta);
148
           hP->Fill(p);
149
           hPTrasverse->Fill(
150
               std::sqrt(std::pow(eventParticles[arrayIndex].GetPx(), 2)
151
                         + std::pow(eventParticles[arrayIndex].GetPy(), 2)));
           hEnergy->Fill(eventParticles[arrayIndex].GetEnergy());
152
153
         }
154
155
         // calculating invariant masses between all pairs of particles
156
         for (int i = 0; i != arrayEnd - 1; ++i) {
           if (eventParticles[i].GetIndex() == K_STAR) { // ignore k star
157
             continue;
158
159
           for (int j = i + 1; j != arrayEnd; ++j) {
160
             if (eventParticles[j].GetIndex() == K STAR) { // ignore k star
161
               continue;
162
163
             }
164
165
             // calculate invariant mass of the pair
             Double_t invMass = eventParticles[i].InvMass(eventParticles[j]);
166
             hInvariantMass->Fill(invMass);
167
168
169
             int i type = eventParticles[i].GetIndex();
170
             int j_type = eventParticles[j].GetIndex();
171
             // discordant
172
             if (eventParticles[i].GetCharge() * eventParticles[j].GetCharge() < 0) {</pre>
173
174
               hInvariantMassDiscordant->Fill(invMass);
175
               // PiK pair
176
177
               if ((i_type == PI_PLUS && j_type == K_MINUS)
178
                   || (i_type == PI_MINUS && j_type == K_PLUS)
                   || (j type == PI PLUS && i type == K MINUS)
179
180
                   || (j_type == PI_MINUS \& i_type == K_PLUS)) {
181
                 hInvariantMassDiscordantPiK->Fill(invMass);
182
             } else { // concordant
183
               hInvariantMassConcordant->Fill(invMass);
184
185
               // PiK pair
186
187
               if ((i_type == PI_PLUS && j_type == K_PLUS)
188
                   || (i_type == PI_MINUS && j_type == K_MINUS)
```

```
189
                    || (j_type == PI_PLUS && i_type == K_PLUS)
190
                    || (j_type == PI_MINUS && i_type == K_MINUS)) {
191
                 hInvariantMassConcordantPiK->Fill(invMass);
192
193
             }
           }
194
195
         }
196
197
         // filling the histogram with the invariant masses from only pairs of
         // decayed particles
198
199
         int i = 100;
200
         while (i < arrayEnd) {</pre>
201
           hInvariantMassDecayed->Fill(
202
               eventParticles[i].InvMass(eventParticles[i + 1]));
203
           i += 2;
204
         }
205
       }
206
207
       //save to file
      TFile* file = new TFile("histo.root", "RECREATE");
208
209
210
       hParticleTypes->Write();
      hPhi->Write();
211
212
      hTheta->Write();
213
      hP->Write();
214
      hPTrasverse->Write();
215
      hEnergy->Write();
216
      hInvariantMass->Write();
217
      hInvariantMassDiscordant->Write();
218
      hInvariantMassConcordant->Write();
219
      hInvariantMassDiscordantPiK->Write();
       hInvariantMassConcordantPiK->Write();
220
221
       hInvariantMassDecayed->Write();
222
223
       file->Close();
224 }
```

Analysis.cpp

```
1 #include "TCanvas.h"
2 #include "TF1.h"
 3 #include "TFile.h"
4 #include "TH1.h"
5
   #include "TStyle.h"
   #include <iostream>
6
7
   #include <string>
9
   std::string ExpectedWithError(Int_t nTot, Double_t probability)
10
   {
11
     return std::string{
12
         std::to_string(nTot * probability) + " ± "
         + std::to_string(std::sqrt((1. - probability) * (nTot)*probability))};
13
```

```
14
   }
15
16
   enum ParticlesIndexesAnalysis
17
18
     PI PLUS = 0,
     PI MINUS,
19
     K PLUS,
20
21
      K_MINUS,
22
      P PLUS,
23
      P MINUS,
24
     K_STAR
25
   };
26
27
   void Analysis()
28
29
     TFile* file = new TFile("histo.root");
30
31
     // read the data from file
32
     TH1F* hParticleTypes
                                      = (TH1F*)file->Get("hParticleTypes");
33
     TH1F* hPhi
                                      = (TH1F*)file->Get("hPhi");
34
     TH1F* hTheta
                                      = (TH1F*)file->Get("hTheta");
35
     TH1F* hP
                                      = (TH1F*)file->Get("hP");
     TH1F* hPTrasverse
                                      = (TH1F*)file->Get("hPTrasverse");
36
                                      = (TH1F*)file->Get("hEnergy");
37
     TH1F* hEnergy
38
     TH1F* hInvariantMass
                                      = (TH1F*)file->Get("hInvariantMass");
39
     TH1F* hInvariantMassDiscordant = (TH1F*)file->Get("hInvariantMassDiscordant");
40
     TH1F* hInvariantMassConcordant = (TH1F*)file->Get("hInvariantMassConcordant");
41
      TH1F* hInvariantMassDiscordantPiK =
42
          (TH1F*)file->Get("hInvariantMassDiscordantPiK");
43
      TH1F* hInvariantMassConcordantPiK =
44
          (TH1F*)file->Get("hInvariantMassConcordantPiK");
45
      TH1F* hInvariantMassDecayed = (TH1F*)file->Get("hInvariantMassDecayed");
46
47
      // rebinning
48
      hPhi->Rebin(5);
49
      hTheta->Rebin(5);
50
      hP->Rebin(5);
51
      hInvariantMassDiscordant->Rebin(20);
52
      hInvariantMassConcordant->Rebin(20);
53
      hInvariantMassDiscordantPiK->Rebin(10);
54
      hInvariantMassConcordantPiK->Rebin(10);
55
56
      // check histo entries
57
      if (hParticleTypes->GetEntries() != 1e7)
58
        std::cout << "hParticleTypes has the wrong number of entries \n";</pre>
59
      if (hPhi->GetEntries() != 1e7)
60
        std::cout << "hPhi has the wrong number of entries \n";</pre>
      if (hTheta->GetEntries() != 1e7)
61
62
        std::cout << "hTheta has the wrong number of entries \n";</pre>
63
      if (hP->GetEntries() != 1e7)
        std::cout << "hP has the wrong number of entries \n";</pre>
64
65
      if (hPTrasverse->GetEntries() != 1e7)
66
        std::cout << "hPTrasverse has the wrong number of entries \n";</pre>
```

```
67
     if (hEnergy->GetEntries() != 1e7)
68
       std::cout << "hEnergy has the wrong number of entries \n";</pre>
69
70
     // particle types proportions
     std::cout
71
72
        << "check that the expected number of particles generated for each type "</pre>
           "corresponds to the number of generated particles of that type within "
73
74
           "errors:\n";
75
     std::cout << "|Particle Type\t| Expected\t\t\t| Generated\t\t|\n";</pre>
     std::cout << "-----
76
77
                "----\n";
     78
79
              << hParticleTypes->GetBinContent(PI PLUS + 1) << " ± "</pre>
80
              << hParticleTypes->GetBinError(PI PLUS + 1) << "\t|\n";</pre>
     81
              << hParticleTypes->GetBinContent(PI MINUS + 1) << " ± "</pre>
82
              << hParticleTypes->GetBinError(PI MINUS + 1) << "\t|\n";</pre>
83
84
     85
              << hParticleTypes->GetBinContent(K PLUS + 1) << " ± "</pre>
86
              << hParticleTypes->GetBinError(K PLUS + 1) << "\t|\n";</pre>
87
     << hParticleTypes->GetBinContent(K_MINUS + 1) << " ± "</pre>
88
              << hParticleTypes->GetBinError(K MINUS + 1) << "\t|\n";</pre>
89
     90
              << hParticleTypes->GetBinContent(P_PLUS + 1) << " ± "</pre>
91
92
              << hParticleTypes->GetBinError(P PLUS + 1) << "\t|\n";</pre>
93
     std::cout << "|p- \t|" << ExpectedWithError(1e7, 0.045) << "\t\t|"
              << hParticleTypes->GetBinContent(P MINUS + 1) << " ± "</pre>
94
95
              << hParticleTypes->GetBinError(P MINUS + 1) << "\t|\n";</pre>
     96
97
              << hParticleTypes->GetBinContent(K STAR + 1) << " ± "</pre>
98
              << hParticleTypes->GetBinError(K STAR + 1) << "\t|\n";</pre>
99
     // add all parameters to the output in the figures
100
101
     gStyle->SetOptStat(11);
102
     gStyle->SetOptFit(1111);
103
104
     // Figure 1: particle types, p, phi,
105
     // theta-----
     TCanvas* Figure1 = new TCanvas("Figure1", "Figure1", 0, 0, 800, 600);
106
107
     Figure1->Divide(2, 2);
108
     // particle types------
109
     Figure1->cd(1);
110
111
112
     // normalize
     hParticleTypes->Scale(1. / hParticleTypes->Integral(), "width");
113
114
115
     // fitting
116
     TF1* particleTypesDistr = new TF1("particleTypesDistr",
117
                                  "[0]*(x<0.5) + "
                                  "[1]*(0.5<x && x<1.5) +"
118
                                  "[2]*(1.5< x && x<2.5) + "
119
```

```
120
                                              "[3]*(2.5< x && x<3.5) + "
121
                                              "[4]*(3.5< x && x<4.5) + "
122
                                              [5]*(4.5< \times \&\& x<5.5) + "
                                              "[6]*(5.5<x && x<6.5)",
123
124
                                              -0.5, 6.5);
125
126
       hParticleTypes->Fit(particleTypesDistr);
127
128
       // fit output
129
       std::cout << "\nParticle Types Distribution Fit: \n"</pre>
130
                      "y = \t A 	ext{ if } (x<0.5) \n"
131
                      "\t B if (0.5 < x \text{ and } x < 1.5) \setminus n "
132
                      "\t C if (1.5 < x \text{ and } x < 2.5) \setminus n "
                      "\t D if (2.5 < x \text{ and } x < 3.5) \setminus n "
133
134
                      "\t E if (3.5 < x \text{ and } x < 4.5) \setminus n "
135
                      "\t F if (4.5 < x \text{ and } x < 5.5) \setminus n "
136
                      "\t G if (5.5 < x \text{ and } x < 6.5) \n";
137
138
       std::cout << "Parameter A: " << particleTypesDistr->GetParameter(0) << " ± "</pre>
139
                  << particleTypesDistr->GetParError(0) << '\n';
       std::cout << "Parameter B: " << particleTypesDistr->GetParameter(1) << " ± "</pre>
140
                  << particleTypesDistr->GetParError(1) << '\n';</pre>
141
142
       std::cout << "Parameter C: " << particleTypesDistr->GetParameter(2) << " ± "</pre>
143
                  << particleTypesDistr->GetParError(2) << '\n';</pre>
       std::cout << "Parameter D: " << particleTypesDistr->GetParameter(3) << " ± "</pre>
144
                  << particleTypesDistr->GetParError(3) << '\n';</pre>
145
146
       std::cout << "Parameter E: " << particleTypesDistr->GetParameter(4) << " ± "</pre>
147
                  << particleTypesDistr->GetParError(4) << '\n';</pre>
148
       std::cout << "Parameter F: " << particleTypesDistr->GetParameter(5) << " ± "</pre>
                  << particleTypesDistr->GetParError(5) << '\n';</pre>
149
       std::cout << "Parameter G: " << particleTypesDistr->GetParameter(6) << " ± "</pre>
150
                  << particleTypesDistr->GetParError(6) << '\n';</pre>
151
152
       std::cout << "Reduced Chi Square: "</pre>
153
154
                  << particleTypesDistr->GetChisquare() / particleTypesDistr->GetNDF()
155
                  << "\n";
156
       std::cout << "Chi Square Probability: " << particleTypesDistr->GetProb()
157
                  << "\n\n";
158
159
       // graphics
160
       hParticleTypes->SetTitle("Particle types' distribution");
161
       hParticleTypes->GetXaxis()->SetBinLabel(1, "#pi+");
162
       hParticleTypes->GetXaxis()->SetBinLabel(2, "#pi-");
       hParticleTypes->GetXaxis()->SetBinLabel(3, "K+");
163
164
       hParticleTypes->GetXaxis()->SetBinLabel(4, "K-");
165
       hParticleTypes->GetXaxis()->SetBinLabel(5, "p+");
166
       hParticleTypes->GetXaxis()->SetBinLabel(6, "p-");
       hParticleTypes->GetXaxis()->SetBinLabel(7, "K*");
167
168
       hParticleTypes->GetXaxis()->SetLabelSize(0.065);
169
       hParticleTypes->GetXaxis()->SetTitleOffset(1.2);
170
       hParticleTypes->GetXaxis()->SetTitle("Particle type");
171
       hParticleTypes->GetYaxis()->SetTitle("Probability of particle type");
172
       hParticleTypes->SetFillColor(kAzure - 2);
```

```
173
      hParticleTypes->SetLineColor(kAzure - 2);
174
      hParticleTypes->SetBarWidth(0.2);
175
      hParticleTypes->SetBarOffset(0.8);
      // if sumw2 is set to true the histogram doesn't get filled in
176
177
      hParticleTypes->Sumw2(kFALSE);
178
      hParticleTypes->Draw("b same");
179
180
      // p-----
181
      Figure1->cd(2);
182
183
      // normalize
184
      hP->Scale(1. / hP->Integral(), "width");
185
186
      // fitting
      TF1* pDistr = new TF1("pDistr", "TMath::Exp(-x/[0])", 0., 5.);
187
188
      pDistr->SetParameter(0, 1);
189
      pDistr->SetParameter(1, 1);
190
      hP->Fit(pDistr);
191
192
      // fit output
      std::cout << "\nP Distribution Fit: y = e^(-x/A)\n";</pre>
193
194
195
      std::cout << "Parameter A: " << pDistr->GetParameter(0) << " ± "</pre>
196
                << pDistr->GetParError(0) << "\n";
197
198
      std::cout << "Reduced Chi Square: "</pre>
199
                << pDistr->GetChisquare() / pDistr->GetNDF() << "\n";</pre>
      std::cout << "Chi Square Probability: " << pDistr->GetProb() << "\n\n";</pre>
200
201
202
      // graphics
203
      hP->SetTitle("Impulse magnitudes' distribution");
      hP->GetXaxis()->SetTitle("Impulse magnitude");
204
205
      hP->GetYaxis()->SetTitle("Probability of impulse magnitude");
      hP->GetXaxis()->SetTitleOffset(1.2);
206
207
      hP->SetLineColor(kAzure - 2);
208
      hP->Draw();
209
210
      // phi-----
211
      Figure1->cd(3);
212
      // normalize
213
      hPhi->Scale(1. / hPhi->Integral(), "width");
214
215
216
      // fitting
      TF1* phiDistr = new TF1("phiDistr", "[0]", 0, 2 * TMath::Pi());
217
218
219
      hPhi->Fit(phiDistr);
220
221
      // fit output
222
      std::cout << "\nPhi Distribution Fit: y = A\n";</pre>
223
      std::cout << "Parameter A: " << phiDistr->GetParameter(0) << " ± "</pre>
224
                << phiDistr->GetParError(0) << "\n";
225
```

```
226
      std::cout << "Reduced Chi Square: "</pre>
227
                << phiDistr->GetChisquare() / phiDistr->GetNDF() << "\n";</pre>
      std::cout << "Chi Square Probability: " << phiDistr->GetProb() << "\n\n";</pre>
228
229
      // graphics
230
      hPhi->SetTitle("Azimuthal angles' distribution");
231
      hPhi->GetXaxis()->SetTitle("Azimuthal angle");
232
      hPhi->GetYaxis()->SetTitle("Probability of azimuthal angle");
233
234
      hPhi->GetXaxis()->SetTitleOffset(1.2);
235
      hPhi->SetLineColor(kAzure - 2);
236
      hPhi->Draw();
237
238
      // theta-----
239
      Figure1->cd(4);
240
241
      // normalize
      hTheta->Scale(1. / hTheta->Integral(), "width");
242
243
244
      // fitting
      TF1* thetaDistr = new TF1("thetaDistr", "[0]", 0, TMath::Pi());
245
246
      hTheta->Fit(thetaDistr);
247
      // fit output
248
249
      std::cout << "\nTheta Distribution Fit: y = A\n";</pre>
250
      std::cout << "Parameter A: " << thetaDistr->GetParameter(0) << " ± "</pre>
251
                << thetaDistr->GetParError(0) << "\n";
252
253
      std::cout << "Reduced Chi Square: "</pre>
254
                << thetaDistr->GetChisquare() / thetaDistr->GetNDF() << "\n";</pre>
255
      std::cout << "Chi Square Probability: " << thetaDistr->GetProb() << "\n\n";</pre>
256
257
      // graphics
258
      hTheta->SetTitle("Polar angles' distribution");
      hTheta->GetXaxis()->SetTitle("Polar angle");
259
260
      hTheta->GetYaxis()->SetTitle("Probability of polar angle");
261
      hTheta->GetXaxis()->SetTitleOffset(1.2);
      hTheta->SetFillColor(kAzure - 2);
262
      hTheta->SetLineColor(kAzure - 2);
263
264
      hTheta->Draw();
265
      // Figure 2: invariant masses graphs -----
266
267
      TCanvas* Figure2 = new TCanvas("Figure2", "Figure2", 0, 0, 800, 600);
268
      Figure2->Divide(3, 1);
269
270
      // Only K*-----
271
      Figure2->cd(1);
272
273
      // fitting
274
      TF1* invariantMassDecayedDistr =
275
          new TF1("invariantMassDecayedDistr", "gaus(0)", 0., 8.);
276
      hInvariantMassDecayed->Fit(invariantMassDecayedDistr);
277
278
      // fit output
```

```
279
       std::cout << "\nK* Invariant mass fit: y = A*exp(-0.5*((x-M)/D)**2)\n";
280
       std::cout << "Parameter A: " << invariantMassDecayedDistr->GetParameter(0)
                 << " ± " << invariantMassDecayedDistr->GetParError(0) << "\n";</pre>
281
       std::cout << "Parameter M: " << invariantMassDecayedDistr->GetParameter(1)
282
283
                 << " ± " << invariantMassDecayedDistr->GetParError(1) << "\n";</pre>
       std::cout << "Parameter D: " << invariantMassDecayedDistr->GetParameter(2)
284
285
                 << " ± " << invariantMassDecayedDistr->GetParError(2) << "\n";</pre>
       std::cout << "Reduced Chi Square: "</pre>
286
287
                 << invariantMassDecayedDistr->GetChisquare()
                         / invariantMassDecayedDistr->GetNDF()
288
                 << "\n";
289
290
       std::cout << "Chi Square Probability: "</pre>
291
                 << invariantMassDecayedDistr->GetProb() << "\n\n";</pre>
292
293
       // graphics
       hInvariantMassDecayed->SetTitle("K* invariant masses");
294
295
       hInvariantMassDecayed->GetXaxis()->SetTitle("Invariant mass");
296
       hInvariantMassDecayed->GetYaxis()->SetTitle("Entries");
297
       hInvariantMassDecayed->SetMarkerStyle(kFullSquare);
298
       hInvariantMassDecayed->SetMarkerSize(0.5f);
299
       hInvariantMassDecayed->Draw();
300
       // Difference of discordant particles' invariant masses-----
301
302
       // subtract
303
       TH1F* hDiffMass = new TH1F(*hInvariantMassDiscordant);
304
       hDiffMass->Add(hInvariantMassConcordant, -1);
305
306
       Figure2->cd(2);
307
       // fitting
308
309
      TF1* diffMassDistr = new TF1("diffMassDistr", "gaus(0)", 0., 8.);
310
       hDiffMass->Fit(diffMassDistr);
311
312
       // fit output
313
       std::cout
314
           << "\nK* discordant invariant mass fit: y = A*exp(-0.5*((x-M)/D)**2)\n";
       std::cout << "Parameter A: " << diffMassDistr->GetParameter(0) << " ± "</pre>
315
                 << diffMassDistr->GetParError(0) << "\n";
316
       std::cout << "Parameter M: " << diffMassDistr->GetParameter(1) << " ± "</pre>
317
                 << diffMassDistr->GetParError(1) << "\n";
318
       std::cout << "Parameter D: " << diffMassDistr->GetParameter(2) << " ± "</pre>
319
                 << diffMassDistr->GetParError(2) << "\n";
320
321
       std::cout << "Reduced Chi Square: "</pre>
322
                 << diffMassDistr->GetChisquare() / diffMassDistr->GetNDF() << "\n";</pre>
       std::cout << "Chi Square Probability: " << diffMassDistr->GetProb() << "\n\n";</pre>
323
324
       // graphics
325
       hDiffMass->SetTitle("Discordant particles' invariant masses");
326
327
       hDiffMass->GetXaxis()->SetTitle("Invariant mass");
328
       hDiffMass->GetYaxis()->SetTitle("Entries");
329
       hDiffMass->SetLineColor(kAzure - 2);
330
       hDiffMass->Draw();
331
```

```
332
      // Difference of discordant PiK particles' invariant masses-----
333
      // subtract
      TH1F* hDiffMassPiK = new TH1F(*hInvariantMassDiscordantPiK);
334
       hDiffMassPiK->Add(hInvariantMassConcordantPiK, -1);
335
336
       Figure2->cd(3);
337
338
339
      // fitting
      TF1* diffMassPiKDistr = new TF1("diffMassPiKDistr", "gaus(0)", 0., 8.);
340
       hDiffMassPiK->Fit(diffMassPiKDistr);
341
342
343
       // fit output
344
       std::cout << "\nK* discordant PiK invariant mass fit: y = "</pre>
345
                    A*exp(-0.5*((x-M)/D)**2)\n";
       std::cout << "Parameter A: " << diffMassPiKDistr->GetParameter(0) << " ± "</pre>
346
                 << diffMassPiKDistr->GetParError(0) << "\n";
347
348
       std::cout << "Parameter M: " << diffMassPiKDistr->GetParameter(1) << " ± "</pre>
                 << diffMassPiKDistr->GetParError(1) << "\n";
349
350
       std::cout << "Parameter D: " << diffMassPiKDistr->GetParameter(2) << " ± "</pre>
                 << diffMassPiKDistr->GetParError(2) << "\n";
351
       std::cout << "Reduced Chi Square: "</pre>
352
                 << diffMassPiKDistr->GetChisquare() / diffMassPiKDistr->GetNDF()
353
354
                 << "\n";
       std::cout << "Chi Square Probability: " << diffMassPiKDistr->GetProb()
355
356
                 << "\n\n";
357
358
      // graphics
359
       hDiffMassPiK->SetTitle("#pi - k invariant masses");
360
       hDiffMassPiK->GetXaxis()->SetTitle("Invariant mass");
361
       hDiffMassPiK->GetYaxis()->SetTitle("Entries");
       hDiffMassPiK->SetLineColor(kAzure - 2);
362
       hDiffMassPiK->Draw();
363
364 }
```

testParticleType.cpp

```
1 #define DOCTEST CONFIG IMPLEMENT WITH MAIN
 2 #include "ParticleType.hpp"
 3 #include "ResonanceType.hpp"
 4 #include "doctest.h"
 5 #include <cstring> //for strcmp()
   #include <iostream>
7
   TEST CASE("Testing ParticleType")
8
9
10
     SUBCASE("Testing Getter methods")
11
       kape::ParticleType a{"a", 0.5, 1};
12
       CHECK(std::strcmp(a.GetName(), "a") == 0);
13
14
       CHECK(a.GetMass() == 0.5);
15
       CHECK(a.GetCharge() == 1);
16
     }
```

```
17
18
      SUBCASE("Testing Print method")
19
20
        kape::ParticleType a{"a", 0.5, 1};
21
        std::cout << "\nPlease check that the 2 printed outputs are the same: \n\n";</pre>
22
        std::cout << "Name:\ta\n";</pre>
23
24
        std::cout << "Mass:\t0.5\n";
25
        std::cout << "Charge:\t1\n\n";</pre>
26
        a.Print();
27
      }
28
   }
29
30
   TEST CASE("Testing ResonanceType")
31
32
      SUBCASE("Testing Getter methods")
33
      {
34
        kape::ResonanceType b{"b", 0.5, 1, 1.};
        CHECK(std::strcmp(b.GetName(), "b") == 0);
35
        CHECK(b.GetMass() == 0.5);
36
37
        CHECK(b.GetCharge() == 1);
38
        CHECK(b.GetWidth() == 1.);
39
      }
40
      SUBCASE("Testing Print method")
41
42
      {
43
        kape::ResonanceType b{"b", 0.5, 1, 1.};
44
        std::cout << "\nPlease check that the 2 printed outputs are the same: \n\n";</pre>
45
46
        std::cout << "Name:\tb\n";</pre>
47
        std::cout << "Mass:\t0.5\n";
        std::cout << "Charge:\t1\n";</pre>
48
49
        std::cout << "Width:\t1\n\n";</pre>
50
        b.Print();
51
      }
52
53
      SUBCASE("Testing Print override")
54
55
        kape::ParticleType* particles[2];
        particles[0] = new kape::ParticleType("ParticleType", 0.5, 1);
56
57
        particles[1] = new kape::ResonanceType("ResonanceType", 1., -1, 1.);
58
59
        std::cout << "\nPlease check that the 2 printed outputs are the same: \n\n";</pre>
60
        std::cout << "Name:\tParticleType\n";</pre>
61
        std::cout << "Mass:\t0.5\n";
62
        std::cout << "Charge:\t1\n";</pre>
63
64
        std::cout << "Name:\tResonanceType\n";</pre>
        std::cout << "Mass:\t1\n";</pre>
65
        std::cout << "Charge:\t-1\n";</pre>
66
67
        std::cout << "Width:\t1\n\n";</pre>
68
69
        for (int i = 0; i < 2; i++) {
```

testParticle.cpp

```
1
   #define DOCTEST_CONFIG_IMPLEMENT_WITH_MAIN
2
   #include "Particle.hpp"
 3
4
   #include "doctest.h"
 5
   TEST CASE("Testing Particle class")
6
7
   {
8
     SUBCASE("Testing AddParticleType()")
 9
10
       CHECK(kape::Particle::GetNParticleType() == 0);
        kape::Particle::AddParticleType("kape", 70., -1);
11
        CHECK(kape::Particle::GetNParticleType() == 1);
12
       kape::Particle::AddParticleType("samu", 63., 4, 1.);
13
       CHECK(kape::Particle::GetNParticleType() == 2);
14
       kape::Particle::AddParticleType("lele", 56., 18);
15
       CHECK(kape::Particle::GetNParticleType() == 3);
16
        kape::Particle::AddParticleType("nick", 79., -100, 0.40);
17
        CHECK(kape::Particle::GetNParticleType() == 4);
18
19
        kape::Particle gebbi{"kape", 10., -3., 0.};
20
21
        CHECK(gebbi.GetIndex() == 0);
22
       CHECK(gebbi.GetMass() == 70.);
23
        gebbi.Print();
24
       gebbi.SetIndex(1);
25
       CHECK(gebbi.GetIndex() == 1);
       CHECK(gebbi.GetMass() == 63.);
26
       gebbi.Print();
27
28
29
        kape::Particle::AddParticleType("nick", 79., +100, 0.40);
        CHECK(kape::Particle::GetNParticleType() == 4);
30
31
32
       kape::Particle::PrintParticleType();
33
      }
34
      SUBCASE("testing with array")
35
36
      {
37
        kape::Particle::AddParticleType("pi+", 0.13957, +1);
                                                                   // pione +
38
        kape::Particle::AddParticleType("pi-", 0.13957, -1);
                                                                   // pione -
39
        kape::Particle::AddParticleType("K+", 0.49367, +1);
                                                                   // kaone +
        kape::Particle::AddParticleType("K-", 0.49367, -1);
40
                                                                   // kaone -
        kape::Particle::AddParticleType("p+", 0.93827, +1);
41
                                                                   // protone +
        kape::Particle::AddParticleType("p-", 0.93827, -1);
42
                                                                   // protone -
43
        kape::Particle::AddParticleType("K*", 0.89166, 0, 0.050); // K*
44
45
       std::array<kape::Particle, 300> eventParticles;
```

46 } 47 }